

De-Shuang Huang
Kang Li
George William Irwin (Eds.)

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Preface

The International Conference on Intelligent Computing (ICIC) was formed to provide an annual forum dedicated to the emerging and challenging topics in artificial intelligence, machine learning, bioinformatics, and computational biology, etc. It aims to bring together researchers and practitioners from both academia and industry to share ideas, problems and solutions related to the multifaceted aspects of intelligent computing.

ICIC 2006 held in Kunming, Yunnan, China, August 16-19, 2006, was the second International Conference on Intelligent Computing, built upon the success of ICIC 2005 held in Hefei, China, 2005.

This year, the conference concentrated mainly on the theories and methodologies as well as the emerging applications of intelligent computing. It intended to unify the contemporary intelligent computing techniques within an integral framework that highlights the trends in advanced computational intelligence and bridges theoretical research with applications. In particular, bio-inspired computing emerged as having a key role in pursuing for novel technology in recent years. The resulting techniques vitalize life science engineering and daily life applications. In light of this trend, the theme for this conference was **“Emerging Intelligent Computing Technology and Applications”**. Papers related to this theme were especially solicited, including theories, methodologies, and applications in science and technology.

ICIC 2006 received over 3000 submissions from 36 countries and regions. All papers went through a rigorous peer review procedure and each paper received at least three review reports. Based on the review reports, the Program Committee finally selected 703 high-quality papers for presentation at ICIC 2006. These papers cover 29 topics and 16 special sessions, and are included in five volumes of proceedings published by Springer, including one volume of *Lecture Notes in Computer Science* (LNCS), one volume of *Lecture Notes in Artificial Intelligence* (LNAI), one volume of *Lecture Notes in Bioinformatics* (LNBI), and two volumes of *Lecture Notes in Control and Information Sciences* (LNCIS).

This volume of *Lecture Notes in Bioinformatics* (LNBI) includes 85 papers covering 10 relevant topics and 2 special session topics.

The organizers of ICIC 2006, including Yunnan University, the Institute of Intelligent Machines of the Chinese Academy of Science, and Queen's University Belfast, have made enormous effort to ensure the success of ICIC 2006. We hereby would like to thank the members of the ICIC 2006 Advisory Committee for their guidance and advice, the members of the Program Committee and the referees for their collective effort in reviewing and soliciting the papers, and the members of the Publication Committee for their significant editorial work. We would like to thank Alfred Hofmann, executive editor from Springer, for his frank and helpful advice and guidance throughout and for his support in publishing the proceedings in the Lecture Notes series. In particular, we would like to thank all the authors for contributing their

papers. Without the high-quality submissions from the authors, the success of the conference would not have been possible. Finally, we are especially grateful to the IEEE Computational Intelligence Society, The International Neural Network Society and the National Science Foundation of China for their sponsorship.

June 2006

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A Constrained Ant Colony Algorithm for Image Registration

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Abstract. Ant Colony optimization takes inspiration from the behavior of real ant colony to solve optimization problems. We attach some constraints to ant colony model and present a parallel constrained ant colony model to solve the image registration problem. The problem is represented by a directed graph so that the objective of the original problem becomes to find the shortest closed circuit on the graph under the problem-specific constraints. A number of artificial ants are distributed on the graph and communicate with one another through the pheromone trails which are a form of the long-term memory guiding the future exploration of the graph. The algorithm supports the parallel computation and facilitates quick convergence to the optimal solution. The performance of the proposed method as compared to those of the genetic-based approaches is very promising.

1 Introduction

Swarm intelligence research originates from work into the simulation of the emergence of collective intelligent behaviors of real ants. Ants are able to find good solutions to the shortest path problems between the nest and a food source by laying down, on their way back from the food source, a trail of an attracting substance – a pheromone. Based on the pheromone level communication, the shortest path is considered that with the greatest density of pheromone and the ants will tend to follow the path with more pheromone. Dorigo and his colleagues were the first to apply this idea to the traveling salesman problem [1]. This algorithm is referred to as ant colony algorithm (ACA). ACA has achieved widespread success in solving different optimization problems, such as the vehicle routing problem [2], the machine tool tardiness problem [3] and the multiple objective JIT sequencing problem [4].

Image registration is to find a correspondence function mapping coordinates from a source image to coordinates of homologous points in a target image. In clinical applications, it can be used to match images taken from the same patient over a period of time. Generally, image registration methods can be divided into intensity-based and landmark-based methods. Intensity-based methods [5, 6] find the deformation function by optimizing some criterion function that incorporates a measure of image similarity and can produce more precise registration results because of using the information of the whole images. Landmark-based methods [7, 8, 9, 10] involve extraction of landmarks that need to be matched. By interpolating discrete landmarks, a dense mapping for the whole image can be obtained quickly.

In this paper, a constrained ant colony model for solving the image registration problem is developed. Our image registration combines intensity and landmark information and exploits the advantages of both classes of information. Ant colony algorithm, which is constrained and modified to deal with image registration, can make algorithm amenable to parallel implementations, compared with other optimal approaches, for its distinct feature -- distributed computation. The proposed parallel algorithm can obtain the optimal solution in a reasonably shorter period of time.

2 The Constrained Ant Colony

2.1 Original Ant Colony

The ant colony algorithms have been introduced with Dorigo's Ph.D thesis. They are based on the principle that by using very simple communication mechanisms, an ant group is able to find the shortest path between any two points. During their trips a chemical trail (pheromone) is left on the ground. The role of this trail is to guide the other ants towards the target point. For one ant, the path is chosen according to the quantity of pheromone. Furthermore, this chemical substance has a decreasing action over time, and the quantity left by one ant depends on the amount of food found and the number of ants using this trail. As illustrated in Fig. 1, when facing an obstacle, there is an equal probability for every ant to choose the left or right path. As the left trail is shorter than the right one and so requires less travel time, it will end up with higher level of pheromone. More ants take the left path, higher pheromone trail is.

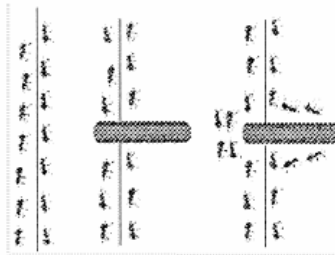


Fig. 1. Ants face an obstacle. When facing an obstacle, there is an equal probability for every ant to choose the left or right path. As the left trail is shorter than the right one and so requires less travel time, it will end up with higher level of pheromone. More ants take the left path, higher pheromone trail is.

The general principles for the ant colony simulation of real ant behavior are as follows.

(1) *Initialization.* The initialization of the AC includes two parts: the problem graph representation and the initial ant distribution. First, the underlying problem should be represented in terms of a graph, $G = \langle N, E \rangle$, where N denotes the set of nodes, and E the set of edges. The graph is connected, but not necessarily complete,

such that the feasible solutions to the original problem correspond to paths on the graph which satisfy problem-domain constraints. Second, a number of ants are arbitrarily placed on the nodes chosen randomly. Then each of the distributed ants will perform a tour on the graph by constructing a path according to the node transition rule described next.

(2) *Node transition rule.* The ants move from node to node based on a node transition rule. According to the problem-domain constraints, some nodes could be marked as inaccessible for a walking ant. The node transition rule is probabilistic. For the k th ant on node i , the selection of the next node j to follow is according to the node transition probability:

$$p_{ij}^k = \begin{cases} \frac{(\tau_{ij})^\alpha (\eta_{ij})^\beta}{\sum_{h \notin tabu_k} (\tau_{ih})^\alpha (\eta_{ih})^\beta} & \text{if } j \notin tabu_k \\ 0 & \text{otherwise} \end{cases} \quad (1)$$

where τ_{ij} is the intensity of pheromone laid on edge (i,j) , η_{ij} is the value of visibility of edge (i,j) , α and β are control parameters, and $tabu_k$ means the set of currently inaccessible nodes for the k th ant according to the problem-domain constraints. The intensity of pheromone laid on edge (i,j) reflecting the previous experience of the ants about this edge is shared memory which provides indirect communication between the ants.

(3) *Pheromone updating rule.* The ant keeps walking through edges to different nodes by iteratively applying the node transition rule until a solution to the original problem is constructed. We define that a cycle of the AC algorithm is completed when every ant has constructed a solution. At the end of each cycle, the intensity of pheromone trails on each edge is updated by the pheromone updating rule:

$$\tau_{ij} \leftarrow \rho \tau_{ij} + \sum_{k=1}^m \Delta \tau_{ij}^k \quad (2)$$

where $\rho \in (0,1)$ is the persistence rate of previous trails, $\Delta \tau_{ij}^k$ is the amount of pheromone laid edge (i,j) by the k th ant at the current cycle, and m is the number of distributed ants. In a real ant system, shorter paths will retain more quantities of pheromone; analogously, in the AC, the paths corresponding to fitter solutions should receive more pheromone quantities and become more attractive in the next cycle. Hence, if we define L_k , the total length of the k th ant in a cycle, as the fitness value of the solution, then $\Delta \tau_{ij}^k$ can be given by

$$\Delta \tau_{ij}^k = \begin{cases} \frac{Q}{L_k} & \text{if edge } (i, j) \text{ is traversed by} \\ & \text{the } k\text{th ant at this cycle} \\ 0 & \text{otherwise} \end{cases} \quad (3)$$

where Q is a constant.

(4) *Stopping criterion.* The stopping criterion of the AC algorithm could be the maximal number of running cycles or the CPU time limit.

2.2 Constrained Ant Colony

For solving image registration, we modify and attach some constraints to the original ant colony model. In original ant colony model, the underlying problem should be represented in terms of a graph $G = \langle N, E \rangle$, which is connected, but not necessarily complete, as shown in Fig. 2 (a). Now, following constraints are added to G for reducing the search space. 1) All the nodes construct a loop. 2) The adjacent node has no less than one edge. 3) The nonadjacent node has no edge. After applying these rules, an example of the graph with constraints is shown in Fig. 2 (b). When ant colony algorithm works on the graph with constraints, we call it constrained ant colony.

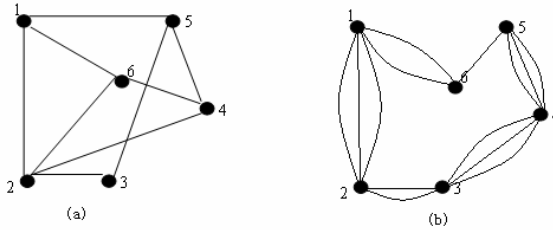


Fig. 2. The original graph and constrained graph. The constrained graph must satisfy following constraints. G. 1) All the nodes N_i construct a loop. 2) The joint node has no less than one edge. 3) The un-joined node has no edge.

3 Image Registration Problem

In this section, we introduce the structure of image registration problem and give some definitions of the notations. The goal of image registration algorithm is to determine a transformation function based on the landmarks from the source image $f_S(\mathbf{i})$ to the target image $f_T(\mathbf{i})$, where $\mathbf{i} \in \mathbf{I} \subset \square^2$, and \mathbf{I} is a 2D discrete interval representing the set of all pixel coordinates in the image. We suppose that the source image is a geometrically deformed version of the target image. That is to say that the points with the same coordinate \mathbf{x} in the target image $f_T(\mathbf{x})$ and in the warped source image $f_w(\mathbf{x}) = f_S^c(\mathbf{g}(\mathbf{x}))$ should correspond. Here, f^c is a continuous version of the image and $\mathbf{g}(\mathbf{x}) : \square^2 \rightarrow \square^2$ is a deformation function to be identified.

3.1 Image Representation

To interpolate the images accurately, the image is represented as a continuous version using uniform B-splines [11]:

$$f^c(\mathbf{x}) = \sum_{\mathbf{i} \in \mathbb{I} \subset \square^2} \mathbf{b}_i \beta_3(\mathbf{x} - \mathbf{i}) \quad (4)$$

where β_3 is a tensor product of B-splines of degree 3, that is $\beta_3(\mathbf{x}) = \prod_{k=1}^2 \beta_3(x_k)$, with $\mathbf{x} = (x_1, x_2)$.

3.2 Transformation Function

We choose the Locally Constrained Deformation (LCD) [12], shown in Eq. (5), as transformation function

$$\mathbf{g}(\mathbf{x}) = \mathbf{x} + \sum_{i=1}^N \alpha_i \rho_{\text{LCD}} \left(\frac{\|\mathbf{x} - \mathbf{p}_i\|}{\mathbf{r}_i} \right) \quad (5)$$

$$\rho_{\text{LCD}}(\mathbf{r}) = \begin{cases} (1 - \mathbf{r}^2)^3 & 0 \leq \mathbf{r} \leq 1 \\ 0 & 1 < \mathbf{r} \end{cases}$$

and it must fulfill the following constraints:

$$\mathbf{g}(\mathbf{p}_i) = \mathbf{q}_i \quad \mathbf{i} = 1 \dots N \quad (6)$$

where α_i is the coefficients, $\mathbf{p}_i \in \square^2$ $\mathbf{i} = 1 \dots N$ constitute a given set of landmark points in the source image, $\mathbf{q}_i \in \square^2$ $\mathbf{i} = 1 \dots N$ are the corresponding landmark points in the target image and N is the number of the landmark points.

3.3 Cost Function

The two images f_T and f_W will not be identical because the assumption that there is a geometrical mapping between the two images is not necessarily correct. Therefore, we define the solution to our registration problem as the result of the minimization $\mathbf{g} = \arg \min_{\mathbf{g} \in \mathbf{G}} \mathbf{E}(\mathbf{g})$, where \mathbf{G} is the space of all admissible deformation functions \mathbf{g} . We choose the sum of squared difference (SSD) criterion as cost function because it is fast to evaluate and yields a smooth criterion surface. The form of SSD is

$$E = \sum_{\mathbf{i} \in I} (f_s^c(\mathbf{g}(\mathbf{i})) - f_T^c(\mathbf{i}))^2 \quad (7)$$

3.4 Optimization Strategy

To minimize the criterion \mathbf{E} in (7), some local iterative algorithms have been cast into the framework [13], but the computation of the derivate is required. Therefore, the

constrained ant colony algorithm is introduced to minimize the criterion and the details are shown in section 4.

4 Constrained Ant Colony for Image Registration

Through the analysis of Eq. (5) and Eq. (6), the transformation function $\mathbf{g}(\mathbf{x})$ can be adjusted by varying the value of \mathbf{r}_i . Thus the optimal solution of \mathbf{r}_i can be obtained to minimize the SSD of two images using constrained ant colony.

4.1 Graph Representation

To apply ant colony, the underlying problem should be represented in terms of a directed graph, $G=\langle N,E\rangle$, which can avoid the ants walking backward. Apparently, for image registration problem, each landmark point p_i should be represented as a node of the graph, $N=P$. We represent the edge E as $\overline{(p_i, p_j, r_k)}$, where r is the action radius of landmark point p_j , as shown in Eq. (5). $ssd(\overline{(p_i, p_j, r_k)})$ is the SSD of the edge $\overline{(p_i, p_j, r_k)}$ and is defined as E in Eq. (7) with only one landmark point p_j and action radius is r_k . In addition, there are many edges between two nodes in our graph, which differs from AC. Now, the problem of image registration is equivalent to finding a closed circuit, which satisfies the minimal SSD, on the directed graph.

4.2 Node Transition Rule

The node transition rule is a probabilistic one determined by the pheromone intensity τ_{ijk} and the visibility value η_{ijk} of the corresponding edge. In the proposed method, τ_{ijk} is equally initialized to any small constant positive value, and is gradually updated at the end of each cycle according to the average quality of the solution that involves this edge. On the other hand, the value of η_{ijk} is determined by a greedy heuristic method, which encourages the ants to walk to the minimal SSD edge. This can be accomplished by setting $\eta_{ijk} = 1/ssd(\overline{(p_i, p_j, r_k)})$.

We now define the transition probability from node i to node j through directed edge $\overline{(p_i, p_j, r_k)}$ as

$$p_{ijk}(t) = \begin{cases} \frac{[\tau_{ijk}(t)]^\alpha [\eta_{ijk}]^\beta}{\sum_{allowed_list} [\tau_{ijk}(t)]^\alpha [\eta_{ijk}]^\beta} & \text{if } j \in allowed_list \\ 0 & \text{otherwise} \end{cases} \quad (8)$$

where *allowed_list* are the accessible nodes by walking ants, and the means of other symbols are same to the Eq. (1).

4.3 Pheromone Updating Rule

The intensity of pheromone trails of an edge is updated at the end of each cycle by the average quality of the solutions that traverse along this edge. We simply apply and modify Eqs. (2) and (3) to update pheromone intensity.

$$\tau_{ijk} \leftarrow \rho \cdot \tau_{ijk} + \sum_{s=1}^m \Delta \tau_{ijk}^s \quad (9)$$

$$\Delta \tau_{ijk}^s = \begin{cases} \frac{Q}{SSD_s} & \text{if the } sth \text{ ant walks } \overline{(p_i, p_j, r_k)} \\ 0 & \text{otherwise} \end{cases} \quad (10)$$

where SSD_s is the SSD of the sth ant's registration result at current cycle.

4.4 Constrained Ant Colony for Image Registration

According to the given definitions as above, the image registration based on constrained ant colony is described as following.

Input:

m : the number of ants.

MAX_CYCLE : the maximal number of running cycles.

1: Construct the directed graph $G = \langle N, E \rangle$ as described in Section 4.1. Set $NC = 1$ (NC is the cycles counter), $\tau_{ijk}(t) = c$ (c is constant), $SSD_{global_best} = \infty$ (SSD_{global_best} saves the minimal SSD of the strip). Compute η_{ijk} on every edge $\overline{(p_i, p_j, r_k)}$.

2: For every ant do

Select a starting node.

Repeat

Move to next node according to the node transition rule using Eq. (8).

until a closed tour is completed.

//a closed tours is completed when the ant arrives at the starting node again.

3: Compute registration results and find out the minimal SSD among the m tours obtained at step2, say $SSD_{current_best}$.

4: If $SSD_{current_best} < SSD_{global_best}$, then $SSD_{global_best} = SSD_{current_best}$.

5: For every directed edge $\overline{(p_i, p_j, r_k)}$ do

Update the pheromone intensity using Eqs. (9) and (10).

6: If ($NC = MAX_CYCLE$), then output SSD_{global_best} and stop;
otherwise, $NC = NC + 1$ and goto step2.

5 Parallel Ant Colony

To solve efficiently large optimization problems, a parallel model of ant colony has been developed. The programming style used is a synchronous master/workers paradigm. The master initializes all kinds of data as stated in section 4.4 step1, and then sends the graph information including the trail density τ_{ijk} and the visibility η_{ijk} to workers. With the graph information, the worker takes charge of searching for a tour composed of the edge and completing image registration. The parallel algorithm works as follows Fig. 3. Each worker returns the SSD of registration result and the tour visited to the master, which later updates the intensity of trail on the edge and controls the flow of the algorithm. By this way all the workers can implement parallel packing by sharing the information from the master.

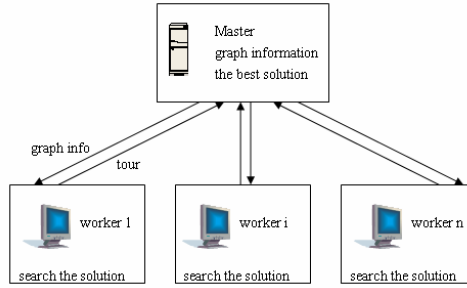


Fig. 3. Synchronous master/workers model for parallel ant colony. The master initializes all kinds of data and the worker takes charge of searching for a tour composed of the edge and completing image registration.

6 Experimental Results

The proposed algorithm has been programmed in VC++ language, and run in Windows 2000 Professional. According to Ref. [12], the action radius of the landmark point is constrained as:

$$r_i \geq 1.71 \| q_i - p_i \| \quad (11)$$

which should be satisfied in the constrained graph. Furthermore, every landmark point has limited action scope and it is constrained as $r_i \leq 15 \| q_i - p_i \|$. Thus between the node p_i and p_j , there are $NUM_j = \lfloor (15 - 1.71) * \| q_j - p_j \| / \Delta \rfloor$ edges, that is to say $\overline{(p_i, p_j, r_k)} \quad k = 1, 2, \dots, NUM_j$, where Δ is used to control the accuracy of the algorithm and set $\Delta = 0.5$. In our implementation, $\alpha = 1.0$, $\beta = 2.0$, $\rho = 0.9$ and $MAX_CYCLE = 200$.

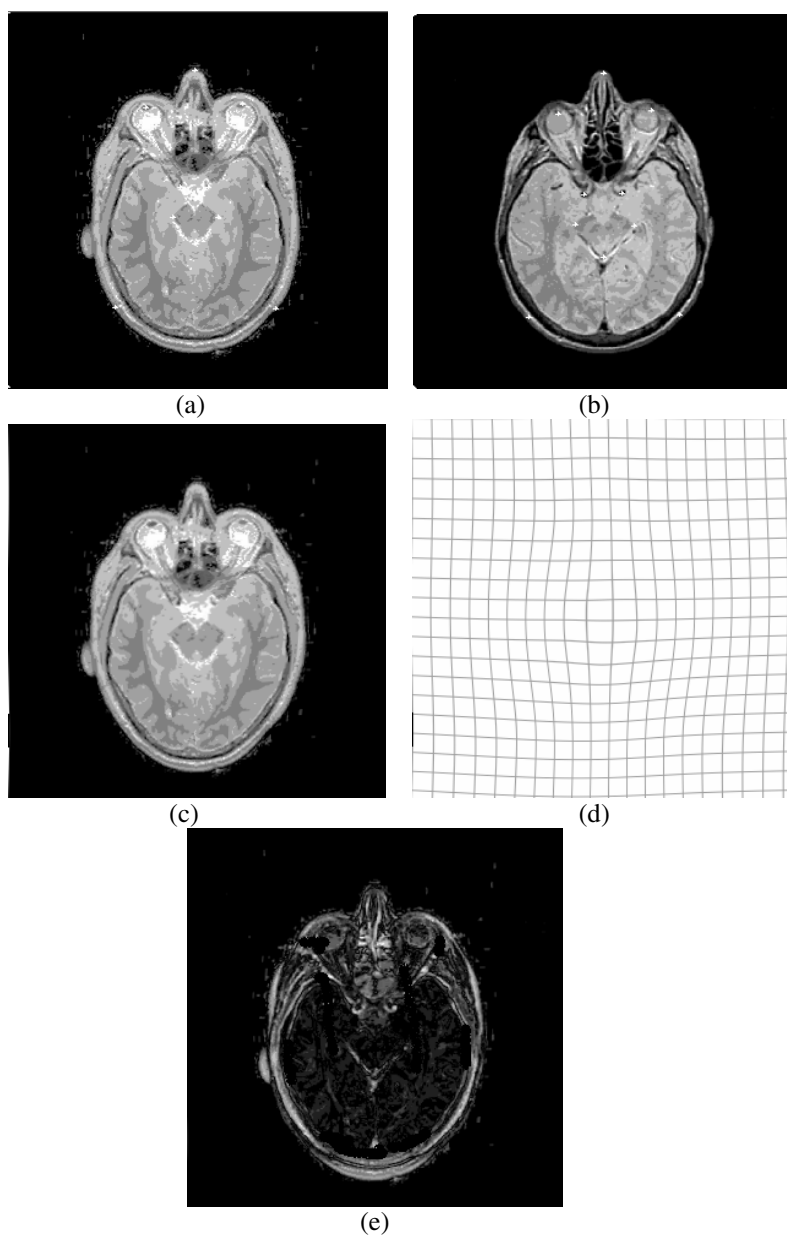


Fig. 4. Registration results. (a) source image; (b) target image; (c) registration result; (d) the underlying grid of (c); (e) difference between (b) and (c).

Fig. 4 shows an experimental result based on the presented algorithm. In the source image Fig. 4(a) and the target image Fig. 4(b), we interactively selected 10 pairs of point-landmarks. The registration result is shown in Fig. 4(c). To assess the form of

the deformation, we have applied the algorithm to a regular grid and the result can be seen in Fig. 4(d). The obvious influence of the deformation is demonstrated in Fig. 4(e) where the reference image is subtracted from the registration result.

In addition, we compare the efficiency of our algorithm to the genetic algorithm. With variable number of the landmark points, we complete four examples whose results are listed in Table 1. In our algorithm, 10 workers are used to search the solutions. It is indicated from the results that our algorithm can converge more quickly to the better solutions because of the parallel implementation.

Table 1. Results from the different algorithms

Examples		Genetic algorithm	Ant colony algorithm
Example 1: 10 points	Time (minute)	10.0	2.9
Example 2: 15 points	Time (minute)	14.3	4.1
Example 3: 20 points	Time (minute)	17.6	6.0
Example 4: 25 points	Time (minute)	19.1	7.7

7 Conclusion

In this paper we have developed a powerful and robust algorithm for image registration, which bases on the constrained ant colony model. The proposed algorithm supports parallel computation and facilitates quick convergence to the optimal solution. The experimental result demonstrates that our algorithm can search the solution space more effectively and obtain the optimal solution in a reasonably shorter period of time.

Acknowledgements

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A Novel ACO Algorithm with Adaptive Parameter

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Abstract. ACO has been proved to be one of the best performing algorithms for NP-hard problems as TSP. Many strategies for ACO have been studied, but little theoretical work has been done on ACO's parameters α and β , which control the relative weight of pheromone trail and heuristic value. This paper describes the importance and functioning of α and β , and draws a conclusion that a fixed β may not enable ACO to use both heuristic and pheromone information for solution when $\alpha = 1$. Later, following the analysis, an adaptive β strategy is designed for improvement. Finally, a new ACO called adaptive weight ant colony system (AWACS) with the adaptive β and $\alpha = 1$ is introduced, and proved to be more effective and steady than traditional ACS through the experiment based on TSPLIB test.

1 Introduction

ACO was first proposed by M. Dorigo and his colleagues as a multi-agent approach to deal with difficult combinatorial optimization problems such as TSP [1]. Since then, a number of applications to the NP-hard problems have shown the effectiveness of ACO [1]. Up till now, Ant Colony System (ACS) [2] and MAX-MIN Ant System (MMAS) [3] are so successful and classical that their strategies such as pheromone global-local update and Maximum-Minimum of pheromone are widely used in recent research [1].

At present, the study on the speed of convergence and the parameter selection is a hot topic [4]. As for the ACO's convergence, W. J. Gutjahr [4-6], T. Stützle [7], M. Dorigo [7-9], A. Fahmy [10], and S. Fidanova [11, 12] have done a lot of work. For its parameter setting, M. Dorigo and L.M. Gambardella presented a formula for the optimal number of ants m based on the value of q_0 and ρ [2]. Watanabe and Matsui proposed an adaptive control mechanism of the parameter candidate sets based on the pheromone concentrations [13]. Pilat and White put forward the ACSGA-TSP algorithm [14] with an adaptive evolutionary parameters β , ρ , q_0 and gave the experimental values of these parameters for some TSP problems. A. C., Zecchin etc [15] applied their work of parametric study to water distribution system optimization.

The performance of ACS is mainly based on the cooperative work of artificial ants. According to pheromone trail and heuristic value, the ants choose components to form the solutions at each iteration. The value of parameters α and β , $\alpha > 0$ and $\beta > 0$, determines the relative importance of pheromone value and heuristic information [2, 9,15]. However, there is few theoretical research on the function of α and β . The experimental study of the various ACO algorithms for the TSP has identified parameter settings that result in good performance: α and β are set to 1 and [2, 5] respectively [8]. The values of α and β are usually set by experiment [3,16-18] in the interval [0, 5].

In this paper, firstly, the theoretical justification of α and β is explained. Secondly, following the justification, an adaptive β strategy is designed to optimize the searching process of ACO algorithm. Then, a new algorithm, called adaptive weight ant colony system (AWACS), is proposed with the adaptive β strategy to improve ACS and its convergence can be proved. In order to test its performance, the numerical experiments on TSPLIB [19] are given, and show AWACS can perform much better than ACS in TSP instances.

2 The Function of the Parameters α and β

In ACO algorithms, like AS [1], ACS [2], MMAS [3] and AS-AR [11], the state transition rule of the artificial ants is given as follows:

$$P_{gs}^k(t) = \begin{cases} \frac{[\tau_{gs}(t)]^\alpha [\eta_{gs}]^\beta}{\sum_{r \in J_k(g)} [\tau_{gr}(t)]^\alpha [\eta_{gr}]^\beta} & \text{if } s \in J_k(g) \\ 0 & \text{otherwise} \end{cases} \quad (1)$$

Where:

P_{gs}^k is the probability with which the ant k chooses to move from city g to city s in iteration t ;

τ is the pheromone;

$\eta = 1/d$ is the reciprocal of distance d_{gs} ($\eta > 0$);

$J_k(g)$ is the set of cities not visited yet when ant k at city g ;

α and β are the parameters that control the relative weight of pheromone trail and heuristic value.

Given $a, b \in J_k(g)$, if $P_{ga}^k(t) > P_{gb}^k(t)$, which means that city a may be chosen by the ant k as the next city to city g with higher probability than city b , then α and β satisfies the following formula:

$$P_{ga}^k(t) > P_{gb}^k(t) \Leftrightarrow [\tau_{ga}(t)]^\alpha [\eta_{ga}]^\beta > [\tau_{gb}(t)]^\alpha [\eta_{gb}]^\beta. \quad (2)$$

When $\tau_{ga}(t) = \tau_{gb}(t)$ or $\eta_{ga} = \eta_{gb}$, for $\forall \alpha, \beta > 0$, the formula above holds, so we

$$\text{have: } P_{ga}^k(t) > P_{gb}^k(t) \Leftrightarrow \begin{cases} \eta_{ga} > \eta_{gb} & \tau_{ga} = \tau_{gb} \\ \tau_{ga} > \tau_{gb} & \eta_{ga} = \eta_{gb} \end{cases}.$$

However, when

$\tau_{ga}(t) \neq \tau_{gb}(t), \tau_{ga}(t) > 0, \tau_{gb}(t) > 0$ and $\eta_{ga} \neq \eta_{gb} (\eta_{ga}(t) > 0, \eta_{gb}(t) > 0)$,

one has

$$P_{ga}^k(t) > P_{gb}^k(t) \Leftrightarrow [\tau_{ga}(t)]^\alpha [\eta_{ga}]^\beta > [\tau_{gb}(t)]^\alpha [\eta_{gb}]^\beta \\ \Leftrightarrow \alpha \log[\tau_{ga}(t)] + \beta \log[\eta_{ga}] > \alpha \log[\tau_{gb}(t)] + \beta \log[\eta_{gb}]$$

$$\Leftrightarrow \log \tau_{ga}(t) - \log \tau_{gb}(t) > \frac{\beta}{\alpha} (\log \eta_{gb} - \log \eta_{ga})$$

$$\Leftrightarrow \begin{cases} \frac{\beta}{\alpha} < \frac{\log \tau_{ga}(t) - \log \tau_{gb}(t)}{\log \eta_{gb} - \log \eta_{ga}} & \eta_{gb} > \eta_{ga} \\ \frac{\beta}{\alpha} > \frac{\log \tau_{ga}(t) - \log \tau_{gb}(t)}{\log \eta_{gb} - \log \eta_{ga}} & \eta_{gb} < \eta_{ga} \end{cases}.$$

Particularly, when $\alpha = 1$, which exists in ACO algorithms like ACS, a conclusion can be drawn:

$$P_{ga}^k(t) > P_{gb}^k(t) \Leftrightarrow \begin{cases} \beta < \frac{\log \tau_{ga}(t) - \log \tau_{gb}(t)}{\log \eta_{gb} - \log \eta_{ga}} & \eta_{gb} > \eta_{ga} \\ \beta > \frac{\log \tau_{ga}(t) - \log \tau_{gb}(t)}{\log \eta_{gb} - \log \eta_{ga}} & \eta_{gb} < \eta_{ga} \end{cases}. \quad (3)$$

From the analysis above, one can see that the values of the parameters α and β can directly impact the path choosing process. They determine the probability order of the candidate paths, and make artificial ants select some paths with higher probability meeting rule (3). In ACS, β determines the relative importance of pheromone versus distance [2]. In ACO algorithms, a higher value of β directs the ants to the paths with the more optimistic heuristic values^[17]. According to Formula (3), it can also hold that the higher β is, the more heuristic value $\eta = 1/d$ is regarded. The relation between β ($\alpha = 1$) and the state transition rule is used to design an ACO algorithm with adaptive β in the next section.

3 Adaptive Weight Colony Ant System

For the sake of convenience, some symbols about the pheromone trail are defined as follows:

$\tau_g^{\max}(t) = \max_{i \in J_k(g)} \{\tau_{gi}(t)\}$ is the highest pheromone trail among all the cities feasible to be selected as next stop to city g .

$\tau_g^{\min}(t) = \min_{i \in J_k(g)} \{\tau_{gi}(t)\}$ is the lowest one.

And $\tau_g^{ave}(t) = |J_k(g)|^{-1} \sum_{i \in J_k(g)} \tau_{gi}(t)$ is the average pheromone trail, where

$|J_k(g)|$ is the number of elements in the set $J_k(g)$.

$\eta_g^{\max} = \max_{i \in J_k(g)} \{d_{gi}^{-1}\}$ is the highest heuristic value of elements in the set $J_k(g)$.

$\eta_g^{\min} = \min_{i \in J_k(g)} \{d_{gi}^{-1}\}$ stands for the lowest heuristic value.

And $\eta_g^{ave} = |J_k(g)|^{-1} \sum_{i \in J_k(g)} \eta_{gi} = |J_k(g)|^{-1} \sum_{i \in J_k(g)} d_{gi}^{-1}$ is the average heuristic value.

Let $\alpha = 1$, two cases are discussed in the following:

$$\textcircled{1} [\tau_g^{\max}(t)]^\alpha [\eta_g^{\min}]^\beta > [\tau_g^{ave}(t)]^\alpha [\eta_g^{\max}]^\beta.$$

It means that the ants will select the paths with the maximum pheromone trail with a very high probability ACS.

According to Formula (3), one has $\beta < \frac{\log \tau_g^{\max}(t) - \log \tau_g^{ave}(t)}{\log \eta_g^{\max} - \log \eta_g^{\min}} = M_1(g, t)$, because it

is obvious that $\eta_g^{\max} > \eta_g^{\min}$ holds in TSPLIB problems.

$$\textcircled{2} [\tau_g^{\min}(t)]^\alpha [\eta_g^{\max}]^\beta > [\tau_g^{\max}(t)]^\alpha [\eta_g^{ave}]^\beta.$$

It means that the ants will select the paths with the maximum heuristic value with a very high probability in ACS.

It is obvious that $\beta > \frac{\log \tau_g^{\min}(t) - \log \tau_g^{\max}(t)}{\log \eta_g^{ave} - \log \eta_g^{\max}} = M_2(g, t)$ holds, when $\eta_g^{\max} > \eta_g^{ave}$

and $\tau_g^{\min}(t) > 0$.

According to the analysis of case ① and ②, ACO may work as a non-heuristic searching when $\beta < M_1(g, t)$, and as a greedy searching without using pheromone trail when $\beta > M_2(g, t)$.

Therefore, a fixed β may not enable ACO to find optimal solution by using both heuristic and pheromone information.

However, the process of ACO will not be in the extreme as non-heuristic or greedy searching when $M_1(g,t) \leq \beta \leq M_2(g,t)$.

So a new adaptive parameter β is designed as follows:

$$\alpha = 1, \beta(g,t) = \frac{\log \tau_g^{ave}(t) - \log \tau_g^{max}(t)}{\log \eta_g^{ave} - \log \eta_g^{max}} (\tau_g^{min}(t) > 0). \quad (4)$$

where $M_1(g,t) \leq \beta(g,t) \leq M_2(g,t)$ can be proved.

Based on the adaptive parameter $\beta(g,t)$ strategy shown in Formula (4), a novel ACO algorithm, which is called adaptive weight ant colony system (AWACS) can be described as follows.

```

Initialize /*  $\beta$  is chosen in [0, 5] randomly,
 $q_0 = 0.6$  */
Loop /* at this level each loop is called iteration */
  Each ant is positioned on a starting node.
  Loop /* at this level each loop is called a step */
    Each ant applies a state transition rule to
    incrementally build a solution following Formula
(1)
    and a local pheromone updating rule in Ref [2]
  Until all ants have built a complete solution
  A global pheromone updating rule is applied in Ref
[2]
   $\beta(g,t)$  is updated ( $g=1,\dots,n$ ) following Formula (4)
Until End_condition

```

The proof of its convergence ($g=1,\dots,n$) is the same as the one in Ref. [7].

According to the work of Ref. [7], it still holds that $\tau_g^{min}(t) > 0$ and $\tau_g^{max}(t) < +\infty$ ($g=1,\dots,n$) when the adaptive parameter $\beta(g,t)$ strategy in Formula (4) is applied. Then, AWACS can be proved to find the optimal solution with probability one following the conclusion given by T. Stützle and M. Dorigo [7-8].

4 Numerical Result

In this section, a comparison of the performance of ACS and AWACS is given based on the experiments for some symmetric TSP instances. There is no local search strategy introduced to ACS and AWACS in the present experiment like

ACS-3-opt. In our experiments, the parameters are set as follows: $m = 10$, $\alpha = \rho = 0.1$, $\tau_0 = (nL_m)^{-1}$. q_0 is set $q_0 = 0.9$ in ACS, and $q_0 = 0.6$ in AWACS, respectively. The initial value of β in AWACS is a random figure changing in the interval $[1, 5]$. The initial feasible solutions of TSP are generated in the way from Ref [2].

The experiments on the first 10 TSP problems, where the distances between cities are measured by integer numbers, have been executed on a PC with an Intel Celson (r) III 1.0GHZ Processor and 256M DDR Memory, and the results are shown in Table 1. The experiments on the next 10 problems, where the distances between cities are measured by real numbers, are executed on another PC with an Intel Pentium III 333MHZ Processor and 256M SDR Memory, and the results are listed in Table 2. It should be noted that every instance is computed 10 times. The ACS and AWACS algorithms are both programmed in Visual C++6.0 for Windows System. They would stop when no better solution could be found in 500 iterations, which is considered as a virtual convergence of the algorithms. The datasets can be found in TSPLIB: <http://www.iwr.uni-heidelberg.de/iwr/comopt/soft/TSPLIB95/TSPLIB.html>.

Table 1. Comparison I of the results obtained by ACS and AWACS

Instance	Optimal	Best (ACS)	Best (AWACS)	Average (ACS)	Average (AWACS)	T _{avg} (s) (ACS)	T _{avg} (s) (AWACS)	Best β (ACS)
st70	654	657	657	675.9	675.5	16.9	27.4	4
rat99	unknown	1188	1188	1211.7	1199.4	53.2	59.7	3
pr107	unknown	44539	44398	44906.3	44783.9	39.5	55.4	4
pr124	unknown	59205	59067	59819.9	59646.6	59.2	42.3	4
eil101	612	614	613	634.6	631.4	22.4	76.3	5
rd100	7858	7909	7861	8100.4	8066.2	59.5	54.1	3
eil51	415	415	415	423.9	423.7	6.7	7.8	3
lin105	14345	14376	14354	14509.3	14465.6	73.7	50.8	4, 5
kroD100	21249	21486	21265	21893	21628.2	25.8	60	5
kroC100	20703	20703	20703	21165.3	20914.9	29.5	67.7	4

Table 2. Comparison II of the results obtained by ACS and AWACS

Instance	Optimal	Best (ACS)	Best (AWACS)	Average (ACS)	Average (AWACS)	T _{avg} (s) (ACS)	T _{avg} (s) (AWACS)	Best β (ACS)
kroA100	21282	21285.44	21285.44	21345.78	21286.33	51.3	51.8	2, 3
kroE100	22068	22078.66	22068.75	22206.62	22117.16	56.3	64.5	5
berlin52	7542	7544.36	7544.36	7544.36	7544.36	8.7	9.8	5
kroB150	26130	26127.35	26127.71	26332.75	26214.10	177.8	164.8	5
ch150	6528	6530.90	6530.90	6594.94	6559.66	373.6	118.1	2
kroB100	22141	22139.07	22139.07	22335.72	22177.47	55.5	68.6	4
kroA150	26524	26618.33	26524.86	26809.08	26685.73	204.5	242.9	5
u159	42080	42075.67	42075.67	42472.04	42168.54	356.7	80.2	1
pr76	108159	108159.4	108159.4	108610.6	108581.7	50.5	42.8	1
pr136	96772	96870.89	96785.86	97854.16	97236.61	344.3	158.9	1,4,5

Table 3. Comparison of standard deviations of the tour lengths obtained by AWACS and ACS

Instance \ Standard deviation	AWACS	ACS $\beta = 1$	ACS $\beta = 2$	ACS $\beta = 3$	ACS $\beta = 4$	ACS $\beta = 5$
kroA100	8.49	460.04	338.84	183.55	625.81	447.03
kroE100	123.82	327.01	467.75	529.73	330.12	366.49
berlin52	0.00	376.98	376.19	357.76	548.34	0.00
kroB150	221.98	447.98	652.57	821.48	664.54	486.91
ch150	54.50	114.76	153.71	109.36	171.66	54.81
kroB100	132.37	554.43	579.73	1091.25	558.86	233.01
kroA150	384.39	522.81	942.11	974.79	640.34	432.72
u159	623.16	726.99	3531.45	2458.43	1509.09	1661.63
pr76	1158.43	1180.56	5058.92	2088.68	1677.73	1411.15
pr136	1300.78	2386.53	5303.40	4572.69	3304.40	2173.27

As shown in the above tables, there might be something like precision and time cost in the result of our experiments different from those in the former research because of the different program tools, systems and computing machines. Another possible reason is that the distances between cities in the first 10 instances are measured by integer numbers. But ACS and AWACS are running in the same setting, so the result remains helpful to compare the performance of these two algorithms.

From Table 1-2, it could be seen that AWACS performs better than ACS with the fixed β . The shortest lengths and the average lengths obtained by AWACS are shorter than those found by ACS in all of the TSP instances. As Table 3 shows, it can be concluded that the standard deviations of the tour lengths obtained by AWACS are smaller than those of ACS with the fixed β . Therefore, we can conclude that AWACS is proved to be more effective and steady than ACS.

ACS has to change the best integer value of parameter β with respect to different instances in the experiments. AWACS can avoid the difficulty about how to choose the experimental value of β , because its adaptive strategy can be considered as a function trying to find the best setting for each path search via meeting the request of Formula 4. Though, the time cost t_{avg} of AWACS is more than ACS in some case, it is less than the sum of time ACS costs with $\beta = 1, 2, 3, 4, 5$ in all of the instances. As a result, the adaptive setting can save much time in choosing the experimental β . Item t_{avg} of AWACS is not less than ACS in all of the instances because it needs to compute the value of $\beta \cdot n$ (number of cities) times in each iteration. However, the adaptive function of AWACS is feasible to use because of its acceptable time cost.

5 Discussions and Conclusion

In this paper, the function and relation of parameters α and β are discussed and proved to be able to influence the city selection in ACO directly. Following this analysis, a new algorithm (AWACS) with adaptive β and $\alpha = 1$ is proposed to improve the function of ACS. Its advantage that AWACS can keep using both heuristic and pheromone information for solution and avoid falling to the extremes as non-heuristic or greedy searching, is based on the adaptive β . Furthermore, AWACS can be proved to meet the precondition for convergence of ACO. In the test instances, AWACS also performs much better than ACS.

With the help of tuning methodologies, it is possible to find the best performing parameter settings in a very reasonable computational time. And the argument given in this paper that the adaptive setting can save time instead of choosing the β value experimentally is convincing as the numerical results show.

It is uncertain theoretically that the adaptive setting of AWACS is the best. Further study is suggested to explore the better management for the optimal setting of α , β and other parameters, which will be very helpful in the application of ACO algorithms.

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Study of Parametric Relation in Ant Colony Optimization Approach to Traveling Salesman Problem

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Abstract. Presetting control parameters of algorithms are important to ant colony optimization (ACO). This paper presents an investigation into the relationship of algorithms performance and the different control parameter settings. Two tour building methods are used in this paper including the max probability selection and the roulette wheel selection. Four parameters are used, which are two control parameters of transition probability α and β , pheromone decrease factor ρ , and proportion factor q_0 in building methods. By simulated result analysis, the parameter selection rule will be given.

1 Introduction

The ant colony optimization emerged as a new heuristic algorithm in the early 1990s [1],[2] is based on the real acting of ant colony. The first ACO algorithm, which is called ant system, and many other ACO algorithms have been tested on combinatorial optimization problems. Like some heuristics derive from nature (HDNs) such as genetic algorithm (GA)[3],[4],[5] and neural network [6],[7],[8],[9], the ACO algorithm can reach state-of-the-art performance when approach to some combinatorial optimization problems (especially to discrete problems), for example, traveling salesman problem (TSP) [10],[11],[12], job shop scheduling problem(JSP)[13],[14], [15]and constraint satisfaction problem[16].

Despite its great performance, by now, the ACO algorithm still has some inherent problems which have not been solved properly. Like other HDNs, the performance of ACO lies on some preset control parameters of algorithms, so selecting the proper setting of control parameters is a crucial problem for the efficiency of ACO algorithm. Some effort had been made to the parametric study, for example, Marco Dorigo *et al* [17] had shown some proper value of a part of ACO parameters and A. C. Zecchin *et al* [18] had done parametric study of ACO when applied it to the water distribution system. However, our work is different from theirs. At first, two tour building methods are used in our algorithm, which are the max probability selection and the roulette wheel selection. And the proper setting of proportion factor of

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building methods which determines the probabilities of two tour building methods is researched in this paper. Second, the parameters in ACO are not investigated separately, they are assumed to be correlated. And after the results analysis, some deeper relationships of parameters will be shown.

By researching the relationship of parameters, we found an effective parameter setting rule to solve combination optimization problem and would develop new ACO algorithms which are more adaptive and competitive.

2 The Ant Colony Optimization Algorithm

2.1 Behavior of Real Ants

By use of pheromone, real ants in the nature can find the shortest path from their nest to the food source rather than use their vision. At the beginning, all ants explore the area around their nest randomly for food. As soon as a food source is found, the ant who finds the source will deposit chemical pheromone along the path as well as carries some food back when it returns to their nest. Ants not only deposit pheromone after them on the ground but also follow the pheromone which was previously deposited by other ants or itself. Depending on the quantity of pheromone on the path, ants choose different paths to go. In Fig.1, a process during which ants explore the shortest path between their nest and a food source is shown. In Fig.1, there are a colony nest (N), a food source (S), and an obstacle (X--Y). From N to S, two paths of unequal length are explored. It is assumed that the path NYS takes two time steps ($2\Delta t$) to traverse while the NXS only takes a single time step ($1\Delta t$) and there is no any other path from N to S except the two. At time $t=0$ (Fig.1 (a)), eight ants are setting out to find food (S) from their nest (N). Because they will select the two paths randomly, it is assumed that each path will be selected by four ants. At time $t=1\Delta t$ (Fig.1 (b)), the ants who select the path NXS have acquired the food and begin to return home while other four ants are still on their way to S. As there is some pheromone on path SXN, the probability of utilizing the path SXN by the ants that get the food is higher, three ants select SXN and one selects SYN. At time $t=2\Delta t$ (Fig.1 (c)), three ants that traverse SXN arrive at the nest and one ant that selects SYN is only half way along the path. Meanwhile, the four ants who traverse the NYS just reach the food source. At that time, the path NXS has more pheromone than NYS as the NXS has been traversed for seven times, while the NYS has been traversed for five times. So, there are three ants the path NXS and one ant selects the path NYS. At $t=3\Delta t$ (Fig.1 (d)), all ants return home. From Fig.1 (d), the shorter path NXS has more pheromone deposited than the longer path NYS (pheromone density of the path is represented by the darkness).

At last, the path NXS has a higher probability of being chosen by ants for it has more pheromone deposited than that of the path NYS.

In addition, the pheromone trails on every path will decay with time. If a path has not been added pheromone for a certain time, its pheromone density will reduce to zero. The decay of pheromone quality will also help ants to find the shorter path quicker for the pheromone on the longer paths receive less pheromone and their faster decay of pheromone will make it less attractive to ants.

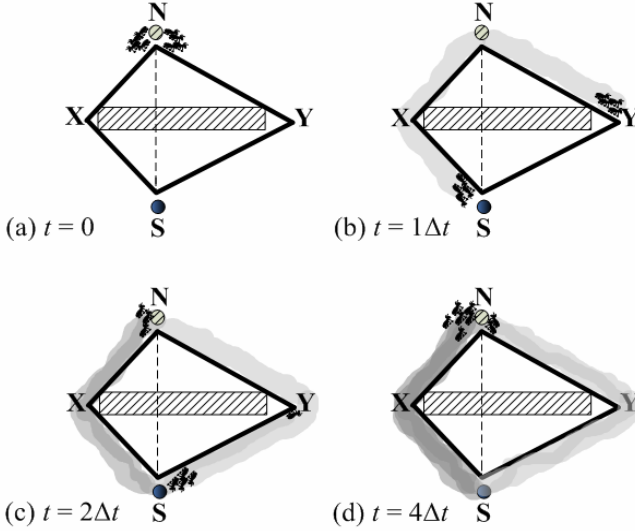


Fig. 1. Example of pheromone evolution in the nature. The real ants can find the shorter path.

2.2 ACO Algorithm Rules

In the past, there are many different ACO algorithms applied to TSP, the ACO algorithm used in this paper is the ant colony system (ACS). The rules of our ACO algorithm are shown in this section.

In our work, the parametric study is done on TSP, and a model of TSP is shown here: Let $Cities = \{0, 1, 2, \dots, n\}$ be a set of cities, $Edges = \{(0, 1), (0, 2), \dots, (n, n-1)\}$ be the set of edges and to each edge $(f, t) \in Edges$, there be a cost measure $C(f, t) = C(t, f)$. The problem of TSP is to find a minimum cost closed tour which visits each city once.

Artificial ants are used in ACO to solve the TSP, they will select the edges to construct the TSP tour depending on the pheromone deposited on them, and meanwhile change the value of pheromone on the edges. In addition, the number of cities is denoted as m and the number of ants is denoted as n .

Random Proportion Rule. The transition probability $(P_k(i, j))$ with which the ant k in city i chooses to go to city j is given by the random proportion rule:

$$P_{(i,j)}^k = \begin{cases} \frac{[\tau_{ij}]^\alpha \cdot [\eta_{ij}]^\beta}{\sum_{l \in tabu[k]} [\tau_{il}]^\alpha \cdot [\eta_{il}]^\beta}, & \text{if } j \notin tabu[k] \\ 0, & \text{otherwise} \end{cases} \quad (1)$$

where τ_{ij} is the pheromone of the edge between city i and city j , η_{ij} is $(1/D_{ij})$, the inverse of D_{ij} the distance between city i and city j . It is introduced that the artificial ants prefer the edges which are shorter and have more pheromone deposited.

State Transition Rule. In the ACO algorithm, each ant builds tour by repeatedly applying the state transition rule. An ant positioned on city i will choose next city j to move depending on the rule:

$$j = \begin{cases} \arg \max_{\substack{j \in \text{tabu} \\ j \neq k}} \{ [\tau_{ij}]^\alpha [\eta_{ij}]^\beta \}, & \text{if } q < q_0 . \\ J, & \text{otherwise} \end{cases} \quad (2)$$

where the q_0 is a parameter, q is a random number uniformly distributed in $[0, 1]$. If $q \leq q_0$ the city with max value of transition probability will be selected to go, otherwise city J will be chosen. J is a random variable selected by applying roulette wheel method to transition probabilities distribution (1).

Local Update Rule. During the tour building process, ants visit edges and change the pheromone amount of them by using the local update rule:

$$\tau_{ij} \leftarrow (1 - \rho) \cdot \tau_{ij} + \rho \cdot \tau_0, \quad (\tau_0 = (n \cdot L_{mn})^{-1}) . \quad (3)$$

where ρ ($0 < \rho < 1$) is a parameter called pheromone decrease factor, τ_0 is the value of pheromone initialized to all edges at the beginning of algorithm. L_{mn} is the length of best tour obtained by Greedy algorithm.

Global Update Rule. After all ants have completed their tours, global update will be performed:

$$\tau_{ij} \leftarrow (1 - \rho) \cdot \tau_{ij} + \rho \cdot \Delta \tau . \quad (4)$$

where

$$\Delta \tau_{(i,j)} = \begin{cases} (L_{T_best})^{-1} & \text{if } \text{edge } (i, j) \in T_best \\ 0, & \text{otherwise} \end{cases} . \quad (5)$$

It is essential to note that the ρ ($0 < \rho < 1$) used in (3) and (4) is very the same algorithm parameter, say, pheromone decrease factor and L_{T_best} is the length of the global best tour T_best . Only the pheromone on edges belong to the global best tour is reinforced in the process.

2.3 ACO Algorithm Parameters

Here a summary of the ACO algorithm parameters which are tested in this paper is shown.

- 1) Decision Policy Control Parameters, α and β .
- 2) Pheromone Decay Factor, ρ .
- 3) Proportion Factor of Building Methods, q_0 .

In addition, in this paper the number of artificial ants is not taken into account, in fact, we set $m=10$ (m is the number of artificial ants) in all experiments according to the optimal number of ants in [10].

A rule of setting parameters will be proposed by researching the different performances in different parameter settings in next section.

3 An Analysis of Optimization Results

At the beginning of this section, it is necessary to reintroduce the two inherent questions of ACO which we intend to solve. First one, how to select the proper setting of

parameters when using ACO algorithm? We only discuss the proper value of α , β , ρ which are used in the algorithm above. And the second, when two or more building tour methods are adopted, how to choose the best one? As two methods, say, max probability selection and roulette wheel selection are applied in our algorithm, and the value of factor q_0 and $(1 - q_0)$ indicates the probabilities of applying the two methods. The problem is researched by analyzing the performances of different values of factor q_0 . In addition, 10 artificial ants are used in the algorithm.

3.1 Combination of α and β

Like some other heuristics, the parameter settings of ACO play a key role on the performance of algorithm. However, there always have so many parameters in the ACO algorithm to deal with. Naturally, we must choose which parameter should be managed first when an ACO algorithm is used. Four parameters are discussed in this

Table 1. Feasible set of combinations of α and β in Oliver_30 (a 30 cities TSP instance). ● : Good combinations. ◐ : Poor combinations. ○ : Bad combinations. The algorithm runs 10 times for each set of parameters.

$\beta \backslash \alpha$	0.0	0.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0	4.5	5.0
0	○	◐	◐	◐	○	○	○	○	○	○	○
1	○	●	●	●	◐	◐	○	○	○	○	○
2	○	●	●	●	◐	◐	○	○	○	○	○
3	○	●	●	●	◐	◐	○	○	○	○	○
4	○	●	●	●	●	◐	◐	◐	○	○	○
5	○	●	●	●	●	●	◐	◐	◐	○	○

paper as known as α , β , ρ and q_0 . As shown in section 2.2, α and β are used in the random proportion rule, q_0 is the factor of the state transition rule while parameter ρ is used in both the local update rule and the global update rule. In this paper, α and β are researched first for the random proportion rule has higher priority than other rules and must be treated first in the algorithm.

Table 2. Feasible set of combinations of α and β in eli51 (a 51 cities TSP instance). ● : Good combinations. ◐ : Poor combinations. ○ : Bad combinations. The algorithm runs 10 times for each set of parameters.

$\beta \backslash \alpha$	0.0	0.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0
0	○	○	◐	◐	○	○	○	○	○
1	○	◐	●	●	◐	◐	○	○	○
2	○	◐	●	●	◐	◐	○	○	○
3	○	●	●	●	●	◐	◐	○	○
4	○	●	●	●	●	◐	◐	◐	○
5	○	●	●	●	●	●	◐	◐	◐

Table 3. Feasible set of combinations of α and β in korA100 (a 100 cities TSP problem). ● : Good combinations. ◐ : Poor combinations. ○: Bad combinations. The algorithm runs 10 times for each set of parameters.

$\alpha \backslash \beta$	0.0	0.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0
0	○	○	○	○	○	○	○	○	○
1	○	◐	●	●	●	◐	○	○	○
2	○	◐	●	●	●	◐	○	○	○
3	○	◐	●	●	●	◐	○	○	○
4	○	◐	●	●	●	◐	◐	◐	○
5	○	●	●	●	●	●	◐	◐	◐

As introduced previously, α and β determine the relative importance of pheromone intensity and desirability respectively, the two parameters are studied together. In our experiment, M_c means the max number of cycles in a single iteration. Different combinations of α and β are investigated with different values of ρ and q_0 , $M_c = 1000$ and the algorithm runs 10 times with each set of parameters. As the result is shown in Table.1, in Oliver_30 instance, the best solution can only be found in certain set of combinations of α and β . All combinations of α and β can be certified in three classes:

a) Good combinations: ACO algorithm finds the global best tour easily in most settings of parameter ρ and q_0 . These combinations are therefore used in the following experiments and they are represented by the symbol ● in Table.1. In addition, the length of global best tour of Oliver_30 obtained by our algorithm is 424.87.

b) Poor combinations: Only in very small selection range of ρ and q_0 , the algorithm can find the global best tour in 1000 cycles. In Table.1, these poor combinations are represented by the symbol: ◐.

c) Bad combinations: The global best solution can not find the very good solution in any setting of other parameters. It is shown in Table.1 that the algorithm has a very bad performance for high value of α .

And similar experiments were done in other TSP instances, and these results are presented in Table 2 and Table 3.

It is represented in the results of the experiments that a high value of α is harmful to obtain the optical solution and selecting proper combinations of α and β seems to be the first step to find the global best solution in the TSP.

3.2 Setting Rules of ρ

The pheromone decrease factor ρ controls the decay of the pheromone on edges. As it results in the graduate decrease of pheromone on paths which are not regularly traversed, the probability of choosing a better path will grow, and it allows the new, better information to guide the search as well. However, the selection to proper value of ρ is a hard work, for in different parameter settings, the proper value varies in a large scale. An example of the change is shown in Table 4. Different value of ρ results in different algorithm performance. Performance measures for each setting of parameters is averaged over 10 runs ($\alpha = 1.0$, $\beta = 5.0$ and $M_c = 1000$). The value of H_n indicates the number of runs in which the algorithm obtains the global optimization with the tour length of 424.87.

Table 4. Algorithm performance with different values of ρ in Oliver_30

ρ	H_n ($q_0=0.3$)	H_n ($q_0=0.6$)	H_n ($q_0=0.9$)
0.05	9	10	8
0.10	10	10	8
0.20	8	5	7
0.50	1	0	0
0.99	0	0	0

A summary of $\rho(0 < \rho < 1)$ can derive from the results above and *Global/Local Update Rule*, when $\rho \rightarrow 1$, great amounts of pheromone are evaporated in each building step and meanwhile the algorithm can hardly get the global best tour, however, when $\rho \rightarrow 0$, the condition is the opposite, the speed of pheromone evaporation becomes slower, and the algorithm has more chance to obtain the global best tour. As shown in Table 4, lower value of ρ results in lower probability of being rolling in local optimization and in this case the algorithm always can find the optimal tour. However, algorithm performances with the same ρ setting are different when they have different value of q_0 . At last, we must keep an eye on parameter q_0 during selecting proper value of ρ .

3.3 Setting Rules of q_0

Two building selection methods (max probability selection and roulette wheel selection) were adopted in the algorithm. It has been introduced previously that the value of factor q_0 and $(1 - q_0)$ indicates the probabilities of applying the two methods in the ACO algorithm. The algorithm performance of an example with different value of q_0 is shown in Fig.2.

It is illustrated in Fig.2 that the performance of applying two methods is better when $\alpha=1.0$, $\beta=2.0$ and $\rho=0.10$. In addition, the length of global best tour of Oliver_30 obtained by the algorithm is 424.87.

When $q_0=0.0$, the algorithm only uses the roulette wheel method to build tour. The tour length varies without tending toward a certain value (in other words, without a converging process) is shown in Fig.2 (a). The maximum probability method is the unique building tour method in Fig.2 (c), however, the global best tour is not obtained in this situation. In fact, the algorithm is rolling in local optimization. In Fig.2 (b), two building methods are applied at the same time, and the algorithm finds the best known tour during a convergence process. However, with different value of q_0 , the transformations of tour length are different.

The similar experiments were done in other TSP instances, for example, the instance att48, a 48 cities TSP problem, and in Table 5 more detail about difference between algorithm performances with different values of q_0 is shown, where $\alpha=1.0$, $\beta=2.0$ and $\rho=0.10$ and M_g is the min generation in which the algorithm gets the best tour of the iteration T_{iter} (not the global best).

As it is shown in Fig.2, and Table 5, the performance of applying single method in the algorithm is worse than applying both methods at the same time, and the selection of proper value of q_0 is significant to the performance of ACO.

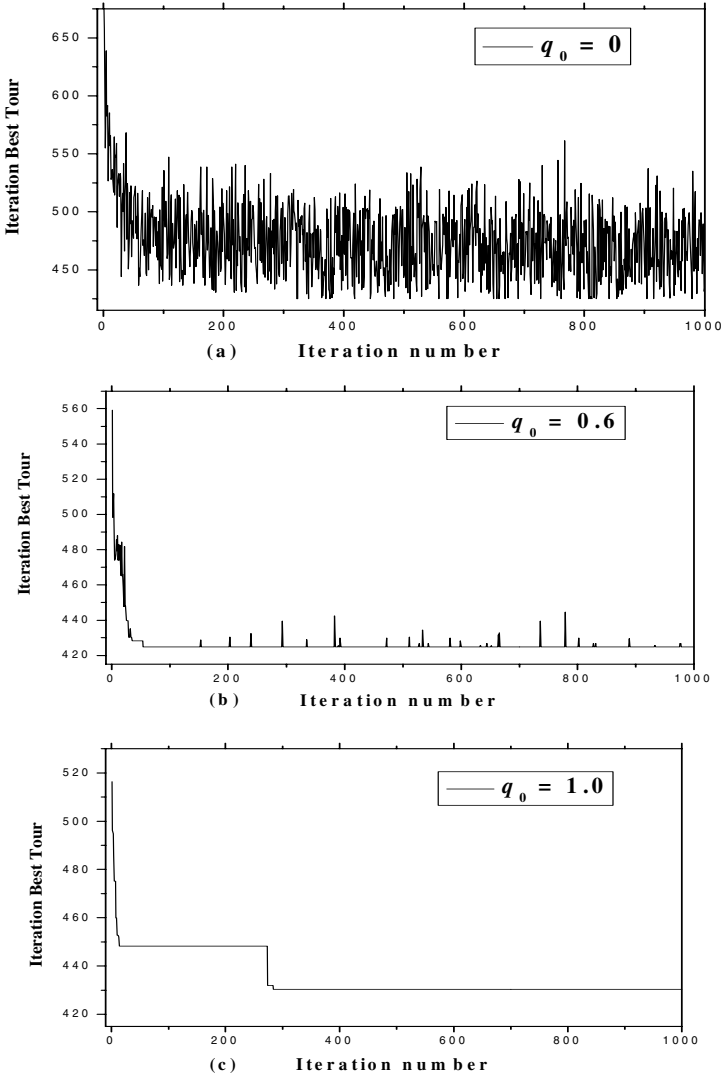


Fig. 2. The algorithm performance in Oliver_30 with different value of q_0 when $\alpha=1.0$, $\beta=2.0$ and $\rho=0.10$. Fig.2 (a) shows the optimization performance when the algorithm only used the roulette wheel method to build tour, Fig.2 (c) shows the performance when only the maximum probability method was used, while in Fig.2 (b) both method were used in the algorithm.

Assuming that there are some relations between q_0 and other parameters, we investigate the ACO behavior on Oliver_30 for different combinations of q_0 and other three parameters. Beside the episode to ρ , it is discovered that the β is more influential to the selection of q_0 . Results are shown in Fig.3, which are obtained by running the algorithm 100 times with $M_c=1000$ for each setting of the parameters.

Table 5. Different performances with different values of q_0 , when $\alpha=1.0$, $\beta=2.0$ and $\rho=0.10$. The results are averaged over 10 runs

	Oliver_30			att48		
	$q_0=0$	$q_0=0.6$	$q_0=1.0$	$q_0=0$	$q_0=0.6$	$q_0=1.0$
Best tour length	424.87	424.87	428.32	33600.56	33538.34	33695.50
M_g	322	57	295	350	105	170

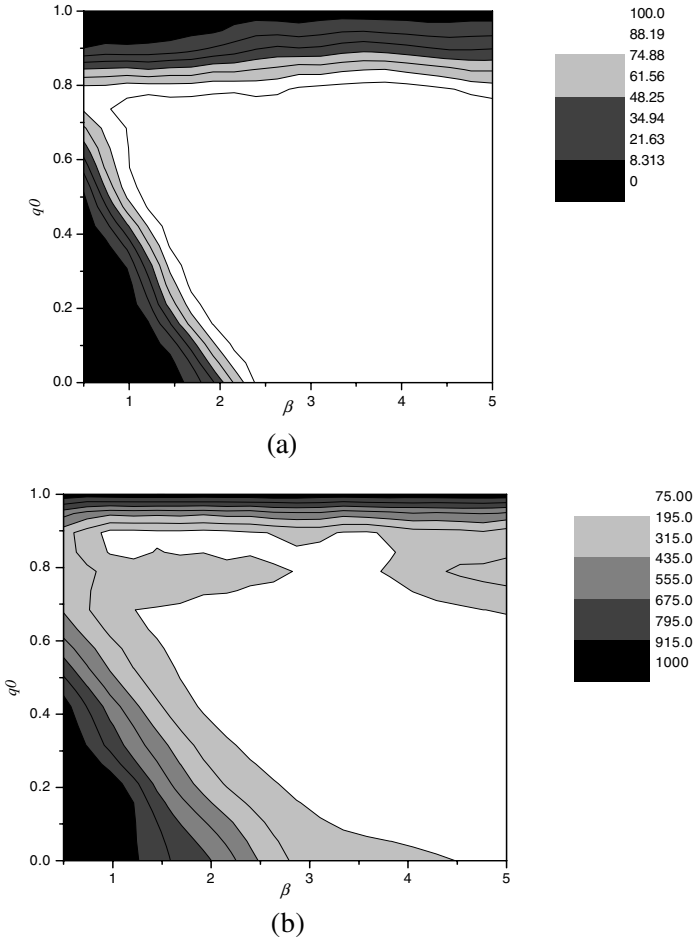


Fig. 3. Different values of M_g and H_n got with different combinations of β and q_0 in Oliver_30. Fig.3 (a) shows the different values of M_g got with different combinations of β and q_0 . M_g is the min generation in which the algorithm gets the best tour of the iteration T_{iter} . Meanwhile, Fig.3 (b) shows Different values of H_n got with different combinations of β and q_0 . H_n is the number of runs in which the algorithm obtains the global optimization.

M_g is the min generation in which the algorithm gets the best tour of the iteration T_{iter} . In Fig.3 (a), centered on the range $3 \leq \beta \leq 5$ and $0.3 \leq q_0 \leq 0.7$, the algorithm has a very well performance, for the global best tour can be obtained in less than 195 cycles. However, M_g increases from right to left as well as from bottom to top. It can be summarized that as the value of β grows, the feasible range of the value of q_0 outspread obviously. In the process, the probability of obtaining the global best tour when q_0 has a low value is growing. It means roulette wheel selection has a better performance in this condition.

In Fig.3 (b), it is shown that with the combinations of β and q_0 which locate in the white area, the ACO can obtain the global best solution for more than 88 times in 100 runs. H_n decreases from right to left as well as from bottom to top. The conclusion which is derived from Fig.3 (b) is as same as the one from Fig.3 (a). When $\beta \rightarrow 5$, the acceptable range of q_0 grows, and the algorithm performance for low value of q_0 becomes better indicating that the roulette selection method can perform more effectively in such condition.

4 Conclusion

The rule derived from the results of TSP instances can summarize as follows: First, select proper values of α and β at the beginning because some combinations of α and β are invalid to obtain the global best solution. In most experiments, the valid set of α is (1.0, 1.5). Second, the value of ρ can influence convergence rate. Don't select the value of ρ solely. For example, keeping an eye on the value of q_0 is necessary. Third, the performance of using two selection methods in the algorithm is better than using single one. And when $\beta \rightarrow 5$, the value of q_0 can be selected in a bigger range and it is shown that the roulette selection method is more effective during the process.

Future work will consider the parameters relation in other combination optimization problems, we also aim at extending our work to practical problems in the real world.

Finally, we aim to propose a universal rule of ACO depend on which can we select the proper value of parameters for other combinatorial optimization problems and to develop some ACO algorithms which can obtain better performance by modifying values of the parameters in the optimization process by themselves.

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Ant Colony System for Optimizing Vehicle Routing Problem with Time Windows (VRPTW)

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Abstract. Research on the optimization of Vehicle Routing Problem with Time Windows (VRPTW) is a significant investigation area of ant colony system (ACS). This paper proposes an enhanced ACS, which embeds the sequential insertion heuristic method, to solve VRPTW. The main idea is to organize two respective ant colonies to successively achieve a multiple objective minimization. Experiments on a series of benchmark problems demonstrate the excellent performance of ACS when compared with other optimization methods.

1 Introduction

Vehicle Routing Problem with Time Windows is a well known combinatorial optimization problem related to many real-life applications, especially in the field of industry. In the past few years, great efforts have been put forward to solve this kind of problems. In 2001, Arbelaitz *et al* [1] proposed a parallelizable system based on simulated annealing to solve VRPTW. The combination of simulated annealing and parallelizable makes a fast and low cost parallel system and is able to reach 85% of the optimal solutions for the Solomon's benchmark problems [1]. In 2004, a multi-agent model based on dynamic generation coalition was proposed, which shows an encouraging performance [2]. Besides, A. Lim *et al* focused their research on an even more restricted VRPTW, with the number of vehicles being constrained. They design an improved Greedy Randomized Adaptive Search Procedure (GRASP) framework. This framework, which embeds a technique of a smoothed dynamic tabu search, proves to be an effective method that outperforms many published algorithms in accuracy [3]. However, the first paper to introduce ACS to the solving of VRPTW appeared earlier than all the above work. In 1999, L. M. Gambardella *et al* presented a multiple ant colony system called MACS-VRTPW [4]. They reduce the complex VRPTW problem to the optimization of a multiple objective function. MACS-VRPTW organizes a hierarchy of artificial ant colonies, each of which uses independent pheromone trails but collaborate each other by exchanging information. Inspired by the idea of MACS-VRPTW, this paper presents an enhanced ACS model, which makes use of two ant colonies with respective goals. The sequential insertion heuristic method is also added

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to improve its performance. In addition, we use the Nearest Neighbor Heuristic (NNH) to generate the initial solution so that ants can start from a favorable beginning. Experimental results show that this ACS outperforms many published methods in solving the benchmark problems.

2 Ant Colony System for VRPTW

Like the neural network [5][6], ACS is a heuristic method derived from natural behaviors. The main idea of ACS is to have a set of ants search in parallel for solutions and cooperate through pheromone-mediated indirect and global communication [7]. This section gives the detailed descriptions of the proposed ACS for VRPTW.

2.1 Definition of Vehicle Routing Problem with Time Windows (VRPTW)

VRPTW represents an important component of many distribution and transportation system services. Accurately, VRPTW refers to a class of problems in which a set of routes for a fleet of vehicles based at a depot must be determined for n geographically dispersed customers. Let $C=\{1,\dots,n\}$ be a set of customers and 0 stands for the depot. Each customer c_i involves a service time S_i and asks for a quantity q_i of goods ($i=1,\dots,n$). Moreover, there is a time window $[b_i, e_i]$ during which c_i has to be served (with b_0 be the earliest starting time and e_0 the latest returning time of each vehicle). $V=\{1,\dots, t\}$ is a set of vehicles, each of which is associated with a capacity constraint Q . In addition, all the tours should begin at the depot and return to the depot.

2.2 Development of the ACS Model for VRPTW

The major goal of this elaborated ACS model is related to two objectives. We use two ant colonies to achieve this multiple objective minimization [4]. The first ant colony named ACS_vehicle is to minimize the vehicle number. The other one called ACS_time is to optimize the solution so that less traveling time is required.

2.3 Ants Search for Solutions in ACS_Vehicle

The ACS_vehicle colony, whose searching process is given in fig.1 (a), seeks for solutions by minimizing the vehicle number. It begins with an initial solution (possibly unfeasible), using one vehicle less than what the Nearest Neighbor Heuristic (NNH) requires. At the beginning, all ants set out from the depot. For ant k , it chooses the next customer according to the state transition rule (1).

$$D_{ij}^k = \begin{cases} j = \arg \max_{j \in \text{fea}[k]} ([\tau_{ij}][\eta_{ij}]^\beta), & \text{if } q \leq q_0 \\ \frac{[\tau_{ij}][\eta_{ij}]^\beta}{\sum_{t \in \text{fea}[k]} [\tau_{it}][\eta_{it}]^\beta}, & j \in \text{fea}[k], \text{ otherwise} \end{cases} \quad (1)$$

τ_{ij} is the amount of pheromone on edge (i, j) and η_{ij} is defined by equation (2). In equation (2), cur_time refers to when the current vehicle will finish serving customer i . $\max(cur_time+t_{ij}, b_j)$ is the time to serve j and thus $(\max(cur_time+t_{ij}, b_j)-cur_time)$

calculates the time span from now to when j begins to be served. ($e_j\text{-cur_time}$) is the measurement of the urgency of j to be served, indicating that those whose time window will expire soon will have the priority to be served first. IN_j is a variable to record the number of times that j fails to be inserted in each iteration [4]. The set $fea[k]$ records the current available customers.

$$\eta_{ij} = 1.0 / ((\max(\text{cur_time} + t_{ij}, b_j) - \text{cur_time}) * (e_j\text{-cur_time}) - IN_j) \quad (2)$$

Once the current vehicle can not serve more customers, ant k starts a new route by adding another vehicle, unless the allowed vehicle number has been reached. By repeatedly applying (1), ant k constructs a solution Ψ_k . Considering the vehicle number constraint and other restrictions, it is possible that not all customers are included in Ψ_k . The sequential insertion heuristic method is then added to help serve as more customers as possible [8]. If Ψ_k is a feasible solution, the allowed vehicle number will decrease.

2.4 Pheromone Updating Rules in ACS_Vehicle

The Local Updating Rule. This rule (3) is used to update the pheromone on the edge which has just been selected by an ant. τ_0 is the initial pheromone amount.

$$\tau_{ij} \leftarrow (1 - \rho) \cdot \tau_{ij} + \rho \cdot \tau_0 \quad (0 < \rho < 1) \quad (3)$$

The Global Updating Rule. This rule (4) is applied twice: one for the solution with the maximum goods and the other for the global best feasible solution [4].

$$\tau_{ij} \leftarrow (1 - \alpha) \cdot \tau_{ij} + \alpha \cdot \Delta\tau_{ij} \quad (4)$$

For the solution with the most goods, $\Delta\tau_{ij}$ is calculated by (5) where L_1 is the sum of distance of all the tours in the solution with the most goods.

$$\Delta\tau_{ij} = \begin{cases} (L_1)^{-1} & \text{if } (i, j) \in \text{the_most_goods_solution} \\ 0 & \text{otherwise} \end{cases} \quad (5)$$

Likewise, for the global best feasible solution, $\Delta\tau_{ij}$ is calculated by (6) where L_{gb} is the sum of distance of this solution.

$$\Delta\tau_{ij} = \begin{cases} (L_{gb})^{-1} & \text{if } (i, j) \in \text{global_best_solution} \\ 0 & \text{otherwise} \end{cases} \quad (6)$$

2.5 Ants Search for Solutions in ACS_Time

The colony of ACS_time is designed in the purpose of minimizing the total transportation time. This process is described in fig.1 (b). Considering that the length of the distance in a solution is proportional to that of the transportation time, we take the total distance of a solution to evaluate its quality. In this way, the searching process of

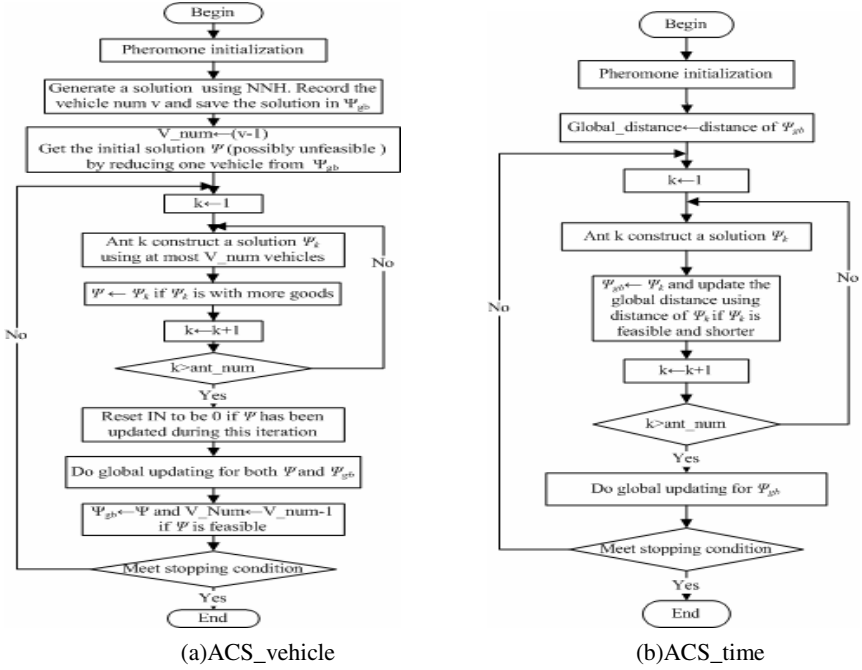


Fig. 1. Flow charts of the searching process for ACS_vehicle and ACS_time respectively

ACS_time is quite similar to that of the ant colony for solving the traveling salesman problem [7]. Therefore, ACS_time applies the same state transition rule and pheromone updating rules as those of the conventional ACS [7].

3 The Numerical Result of ACS for VRPTW

The proposed ACS for VRPTW has been tested on a set of benchmark problems, which are divided into three groups as *C*, *R* and *RC*. Group *C* consists of clustered customers whose time windows are generated based on a known solution. Group *R* have customers' location generated uniformly randomly over square. Group *RC* are combinations of randomly placed and clustered customers. The difference of these three types is the width of time windows for each customer.

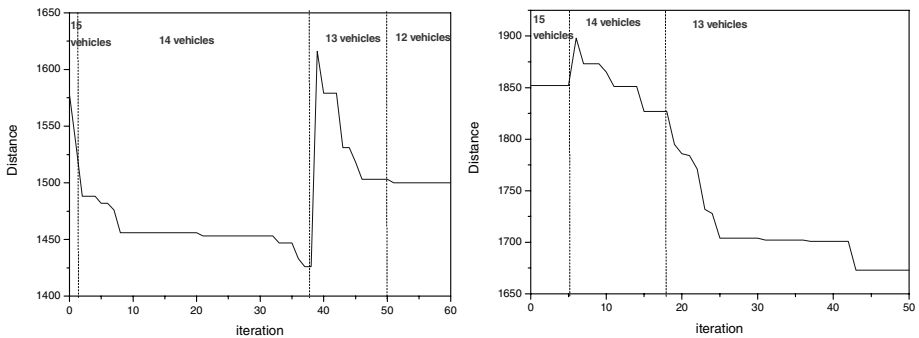
3.1 Results on Benchmark Problems

Table.1 shows some satisfying experimental results. Each test is performed 10 times. We can see that for R103, R104 and RC102, ACS requires less vehicles than all the listed algorithms while for C101, C107, R106 and RC101, it can obtain solutions almost close to that of the other algorithms.

Fig.2 shows the computing process in the respective tests for R103 and RC102, from which we can see the process of the total distance of the optimal solution against the iteration count. As the iteration increases, the vehicle number decreases. Moreover, during those iterations with the same vehicle number, the total distance decreases.

Table 1. The experimental results of ACS for some benchmark problems

Problem	Optimal Solution by other algorithms			Optimal Solution by ACS	
	Number	Distance	Author	Number	Distance
C101	10	828.94	RT [9]	10	833
C107	10	827.3	KDMSS [10]	10	837
R103	13	1292.68	LLH[11]	12	1500
R104	11	971.5	IV[12]	10	1217
R106	13	1234.6	CR[13]+KLM [14]	13	1259
RC101	15	1619.8	KDMSS [10]	15	1623
RC102	14	1457.4	CR[13]+KLM [14]	13	1673

**Fig. 2.** Schematic illustrations of the computing process for R103 and RC102 respectively

4 Conclusion

In this paper, an enhanced ACS is presented to solve the VRPTW. This ACS model makes use of two respective ant colonies which are designed to obtain respective goals. With the initial solution generated by the Nearest Neighbor Heuristic, ACS is able to start from a favorable beginning. In addition, the sequential insertion heuristic method is embedded as an auxiliary skill. An extensive computational study on a set of benchmark problems has been conducted and the experimental results show that the proposed ACS is competitive when compared with other methods.

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A Hybrid Particle Swarm Optimization for Binary CSPs

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Abstract. The target of solving constraint satisfaction problems(CSP) is to satisfy all constraints simultaneously. The CSP model is transformed into a discrete optimization problem with boundary constraints and is solved by particle swarm optimization(PSO) in this paper. To improve the performance of the proposed PSO algorithm, ERA(Environment, Reactive rules, Agent) model is used to proceed with local search after the process of boundary constraints. Further improvement including nohope and tabu list are also combined with PSO. When particles can not explore more search space, nohope is introduced to improve the activities of particles. Tabu list is used to avoid cycling in the global best particle. We experiment with random constraint satisfaction problem instances based on phase transition theory. Experimental results indicate that the hybrid algorithm has advantages on the search capability and the iterative number.

1 Introduction

Particle Swarm Optimization (PSO) is a stochastic search technique developed by Kennedy and Eberhart[1] based on the simulation of social behavior metaphor, which is inspired by the behavior of bird flocking and fish schooling. PSO exploits a population of potential solutions to probe the search space. It initializes the population with random candidate solutions, called particles. Each particle is assigned a randomized velocity and is iteratively moved through the search space. It benefits from the experience of its own and that of the other members of the population.

PSO is widely used as optimizer for nonlinear functions, many experimental results show that PSO is a excellent stochastic search method on numeric optimization problems. Recently PSO is proposed to solve constrained optimization

problems[2],[3],[4] and integer programming[5]. Discrete PSO is a variant of the basic PSO and is proposed to solve binary constraint satisfaction problems[7]. Constraint satisfaction problems are usually discrete. In this paper constraint satisfaction problems are modeled as discrete constrained optimization problems and are solved by non-discrete PSO.

The remainder of this paper is organized as follows: Section 2 provides a short overview of constraint satisfaction problem, outlining the basic concept of CSP and how it can be adapted to be solved by PSO. The hybrid methods of particle swarm to solve binary CSPs are introduced in Section 3. The hybrid methods include: handling boundary constraints with *Periodic* mode, rounding real value position to integer value, combining ERA model to particle swarm as a local search technique, adding nohope to increase the opportunity for searching and adding tabu list to prevent cycle in the search procedure. Some experimental results are given in Section 4. All instances used in our test are generated by random CSP model under phase transition theory, which are the hardest to be solved and become the baseline to evaluate the efficiency of a algorithm. Section 5 is the conclusion and future work.

2 Constraint Satisfaction Problem

Constraint Satisfaction Problems (CSPs) are the most exciting research area of artificial intelligence over last decades. In real life, many problems such as timetabling, resource allocation, planning, configuration, vision etc. can be modeled as some certain type CSPs. It is a powerful tool to model and to solve many kinds of combinatorial problems, which has attracted widespread commercial interest as well. Most of those combinatorial problems are NP-Complete in general.

Researching into solving CSPs has been lasted for a long time and can be classified as complete and incomplete, depending on whether they can find all solutions or find a random solution. complete algorithms can detect infeasibility but the computational cost is expensive for large problem instances. There are no polynomial algorithms to solve CSPs so far. The dominating idea is backtracking that explores the search space in a systematic and complete way. Backtracking finds values for variables subject to a set of constraints, which selects an unlabelled variable to instantiate each time. When the instantiated variable doesn't meet with the constraints, the algorithm backtracks to a suitable search point. Backtracking algorithm traverses the entire solution space to get solutions. Different complete directions of solving CSPs have been approached: finding the CSPs' solutions from the possible solution space[9], reducing a CSP to a simpler or equivalent problem[10], and synthesizing the CSPs' solutions from partial solutions[11]. The desirable features of system and completeness in backtrack search become intractable on hard combinatorial problems for the exponential time complexity. This is particularly true when the problem is huge and system reduction cannot reduce the problem enough to make complete search feasible.

Hence, incomplete search approaches have been proposed that leave out combinatorial explosion. Incomplete methods are much faster, but can not guarantee

finding solution within a limited amount of time or concluding the problem is infeasible. Incomplete methods in solving CSPs include: a number of local search approach, such as min-conflict heuristic[12], ERA model[13]; swarm intelligence based methods, such as ant colony optimization[6], discrete particle swarm optimization[7], genetic algorithm[8] etc.

A constraint network or Constraint Satisfaction Problem (CSP) is a triplet (X, D, C) , here $X = \{x_1, x_2, \dots, x_n\}$ is a set of Variables, which may take on values from a set of domains $D = \{D_1, D_2, \dots, D_n\}$, and a set of constraints $C = \{C_1, C_2, \dots, C_m\}$. A constraint C_i on the ordered set of variables $X(C_i) = (X_1, \dots, X_n)$ is a subset of the Cartesian product $D(X_1) \times \dots \times D(X_n)$ that denotes the compatible pairs of value for variable X_1, \dots, X_n . A binary constraint C_{ij} on variable X_i and X_j is a set of pairs, C_{ij} allows for X_i to take the value v_i and X_j to take the value v_j iff $(v_i, v_j) \in C_{ij}$ and we say the binary constraint is *satisfied* otherwise it is *violated*. We call a CSP binary constraint satisfaction problem iff all the constraints in CSP are binary constraints. A solution of a constraint satisfaction problem is an assignment of values to the set of X such that all the constraints are satisfied simultaneously.

In this paper, we formulate a CSP as a discrete constrained optimization problem with a goal of minimizing $f(x)$ subject to a set of constraints.

$$f(x) = \sum_{i=1}^{|C|} g(C_i) \quad (1)$$

$$\text{s.t. } g(C_i) = 0 \quad \forall i \in 1, 2, \dots, |C|$$

where $g(C_i) = 0$ if constraint C_i is satisfied, and $g(C_i) = 1$ if C_i is violated. if all constraints are satisfied, i.e. $f(x) = 0$, say a solution for the CSP is found. Now the main task is to solve the optimization problem, which is a more natural way for particle swarm optimization.

In the next section, particle swarm is adopted to solve the above CSP model and some additional techniques are combined with particle swarm to improve the performance.

3 Particle Swarm for Binary CSPs

Particle swarm is a general heuristic exploration technique which maintains a swarm of candidate solutions, referred to as *particle*. Particle swarm performs effective exploration through memory and feedback. Particles flow through hyper-dimensional search space, attracting towards the best position found by the neighborhood particle and the best historic position by themselves.

Assume that the search space is N-dimensional, i.e. the number of parameters the function being optimized, then the i-th particle in the swarm could be presented with a N-dimensional vector, $X_i = (x_{i1}, x_{i2}, \dots, x_{iN})$. The velocity of this particle can be presented as $V_i = (v_{i1}, v_{i2}, \dots, v_{iN})$. The best historic position visited by the i-th particle can be denoted as $P_i = (p_{i1}, p_{i2}, \dots, p_{iN})$. g is defined as the index of the best neighborhood. For the popular PSO, the main manipulation according to the following two equations:

$$v_{ij}^{t+1} = \omega v_{ij}^t + c_1 r_{1j} (p_{ij} - x_{ij}^t) + c_2 r_{2j} (p_{gj} - x_{ij}^t) \quad (2)$$

$$x_{ij}^{t+1} = x_{ij}^t + v_{ij}^{t+1} \quad (3)$$

where $i = 1, 2, \dots, S$, and S is the size of the swarm; $j = 1, 2, \dots, N$; $t = 1, 2, \dots$, is the number of iteration; ω is the inertia weight; c_1 and c_2 are acceleration coefficients; $r_{1j}, r_{2j} \sim U(0, 1)$.

The optimization model of equation 1 transforms the constraints in CSP model into variables of the optimization model. The original variables in CSP are encoded into the positions of the particles, and the dimension of the particle now is $|X|$. The number of constraints satisfied denotes the partial solution's size of CSP. More constraints are satisfied, nearer approaching global solution. Thus the formulation of $f(x)$ is a straightforward method to compute fitness for particle. When calculating the fitness of a particle, first the consistencies of all constraints are checked with the values of the current positions presented by CSP model's variables, then $f(x)$ is computed by these consistency to determine fitness. Usually particle swarm is used to solve continuous optimization problems while the typical CSPs are discrete, thus we need discretize the values of positions. Rounding off the real value into the nearest integer value as [5] did is adopted in this paper.

3.1 Constraint Handling Technique

Constraint process is the key point in solving constrained optimization problems. While PSO is a computational procedure without constraint process, something else may be adopted to do this operation when a PSO algorithm is used to solve constrained optimization problems. [14] grouped the constraint handling methods into four categories: preserving feasibility of solutions; penalty functions; making a clear distinction between feasible and infeasible solutions; and other hybrid methods. There have two kinds of constraint in equation 1. One is the relations existing among the value pairs. Since the target is to satisfy all constraints in CSPs. We treat these relations as variables of equation 1 and the number of constraint violations as the fitness of particles. Thus constraints in CSPs need not process directly. The other is boundary constraint. CSPs are usually boundary but PSO does not discuss the bounds of particles' positions. Extra technique is needed to process boundary constraints. The simplest way is truncation. A value is less than the minimal bound then we set the minimal bound to it, and a value is greater than the maximal bound we set the maximal bound to it. [2] proposed a *Periodic* mode technique to handle boundary constraints. Experimental results denote its effectiveness and we adopt it in our hybrid algorithm. The formulations are as follows:

$$x_i = \begin{cases} u_i - (l_i - x_i)\%s_i & \text{if } x_i < l_i \\ l_i + (x_i - u_i)\%s_i & \text{if } x_i > u_i \\ x_i & \text{if } x_i \in [l_i, u_i] \end{cases} \quad (4)$$

where $\%$ is the modulus operator, $s_i = u_i - l_i$ is the range of the i th dimension, l_i is the minimal bound, and u_i is the maximal bound.

After the process with *Periodic* mode, particles return to the feasible domain. Then ERA model can proceed with local search.

3.2 Velocity Transformation

The velocity of a particle is composed of three components: v^t , the velocity reserved last time; $p - x^t$ and $p_g - x^t$. The new velocity may a big value thus the result of the new position added by the old position and the new velocity may have large offset compares with the old position. The addition of a position and a new large velocity actually increases the chaos in the swarm and weaken the quality of the local search. To get more powerful global search capacity but not to decrease the solution quality reached by the local search, we transform the velocities into the interval $[-1, 1]$. The elements in a velocity is partitioned into two set, $Pos_v = \{v_{ij} | v_{ij} > 0, v_{ij} \in V_i, i = 1, 2, \dots, S, j = 1, 2, \dots, N\}$ and $Neg_v = \{v_{ij} | v_{ij} < 0, v_{ij} \in V_i, i = 1, 2, \dots, S, j = 1, 2, \dots, N\}$, where S is the population size and N is the dimension. Then the transformation formula is as follows:

$$v'_{ij} = \begin{cases} \frac{v_{ij}}{\sum_{k=1, v_{ik} \in Pos_v}^N v_{ik}} & \text{if } v_{ij} > 0 \\ \frac{v_{ij}}{\sum_{k=1, v_{ik} \in Neg_v}^N |v_{ik}|} & \text{if } v_{ij} < 0 \end{cases} \quad (5)$$

3.3 Hybrid ERA Model with Particle Swarm

ERA(Environment, Reactive rules, Agent) model[13] is similar to min-conflicts heuristic[12] though it is a distributed multi-agent system based on the theory of artificial life. Both of them are local search approach. Both of their search strategies are based on variables' conflicts. [13] compared ERA model with min-conflicts heuristic and pointed out the ERA model is superior to min-conflicts. In ERA, each agent represents a variable in CSP. Agents live in lattice environment, and sense the local and global information around them. The environment records agents' current state and computes the constraint violations for each value in the domains of all variables. each agent can only move within a row it located in and has predefined local reactive behaviors: *better_move*, *least_move* and *random_move*. Agents select them with some certain probability under the pressure of environment that based on constraint violations. *better_move* is to find a position with less violation number with a probability of *better_p*, *least_move* is to find the least violation number position with a probability of *least_p*, and *random_move* is to move randomly with a probability of *random_p*. *better_move* has less time complexity than *least_move* and may be more efficient at the early search stage. While obviously the *least_move* can accelerate convergence to local optima or global optima. *random_move* is a necessary technique to avoid getting stuck in local optima.

Three local behaviors have been analyzed in [13], and pointing out that maybe exist $random_p < better_p < least_p$ for general purpose. Their experiments also indicate $least_p / random_p = n$ (here n is the domain size of the specified problem) may be a good choice. We use this empirical setting for our test. From

the algorithmic description of the ERA it can be concluded that there exists a approximate formulation, namely $better_p + random_p + least_p = 1$. Thus if $better_p$ is specified, we can compute $random_p$ and $least_p$ with empirical approximate formulations:

$$random_p = (1 - better_p)/(d + 1) \quad (6)$$

$$least_p = random_p \times d \quad (7)$$

where d is the domain size of a constraint satisfaction problem (assuming all variables have the same domain size).

In this paper, ERA model is organized to carry out local search procedure after the update of particles' positions.

3.4 Further Improvement with Nohope and Tabu List

It is hard to find the solution when the particles wander about some local attractors. ERA model uses *random_move* to increase the opportunity to explore more search space. The similar mechanism is used in our algorithm by increasing the *random_p*. DPS redistributes all the particles in the search space while we only increase the probability of random selection on global best particle on consideration of performance. Thus it is a variant of nohope in our algorithm. Stochastic search algorithm may also repeatedly enter into the same state, i.e. particle swarm optimization find a position repeatedly. It is useless in the search procedure, especially after the nohope activity. We introduce a short tabu list to avoid cycling. Each time the global best position is recorded, and is compared with the elements in the tabu list after the specified times (we allow some repeat in searching procedure but a threshold is given). if the global best position already exists in the tabu list, nohope activates to increase the randomness. When the global best particle arrives at a new position (i.e. a less fitness it approaches) we add it into the tabu list. a first-in-first-out queue is used for tabu list in our algorithm and only global best particle uses nohope and tabu list.

The pseudocode of the entire hybrid algorithm is as follows:

```

main procedure
  initialize positions and velocities randomly with real number
  handle boundary constraints with equation 4
  ERA-LocalSearch with better move = 0.15
  evaluate fitness
  while(fitness != 0 and iteration < maxIteration) {
    update velocities with equation 2
    transform velocities
    update positions with equation 3
    handle boundary constraints with equation 4
    ERA-LocalSearch with better move = 0.15
    if(the gbest particle is stagnated for no-hope threshold times) {
      ERA-LocalSearch with better_move = 0.1
    }
    evaluate fitness
  }

```

4 Experimental Results

To compare the performance of hybrid PS algorithm with that of DPS proposed in [7] and ERA model (a multi-agent oriented stochastic search model), first we choose the Model E class with 15 variables and 15 domain elements as DPS did, and choose JavaCsp (JavaCsp is a random binary constraint satisfaction problem instance generator)¹ to generate instances. Model E has one parameter named p . The generation process is to select uniformly, independently and with repetition, $pd^2n(n-1)/2$ conflicts out of the $d^2n(n-1)/2$ possible, where d is the domain size and the n is the number of variables. In our observation, the phase transition point is approximately 0.31 in the development of JavaCsp. Thus we set parameter p at 11 values equals spaced between 0.21 and 0.31 instead of between 0.2 and 0.38. Random constraint satisfaction problem theories proved these values located in the *mushy region*, where interesting instances with few solutions can be sampled. Each value of p we sample 5 instances; each instance has at least one solution. In our test all algorithms stop when it has found a solution or when it has performed 10^6 evaluations in each case. 10^6 evaluations are considered no more solution can be found and are excluded from experimental results. 10 runs are performed for each instance. The experiments are made on PC(Intel Celeron CPU 1.8GHz, 512M RAM, Window XP SP2 and JDK 1.5).

Table 1. Comparison results with the success rate and the mean iteration of Model E class

p	ERA		DPS		HPS	
	succ.	mean iter.	succ.	mean iter.	succ.	mean iter.
0.21	50/50	5.7	50/50	102.84	50/50	3.4
0.22	50/50	13.7	50/50	2679.3	50/50	3.5
0.23	50/50	33.2	50/50	389.4	50/50	4.1
0.24	50/50	20.2	45/50	3344	50/50	6.9
0.25	50/50	41.8	45/50	8086.8	50/50	14.5
0.26	50/50	152.5	35/50	50057	50/50	28.1
0.27	50/50	183.8	35/50	42740.2	50/50	44.5
0.28	50/50	396.8	20/50	110818.6	50/50	110.7
0.29	50/50	564.1	15/50	77904.8	50/50	43.9
0.30	50/50	4377.4	0/50	–	50/50	485.4
0.31	50/50	53312.1	0/50	–	50/50	3390

The parameters of DPS in this test are set the quasi-optimal values described in [7]. Those values include: swarm size is 50, deflection = $2/n$, where n is the number of variables, $\varphi_1 = \varphi_2 = 1$. The parameter setting for ERA model has only one value to be tuned for experimental convenience, given by our experience, where *better move* = 0.15. We adapt the c source code from book "Swarm

¹ http://www.xs4all.nl/~bcraenen/JavaCsp/resources/javacsp_1.0.2.jar.

Intelligence” to Java version in our test². For our hybrid PSOs parameters, fixed values, consider as default, are used: $c_1 = c_2 = 2$; ω is gradually decreased from 0.9 but never below 0.4. V_{max} , to prevent the swarm from explosion, is still reserved in the newly developed algorithm. In our experiments V_{max} is always fixed, to the value of $V_{max} = 4$. the size of the swarm in our algorithm is set 10 instead of the DPS’s quasi-optimal parameter setting with 50. We also use the same parameter setting in ERA model to the hybrid particle swarm algorithm except for the nohope phase. In the nohope phase we give more random opportunity to the algorithm to get out of local optimum. The parameter change to *better move* = 0.1.

We test 11 instances with model E. All the 11 instances are solved by ERA and HPS but only 9 by DPS. When $p = 0.31$, i.e. p is near the phase transition point, the average iterations are increased with both ERA and HPS. But HPS reduces the iterations dramatically comparing with ERA both in the *mushy region* and at the phase transition point.

Table 2. Comparison results with the success rate and the mean iteration of partial instances generated by Model RB

<i>instances</i>	ERA		HPS	
	succ.	mean iter.	succ.	mean iter.
frb30-15-1.csp	3/10	265785	6/10	388744.7
frb30-15-2.csp	10/10	142236.6	10/10	23619.4
frb30-15-3.csp	0/10	–	1/10	481845
frb30-15-4.csp	10/10	77513	10/10	8913
frb30-15-5.csp	3/10	424908	10/10	170257.6
frb35-17-1.csp	0/10	–	1/10	679207
frb35-17-2.csp	0/10	–	2/10	457798
frb35-17-3.csp	1/10	797702	3/10	745382
frb35-17-4.csp	5/10	470313.2	9/10	289837.2
frb35-17-5.csp	1/10	534781	3/10	566332
frb40-19-1.csp	8/10	291275.4	10/10	156683.1
frb40-19-2.csp	2/10	496059	5/10	349026.2
frb40-19-3.csp	2/10	402676	3/10	552553.3
frb45-21-4.csp	0/10	–	1/10	167119

Further random constraint satisfaction problem theories are proved there exists exactly critical values at which the phase transitions occur. The hardest instances to solve are concentrated in the sharp transition region and become remarkable benchmark to evaluate the efficiency of the newly developed algorithms. These efforts result in the Model RB [15], the state of the art in random CSP Model theory, which is a revision to the standard Model B. Those studies also revise the drawback of Model E and produce in a simple model to generate

² <http://www.swarmintelligence.org/SIBook/cdos.zip>.

hard satisfiable instances[16]³. Now we use the benchmark problems generated from Model RB to test our algorithm⁴. In our experiments the repetitive constraint instances are omitted. The parameter setting unchange with the above setup. The DPS is completely defeated by these benchmarks and does not appear in the experimental results any longer.

In the test of 20 instances based on Model RB theory, ERA model can solve 10 instances while our hybrid particle swarm algorithm can tackle 14 instances. There are two instances with 40 variables and four instances with 45 variables are unsolved by the hybrid particle swarm algorithm. In the 14 instances, our hybrid particle swarm algorithm always has higher success rate on finding solutions and has less mean iterations for most instances comparing with ERA model.

5 Conclusion and Future Work

Backtracking is an ordinary way in solving constraint satisfaction problems, which selects an unlabelled variable to instantiate each time. When the instantiated variable doesn't meet with the constraints, the algorithm backtracks to a suitable search point. Backtracking algorithm traverses the entire solution space. The system and completeness in backtrack search become intractable on hard combinatorial problems for the exponential time complexity. This is especially true when the problem is huge and system reduction cannot reduce the problem enough to make complete search feasible. Particle swarm optimization is a global stochastic search technique and has excellent performance on continuous optimization problems. In this paper, CSPs are transformed into discrete constrained optimization problems and solved by PSO. Evidence denotes PSO for integer programming is superior to branch and bound but is not so good to discrete constrained problems in our experience. To improve the performance of pso for CSPs, ERA model is introduced as a local searcher in PSO. After the update of positions, ERA model is activated on rounded position to get better solution quality. Meanwhile nohope and tabu list are combined with PSO for avoiding sticking in the local optima and in the useless loop throughout the search procedure. Experimental results indicate the hybrid algorithm has advantages either on search capability or iterative number. The hybrid algorithm could reduce the iterative number dramatically on any instance generated by random constraint satisfaction problem generator developed based on phase transition theory and can find more solution on these instances. While we know some instances based on Model RB are not tackled yet and that is the effort in our further work.

³ <http://www.cril.univ-artois.fr/~lecoutre/research/tools/RBGenerator.jar>.

⁴ <http://www.nlsde.buaa.edu.cn/~kexu/benchmarks/benchmarks.htm>. or <http://www.cril.univ-artois.fr/~lecoutre/research/benchmarks/benchmarks.html#instances>. the former also includes the solved results comparison with CSP Solver Competition.

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A New Hybrid Algorithm of Particle Swarm Optimization

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Abstract. This paper presents a new hybrid algorithm of particle swarm optimization (PSO) called PSOSA, in which the mechanism of modified simulated annealing (SA) is embedded into standard PSO algorithm. The proposed algorithm not only keeps the characters of simple and easy to be implemented, but also enhances the ability of getting rid of local optimum and improves the speed and precision of convergence. The testing results of several benchmark functions with different dimensions show that the proposed algorithm is superior to standard PSO and the other PSO algorithms.

1 Introduction

Particle Swarm Optimization (PSO) was a swarm intelligence optimization which was proposed by Kennedy and Eberhan in 1995[1], [2], whose basic thinking was to find the optimal value through cooperation and sharing information among individuals of swarm. Compared with other optimizations, PSO is simple, high speed, large scope and easy to be implemented by programs. However, it is outstanding that it was easy to be got into local optimum. When the particle swarm was got into the local optimum, the particle swarm lost the ability of finding other optimal value. In order to overcome shortcoming of standard PSO, the many improved methods had been proposed [3]-[13]. Both Eberhart and Angeline conclude that hybrid models of the standard GA and the PSO could lead to further advances. In this paper, we present such a new hybrid model called PSOSA. The PSOSA model merges the modified simulated annealing (SA) into PSO, whose basic concept includes two steps: First, the standard PSO algorithm was performed for particle swarm. Afterwards, individual's own best position was taken as initial state variables for modified SA. The paper describes the new hybrid particle swarm optimization algorithm and compares it with the standard PSO and other PSOs.

2 Standard Particle Swarm Optimization

PSO simulates the behaviors of bird flocking and used it to solve the optimization problems. PSO is initialized with a group of random particles (solutions) and then

searches for optima by updating generations. In every generation, each particle is updated by following two "best" values. The first one is the best solution (fitness) it has achieved so far. This value is called *pbest*. Another "best" value that is tracked by the particle swarm optimizer is the best value, obtained so far by any particle in the population. This best value is a global best and called *gbest*. The velocity and positions of each particle is updated according to their best encountered position and the best position encountered by any particle with following equation.

$$v_{i+1} = w * v_i + c_1 * rand * (pbest - p_i) + c_2 * rand * (gbest - p_i). \quad (1)$$

$$p_{i+1} = p_i + v_{i+1}. \quad (2)$$

Where v_i is the particle velocity, p_i is the current particle position (solution), w is the inertia weight, the *pbest* and *gbest* are defined as stated before, *rand* is a random number between [0,1]. c_1 , c_2 are learning factors, usually $c_1 = c_2 = 2$. If the velocity is higher than a certain limit called V_{max} , this limit will be used as the new velocity for this particle in this dimension, thus keeping the particles within the search space.

3 Hybrid Algorithm of Particle Swarm Optimization (PSOSA)

When the optimal particle of particle swarm is got into local optimum, the particle swarm is very hard to jump out of the local optimum with standard PSO. The SA has the character of probability-sudden-jump so as to be able to jump out of the local optimum and approach the global minimum.

3.1 Simulated Annealing

Simulated Annealing (SA) was proposed by Metropolis in 1953 and Kirkpatrick successfully applied it in combined optimization in 1983 [13], which simulated the thermodynamics process of cooling of hot metal, that is, physical annealing process. It is able to jump out of the local optimum and approaches the global minimum whose essential reason is that it receives new state variable through probability judgment, which has been strictly proved in theory.

In order to find the optimal value, SA usually requires higher initial temperature, lower velocity of decreasing temperature, lower terminating temperature and enough samples in different temperature, so the process of SA is usually very long, which is the outstanding defect. In order to overcome this defect, the SA is modified below:

(1) The generator function of state variable take function express with Gaussian mutation as follows.

$$new_pbest_d = pbest_d * (1 + \eta * \sigma) \quad (3)$$

where σ is a random number with Gaussian (0,1) distribution. Thus it could not only produce the lesser disturbance scope with the bigger probability to perform local searching, but also appropriately produce the bigger disturbance scope to jump out of local optima. The initial value of η is set 1.0, $\eta = \eta(1-interdec)$, *interdec* is a small constant.

(2) In order to decrease the iterative times, the sample stable principle is revised, that is, the process ends once the function value of new state variable is better than that of last generation individual.

3.2 PSOSA Optimization Strategy

Obviously, the modified SA disables the condition of global convergence so that it is hard to ensure the algorithm can converge to the global minimum. The concept of combining PSO with SA proposed in this paper merges the SA which has the ability to get rid of local minimum so as to avoid the premature convergence in the process of optimization; meanwhile, the parallel sample process can raise the time performance of optimization. The steps of PSOSA are described as follows:

- Step 1:* Set initial parameters of PSO: learning factor: c_1 , c_2 ; swarm scale: m ; maximum evolution generations: \maxIter ; SA: $\maxN1$, $\maxN2$;
- Step 2:* Generate m particle swarms randomly and determine the initial temperature of SA, $temp = Temp0$;
- Step 3:* updated velocity and position of the particle swarm according to formula (1) and (2);
- Step 4:* If it meets the convergence condition, be over; else operate the modified SA on particle swarm:
- ```

while TrailN < maxN1
 for $j=1$ to SwarmSize
 while AcceptN < maxN2
 Perform mutation on the optimal position p_j of each
 individual of population according to formula (3).
 Calculating the fitness value new_fpbest of p_j .
 if $new_fpbest < fpbest$
 Renew the corresponding individual's own the best fitness
 $fpbest$ and position $pbest$, break;
 else if $\min\{1, \exp[-(fpbest - fbest)/temp]\} > \text{random}[0, 1]$,
 Renew the corresponding individual's own current fitness
 $fitnest$ and position p_j , break;
 end if
 AcceptN = AcceptN + 1;
 end while
 end for
 temp = temp * TempRatio;
 TrailN = TrailN + 1;
end while

```
- Step 5:* If reach the maximum evolution generations or getting a satisfying value, end the optimization, else turn to step 3.

In the above algorithm, linearly decreasing weight was used. The initial temperature of SA is determined by formula (4) according to the maximum fitness( $f_{worse}$ ) and minimum fitness( $f_{best}$ ) of initial swarm.

$$Temp0 = -(f_{worse} - f_{best})/\ln(Pr) \quad (4)$$

where  $Pr$  is also small constant seeing reference [13].

The PSOPA merges two different optimizations mechanisms into a whole which is in favor of enriching the search behavior during optimization process and enhancing the searching ability and efficiency in global and local. PSO enables SA to be parallel SA. Meanwhile, the SA enhances and complements the ability of PSO getting rid of local minimum, which avoid getting into local minimum and approach global minimum.

## 4 Experiments Setting and Results

For comparison, six benchmark functions that are commonly used in the evolutionary computation literature are used. All functions have same minimum value, which are equal to zero. The f0 and f3 are unimodal functions. The rest are multimodal functions.

The function f0 is the Sphere function:

$$f_0(x) = \sum_{i=1}^n x_i^2, x_i \in [-1000, 1000]. \quad (5)$$

The function f1 is the Rastrigrin function:

$$f_1(x) = \sum_{i=1}^n (x_i^2 - 10 \cos(2\pi x_i) + 10), x_i \in [-5.12, 5.12]. \quad (6)$$

The function f2 is the Griewank function:

$$f_2(x) = \frac{1}{4000} \cdot \sum_{i=1}^n x_i^2 - \prod_{i=1}^n \cos\left(\frac{x_i}{\sqrt{i}}\right) + 1, x_i \in [-600, 600]. \quad (7)$$

The function f3 is the Rosenbrock function:

$$f_3(x) = \sum_{i=1}^n (100(x_i^2 - x_{i+1})^2 + (1 - x_i)^2), x_i \in [-30, 30]. \quad (8)$$

The function f4 is the Ackley function:

$$f_4(x) = -20 \times \exp\left(-0.2 \sqrt{\frac{1}{n} \sum_{i=1}^n x_i^2}\right) - \exp\left(\frac{1}{n} \sum_{i=1}^n \cos(2\pi x_i)\right) + 20 + e, \quad (9)$$

$$x_i \in [-30, 30]$$

The function f5 is the Schaffer function:

$$f_5(x) = 0.5 + \frac{(\sin \sqrt{x^2 + y^2})^2 - 0.5}{(1.0 + 0.001(x^2 + y^2))}, x, y \in [-5.12, 5.12]. \quad (10)$$

For the purpose of comparison, we had 50 trial runs for benchmark functions above. The number of particle was set to 30. Three different dimensions of each function are used for comparison: 10, 20 and 30 (2 for Schaffer function). The goal value of Sphere, Rastrigrin, Griewank, Ackley and Schaffer functions were set to be 1.0e-10 and the goal value of Rosenbrock function was set to be 1.0e-6. For each algorithm, the maximum number of evaluations allowed was set to 300,000 (10,000 generations for PSO). Table 1 lists the Vmax values for all the functions, respectively. The acceleration constants were set as:  $c_1=c_2=2$ . The results for the benchmark functions are shown in table 2. In the table 2, the Avg/Std stands for average value and standard deviation of fitness value of 50 trail runs, the fevals stands for the average calculation times of function, Ras stands for the ratio of times of reaching goal value and the times of experiment. All results below  $10e-10$  were reported as '0'.

Figures 1–6 show typical convergence results of PSO and PSOSA. In each case it is seen that PSOSA performs better than PSO. On functions f0 and f4, there is almost a consistent performance pattern for both algorithm, they both converge

**Table 1.** Initial range of benchmark functions

| Function | Vmax | Function | Vmax |
|----------|------|----------|------|
| f0       | 1000 | f1       | 10   |
| f2       | 600  | f3       | 100  |
| f4       | 30   | f5       | 1    |

**Table 2.** The results of standard PSO and PSOSA

| Fun | Dim | StdPSO        |           |       | PSOSA             |           |       |
|-----|-----|---------------|-----------|-------|-------------------|-----------|-------|
|     |     | Avg/Std       | fevals    | Ras   | Avg/Std           | fevals    | Ras   |
| f0  | 10  | 0/0           | 140625.00 | 50/50 | 0/0               | 686.76    | 50/50 |
|     | 20  | 0/0           | 188412.00 | 50/50 | 0/0               | 718.56    | 50/50 |
|     | 30  | 0/0           | 221370.60 | 50/50 | 0/0               | 741.56    | 50/50 |
| f1  | 10  | 1.433/1.067   | 276194.40 | 12/50 | 0/0               | 365.22    | 50/50 |
|     | 20  | 11.860/4.644  | 300000    | 0/50  | 0/0               | 369.40    | 50/50 |
|     | 30  | 26.824/6.587  | 300000    | 0/50  | 0/0               | 385.76    | 50/50 |
| f2  | 10  | 0.062/0.024   | 300000    | 0/50  | 0/0               | 779.54    | 50/50 |
|     | 20  | 0.035/0.030   | 284053.20 | 7/50  | 0/0               | 800.18    | 50/50 |
|     | 30  | 0.016/0.018   | 269449.80 | 18/50 | 0/0               | 771.94    | 50/50 |
| f3  | 10  | 6.609/16.563  | 300000    | 0/50  | 3.22E-07/3.02E-07 | 194891.70 | 50/50 |
|     | 20  | 18.645/22.067 | 300000    | 0/50  | 3.29E-07/3.03E-07 | 354951.43 | 50/50 |
|     | 30  | 44.687/72.424 | 300000    | 0/50  | 4.02E-07/3.22E-07 | 356490.00 | 50/50 |
| f4  | 10  | 0/0           | 155889.00 | 50/50 | 0/0               | 612.34    | 50/50 |
|     | 20  | 0/0           | 207005.40 | 50/50 | 0/0               | 621.48    | 50/50 |
|     | 30  | 0/0           | 244439.00 | 50/50 | 0/0               | 621.80    | 50/50 |
| f5  | 2   | 0.0001/0.002  | 857.58    | 47/50 | 0/0               | 491.10    | 50/50 |

exponentially toward the fitness optimum. However the convergence speed of PSOSA is much faster than that of PSO. In experiments with the f1, f2 functions the PSOSA clearly performs best and it finds the global optimum in all cases, and the PSO could not find the global optimum except several times when the test function is of low dimensionality for f1 and higher dimensionality for f2. For function f3

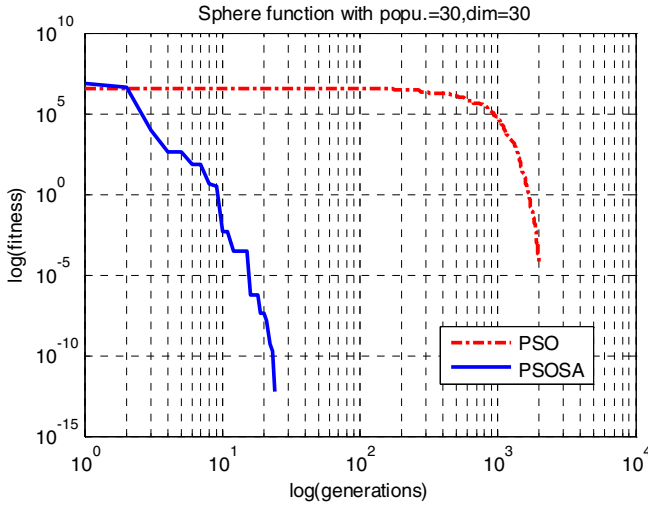


Fig. 1. Performance comparing of PSOSA and PSO on Sphere function

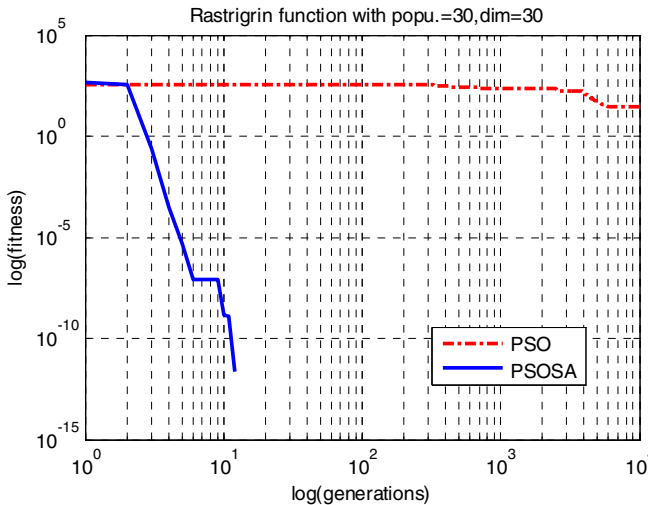


Fig. 2. Performance comparing of PSOSA and PSO on Rastrigrin function



PSOSA achieved the goal in any case, whereas PSO could not reach once. With function f5, PSO could not completely achieve the global optimum in all 50 runs. The stability of PSO is not good as PSOSA. By compare the results, it is easy to see that PSOSA have excellent performance. The performance of PSOSA is remarkably superior to PSO.

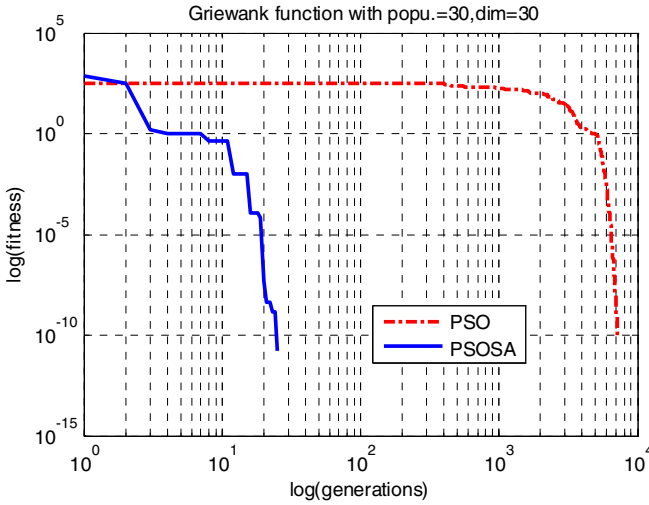


Fig. 3. Performance comparing of PSOSA and PSO on Griewank function

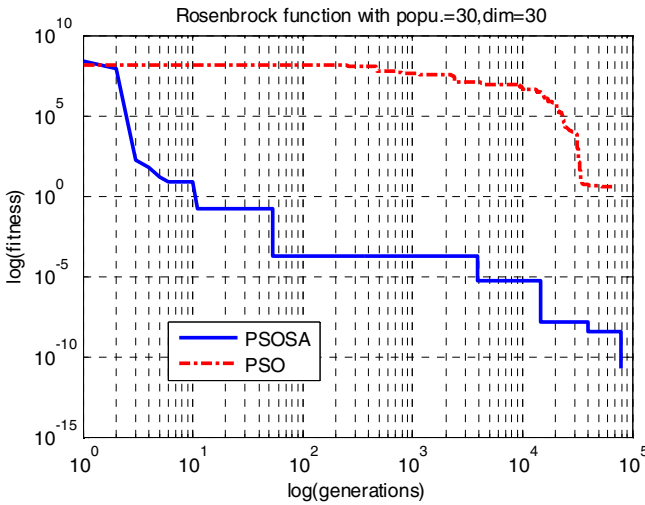


Fig. 4. Performance comparing of PSOSA and PSO on Rosenbrock function

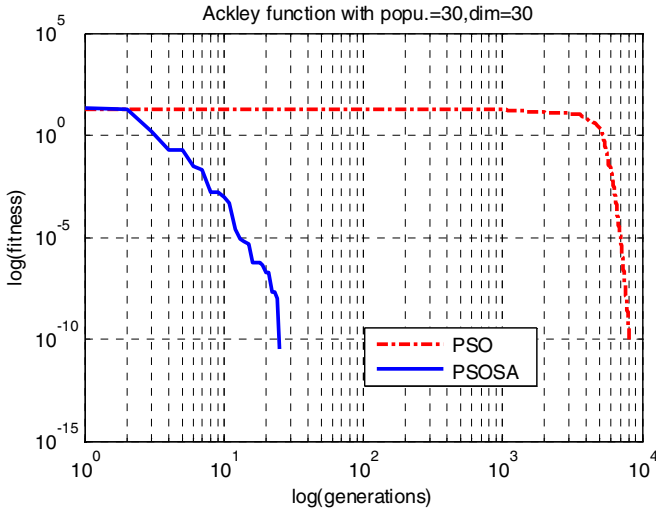


Fig. 5. Performance comparing of PSOSA and PSO on Ackley function

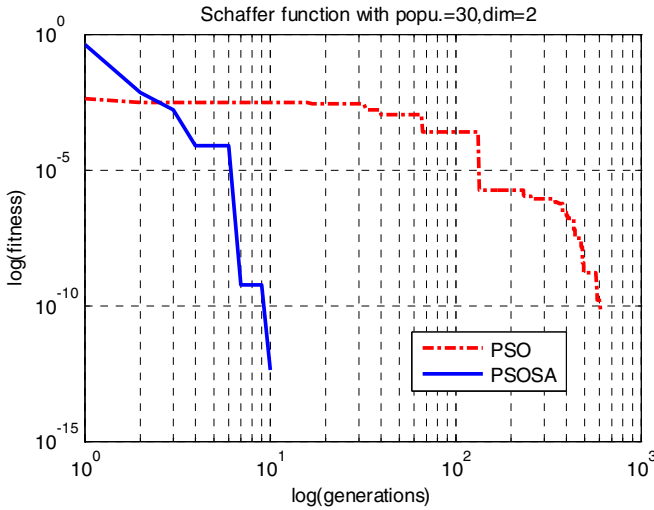


Fig. 6. Performance comparing of PSOSA and PSO on Schaffer function

## 5 Discussion

This paper has proposed a new particle swarm optimization algorithm called PSOSA. The implementation of this algorithm is simple based on SA. The new algorithm is shown to outperform PSO on all benchmark functions, being less susceptible to premature convergence, and less likely to be stuck in local optima. The many PSO algorithms about improvement of performance have recently been proposed by

researchers. Lovbjerg, Rasmussen, and Krink also proposed hybridizing the algorithm borrowing the concepts from Genetic Algorithms [7]. Table 3 lists a representative set of results from [7]. The table also lists the corresponding average best fitness of the PSOSA and the standard GA. To make a fair comparison, the maximum number of evaluations allowed was set to 20,000, 30,000 and 40,000 for PSOSA algorithm when the number of particle is set to 20. Note that the numerical value 0 was obtained under Matlab. The number of the parenthesis in table 3 represents evaluations achieving the goal value.

In experiments with the Sphere function the PSOSA achieved the global minimum and had much faster convergence than both the standard GA and the Hybrid model. The GA and the Hybrid model found similar values. With the Rosenbrock function, the PSOSA had a better performance than both the GA and the Hybrid model. The Hybrid model only had a fitness value which is obviously better than standard GA when the test function was of low dimensionality. When the dimensionality of the test functions was higher, the GA accomplished almost the same results as the Hybrid model. In the experiments with the Griewank function, the GA failed to achieve a reasonable result compared to the other models. The PSOSA model had a faster convergence than the Hybrid model and standard GA. In experiments with the Rastrigin function, the PSOSA model was better than both the standard GA and the Hybrid.

**Table 3.** Performance comparison between PSOSA and Hybrid and GA for benchmark functions

| function   | Dim | Gen. | PSOSA             | Std. GA             | Hybrid              |
|------------|-----|------|-------------------|---------------------|---------------------|
| sphere     | 10  | 1000 | 0 ± 0(14902.77)   | 2.43E-04 ± 1.14E-05 | 2.42E-04 ± 2.17E-05 |
|            | 20  | 1500 | 0 ± 0(14905.47)   | 0.00145 ± 6.22E-05  | 0.00212 ± 2.75E-04  |
|            | 30  | 2000 | 0 ± 0(14866.37)   | 0.00442 ± 1.78E-04  | 0.01203 ± 6.33E-04  |
| Rosenbrock | 10  | 1000 | 0.17856 ± 1.25988 | 109.810 ± 6.212     | 43.521 ± 16.047     |
|            | 20  | 1500 | 0.00043 ± 0.00111 | 146.912 ± 10.951    | 169.112 ± 21.535    |
|            | 30  | 2000 | 0.57431 ± 4.05976 | 199.730 ± 16.285    | 187.033 ± 22.960    |
| Griewank   | 10  | 1000 | 0 ± 0(651.57)     | 283.251 ± 1.812     | 0.09078 ± 0.03306   |
|            | 20  | 1500 | 0 ± 0(699.57)     | 611.266 ± 3.572     | 0.00459 ± 0.01209   |
|            | 30  | 2000 | 0 ± 0(703.90)     | 889.537 ± 3.939     | 0.09911 ± 0.00106   |
| Rastrigin  | 10  | 1000 | 0 ± 0(702.73)     | 3.1667 ± 0.2237     | 3.0599 ± 0.1535     |
|            | 20  | 1500 | 0 ± 0(777.10)     | 16.8732 ± 0.6007    | 11.6590 ± 0.3602    |
|            | 30  | 2000 | 0 ± 0(728.57)     | 49.3212 ± 1.1204    | 27.8119 ± 0.8059    |

There are many modified versions of PSO algorithms at present besides the Hybrid algorithm. Table 4 shows a comparison of the performances in the PSOSA model, the DPSO modal [5], HPSO modal [9] and AEPSo modal [12] with regards to the optimum found. In all algorithms, the size of particle was set to 20, the dimension of test functions was set to 30, and the maximum number of evaluations allowed was 120,000. These comparisons suggest that PSOSA outperforms many of the recent improved PSO algorithms.

**Table 4.** Performance comparison between PSOSA and other PSOs for benchmark functions

| Function   | Algorithm | Min     | Mean     | Deviation | Max      |
|------------|-----------|---------|----------|-----------|----------|
| Rosenbrock | DPSO      | 8.0e-02 | 34.02    | 35.10     | 1.4e+02  |
|            | HPSO      | 5.8e-02 | 1.1e+02  | 1.5e+02   | 7.2e+02  |
|            | AEPSO     | 2.8e-03 | 14.00    | 19.91     | 76.71    |
|            | PSOSA     | 7.6e-10 | 0.000031 | 0.000095  | 6.1e-004 |
| Griewank   | DPSO      | 4.4e-12 | 2.5e-02  | 3.0e-02   | 0.154    |
|            | HPSO      | 1.1e-16 | 1.5e-02  | 2.1e-02   | 8.5e-02  |
|            | AEPSO     | 0       | 1.2e-02  | 1.6e-02   | 6.6e-02  |
|            | PSOSA     | 0       | 0        | 0         | 0        |
| Rastrigin  | DPSO      | 7.2e-09 | 0.201    | 0.498     | 2.058    |
|            | HPSO      | 12.93   | 29.07    | 8.963     | 55.83    |
|            | AEPSO     | 0       | 0.577    | 1.084     | 3.980    |
|            | PSOSA     | 0       | 0        | 0         | 0        |

## 6 Conclusion

The paper proposes a new hybrid algorithm of PSO called PSOSA, which modify the SA and embedded it into the standard PSO so as to form a newly effective optimal algorithm. This algorithm not only keeps the characters of simple and easy to be implemented, but also strengthens the ability of getting rid of local optimum and raises the speed and accuracy of convergence. The testing results of typical benchmark functions with different dimensions demonstrate that the proposed algorithm is superior to particle standard PSO and other PSOs.

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# A Novel Particle Swarm Optimizer Using Optimal Foraging Theory

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**Abstract.** Based on the research of optimal foraging theory (OFT), we present a novel particle swarm optimizer (PSO) to improve the performance of standard PSO (SPSO). The resulting algorithm is known as PSOOFT that makes use of two mechanisms of OFT: a reproduction strategy to enhance the ability to converge rapidly to good solutions and a patch-choice based scheme to keep a right balance of exploration and exploitation. In the simulation studies, several benchmark functions are performed, and the performance of the proposed algorithm is compared to the standard PSO (SPSO). The experimental results show that the PSOOFT prevents premature convergence to a high degree, but still has a more rapid convergence rate than SPSO.

## 1 Introduction

In 1995, James Kennedy and Russell Eberhart applied Craig Reynolds's model to the problem of finding optima in a search space, which can be compared to a flock of birds looking for a food source, and created the PSO algorithm [1, 2]. Due to its simplicity in implementation and high computational efficiency in solving optimization problems, it has already come to be widely used in diverse scientific areas [3, 4].

However, it was pointed out that PSO usually suffers from premature convergence, tending to get stuck in local optima when strongly multi-modal problems are being optimized.

Various attempts have been made to improve the performance of basic PSO, which can be classified here as follows

- i. tuning the parameters in the velocity and position update equations of PSO[5, 6, 7]
- ii. designing different population topologies [8, 9, 10, 11]
- iii. combining PSO with other search techniques [12, 13,14]
- iv. incorporating bio-inspired mechanisms into the basic PSO[15, 16]
- v. utilizing multi-population scheme instead of single population of the basic PSO [17, 18, 19, 20]

Nature always presents us with a wide variety of simple biological models which have the bonus effect of increasing our knowledge of how to design more powerful

intelligent algorithm. Because the underlying idea of PSO is to mirror the social behavior of a flock of birds during the search of food, it is natural to think that if some biological models in optimal foraging theory can be employed to improve the performance of SPSO.

Optimal foraging theory formulates the foraging problem as an optimization problem and via computational or analytical methods can provide an optimal foraging “policy” that specifies how foraging decisions are made [21]. Based on the research of OFT, we introduce two biological-inspired mechanisms as a first approach to enhance exploration without hurting the ability to converge rapidly to good solutions. The first mechanism is based on an analogy with reproduction in nature and aims to enhance the ability of convergence rate. The second mechanism is based on a patch choice scheme found in animal groups, where the particles (birds) are attracted to the position of the best particle with a predefined probability and simultaneously migrate to other place in the searcher domain with another predefined probability.

We compare the performance of PSOOFT to that of the SPSO. In the next section the SPSO is reviewed. Description of the proposed algorithm PSOOFT is given in section 3. Next, experimental settings and experimental results are given in section 4. Finally, section 5 concludes the paper.

## 2 Review of Standard PSO (SPSO)

Similar to some evolutionary computation techniques such as genetic algorithms (GA) and evolutionary strategy (ES), PSO is a population-based stochastic optimization technique that belongs to the category of swarm intelligence [4] method. Although PSO bears some resemblances to evolutionary computation techniques, some evolution operators such as crossover, mutation and selection are not performed in PSO.

In PSO, the potential solutions, called particles, fly in a  $D$ -dimension search space with a velocity that is dynamically adjusted according to its own experience and that of its neighbors. The  $i$ th particle is represented as  $\vec{x}_i = (x_{i1}, x_{i2}, \dots, x_{iD})$ , where  $x_{id} \in [l_d, u_d]$ ,  $d \in [1, D]$ ,  $l_d, u_d$  are the lower and upper bounds for the  $d$ th dimension, respectively. The velocity for particle  $i$  is represented as  $\vec{v}_i = (v_{i1}, v_{i2}, \dots, v_{iD})$ , which is clamped to a maximum velocity vector  $\vec{v}_{\max}$ . The best previous position of the  $i$ th particle is recorded and represented as  $P_i = (P_{i1}, P_{i2}, \dots, P_{iD})$ , which is also called *pbest*. The index of the best particle among all the particles in the population is represented by the symbol  $g$ , and  $P_g$  is called *gbest*. At each iteration step  $t$ , the particles are manipulated according to the following equations:

$$v_i(t+1) = v_i(t) + R_1c_1(P_i - x_i(t)) + R_2c_2(P_g - x_i(t)). \quad (1)$$

$$x_{id} = x_{id} + v_{id}, \quad i = 1, 2, \dots, S \text{ and } j = 1, 2, \dots, D. \quad (2)$$

where

- $S$  number of particles;
- $D$  number of dimensions in a particle;
- $w$  inertia weight;
- $c_1, c_2$  acceleration constants;
- $R_1, R_2$  random vectors with components uniformly distributed in  $[0, 1]$ .

Shi and Eberhart [5] later introduced an inertia term  $w$  by modifying (1) to:

$$v_i(t+1) = w \times v_i(t) + R_1c_1(P_i - x_i(t)) + R_2c_2(P_g - x_i(t)). \quad (3)$$

They proposed that suitable selection of  $w$  will provide a balance between global and local explorations, thus requiring less iterations on average to find a sufficiently optimal solution. As originally developed,  $w$  often decreases linearly from about 0.9 to 0.4 during a run. In general, the inertia weight  $w$  is set according to the following equation:

$$w = w_{\max} - \frac{w_{\max} - w_{\min}}{iter_{\max}} \times iter. \quad (4)$$

where

- $w_{\max}$  the initial weight;
- $w_{\min}$  the final weight;
- $iter$  the current iteration number;
- $iter_{\max}$  the maximum number of allowable iterations.

### 3 A Novel PSO Based on Optimal Foraging Theory

#### 3.1 Optimal Foraging Theory (OFT)

Animals as a group are what we call ingestive heterotrophs, which means they are unable to produce their own food and they must eat things to get nutrition. Obviously getting food is one of the most important and basic needs common to all animals, second only to reproduction. If successful reproduction is the ultimate destination of animals, then food is the fuel that allows the animal to reach its destination. Foraging behavior of animals has received much attention from behavioral biologists, on both empirical and theoretical grounds.



Foraging theory [21, 22] is based on the assumption that animals search for and obtain nutrients in a way that maximizes their energy intake  $E$  per unit time  $T$  spent foraging. Hence they try to maximize a function like  $E/T$ .

Maximization of such a function provides nutrient sources to survive and additional time for other import activities such as mating and reproducing. Successful foraging behaviors promote survival of foragers. On the other hand, animals that have poor foraging strategies will be eliminated by natural selection.

For many animals, nutrients are distributed among patches, e.g., a dike with rice paddies, a bush with berries and a group of trees with fruit. Foraging involves two essential decisions. The first is whether to enter a patch and search for food, and the second is to judge whether to continue searching for food in the current patch or to pursue alternative patches with more profitable nutrients than the current patch.

### 3.2 PSOFT

Because the main concept of the PSO is to mimic the behavior of a swarm which search for food resources on a field, it is therefore natural to ask if optimal foraging theory can be employed to improve the performance of SPSO. Inspired the research discussed above, we found that two aspects of OFT is suitable to be incorporated into the SPSO model.

**Table 1.** Procedure for the implement of patch choice scheme

---

|                                                                                                                                                                                                                                                                                   |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Step 1: Search within neighborhood of the birds' previous best positions with probability $PC$                                                                                                                                                                                    |
| Step 1.1: Select the original top $SR$ individuals used for chaotic local search.<br>Set $k = 0$ , and the maximum chaotic iteration $K$ ;                                                                                                                                        |
| Step 1.2: For each individual, generate an initialized $D$ -dimensional vector<br>$z^0 = [z_1^0, z_2^0, \dots, z_D^0]$ , $z_d^0 \in (0, 1)$ and that $z_d^0 \notin \{0.25, 0.5, 0.75\}$                                                                                           |
| Step 1.3: Determining the chaotic variables for the next iteration using:<br>$z_i^{k+1} = uz_i^k (1 - z_i^k)$ ( $i = 1, 2, \dots, SR, u = 4$ ).                                                                                                                                   |
| Step 1.4: Do the local search within the neighborhood of the current best position of the birds according to $X_i^{k+1} = pbest_i + \alpha_i(2z_i^{k+1} - 1)$ . $\alpha_i$ is the radius of the local search and 0.1 that of the given value range of the corresponding variable. |
| Step 1.5: Evaluating the new solution with $X_i^{k+1}$                                                                                                                                                                                                                            |
| Step 1.6: For each bird, update $pbest$ when the new solution is better than it; let $k = k + 1$ and go back to Step 1.1.                                                                                                                                                         |
| Step 1.7: Terminate if the maximum chaotic iteration is reached.                                                                                                                                                                                                                  |
| Step 2: Migrate to other palace in the searcher domain with probability $1 - PC$<br>$X_i = rand(S, D) * (u_d - l_d) + l_d$ .                                                                                                                                                      |

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**Table 2.** The pseudo code for PSOFT

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Initialize step: Set  $S, D, u_d, l_d, c_1, c_2, w_{\max}, w_{\min}, NR, PC, K$ . Random generate  $X_0^d \in D$  in  $R^n$ , and  $V_0^d \in [0, V_{\max}]$   $d = 1, 2, \dots, D$

Set  $k := 0$

While (the termination conditions are not met)

**FOR** (each particle  $i$  in the swarm)

**Calculate fitness:** calculate the fitness value of current particle:  $F(X_i)$

**Update  $pbest$  and  $gbest$ :** compare the fitness value of  $pbest$  with  $F(X_i)$ . If  $F(X_i)$  is better than  $pbest$ , then set the  $pbest$  to the current position  $X_i$ ; Further more, if  $F(X_i)$  is better than  $gbest$ , the reset  $gbest$  to the current index in particle array

**Update the velocity and positions:** calculate velocities  $V_i$  and position  $X_i$  using Eq.1. and Eq.2, respectively

**Limit the velocity:** If  $V_i > V_{\max}$  then  $V_i = V_{\max}$ . If  $V_i < V_{\min}$  then  $V_i = V_{\min}$

**Reproduce particles:** If  $Mod(k, Nr) = 0$ , sort particles fitness value in order. The  $SR$  particle with higher values die and the other  $SR$  particle with the best value split (and the copies that are made are placed at the same location as their parent).

**Select Patch:** If  $rand < PC$ , Step 1 is performed, Otherwise Step 2 is performed.

**END FOR**

Set  $k := k + 1$

**END WHILE**

---

### A. Reproduction

The birds incorporate some kind of pressure towards successful behavior, that is, birds that reach valleys must have some kind of reproductive reward, by generating more offspring-or by simply having a higher probability of generating offspring in each time step (suppose that the swarm is requested to find the lower values of one complex function).

After a given time step  $NR$ , a reproduction step is taken. Suppose that the population size is  $S$ . Let  $SR = S/2$  be the number of population members who have had sufficient nutrients so that they will reproduce.

This reproduction procedure is performed as follow. The birds in the population are sorted in ascending order according to the value of the fitness function. Under this way, the population is divided into healthy part and unhealthy part, in which the  $SR$  birds with relatively lower fitness value are regarded as healthy one and possess the opportunity to reproduce, while the  $SR$  birds with higher fitness value indicated that they did not get as many nutrients during their lifetime of foraging and hence are unhealthy and thus unlikely to reproduce; then the  $SR$  unhealthy birds die and the

other *SR* healthiest birds each split into two young birds, under this way the positions and velocities of the *SR* unhealthy birds is replaced by the *SR* healthy birds. It should be stressed that the personal best information associated with each of the birds is remained unchanged.

### B. Patch Choice

To better understand how the patch choice model is incorporated in PSO, consider the following scenario: a group of birds are randomly searching food in an area. There are some pieces of food in the area being searched and only one piece of food is with more nutrients.

Suppose that  $X$  is the position of a bird and  $F(X) X \in R^D$  represents how much nutrients substances it get. Hence *pbest* can be regarded as the previous position of the pieces of food searched by the birds and *gbest* is the position where the best nutrients patch has been found. In each iteration time, the top *SR* healthy birds among the swarms search for the nearest resource within neighborhood of their previous best positions with probability  $PC$ , and migrate to other palace in the searcher domain with probability  $1-PC$ .

Because the underlying concept of chaotic local search [23] is similar to the bird's local search scheme, it was adopted to mimic the implement of the bird's local search around the neighborhood of the patches.

The procedure for the implement of patch choice model is described as Table 1. The overall procedure of PSOOFT is shown in Table 2.

## 4 Experiment and Result

In this section, six nonlinear benchmark functions that are commonly used in evolutionary computation literature [24, 25] are performed. The first two are unimodal while the latter three are multimodal with many local minima. They are listed in Table 3.

**Table 3.** Test functions

|            |                                                                                                                                                 |
|------------|-------------------------------------------------------------------------------------------------------------------------------------------------|
| Sphere     | $f_1(x) = \sum_{i=1}^D x_i^2$                                                                                                                   |
| Rosenbrock | $f_2(x) = \sum_{i=1}^D 100 \times (x_{i+1} - x_i^2)^2 + (1 - x_i)^2$                                                                            |
| Rastrigrin | $f_3(x) = \sum_{i=1}^D (x_i^2 - 10 \cos(2\pi x_i)) + 10$                                                                                        |
| Griewank   | $f_4(x) = \frac{1}{4000} \sum_{i=1}^D x_i^2 - \prod_{i=1}^D \cos\left(\frac{x_i}{\sqrt{i}}\right) + 1$                                          |
| Ackley     | $f_6(x) = -20 \exp\left(-0.2 \sqrt{\frac{1}{30} \sum_{i=1}^D x_i^2}\right) - \exp\left(\frac{1}{30} \sum_{i=1}^D \cos 2\pi x_i\right) + 20 + e$ |

For comparison, both the SPSO and PSOFT were tested on those benchmark functions, when minimization was the focus.

The size of the population used for each problem as well as the initial hypercube into which the initial population was randomly taken, are presented in table 4.

The SPSO and PSOFT parameters were set to the values  $c_1 = c_2 = 2$ , and a linearly inertia weight starting at 0.9 and ending at 0.4 was used. The maximum velocity of each particle was set to be half the length of the search space in one dimension. In addition, for PSOFT the parameter  $NR, PC, K$  are set as 20, 0.8, 1000, respectively. A total of 50 runs for each experimental setting are conducted.

The experiment results (i.e. the best, worst, mean and standard deviation of the function values found in 50 runs) for each algorithm on each test function are listed in Table 5. From the values in table 5 we can conclude that the results obtained by PSOFT are clearly better for all the test functions. Furthermore, with the PSOFT concept, the standard deviation of the final solution for 50 trials was found to be significantly low for each function, which demonstrated the results generated by PSOSOT is more robust than that obtained by SPSO.

**Table 4.** Parameters of the test functions

| Test Problem | Dim. | Popul. Size | Initial Hypercube        |
|--------------|------|-------------|--------------------------|
| Sphere       | 30   | 40          | [50,100] <sup>n</sup>    |
| Rosenbrock   | 30   | 40          | [15,30] <sup>n</sup>     |
| Rastrigrin   | 30   | 40          | [2.56,5.12] <sup>n</sup> |
| Griewank     | 30   | 40          | [300,600] <sup>n</sup>   |
| Ackley       | 30   | 40          | [16,32] <sup>n</sup>     |

**Table 5.** Comparison between PSOFT and PSO

| Algorithm  | Mean         | Worst       | Best        | Stddev      |
|------------|--------------|-------------|-------------|-------------|
| Sphere     |              |             |             |             |
| SPSO       | 1.9909e-005  | 5.9520e-005 | 4.2271e-006 | 1.9601e-005 |
| PSOFT      | 1.0452e-049  | 1.0452e-048 | 6.3415e-089 | 1.0925e-049 |
| Rosenbrock |              |             |             |             |
| SPSO       | 3.7921e+002  | 2.6053e+003 | 1.5444e+001 | 7.5566e+002 |
| PSOFT      | 2.8.428e+001 | 2.8820e+001 | 2.7832e+001 | 3.2630e-001 |
| Rastrigrin |              |             |             |             |
| SPSO       | 5.0301e+001  | 8.5576e+001 | 2.5870e+001 | 1.2516e+001 |
| PSOFT      | 3.0516e+000  | 5.0148e+000 | 1.0102e+000 | 2.3450e-001 |
| Griewank   |              |             |             |             |
| SPSO       | 2.1100e-002  | 1.713e-001  | 3.5229e-006 | 4.0300e-002 |
| PSOFT      | 1.7325e-005  | 6.7082e-004 | 1.3245e-006 | 9.8268e-005 |
| Ackley     |              |             |             |             |
| SPSO       | 1.98091e+001 | 2.1015e+001 | 8.600e-003  | 3.9017e+000 |
| PSOFT      | 1.8285e-008  | 8.2331e-007 | 1.5637e-10  | 1.1653e-007 |

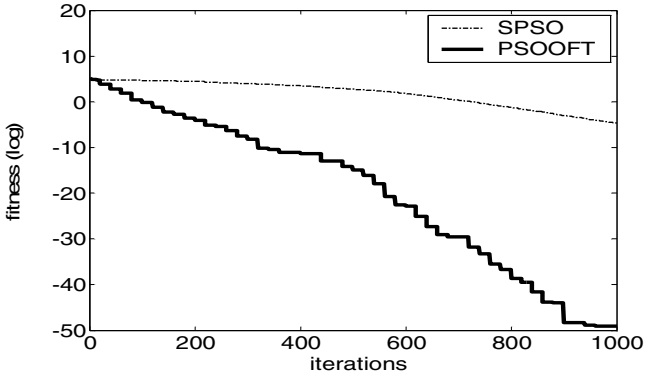


Fig. 1. Mean relative performance for Sphere function

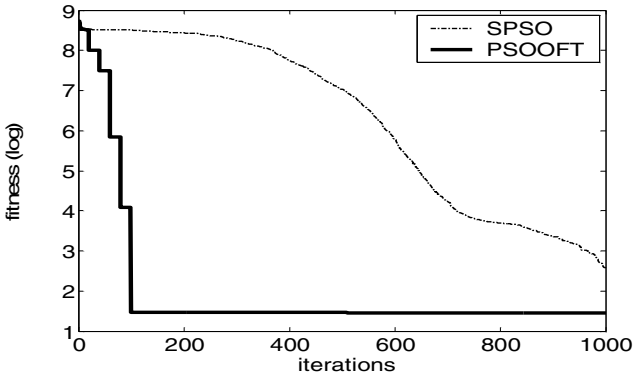


Fig. 2. Mean relative performance for Rosenbrock function

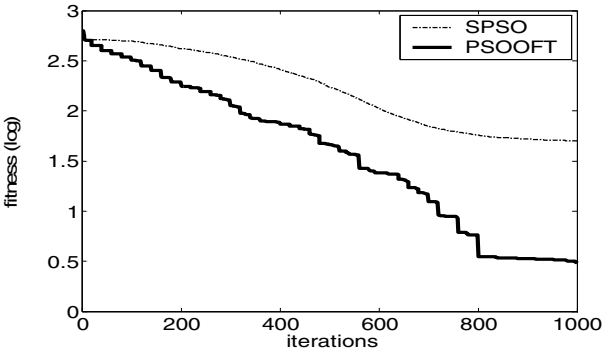
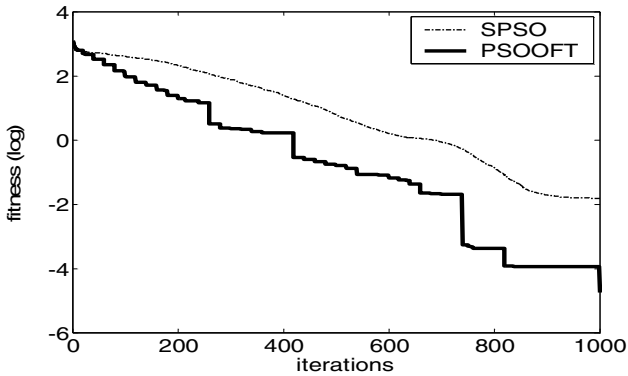
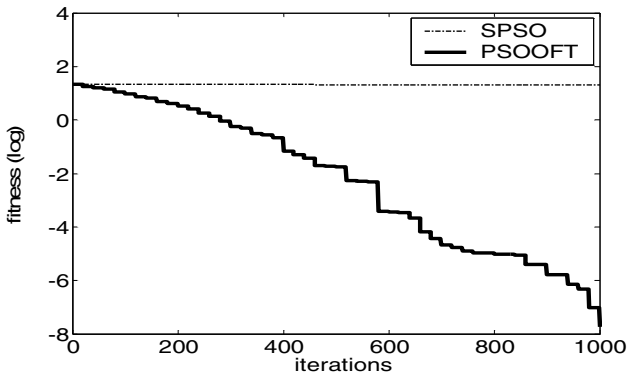


Fig. 3. Mean relative performance for Rastrigrin function



**Fig. 4.** Mean relative performance for Griewank function



**Fig. 5.** Mean relative performance for Ackely function

The graphs presented in Figs.1-5 illustrated the evolution of best fitness for both algorithms, averaged for 50 runs of each algorithm. In a general analysis of the graphs in Figs.1-5 we can see it clearly PSOFT converged faster and to a better value than the SPSO for all the test cases. The experiment with Ackley function illustrated this point very clearly. For SPSO there was almost no progression after the first 100 iterations, PSOFT kept improving the best fitness in the swarm until the end of each run.

## 5 Conclusions and Future Work

Based on the research of Optimal Foraging Theory, two biological-inspired mechanisms (reproduction and patch choice) are introduced into SPSO and thus a novel particle swarm optimizer is presented. The resulting algorithm is referred to as PSOFT, with the reproduction mechanism being the main responsible for the improvement of convergence rate, while the patch choice scheme clearly helped the algorithm escape local minima and yield promising results. A set of 5 benchmark

functions has been used to test the performance of PSOOFT in comparison with SPSO. The performance comparisons indicate that PSOOFT is superior to SPSO in both solution quality and convergence rate.

PSO is a relatively new optimization technique and there is plenty of space for possible improvements. Our future work will continue to develop new PSO variants to improve its performance, in particular by incorporated some biological-inspired models into the basic PSO. In addition, some extensive application on more complicated practical optimization problems will be performed to illustrate those new PSO variants. The authors invite any comments on this paper to be sent to the first author.

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# A Smart Particle Swarm Optimization Algorithm for Multi-objective Problems

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**Abstract.** Maintaining the diversity and convergence of Pareto optimal solutions is a desired task of optimization methods for multi-objective optimization problems(MOP). While accelerating the computing speed is important for algorithms to solve real-life MOP also. A Smart Particle Swarm Optimization algorithm for MOP(SMOPSO) is proposed. By setting the cooperative action of all the objective functions as the global best guide of swarm and selecting the closest or farthest archive member as the personal best guide of each particle, the SMOPSO method can find many Pareto optimal solutions in less iteration steps. Three well-known test functions have been used to validate our approach. Results show that the SMOPSO method is available and rapid.

## 1 Introduction

Problem with multiple objectives are present in a great variety of real-life optimization problems[1]. Since different objectives may be conflict with each other, multi-objective optimization problems(MOP) often have no unique optimal solution. Indeed the goal of MOP is to find a set of equilibrium solutions in one simulation run, which called Pareto-Optimal solutions, in stead of a single optimal solution. Evolutionary algorithms(EA) have proved very efficient in solving multi-objective optimization problems[2]. Different from evolutionary computation techniques, nowadays a new algorithm called Particle Swarm Optimization(PSO), is motivated from the simulation of insects and animals social behavior. A PSO consists of a population of particles, which on the contrary to evolutionary algorithms, survive up to the last generation[7]. Particles in the swarm search the variable space by moving with a special speed toward the best position using their experience from the past generations and communication among particles. PSO algorithm has proved very efficient in solving a number of problems in science and engineering.

Recently, investigators are paying more and more interest on PSO to solve MOP[1,2,3,4,7,6,7,8,9]. Change a PSO to a multi-objective PSO(MOPSO) requires a redefinition of what a guide is in order to obtain a front of optimal solutions[4]. Researchers proposed different strategies to find the best global guide for each particle, such as dynamic neighborhood[3], dominated tree[6], sigma dominance approach[7,8,9], a grid method[5], etc. , which will be discussed in section3. All of these methods focus on maintaining the diversity and

convergence of Pareto optimal solutions. Nevertheless computing speed of an algorithm is more important for solving many practical problems. Reducing the iteration step, population size and generation of algorithms can accelerate the computing speed. But it is difficult to keep the diversity and convergence of solutions at the same time. In this paper we present a new method to select the best global and personal guide for each particle in the swarm at each interval, which can find many Pareto optimal solutions rapidly.

The paper is organized as follows. In section 2, the basic concepts about MOP are defined. In section 3, the general PSO model is introduced firstly. Then researches on Multi-Objective PSO(MOPSO) in the literature are described briefly. In section 4, a smart MOPSO method is proposed, which can find more Pareto optimal solutions in less iteration step with small population size and generation, by redefining the global best and the personal best of particles. And the experiments and comparisons are given in section 5, which proved the conclusion. At last discussion conclusions and future works are describes in section 6.

## 2 Basic Concepts

The general Multi-Objective Optimization Problem can be defined as:

**Definition 1.** Find a vector  $\vec{x} = [x_1, x_2, \dots, x_n]^T \in \Omega$ , which minimizes the objective functions:  $F(\vec{x}) = (f_1(\vec{x}), f_2(\vec{x}), \dots, f_k(\vec{x}))^T$ , and satisfies the constrains:  $G(\vec{x}) = (g_1(\vec{x}), g_2(\vec{x}), \dots, g_l(\vec{x}))^T$ , where  $k, l \in N$ , indicate the number of objective functions and constrains,  $\Omega \in R^n$  is the set of feasible solutions.

Different objective functions restrict each other usually. The optimization of one objective may worsen others. A rather practical approach to deal with multi-objective problems is to find a Pareto Set, instead of a single aggregate objective-dependent global optimum. The concepts of Pareto optimal are defined as follows.

**Definition 2.** (Pareto Dominance): A vector  $\vec{x} = [x_1, x_2, \dots, x_n]^T$  is said Pareto dominate, denoted by  $\vec{x} \prec \vec{y}$ , if  $\forall i \in \{1, 2, \dots, k\} : f_i(\vec{x}) \leq f_i(\vec{y})$ , and at least one  $i, f_i(\vec{x}) < f_i(\vec{y})$ .  $\vec{x}$  is weakly dominate  $\vec{y}$ , denoted by  $\vec{x} \preceq \vec{y}$ , if  $\forall i \in \{1, 2, \dots, k\} : f_i(\vec{x}) \leq f_i(\vec{y})$ .

**Definition 3.** (Pareto Optimality): A vector  $\vec{x}^* = [x_1^*, x_2^*, \dots, x_n^*]^T$  is a Pareto optimal, if  $\forall \vec{x} \in \Omega$  satisfies  $f_i(\vec{x}^*) \leq f_i(\vec{x}), \forall i \in \{1, 2, \dots, k\}$ , and at least one  $i$  such that  $f_i(\vec{x}^*) < f_i(\vec{x})$ .

**Definition 4.** (Pareto Optimal Set): The non-dominated set of the entire feasible search space is the Pareto optimal set, which is defined as:  $P^* = \{\vec{x}^* \in \Omega | \vec{x}^* \prec \vec{x}, \forall \vec{x} \in \Omega\}$ .

**Definition 5.** (Pareto Optimal Front): The Pareto Optimal Set in the objective space is called Pareto Optimal Front, which can be defined as:  $F^* = \{F(\vec{x}^*) = (f_1(\vec{x}^*), f_2(\vec{x}^*), \dots, f_k(\vec{x}^*)) | \vec{x}^* \in P^*\}$ .

### 3 Particle Swarm Optimization

#### 3.1 General PSO

Particle swarm optimization(PSO) was first proposed by Kenedy and Elberhart in 1995[10], which was inspired by the choreography of a bird flock. PSO is a stochastic search algorithm that conducts searches using a population of particles. The status of a particle can be described by its position and velocity. The new velocity and position of a particle for the next interval are calculated using the following equations:

$$V_i^{k+1} = \omega * V_i^k + c_1 * rand1 * (pBest_i^k - P_i^k) + c_2 * rand2 * (gBest^k - P_i^k) \quad (1)$$

$$P_i^{k+1} = P_i^k + V_i^{k+1} \quad (2)$$

where  $V_i^k$  and  $P_i^k$  indicate for velocity and position of particle  $i$  at interval  $k$ .  $pBest_i^k$  represents the best position of particle  $i$  in its past experience at interval  $k$ , and  $gBest^k$  is the best position of the population.

The formulation includes three components. First is the particle present velocity, dedicating the particle current status, it can balance global and local searching capability. Second is cognition model, expressing the particles cognition ability, it can make particles have enough global searching capability avoiding local maximum. Last is social model, representing communication among particles. Particles land the best position effectively with three components acting together. Otherwise, as a particle adjusting its position according to velocity, it must keep the velocity in the range of min-velocity and max-velocity.  $\omega, c_1, c_2 \geq 0$ .  $\omega$  is the inertia weight.  $c_1$  and  $c_2$  convey the weight information of cognition model and social model.  $rand1$  and  $rand2$  are two random values in the range  $[0, 1]$ . Shi and Eberhart[11] find that bigger inertia weight benefits particles search the problem space entirely, smaller inertia weight is in favor of local searching. They first introduced a linearly decreasing inertia weight to PSO. For more details about PSO algorithm, readers can be referred to [10,11,12].

Since PSO has few parameters to adjust and is easy to implement[12], it has been applied in a lot of areas. Multi-objective optimization problem is one of the most studied application areas of PSO algorithms[12].

#### 3.2 Previous Research in Multi-objective PSO

During the past decade, several Multi-Objective Particle Swarm Optimization (MOPSO) methods have been proposed. In this section, we discussed briefly some of these methods.

Hu and Eberhart[3] use a dynamic neighborhood strategy to select the global best. In their method distances of a particle to other particles are calculated in terms of the first objective called *fixed objective*. Based on the calculated distances, local neighbors of each particle are found. Then the local best particle is selected in terms of the second objective values among the neighbors. Since the

*fixed objective* must be selected firstly, a priori knowledge about the objective functions must be known.

Parsopoulos and Vrahatis[4] use a weighted aggregate approach and vector evaluated PSO dealing with on a number of two dimensional problems. The weighted aggregate algorithms need to be run several times, and get a single global best at each run. The vector evaluated PSO uses one swarm for each objective, and select the best particle of each swarm act as the global best particle guide each other. For example, the best particle of the second swarm is used determine the velocities of the first swarm. The main problem with [3] and [4] is their formulation purely for two-dimension problems.

Coello and Lechuga[5] proposed a grid method. The objective space is divided into many small hypercubes, and a fitness value is assigned to each hypercube depending on the number of elite particles that lie in it. The more elite particles the hypercube have, the less fitness value of it. Then select one of the hypercubes by roulette-wheel. Global best is a random particle selected from the selected hypercube. So, it is possible that a particle doesn't select a suitable guide as its local guide[7].

Fitzgibbon and Singh[6] used a dominated tree (D-Tree) for storing the particle, which consists of a list of composite points ordered by the weakly dominates relation. In this method the selection of the best global guide for a particle in the population is based on its closeness to a particle in the archive. The D-Tree method is said to be better than grid method proposed by Coello and Singh.

Bartz and Konstantinos[2] proposed a PSO using enhanced archiving techniques called DOPS. DOPS integrates well-known archiving techniques from evolutionary algorithms into PSO.

Cagnina and Esquivel[1] presented a hybrid PSO approach, including elitist policy, a mutation operator and a grid which is used as a geographical location over objective function space. This hybrid PSO method is an inspiration of multi-objective evolutionary algorithms also.

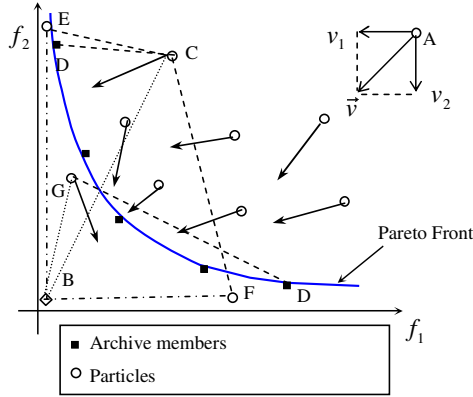
Mostaghim and Teich[7,8,9] proposed a sigma method for finding the suitable global best for each particle. Sigma values are calculated for each individual in the archive and new generation. Each particle selects the archive member with minimal sigma value to its sigma value as its social leader. And the sigma MOPSO method fixes the size of the archive to a certain amount using the idea of sigma dominance. Comparing to MOGA and D-Tree method, the Sigma MOPSO method has a better diversity and convergence.

## 4 Smart PSO for Multi-objective Problem

It is the cognition model and social model that guide a particle fly away its current position toward a better position in the search space, which we can find from the velocity and position updating formula(1) and (2). So, selection of the global best ( $gBest$ ) and the personal best ( $pBest$ ) is the key for PSO to solve multi-objective problems. The previous researches in MOPSO are focus on selection

*gBest* from archive members. This paper, we present new selection methods of *gBest* and *pBest*, which can guide swarm members convergent rapidly and maintain the diversity of solutions.

In figure1, we can see how dose a particle fly in the two dimensional objectives space. For example, if there is only one objective function  $f_1$  or  $f_2$ , particle A will fly along  $v_1$  or  $v_2$ . Since two objective functions affect on the particle at the same time, particle A will fly along  $\vec{v}$  in stead of  $v_1$  or  $v_2$ , until land the Pareto Front.



**Fig. 1.** Particles fly in the two-dimensional objective space

So the first important thing for MOPSO is how to guide particles fly along the direction incorporating all objective functions. The method we presented is to find the cooperative action of all objective functions as global best guide. Firstly, best particles for each objective function of MOP are selected by calculating the fitness values of every particles under each function. Secondly, the mean value of those particles is calculated. Then the mean value is set as *gBest* for particles of the swarm. As shown in figure 1, particle E is the best particle for objective  $f_1$ , particle F is the best particle for function  $f_2$ , point B indicates for the *gBest* of two dimensional problems. In fact, point B is not the true position of *gBest*, but a virtue position.

Particles directed by point B will fly across the Pareto Front and converge at a certain point. Then the next important problem is how to guide particles fly along the Pareto Front. Here we use archive members serve as the personal best to guide particles fly back to Pareto front. Firstly, the distances between each particle and non-dominate archive solutions are calculated. Then the archive member with minimal distance to one particle will be selected as *pBest* of a particle. For instance, the particle C in figure1 will fly toward Pareto front under the cooperative direction of point D, E and F. As iteration steps increasing, particles may fly slower and slower since they are too close to the Pareto front. Sometimes, those particles may gather together. So we add an additional strategy to disperse those clustering particles. That is guiding particles fly toward the

remotest archive member with maximal distance to themselves. And set a *distance valve* as the boundary. While the distance between a particle and its closest archive member is less than the *distance valve*, its remotest archive member will be chosen as its *pBest*, otherwise its closest archive member will be chosen. The distance between particle  $p$  and archive member  $a$  can be calculated by formula:

$$Dis(p, a) = \|p - a\| = \left\{ \sum_{i=1}^n (p_i - a_i) \right\}^{\frac{1}{2}} \quad (3)$$

The structure of SMOPSO for multi-objective optimization discussed above is shown in table1. First, particles are initialized randomly. In step 3, the non-dominated solutions are selected according to the Pareto optimal definitions. In step 4 and 5, *gBest* and *pBest* are selected using the strategies proposed in this paper. Generations are updated by formula (1) and (2) in step 6. Iterating step 2 to step7, the algorithm finds non-dominate solutions in the objective space, and updates archive with the new generations.

**Table 1.** Structure of SMOPSO Algorithm

|                                                                                                            |
|------------------------------------------------------------------------------------------------------------|
| Begin                                                                                                      |
| Step 1: Set $k = 0$ and initialize particles.                                                              |
| Step 2: Calculate fitness vale of particles under each objective.                                          |
| Step 3: Select the non-dominated solutions, keep in the archives and remove the dominated archive members. |
| Step 4: Find the <i>gBest</i> of particle swarm.                                                           |
| Step 5: Find the <i>pBest</i> of each particle.                                                            |
| Step 6: Update generation.                                                                                 |
| Step 7: $k = k + 1$ . Go to step2 unless a termination criterion is met.                                   |
| End                                                                                                        |

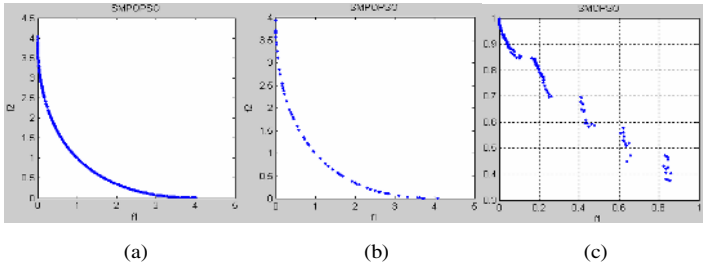
## 5 Experiments

Following experiments have been performed on different test functions which selected from [13]and[7], shown in table 2.  $T_1$  is a simple two-dimensional objective problem with only one parameter.  $T_2$  is a composition of three functions  $f_1, f_2, g$  with thirty parameters, which  $g$  is the constrain function. And this two-dimensional objective problem has a discontinuous Pareto Front.  $T_3$  is a typical three-dimensional objective problem, and always acts as a test function for multi-objective optimizing algorithms. Its Pareto Front satisfies the formula:  $f_1(\vec{x}) + f_2(\vec{x}) + f_3(\vec{x}) = 1$ .

Set  $\omega, c_1, c_2$  as:  $\omega = 0.8 - (0.8 - 0.4)/k, c_1 = 0.4 + (0.8 - 0.4)/k, c_2 = 0.4 + (0.8 - 0.4)/k$ , which  $k$  denotes the generation index. Tests are done for 200 particles, 10 generations and 100 particles, 3 generations on  $T_1$  with 0 *distance valve* separately. Figure 2 (a) and (b) show the results of those tests. And set population size as 200 run for 10 generations on  $T_2$  and  $T_3$  with *distance valve* 0. 1 and 0. 35 separately. Tests are done for the Sigma MOPSO[4,5,6] method

**Table 2.** Test Functions: $T_i$ 

| Test  | Functions                                                                                                                                                                                            | Constrains                                           |
|-------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------|
| $T_1$ | $f_1(x) = x^2$<br>$f_2(x) = (x - 2)^2$                                                                                                                                                               | $x \in [-5, 7]$                                      |
| $T_2$ | $g(x_2, x_3, \dots, x_n) = 1 + 9 * (\sum_{i=2}^n x_i) / (n - 1)$<br>$f_1(x_1) = x_1$<br>$f_2(\vec{x}) = 1 - f_1 / \sqrt[n]{f_1/g} * \sin(10 * \pi * f_1)$                                            | $x_i \in [0, 1]$<br>$n = 30$<br>$i = 1, 2, \dots, n$ |
| $T_3$ | $f_1(\vec{x}) = (1 + x_3) * \cos(x_1 * \pi / 2) * \cos(x_2 * \pi / 2)$<br>$f_2(\vec{x}) = (1 + x_3) * \cos(x_1 * \pi / 2) * \sin(x_2 * \pi / 2)$<br>$f_3(\vec{x}) = (1 + x_3) * \sin(x_1 * \pi / 2)$ | $x_i \in [0, 1]$<br>$i = 1, 2, 3$                    |

**Fig. 2.** Test results on function 1 and 2

on  $T_3$  also. The parameters of the Sigma MOPSO method are: 200 particles, 10 generations with turbulence 0.07.

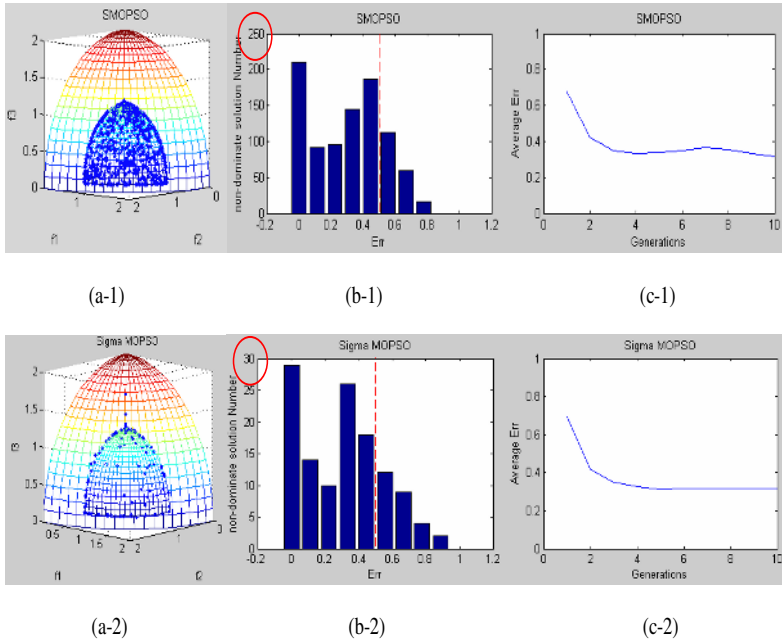
Comparing figure 2 (b) with (a), we can see that the algorithm presented in this paper can cover the Pareto Front even the population size and generation are very small. This characteristic is very important to accelerate the computing speed. Figure 2 (c) shows the test result on test function 2. In fact several tests have been done on  $T_2$ . Increasing the populations size and generation, SMOPSO will find more solutions.

Figure 3 show the results on  $T_3$ . In those tests, we get 998 solutions by using the SMOPSO method and only 168 solutions by using the Sigma PSO method. Comparing the SMOPSO method with the Sigma method, the SMOPSO method can find more solutions on the front just in ten iteration steps, show in figure 3 (a-1) and (a-2). Sometimes the solutions may gather at some area of the Pareto Front. Some heuristic technique such as dynamic adaptive *distance value*, selective archiving, heuristic initialization, etc. , will be used to improve the algorithm for keeping diversity of solutions in future.

In order to evaluate the convergence of algorithms, we calculate the difference between archive member and Pareto optimal solution, which is defined as:

$$err = 1 - (f_1(\vec{x}) + f_2(\vec{x}) + f_3(\vec{x})), \quad \forall i \in Archive. \quad (4)$$

Hence we can calculate the histogram which is the amount of points with a certain *err* and the trendline which is the line of archive members average



**Fig. 3.** Comparison of the SMOPSO and the Sigma MOPSO method applied on  $T_3$

*err* value at each interval. Figure 3(b-1), (b-2), (c-1) and (c-2) show that both the SMOPSO method and the Sigma method can find solutions with  $err < 0.5$ , and both methods have a very rapid convergent speed. But the SMOPSO method can find more solutions with same population size and iteration step. This characteristic indicates that the SMOPSO method can find more Pareto-optimal solutions of the multi-objective problems in a very short time, and can maintain the diversity and convergence of solutions simultaneous.

## 6 Conclusion and Future Work

A new method called smart particle swarm optimization for multi-objective problems (SMOPSO) is described in this paper. By taking into account the actions of all objective functions, the global best is selected. By calculating the distance between the particles and archive members, personal best positions are chosen. Using these global best and personal best selection strategies, SMOPSO can find solutions with a good diversity and convergence, and can converge on the Pareto Front with very little population size and generation, as our experiments on function 1, 2, and 3 shown. That is a very important character of the SMOPSO method proposed in this paper. Since smaller population and generation can accelerate computing speed, the SMOPSO method is fit for real-life multi-objective optimization problems which need to be solved in a very short time especially.



In the future, we would like to investigate and compare the influence of the different *distance valve* on the SMOPSO method, and apply the SMOPSO method for more test functions with higher number of objectives.

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# Adaptive Particle Swarm Optimization with Feedback Control of Diversity

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**Abstract.** Swarm-diversity is an important factor influencing the global convergence of particle swarm optimization (PSO). In order to overcome the premature convergence, the paper introduced a negative feedback mechanism into particle swarm optimization and developed an adaptive PSO. The improved method takes advantage of the swarm-diversity to control the tuning of the inertia weight (PSO-DCIW), which in turn can adjust the swarm-diversity adaptively and contribute to a successful global search. The proposed PSO-DCIW was applied to some well-known benchmarks and compared with the other notable improved methods for PSO. The relative experimental results show PSO-DCIW is a robust global optimization method for the complex multimodal functions, which can improve the performance of the standard PSO and alleviate the premature convergence validly.

## 1 Introduction

Particle swarm optimization (PSO) is a novel evolutionary algorithm that is inspired originally by the social and cognitive behavior lying in the bird flocking. Since the original version introduced in 1995 by Kennedy and Eberhart [1], PSO has attracted lots of attentions from researchers around the world and lots of research results have been reported in the literatures. As one of stochastic algorithms, PSO owns some attractive features such as simple model, few parameters, and easy implementation. Now, PSO has been applied successfully in many areas [2-6], including neural networks, multidimensional complex problems, multiobjective optimizations, and some project applications, etc.. However, like others stochastic algorithms, PSO also suffers from the premature convergence problem, especially in the large scale and complex problems.

As far as the premature convergence is concerned, a main reason is that a fast information interaction among particles in PSO leads to the swarm diversity declining and the particle clustering quickly. Some techniques have been proposed to avoid the premature convergence. Suganthan introduced the spatial neighborhood into PSO [7]; Li used species to choose the neighborhood adaptively [8]. Lovbjerg adopted the

concepts of “subpopulation” and “breeding” in Genetic Algorithms (GAs) to increase the diversity [9]; Riget developed an attractive and repulsive PSO(ARPSO) to adjust the diversity[10]; Shi and Eberhart modified the parameters to keep the balance between the exploration and the exploitation [11,12]., etc.. According to the relative literatures, those methods can improve the global convergence ability of PSO in certain degree but fewer can solve the premature convergence problem truly.

In order to overcome the premature problem, The paper introduced a negative feedback mechanism into particle swarm optimization and developed an adaptive PSO. The improved method takes advantage of the swarm diversity to control the tuning of the inertia weight (PSO-DCIW), which not only can vary the swarm diversity in turn, but also can manipulate the exploitation and the exploration adaptively. The proposed PSO-DCIW is used to some benchmark optimizations and compared with the other notable improvements for PSO, the results show PSO-DCIW can overcome the premature problem validly, and performs very well on the complex multimodal optimizations.

The remaining of the paper is organized as the follows. Section 2 provides some relative work on PSO. Section 3 describes the PSO-DCIW method in details. Section 4 presents the experiments and the relative results. Finally, Section 5 concludes with some remarks.

## 2 Some Relative Works

### 2.1 The Standard PSO (SPSO)

Since the original version of PSO proposed in 1995[1], lots of work has been done to develop it. In order to control the global exploration and the local exploitation validly, Shi and Eberhart [11] introduced a concept of inertia weight to the original PSO and developed a modified PSO. Compared with the original version, the modified PSO gets a notable improvement of the performance, so it is often referred to as the standard PSO version(SPSO) and adopted by many following researches. The SPSO version can be described by the following update equations:

$$v_{id}(t+1) = \omega v_{id}(t) + c_1 r_1 (P_{id}(t) - x_{id}(t)) + c_2 r_2 (P_{gd}(t) - x_{id}(t)). \quad (1)$$

$$x_{id}(t+1) = x_{id}(t) + v_{id}(t+1). \quad (2)$$

Supposed the particles flying through a  $d$ -dimensional space,  $X_i$  and  $V_i$  represent the position vector and velocity vector of the  $i$ th individual respectively, while  $P_i$  represents the personal best position of  $i$ th individual and  $P_g$  represents the global best position in the swarm; the inertia weigh  $\omega$  is a scaling factor controlling the influence of the old velocity on the new one;  $c_1$  and  $c_2$  are constants known as “cognitive” and “social” coefficients which determine the weight of  $P_i$  and  $P_g$  respectively;  $r_1$  and  $r_2$  are two random numbers generated by the uniform distribution in the range  $[0,1]$  separated.

## 2.2 Some Improved SPSO Based on the Parameters

Many works have been done to study the parameters set of SPSO. Shi and Eberhart have analyzed the effect of the inertia weight through empirical experiments, and found that a larger  $\omega$  can bring a better global convergent ability while a smaller  $\omega$  can manipulate a better local search[12]. So, they manipulated SPSO with a linearly decreased  $\omega$  over time (PSO-LDIW), where  $\omega$  is given by the following equation:

$$\omega = (\omega_1 - \omega_2) \times \frac{(MAXITER - iter)}{MAXITER} + \omega_2 . \quad (3)$$

Here  $\omega_1$  and  $\omega_2$  are the initial and final values of the inertia weigh respectively,  $iter$  is the current iteration number and  $MAXITER$  is the maximum number of the iteration.

Moreover, Shi and Eberhart have proposed a random modification for the inertia weight (PSO-RDIW) to fit PSO with the dynamic problems effectively, where  $\omega$  is modified randomly by the following equation:

$$\omega = 0.5 + rand(0,1) / 2 . \quad (4)$$

According to the relative literatures, the two versions show rapid convergence, but often perform well in unimodal functions while are failure in multimodal functions. Later, Shi and Eberhart introduced a fuzzy controller to modify the inertia weight dynamically [13]. The adaptive fuzzy inertia weight controller is a promising technique for optimizing the parameter, but difficult for implementation.

Considering the two acceleration coefficients may have great influence on the performance of PSO, Ratnaweera et al. have developed SPSO with time-varying acceleration coefficients (PSO-TVAC)[15]. The method has the same motivation and the similar techniques as the PSO-LDIW, in which, the cognitive coefficient  $c_1$  is decreased linearly and the social coefficient  $c_2$  is increased linearly over time.

Though the methods with the time-varying parameters can make a good exploration in the early search and keep a fast convergence in the last search, they couldn't take advantage of any search information to modify the parameters and overcome the premature problem essentially. If the global solution just appears in the forepart search, the time-varying parameters can ensure the search converge to the global optimum with a rapid speed, or the time-varying parameters will lead to the search easily to be trapped in the local optimum.

## 3 PSO with Diversity-Controlled Inertia Weight (PSO-DCIW)

### 3.1 The Motivation of PSO-DCIW

As far as the premature convergence is concerned, the main reason is that a fast information interaction among particles in PSO leads to the swarm-diversity declining and the particle clustering quickly. In order to improve the global performance of SPSO, a more feasible idea is trying to maintain an appropriate swarm-diversity according to the current search state, and to modify the parameters under the guide of the search information.

Before the idea about the adaptive diversity-controlled PSO comes into being, let's go back to analyze the simulated behavior of PSO. How to do and what can prompt PSO to be a successful and robust optimization? Maybe, the answer just lies in its headstream---Swarm Intelligence. In general, Swarm intelligence can be defined as "the emergent complex intelligence inspired by the collective behavior of social insect colonies and other animal societies."[16]. Here, the swarm consists of some individuals that exhibit simple behaviors. In the swarm, no one is in charge, no one give out direct orders; but every individual can perceive and receive amount of information from different directions. The information interactions among individuals can be characterized as varieties of feedbacks lying in a self-organization system, which not only occur in the individual lever, but also take place between the individual lever and the swarm lever.

Based on the concept of Self-organization, the PSO system should be considered as a dynamic closed system, and its dynamic behaviors should be understood from two aspects: its low-lever ---the individual lever and its high-lever---the swarm lever, an emergence of a high-lever quality in such a system is mainly due to the internal interactions between the two levers. One aspect, the low-lever particles in the swarm continually interact the local information each other and try to get a collective output cooperatively; another aspect, each particle can perceive the swarm-lever state and make some decisions to modify its behavior intelligently. In other words, the swarm-lever outputs have an important influence on the behaviors of the particles, which just provide a guiding direction and prompt a higher-lever quality to emerge in the swarm.

According to the analysis above, we introduced a negative feedback mechinism into particle swarm optimization and developed an adaptive PSO. The improved method takes advantage of the swarm-diversity as the swarm-lever information to control the tuning of individual's parameter (inertia weight) that is referred to as PSO-DCIW here. Its architecture is discussed in details in the following part.

### 3.2 The Architecture of PSO-DCIW

According to Fig.1., PSO-DCIW can be regarded as a control system with a negative feedback. Here, the swarm is a dynamic component that consists of  $N$  particles modified by the PSO optimizer. Its dynamic properties can be described by the swarm-diversity  $Do$  and the best position  $Pgo$ . As far as the optimization problem is concerned, the swarm is anticipated to keep the swarm diversity with a relative steady variation to give a good output of  $Pgo$ . Obviously, the outputs of the system mainly

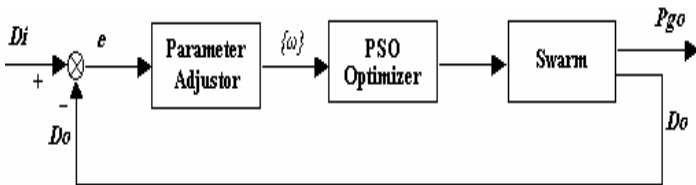


Fig. 1. The architecture of PSO-DCIW

depend on the appropriate parameters of the PSO optimizer, good parameters setting will lead to good outputs. So, how to design the parameter adjustor is the main consideration for PSO-DCIW

Here, we design the parameter adjustor into a ratio controller, whose ratio coefficient is denoted as  $Kp$ . During a search, the adjustor is expected to modify the inertia weight under the control of the swarm-diversity through the negative feedback, which can in turn adjust the swarm-diversity adaptively. Supposed  $Di(t) = Do(t-1)$  in the  $t$ th iteration, the current input  $e$  of the parameter adjustor can be calculated by the following:

$$e(t) = \frac{Di(t) - Do(t)}{Di(t)} = \frac{Do(t-1) - Do(t)}{Do(t-1)}. \quad (5)$$

So, the output of the parameter adjustor  $\omega$  is given by the follows:

$$\omega(t) = Kp \times e(t) = Kp \left(1 - \frac{Do(t)}{Do(t-1)}\right). \quad (6)$$

Obviously, PSO-DCIW is different from PSO-LDIW essentially. PSO-DCIW modifies the tuning of the inertia weight adaptively under the control of the swarm diversity. During the search, if the swarm-diversity  $Do$  decreases quickly, a bigger  $\omega$  will be offered to the following optimizer and lead to the exploration enhancing in the next iteration; if  $Do$  decreases very slowly, a smaller  $\omega$  will be got to enhance the exploitation in the next iteration; if  $Do$  fluctuates with an increase in a special iteration, a negative value of  $\omega$  will be provided to inverse the flying of the particles which in turn lead to the diversity decreasing. Through the negative feedback, PSO-DCIW can alleviate the acute fluctuation of diversity, especially in the forepart search, which contributes to the balance between the exploration and exploitation, and prevents the search from being trapped in the local optimum early.

Here, the swarm-diversity  $D(\cdot)$  is computed according to the diversity-measure proposed by the literature [10]:

$$D(t) = \frac{1}{|S| \cdot |L|} \cdot \sum_{i=1}^{|S|} \sqrt{\sum_{j=1}^N (P_{ij}(t) - \bar{P}_j(t))^2}. \quad (7)$$

Where  $S$  is the swarm,  $|S|$  means the size of the swarm,  $|L|$  is the length of the longest diagonal in the search space,  $N$  is the dimension of the objective problem,  $P_{ij}$  is the  $j$ th value of the  $i$ th particle and  $\bar{P}_j$  is the  $j$ th value of the average point  $\bar{P}$ .

During the iterations, the optimizer manipulates each particle flying through the different inertia weigh provided by the parameter adjustor. The update equation of the velocity for each particle is described as the follows:

$$v_{id}(t+1) = \alpha(t)v_{id}(t) + c_1r_1(P_{id}(t) - x_{id}(t)) + c_2r_2(P_{gd}(t) - x_{id}(t)). \quad (8)$$

### 3.3 The Pseudocode of PSO-DCIW

```

PSO-DCIW main {
 t=0;
 Initialize the swarm and Evaluate the swarm $S(0)$
 Get the best solution $P_{go}(0)$ and Calculate the swarm-diversity $Do(0)$
 while (not (Termination criteria)) {
 t=t+1
 $Di(t) = Do(t-1)$
 Calculate $e(t) = (Di(t) - Do(t)) / Di(t)$
 Calculate $\omega(t) = K_p * e(t)$
 Update the swarm and Evaluate the swarm $S(t)$
 Update $P_{go}(t)$ and $Do(t)$
 }
}

```

**Fig. 2.** The pseudocode for PSO-DCIW

## 4 Experiments and Results

### 4.1 The Benchmark Functions

Four well-known benchmarks have been used to test the performances of PSO-DCIW in the experiments, which are widely adopted in the relative researches about PSO and evolutionary algorithms[10,12,15,17].

$$f_1 = \frac{1}{4000} \sum_{i=1}^N x_i^2 - \prod_{i=1}^N \cos\left(\frac{x_i}{\sqrt{i}}\right) + 1 \cdot \quad (9)$$

$$f_2 = 20 + e - 20 \exp(-0.2 \sqrt{\frac{1}{n} \sum_{i=1}^n x_i^2}) - \exp\left(\frac{1}{n} \sum_{i=1}^n \cos 2\pi x_i\right) \cdot \quad (10)$$

$$f_3 = \sum_{i=1}^N (x_i^2 - 10 \cos(2\pi x_i) + 10) \cdot \quad (11)$$

$$f_4 = \frac{1}{N} \sum_{i=1}^N (x_i^4 - 16x_i^2 + 5x_i) \cdot \quad (12)$$

All of the above benchmarks are complex multimodal functions with many local optima. They are very difficult to solve for many optimization algorithms. The basic information of the test functions is listed in Table.1.

**Table 1.** Basic information about benchmarks

| Benchmark                    | Solution space    | Global minimum |
|------------------------------|-------------------|----------------|
| $f_1$ -Griewank              | $[-600, 600]^N$   | 0              |
| $f_2$ -Ackley                | $[-32, 32]^N$     | 0              |
| $f_3$ -Rastrigin             | $[-5.12, 5.12]^N$ | 0              |
| $f_4$ -2 <sup>n</sup> minima | $[-5, 5]^N$       | -78.3323       |

## 4.2 Experimental Results and Discussions

A series of experiments have been done to make some comparisons on the performance between PSO-LDIW, PSO-RDIW and PSO-DCIW. In PSO-DCIW, the inertia weight  $\omega$  is controlled by  $Kp$ . Based on some preliminary experiments, a good range for the value of  $Kp$  is (0.9~1.6), here  $Kp = 1.4$  in the following experiments. The set of parameters in PSO-LDIW is same as the one adopted by the literature [12], where the inertia weight  $\omega$  is linearly decreased from 0.9 to 0.4 over time, and the

**Table 2.** Comparison between PSO-DCIW and PSO-LDIW, PSO-RDIW. All results were averaged over 50 runs, where the max iteration is 100 times of the dimension in each run. The swarm size adopted by every algorithm is 100.

| Function | Dimension | PSO-LDIW                 | PSO-RDIW                 | PSO-DCIW                 |
|----------|-----------|--------------------------|--------------------------|--------------------------|
|          |           | Mean Best<br>(Std Dev)   | Mean Best<br>(Std Dev)   | Mean Best<br>(Std Dev)   |
| F1       | 10        | 0.062731<br>(0.009796)   | 0.047974<br>(0.007509)   | 0.062245<br>(0.008452)   |
|          | 20        | 0.031701<br>(0.006027)   | 0.020712<br>(0.004072)   | 0.030051<br>(0.007075)   |
|          | 30        | 0.018148<br>(0.038629)   | 0.010826<br>(0.002191)   | 0.020908<br>(0.008824)   |
| F2       | 10        | 2.11e-014<br>(1.69e-014) | 6.38e-015<br>(2.93e-015) | 5.98e-015<br>(2.87e-015) |
|          | 20        | 1.65e-011<br>(8.70e-012) | 1.13e-014<br>(4.14e-015) | 2.25e-014<br>(5.24e-015) |
|          | 30        | 1.48e-009<br>(3.94e-010) | 1.96e-014<br>(3.04e-015) | 1.36e-013<br>(7.56e-014) |
| F3       | 10        | 4.18881<br>(2.778225)    | 1.02595<br>(0.261539)    | 1.52714<br>(0.381425)    |
|          | 20        | 15.7028<br>(8.53195)     | 11.9821<br>(2.41478)     | 10.1588<br>(2.11328)     |
|          | 30        | 30.6257<br>(14.0846)     | 36.9387<br>(7.09514)     | 21.5464<br>(4.02996)     |
| F4       | 10        | -76.1303<br>(0.41612)    | -78.3321<br>(6.36e-005)  | -78.3323<br>(4.44e-006)  |
|          | 20        | -64.9035<br>(1.93951)    | -77.6004<br>(0.138039)   | -78.3123<br>(0.056546)   |
|          | 30        | -56.6634<br>(3.08283)    | -73.5734<br>(0.727718)   | -78.2758<br>(0.032646)   |



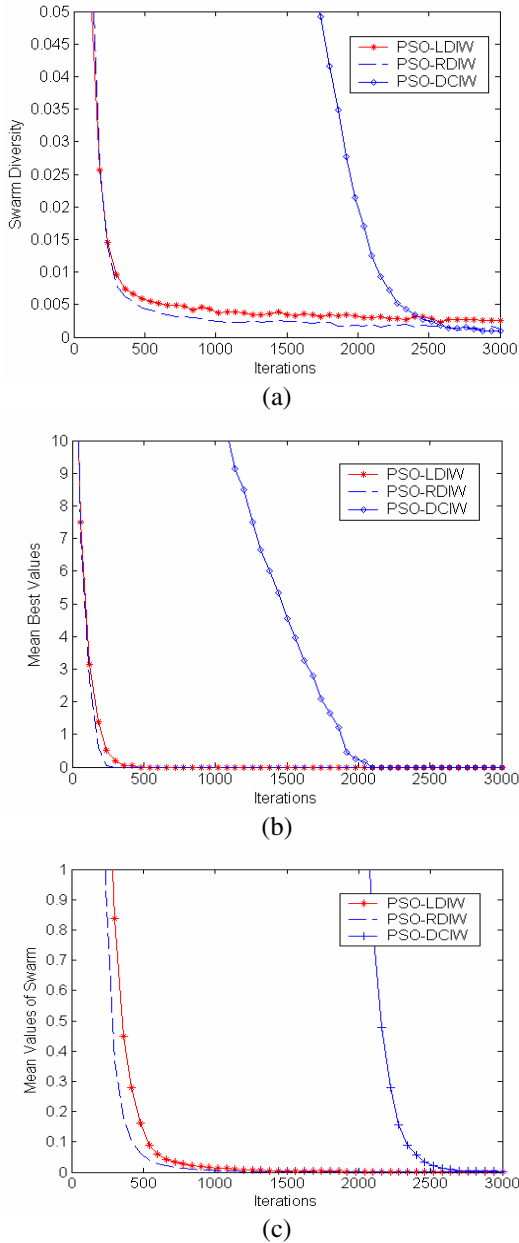
coefficients  $c_1 = c_2 = 2.0$ ; In PSO-RDIW, the inertia weight  $\omega$  is produced randomly according to Equation (4) and  $c_1 = c_2 = 1.49$ , which have proved a successful set of parameters [13]. In each experiment, the velocity is limited by the solution boundary of the objective function, that means  $V_{\max} = X_{\max}$ . Some important results are showed in the following table and figures.

In Table 2, PSO-DCIW is compared with PSO-LDIW and PSO-RDIW respectively. The final experimental results averaged over 50 runs are given, including the mean best function values and the standard deviation got by each algorithm. For  $f_1$ , PSO-DCIW performs worse than PSO-RDIW, but as well as PSO-LDIW. For  $f_2$ , the performance of PSO-DCIW is similar to the one of PSO-RDIW, and better than the one of PSO-LDIW. In the case of  $f_3$ , PSO-DCIW outperforms both two other methods a little. A notable difference in the performance between DCPSO and the other two methods occurs in the function  $f_4$ .  $f_4$  is a multimodal function with  $2^n$  minima and difficult to optimize, for its local minima increases exponentially with the dimension of the function increasing. Obviously, PSO-DCIW outperforms PSO-LDIW and PSO-RDIW a lot in  $f_4$ , which means PSO-DCIW is easy to escape from the local minima and converge to the global minimum robustly, while PSO-LDIW and PSO-RDIW seems easy to be trapped in local minima when facing to a very complex problem.

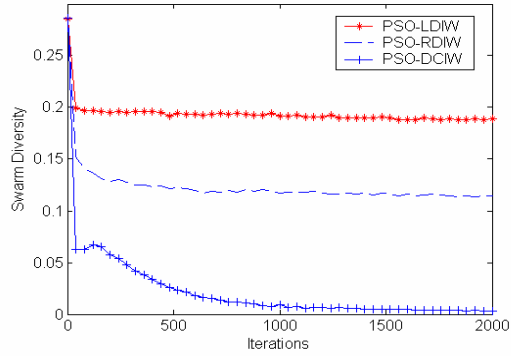
The results in Table 2 show PSO-DCIW performs better than or similar to PSO-LDIW and PSO-RDIW on the complex multimodal functions. The reason maybe lies in that PSO-DCIW takes advantage of the diversity feedback to guide the search. The following figures can make it clear.

Fig.3. and Fig.4. illustrate the dynamic processes of the swarm-diversity, the mean best value and the mean value of the swarm during the search, where PSO-DCIW, PSO-LDIW and PSO-RDIW were applied to  $f_2$  and  $f_4$  respectively. Compared with the other two methods, PSO-DCIW has a slower convergent speed with a higher swarm diversity in the forefront of the search, but it can converge to the global optimum with a smaller diversity in the end of the search. That mainly owns to the negative feedback of diversity to modify the parameters adaptively. Considering the optimization algorithm, the swarm diversity curve got by PSO-DCIW seems to be the best one, which keeps a higher swarm diversity in the early search and decreases slowly to a smaller value with the search going. In other words, such swarm diversity curve contributes to the improvement of PSO-DCIW in the global convergent performance.

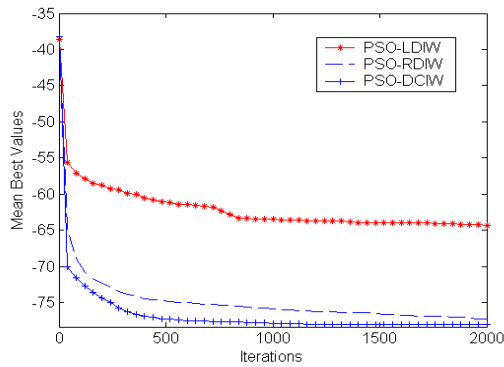
For PSO-LDIW and PSO-RDIW, the function  $f_4$  is more difficult to optimize. Though PSO-LDIW keeps the highest diversity in the most search, it fails to converge to the global optimum with a weak exploitation in the end. Compared with PSO-LDIW, PSO-RDIW has a notable improvement of the performance for  $f_4$ , but it still performs worse than PSO-DCIW a lot. According to Fig.4., it's easy to know that PSO-DCIW is the best method for  $f_4$ . Owing to the feedback control of the diversity, PSO-DCIW can modify the exploration and the exploitation adaptively, which leads to the search converge to the global optimum successfully. Its swarm diversity curve can prove the point. In other words, PSO-DCIW is easy to escape from the local minima and outperforms the other two methods with a robust performance when faced to the complex optimization problems.



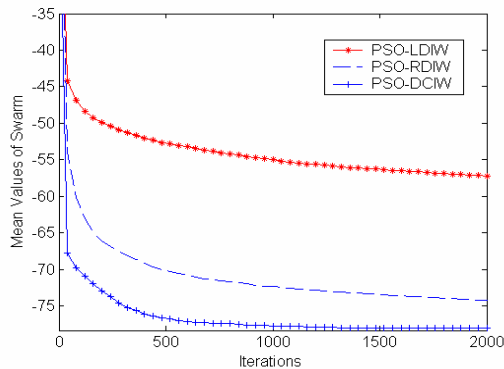
**Fig. 3.** Comparison among PSO-DCIW, PSO-LDIW and PSO-RDIW based on  $f_2$ . All results were averaged over 20 runs, where the dimension of  $f_2$  is 30, the max iteration is 3000 and the swarm size is 100. (a) shows the swarm diversity, (b) shows the mean best values, and (c) illustrates the mean values of the swarm.



(a)



(b)



(c)

**Fig. 4.** Comparison among PSO- DCIW, PSO-LDIW and PSO-RDIW based on  $f_4$ . All results were averaged over 20 runs, where the dimension of  $f_4$  is 20, the max iteration is 2000 and the swarm size is 100. (a) shows the swarm diversity, (b) shows the mean best values, and (c) illustrates the mean values of the swarm during a search.

## 5 Conclusions

The paper has introduced a negative feedback mechanism into particle swarm optimization and developed an adaptive PSO. The improved method takes advantage of the swarm diversity to control the modification of the inertia weight (PSO-DCIW), which in turn can adjust the diversity and contribute to a successful global search. The proposed PSO-DCIW was applied to some well-known benchmarks and compared with two notable improved methods that are referred to as PSO-LDIW and PSO-RDIW. The relative experimental results show PSO-DCIW performs better than or similar to PSO-LDIW and PSO-RDIW on the complex multimodal functions. Owing to the feedback control of the diversity, PSO-DCIW can modify the exploration and the exploitation adaptively, which leads to the search converge to the global optimum successfully. When faced to more complex optimization with lots of local minima, PSO-DCIW is easy to escape from the local minima and converges to the global minimum robustly, while PSO-LDIW and PSO-RDIW seems easy to be trapped in local minima. All analysis and experimental results prove the method with the diversity feedback can improve the performance of the standard PSO validly, and PSO-DCIW is a robust global optimization method for complex multimodal optimizations.

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# An Improved Particle Swarm Algorithm and Its Application to Power System Transfer Capability Optimization

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**Abstract.** In this paper, an algorithm based on PSO (Particle Swarm Optimization) for power system transfer capability calculation is presented. A dual fitness scheme that takes both objective and constraint into account is adopted to evaluate the survival chance of any particle, thus avoid the drawbacks of traditional penalty method. In the evolution process, if the population best particle has no update during a prescribed number of consecutive generations, it is regarded as a local optimum solution and the searching space around this particle is locked to prevent other particles flying into it. And this particle is saved as one of the candidate solution. In the end, by comparing the fitness of all saved particles and the current population best particle the optimum value can be obtained. This improved particle swarm algorithm is then successfully applied to IEEE118 bus system optimization problem. Compared with a traditional well-known method, sequential quadratic programming, our proposal obtains better solutions for this problem.

## 1 Introduction

Available transfer capability (ATC) is the power transfer capability remaining in the physical transmission network for further commercial activity over and above already committed uses [1].

Under the development of power system, large amount of power are transferred from power plants to load center via transmission lines. It becomes a truth that the load centers stand far from the power plants. In power market circumstance, the electric power transfer is an important business for power company. So whether under the traditional electric circumstance or deregulated circumstance, to system operators, ATC calculation has a great significance.

Three main methods have been presented for ATC calculation: power transfer distribution factor method (PTDF) [2], continuous power flow method (CPFlow) [3] and optimization power flow method (OPF) [4]. Because PTDF method needs no

iteration, ATC value can be acquired very quickly. But this method will lead to unacceptable error in heavy load power system with less reactive power supporting because its mathematical model is built on the direct flow model, and the affection of voltage and reactive power is ignored. CPFlow method bases on the homotopy theory. It solves the diffusion problem when system operation point is very close to addle-node in power calculation with common methods. But this method has to define the specified power transfer model firstly (this means that the selling power area defines the generation increasing pattern and buying power area defines the load increasing pattern). This will lead to conservative solution acquired. In OPF method, ATC problem is looked as an optimization problem. The objective function is the maximum transfer capability and equality constraints are power equations. Branch thermal constraints, bus voltage constraints and devices capability constraints are inequality constraints. On the basis of this mathematical model, kinds of optimization methods, such as sequence quadratic programming [4], primal-dual interior point method [5], Benders decomposition method [6] etc. are applied for ATC calculation. But OPF methods based on Newton criteria can only acquire the local optimization solution because the static feasible field of power system is always no convex.

In generally, optimization problem of power system is a nonlinear problem characterized by its feasible field no convex, discrete variants and continuous variants coexistence, and sometimes with a discontinuous objective function. So the traditional optimization methods based on Newton criteria always get the local optimization solution. And at the same time, with the enlargement of the size of power system analyzed, these methods will inherently bring out the "dimension disaster". As a new evolutionary computation tool, particle swarm optimization (PSO) is becoming a hot research point in these years. It has no special requirements for optimization object so it can be used to solve widely array of the optimization problems. In this paper, an improved Particle Swarm Optimization (IPSO) is introduced to solve the ATC calculation in power system.

## 2 PSO Introduction

### 2.1 PSO Definition

PSO is a population based optimization method first proposed by Eberhart and Kennedy in 1995 [8]. Just similar with Genetic Algorithm [9], PSO takes the concept of "population" and "evolution", and also operates basing on the fitness value. Here, it's assumed that the population consists of  $m$  particles and the search space is  $n$  dimension.

Every particle has the following three properties: a current position in search space,  $x_i$ ; a current velocity,  $v_i$ ; and the personal best position,  $p_i$ , corresponds to the position in search space where particle  $i$  obtains the best fitness determined by the objective function and constraint condition. The best personal best position in the population is called the global best position, which denoted as  $p_g$ . In the first iteration,  $p_i$  is the initial position of each particle. In the following iteration, each

particle new position is attracted by the position of  $p_i$  and  $p_g$ . This can be expressed as following equations:

$$v_{ij}(t+1) = wv_{ij}(t) + c_1r_{1j}(t)(p_{ij}(t) - x_{ij}(t)) + c_2r_{2j}(t)(p_{gj}(t) - x_{ij}(t)) . \quad (1)$$

$$x_{ij}(t+1) = x_{ij}(t) + v_{ij}(t+1) \quad (2)$$

where,  $j$  denotes the search space dimension,  $j = 1, 2, \dots, n$ ;  $i$  denotes the number of particles,  $i = 1, 2, \dots, m$ ;  $t$  denotes the iteration times;  $w$  is the inertia weight;  $c_1$   $c_2$  are acceleration coefficients;  $r_{1j} \sim U(0, 1)$  and  $r_{2j} \sim U(0, 1)$  are used to effect the stochastic nature of the algorithm. In order to reduce the likelihood of the particle leaving the search space, the value of each dimension of every particle velocity is clamped to the range  $[-v_{j\max}, v_{j\max}]$ . The value of  $v_{\max}$  is usually chosen to be  $k\mathbf{x}_{\max}$ , with  $0.1 \leq k \leq 1$ , where  $\mathbf{x}_{\max}$  denoted the domain of search space.

## 2.2 Improved PSO Method

Paper [10] by *Boeringer et al.* investigated PSO and other evolutionary computation then he pointed out that PSO attractive features include the ease implementation and fast convergence, but it is also inclined to convergence at the local optimization solution. Yi-xiong Jin further analyzed this phenomenon then he concluded that with the process of evolution, the global best position is lack of self-evolution and whole population evolution halt lead to this [11]. To solve this problem, the author suggested an improved PSO method. If the global best position has not been changed for some generations, this position should be looked as a local optimum solution and the following searches around this point should be nonsense. So the searching space around this point within the specified radius should be locked to prevent other particles flying into. And the particles already locate in this space should die and be replaced with the new particles yielded randomly to keep the total number of the population unchanged. When the whole iteration finished, one or more of this kind local optimum position are acquired. The approximate global optimum solution can be determined after compare the fitness of these saved particles or making a deeply search around them.

When calculate the particles fitness, the traditional method always take penalty function to handle constraint conditions. It needs experience and patience to define the proper form of penalty function. The author of [12] suggested each particle has two fitness, objective fitness and constraint fitness and compare this two fitness to determine the particle quality. Paper [13] ranks the particle in the value of fitness and the constraint fitness has a priority than objective fitness. In this way, the feasible particle fitness is better than infeasible particle. So in the process of evolution, other particles are inclined to be attracted by feasible solution. This method can consolidate acquiring the optimum point and making particles enter into the feasible field and no need to set the proper weight of constraint fitness and objective fitness. 3 ATC Calculation With IPSO Method.



### 2.3 ATC Mathematical Model of Power System

For a power system operating with high reliability, it should satisfy three kinds of constraint, i.e., line thermal constraint, bus voltage magnitude constraint, and system stability constraints(which can be classified into static voltage stability, transient power & angle stability, dynamic power & angle stability ). In ATC calculation, different constraints considered make up of different calculation model. In this paper, two hypotheses are assumed, that is each control variant changed slowly and system has enough damping to keep the dynamic stability. So the dynamic stability problem is not concerned here. As for transient problem, it can be checked up when ATC result acquired. So the ATC model built here just satisfies the first two constraints.

As an optimization problem, the objective function can be defined as the sum of the group of generators' outputs (these generators are denoted as set S) and the group load buss' load (these buss are denoted as set R) [4]. In this way, two kinds of variants: generator's output and the bus load, are optimized and the maximum ATC value between the areas can be acquired (of course, the initial value on the tie lines will be subtracted from the optimum power value on these lines when ATC value exported). This objective function can be expressed as following equation:

$$\max f(\bullet) = \sum_{k \in S} P_{Gk} + \sum_{d \in R} P_{Ld} \quad . \quad (3)$$

The equality constraints of this model are:

$$\begin{cases} P_i - V_i \sum_{j=1}^N V_j (G_{ij} \cos \theta_{ij} + B_{ij} \sin \theta_{ij}) = 0 \\ Q_i - V_i \sum_{j=1}^N V_j (G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij}) = 0 \end{cases} \quad . \quad (4)$$

Where,  $P_i, Q_i$  are the net active power and reactive power injected into bus  $i$ ;  $V_i \angle \theta_i$  is the voltage on bus  $i$ ;  $\theta_{ij} = \theta_i - \theta_j$  is the phase difference between the voltages of bus  $i, j$ ;  $G_{ij} + jB_{ij}$  is the corresponding element in system admittance matrix and  $N$  is the total number of bus.

The net active power and reactive power injected in bus  $i$  is:

$$P_i = P_{Gi} - P_{Li}, \quad Q_i = Q_{Gi} - Q_{Li} \quad i = 1, 2, \dots, N$$

Where,  $P_{Gi}, Q_{Gi}$  are the active power and reactive power outputs of generator on bus  $i$ ;  $P_{Li}, Q_{Li}$  are the active power and reactive power of load on bus  $i$ ; other terms,  $P_{Gi} (i \notin S), P_{Li} (i \notin R), Q_{Li} (i \notin R)$  are constant;  $P_{Gi} (i \in S), P_{Li} (i \in R), Q_{Li} (i \in R)$  are variants, corresponding to the each dimension of the particles; and the load power factors are assumed as constant here.

As discussed in the first part of this section, ATC calculation model here is a power system static model. So inequality constraints, that is, bus voltage magnitude limit, line thermal stable capacity and devices capacity limit, should be satisfied. All these inequality constraints can be expressed in mathematical form as:

$$\left\{ \begin{array}{l} V_{j,\min} \leq V_j \leq V_{j,\max} \quad j = 1, 2, \dots, N \\ 0 \leq I_{ij} \leq I_{ij}^{\max} \\ P_{Gi,\min} \leq P_{Gi} \leq P_{Gi,\max} \quad i = 1, 2, \dots, N_g \\ Q_{iG,\min} \leq Q_{iG} \leq Q_{iG,\max} \\ 0 \leq P_{Lk} \leq P_{Lk\max} \quad k = 1, 2, \dots, N_l \\ Q_{Lk\min} \leq Q_{Lk} \leq Q_{Lk\max} \end{array} \right. \quad (5)$$

Where,  $N$  is the total number of buses;  $N_g$  is the total number of generators;  $N_l$  is the total number of loads;  $V_{j,\min}, V_{j,\max}$  are the bus  $j$  voltage magnitude lower limit and upper limit;  $P_{Gi,\min}, P_{Gi,\max}$  are active power lower limit and upper limit of generator  $i$ ;  $Q_{iG,\min}, Q_{iG,\max}$  are reactive power lower limit and upper limit of generator  $i$ ;  $P_{Lk,\max}, Q_{Lk,\min}, Q_{Lk,\max}$  are the upper limit and lower limit of bus  $k$ , and this three variants are determined by the capacity of distribution devices attached with bus.

## 2.4 ATC Calculation Procedure Using IPSO

As discussed above, the procedure of ATC calculation with IPSO method is:

- (1) Set the total number  $n$  of the particles in the population, acceleration coefficients  $c_1 c_2$ , inertia weight  $w$ , the maximum life *liter* of global best position, the maximum iteration times *maxiter* and the lock radius *radius*. Here,  $n = 40$ , *liter* = 20, *radius* = 5,  $c_1 = c_2 = 1.49618$ ,  $w = 0.7298$ , *maxiter* = 1000.
- (2) Input the initial data, set maximum velocity and position range of particle's each dimension, define the selling and buying area, then evaluate the initial fitness of each particles. The personal best position of each particle is the particles' initial value itself.
- (3) According to the position of each particle, calculate the solution of the power equation. If equation diverging or the slack generator's active output over its upper limit, a new particle should be yielded randomly to replace this particle and power equation should be calculated again until all particles satisfy the power equation.
- (4) Basing the calculation result of power equation, calculate the object fitness and constraint fitness of each particle. According to fitness of particles update the global best position and personal best position of each particle.
- (5) Basing the equation (1) (2) update the value of each particles. If some particles enter into the lock area, they die and should be replaced by new particles which are yielded randomly.
- (6) Compared with the last generation, if the global best position has no change, its life adds 1. If it changed, to the new global best position, its life is set 1. If the global best position life is equal with variant *liter*, this global best position should be saved as a local optimization solution. And the searching space around this point within radius of *radius* should be locked. All particles which fly into this locked space die and are replaced with the new particles yielded randomly to keep the total number of the

population unchanged. Then just like the method introduced above, define the new global best position in this new population and its life is set 1.

(7) Evaluate whether the iteration times equal *maxiter* or not. If not, go to (3).

(8) Acquire the global optimization solution. All saved best position values are compared and the best one is exported. Calculate the power equation corresponding to this best position and the power increment on the tie line between selling area and buying area is the ATC result in this case.

### 3 Case Study and Discussion

The proposed IPSO method has been test on IEEE 118 test system. The raw data of IEEE 118 test system has no line thermal capacity. Here, for the need of calculation, each line’s thermal capacity is assumed. The whole area is divided into three areas. Doing this has no any bad effect on the test validity of IPSO. Here a comparison with traditional OPF method, sequence quadratic programming (SQP), was made. Use MATLAB 7.0 to write the program and run this program on pc computer with P4 2.9G processor. The result is showed in table 1:

**Table 1.** ATC value between areas of IEEE118 system and its contrast with SQP method

| Area Pairs<br>(Selling->Buying) | ATC Result (MW) |         | Calculation CPU Time (s) |         |
|---------------------------------|-----------------|---------|--------------------------|---------|
|                                 | IPSO            | SQP     | IPSO                     | SQP     |
| 1—>2                            | 376.68          | 369.203 | 2485                     | 1482.5  |
| 1—>3                            | 768.23          | 467.68  | 2558                     | 3008.49 |
| 2—>1                            | 412.06          | 303.049 | 2471                     | 3346.46 |
| 2—>3                            | 1120.2          | 447.343 | 2581                     | 2621.59 |
| 3—>1                            | 441.64          | 239.27  | 2503                     | 2159.83 |
| 3—>2                            | 324.89          | 368.31  | 2495                     | 2177.69 |

Table 1 shows that IPSO method can be used to solve ATC problem. Compared with SQP, IPSO can find the much better solution than the latter. And the number of the saved best particles shows that IPSO is inclined to converge at its local optimization point. The method presented in this paper can choose the best one of the all saved local optimization solution as the approximate global optimization solution. And the space around this local best point is locked to prevent other particles flying into it. In this way, the drawback of PSO method can be avoided.

But from the last field of the table 1, the time consumed in IPSO is also unbearable. This will limit the IPSO method application to ATC online calculation. But for some special case, this method can be used to get the maximum ATC value between areas and the result can be used as a signal to guide the system operators dispatching.

## 4 Conclusion

Different from the traditional OPF method basing on Newton criteria, IPSO method is introduced in this paper to solve the ATC problem in power system. Numerical simulation on IEEE 118 test system indicates that this method can solve the ATC problem and the much better solutions are acquired. This result can be used as a guidance signal to system operators dispatching.

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# An Improved Particle Swarm Optimization Algorithm with Disturbance Term

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**Abstract.** The standard particle swarm optimization (PSO) algorithm, existing improvements and their influence to the performance of standard PSO are introduced. The framework of PSO basic formula is analyzed. Implied by its three-term structure, the inherent shortcoming that trends to local optima is indicated. Then a modified velocity updating formula of particle swarm optimization algorithm is declared. The addition of the disturbance term based on existing structure effectively mends the defects. The convergence of the improved algorithm is analyzed. Simulation results demonstrated that the improved algorithm have a better performance than the standard one.

## 1 Introduction

The particle swarm optimization (PSO) is an optimization algorithm based on swarm intelligence theory, introduced by Kennedy and Eberhart[1], which developed out of work simulating the movement of flocks of birds. It guides optimization search through swarm intelligence produced by cooperation and competition of the particles. Compared to evolutionary computation techniques, PSO reserved global search strategy based on swarm, but its model implement more easily and avoid complicated genetic operation[2]. Its peculiar memory function gives it the ability to adjust its search strategy dynamically by tracing the current search condition. So it is a more efficiency parallel stochastic search algorithm than evolutionary algorithm.

PSO is initialized with a group of random solutions of the objective function. The individuals in the group are called as particles. Each particle has its own position  $x$ , transfer vector  $v$ , and its own  $p$  which represents the best position visited by the particle so far. All particles share  $pg$ , or the best position visited by all the particles so far. A particle forms a new transfer vector and position by tracing the two “best” values. The following equations characterized the particle’s movement of PSO:

$$v_{id}^{k+1} = w \times v_{id}^k + c_1 \times r_1 \times (p_{id} - x_{id}^k) + c_2 \times r_2 \times (pg_d - x_{id}^k). \quad (1)$$

$$x_{id}^{k+1} = x_{id}^k + v_{id}^{k+1}. \quad (2)$$

Where  $w$  is called the inertia weight in the (0,1) range,  $c_1, c_2$  are learning parameters, the most common setting is  $c_1 = c_2 = 2$ ,  $r_1, r_2$  is a number chosen randomly from the uniform distribution in the (0,1) range. The value of  $v$  is clamped to the range  $[-v_{\max}, v_{\max}]$  to reduce the likelihood that the particle might leave the search space.

The PSO algorithm is simple in concept, easy to implement and computational efficient. The pseudocode for a PSO procedure is as following:

```

Begin;
Generate random population of N solutions (particles);
 For each individual $i \in N$: calculate fitness (i);
 Initialize the value of the weight factor, w ;
 For each particle;
 Set p_i as the best position of
particle i;
 If fitness (i) is better than p_i ;
 $p_i = \text{fitness (i)}$;
 End;
 Set pg as the best fitness of all particles;
 For each particle;
 Calculate particle velocity
according to Eq. (1);
 Update particle position according
to Eq. (2);
 End;
 Update the value of the weight factor, w ;
Check if termination = true;
End

```

Like the other evolutionary algorithms, PSO is a population based search algorithm with random initialization, and there are interactions among population members. Unlike the other evolutionary algorithms, in PSO, each particle flies through the solution space, and has the ability to remember its previous best position, survives from generation to generation. Furthermore, compared with the other evolutionary algorithms, e.g. evolutionary programming, the original version of PSO is faster in initial convergence while slower in fine tuning[3],[4].

## 2 An Analysis to the Formula of Standard PSO

The new velocity  $V_{id}^{k+1}$  in equation can be seen as a sum of three terms. The first term  $w \times V_{id}^k$  is just the current velocity of the particle and can be thought of as a momentum term. The second term  $c_1 \times r_1 \times (p_{id} - x_{id}^k)$ , which is associated with a local search, is proportional to the vector  $(p_{id} - x_{id}^k)$  and points from the particle's current position back towards its personal best position. The third term  $c_2 \times r_2 \times (pg_d - x_{id}^k)$ , which is associated with a global search, is proportional to  $(pg_d - x_{id}^k)$  and points towards the global best position. The cooperation of the three terms make particle change its own velocity and position stochastically when particle trace the individual best position and global best position, and then realize global and local search.

## 3 The Inherent Shortcoming of Standard PSO and Its Improvements

It is found from the velocity equation that the whole searching process of PSO is the process that particle depends on its "memory" ability and share information mechanism to trace the present best solution with some stochastic. In the early stage of the algorithm, because the individual best position  $p$  and global best position  $pg$  change frequently, the algorithm has strong global search ability and converges rapidly. But at the end stage of the algorithm, because of the relative stabilization of  $p$  and  $pg$  as well as the "compatibility" of particles, the velocity of particle will primarily determined by the first term and become smaller and smaller until drop down to zero. At this moment the position updating gets into stagnation state, and finally makes the algorithm only get local optima. More important the standard PSO algorithm can't drive particles get rid of that state. It is the main shortcoming of the standard PSO algorithm.

In order to improve this shortcoming and get better results, numerous improvements to the standard PSO have been proposed. These improvements probably can be separated into two types. The first type, such as inertia weight[5], fuzzy inertia weight[6], stochastic inertia weight, adaptive inertia weight[7] and so on, is to change the inertia weight  $w$  to make the algorithm has strong global searching ability in the early and also strong local searching ability in the evening. The second type tries to change the structure of the algorithm or associated with other optimization algorithms (e.g. genetic algorithm) such as Constriction factor<sup>[8]</sup>, sequential niche technique[9], PSO with area of influence[10], Parallelizing PSO[11] and so on. Compared to the standard algorithm, these improved PSO always have better performance. But these improvements either can be applied in some aspects only or must design it's parameters in advance when used in practical problem. Especially these improvements didn't change the three terms composed structure of standard PSO, that's the reason that they can't solve the shortcoming of standard PSO thoroughly.

On account of the reason mentioned above, this paper presents a improved particle swarm optimization algorithm (PSO-DT) which add a disturbance term to the velocity updating equation based on the prototype of the standard PSO trying to improve (or avoid) the shortcoming of standard PSO. Of course, the PSO-DT doesn't exclude the improvement methods introduced above if they are indeed effective.

It must be pointed out that before our work several papers have used disturbance to improve the performance of Standard PSO. The typical papers are PSO with passive congregation[12] (PSOPC) and PSO with disturbance[13] (PSOD). In PSOD, it judge whether premature phenomenon occur and initialize the particle position entirely when it's true. Because this method throws over all former information of Particles, experiments show it can't get better performance. Compared to PSOPC, the method proposed by this paper realizes more easily and almost have the same effect to PSOPC.

#### 4 The Improved PSO with Disturbance Term (PSO-DT)

Velocity updating equation:

$$V_{id}^{k+1} = w \times V_{id}^k + c_1 \times r_1 \times (p_{id} - x_{id}^k) + c_2 \times r_2 \times (p_{gd} - x_{id}^k) + a \times (r_3 - 0.5). \quad (3)$$

We call  $a \times (r_3 - 0.5)$  as disturbance term.

Position updating equation:

$$x_{id}^{k+1} = x_{id}^k + v_{id}^{k+1}. \quad (4)$$

Where  $a$  is a small constant,  $r_3$  is a number randomly distribution in the (0, 1) range, the others parameters is the same as standard PSO.

In the early calculation, because  $a$  is very small compared to anterior three terms, and the mean value of  $(r_3 - 0.5)$  equal to zero, the disturbance term even can be ignored since it exert little impact on the updating and searching capability of the whole optimization. While in the middle and later phases, when the velocity becomes slower and slower, the disturbance term ensures the searching velocity of particles will not drop down to zero, and as a result, the optimization will not stagnate, thus enabling the update to continue and overcoming the defects of easily falling into local optima of the standard PSO, therefore getting a more exact solution.

In order to testify what analyzed above, we take a simple simulation.

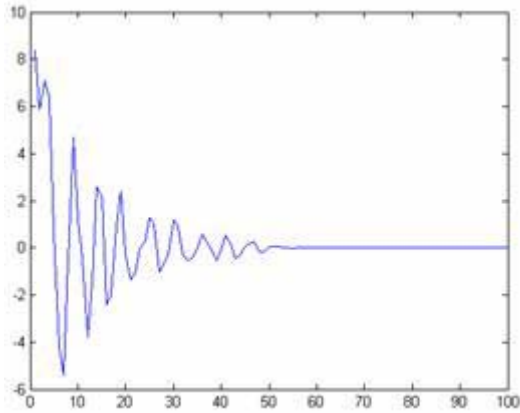
Given function:

$$f(x) = 3x^2 + 2x + x^2 \sin x \quad x_i \in [-10, 10].$$

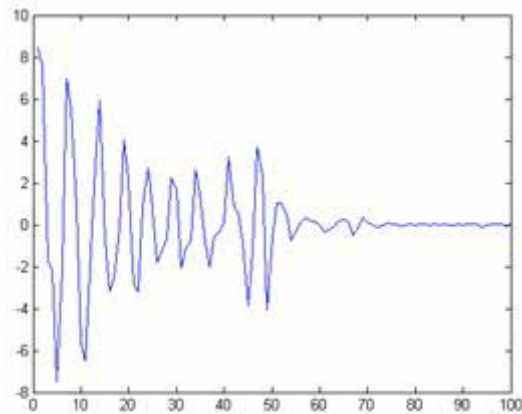
Simulate particle velocity according to equation (1) and (3). Set parameter value  $a = 0.04$ ,  $c_1 = c_2 = 2$ ,  $w_{\max} = 0.9$ ,  $w_{\min} = 0.4$ , generations=100. For the sake of watching conveniently, we set one particle only. Fig.1 and Fig.2 show the search curve of the standard PSO algorithm and PSO-DT algorithm respectively.



It is found from Fig.1 and Fig.2 that both standard PSO and PSO-DT have strong global search ability in the early stage of the algorithm. But the velocities of standard PSO algorithm decrease very quickly and equal to zero after 50 generations. However, because of the effect of the disturbance term, the velocity of PSO-DT decreases more reasonable. Even after 70 generations, the velocities of PSO-DT still not drop down to zero, as a result the searching processing continues.



**Fig. 1.** Search curve of the standard PSO



**Fig. 2.** Search curve of the PSO-DT

The inherent drive for searching in particle swarm optimization is its randomness, so the participation of the disturbance term conforms to this principle. Experiments show that when the value of  $a$  is between 0 and 1, better performance than standard PSO can be realized.

## 5 Convergence Analysis of PSO-DT

Equations (3) and (4) which determine the behavior of particles are so complicated that we cannot analyze them as they are. Therefore we notice only one dimension of one particle, vector notation can be thrown out, and equations (3) can be transformed:

$$v^{k+1} = w \times v^k + (\Phi_1 + \Phi_2) \times (p - x^k) + c. \quad (5)$$

Where

$$c_1 \times r_1 = \Phi_1, c_2 \times r_2 = \Phi_2, \text{ and } a \times (r_3 - 1) = c$$

Then assume

$$\Phi_1 + \Phi_2 = \Phi, p - x^k = y^k$$

Now equations (5) and (3) become:

$$v^{k+1} = w \times v^k + \Phi \times y^k + c. \quad (6)$$

$$y^{k+1} = -w \times v^k + (1 - \Phi) \times y^k. \quad (7)$$

Transform (6) and (7) to matrix form:

$$\begin{bmatrix} v^{k+1} \\ y^{k+1} \end{bmatrix} = \begin{bmatrix} w & \Phi \\ -w & 1 - \Phi \end{bmatrix} \begin{bmatrix} v^k \\ y^k \end{bmatrix} + \begin{bmatrix} c \\ 0 \end{bmatrix} = M \begin{bmatrix} v^k \\ y^k \end{bmatrix}. \quad (8)$$

Moreover, by using matrix Q which is diagonalization matrix of M and  $\lambda$  which is an eigenvalue of M, this equation can be transformed as:

$$\begin{bmatrix} v^k \\ y^k \end{bmatrix} = Q \begin{bmatrix} \lambda_1^k & 0 \\ 0 & \lambda_2^k \end{bmatrix} Q^{-1} \begin{bmatrix} v^0 \\ y^0 \end{bmatrix} + \begin{bmatrix} c \\ 0 \end{bmatrix}. \quad (9)$$

Where

$$\lambda_{1,2} = \frac{w + 1 - \Phi \pm \sqrt{(w + 1 - \Phi)^2 - 4w}}{2}. \quad (10)$$

Equation (9) indicates that the condition in which a particle convergence is  $|\lambda| < 1$ . All of the above equations conclude that when equations (11) and (12) are satisfied, the dynamics of a particle become convergent, otherwise they becomes divergent.

$$0 < \Phi < 2 \times w + 2. \quad (11)$$

$$0 \leq w < 1. \quad (12)$$

Analysis above indicates that the convergence condition of PSO-DT is the same to standard PSO, that's to say, the improved particle swarm optimization algorithm doesn't change the convergence condition of standard particle swarm optimization algorithm.

## 6 Simulation and Discussion

To test the performance of PSO-DT, some well-studied benchmark functions have been used. These benchmark functions stated as follows:

(1) Rosenbrock :

$$f_1(x) = \sum_{i=1}^{n-1} (100(x_{i+1} - x_i^2)^2 + (x_i - 1)^2) \quad x_i \in [-30, 30]$$

(2) Rastrigrin :

$$f_2(x) = \sum_{i=1}^n (x_i^2 - 10 \cos(2\pi x_i) + 10) \quad x_i \in [-5.12, 5.12]$$

(3) Griewank :

$$f_3(x) = \frac{1}{4000} \sum_{i=1}^n x_i^2 - \prod_{i=1}^n \cos\left(\frac{x_i}{\sqrt{i}}\right) + 1 \quad x_i \in [-100, 100]$$

(4) This function is proposed by paper [14], and has been studied by many papers:

$$\begin{aligned} \min_{x,y} f_4(x, y) &= 0.6224(0.0625y_1)x_1x_2 + 1.7781(0.0625y_2)x_1^2 \\ &\quad + 3.1661(0.0625y_1)^2x_2 + 19.84(0.0625y_1)^2x_1 \end{aligned}$$

s.t.

$$g_1(x, y) = 0.0193x_1 - 0.0625y_1 \leq 0$$

$$g_2(x, y) = 0.00954x_1 - 0.0625y_2 \leq 0$$

$$g_3(x, y) = 750 \times 1728 - \pi x_1^2 x_2 - 4\pi x_1^3 / 3 \leq 0$$

$$g_4(x, y) = x_2 - 240 \leq 0$$

In our tests the dimensions of function (1), (2) and (3) is 30. And swarm size of 30 is used in each experiment. The maximum numbers of iterations allowed is 5000. Both standard PSO and PSO-DT have used the inertia weights approach. Where  $c_1 = c_2 = 2$ ,  $w_{\max} = 0.9$ ,  $w_{\min} = 0.4$ .

The following tables show the experiment results of the two version's PSO to benchmark functions listed above. Where ET (excellent times) express the times that simulation results is better than given value. The given value of function 1,2,3,4 respectively is: 100, 20, 0.02, and 6050. Each algorithm for each of the functions executed 20 times.

**Table 1.** Results for standard PSO

| func  | Best     | Worst    | Mean       | ET | St Dev   |
|-------|----------|----------|------------|----|----------|
| $f_1$ | 48.32888 | 257.8889 | 143.654768 | 8  | 73.2364  |
| $f_2$ | 14.92438 | 35.8185  | 24.475976  | 6  | 6.6187   |
| $f_3$ | 0        | 0.083067 | 0.0175379  | 16 | 0.0230   |
| $f_4$ | 5942.451 | 6487.137 | 6150.44682 | 8  | 157.8443 |

**Table 2.** Results for PSO with disturbance term

| func  | Best     | Worst    | Mean        | ET | St Dev   |
|-------|----------|----------|-------------|----|----------|
| $f_1$ | 25.18652 | 152.4703 | 75.169113   | 14 | 41.8212  |
| $f_2$ | 10.99649 | 26.92238 | 19.415621   | 15 | 4.9320   |
| $f_3$ | 0        | 0.039353 | 0.0114451   | 17 | 0.0115   |
| $f_4$ | 5921.023 | 6266.626 | 6032.225161 | 15 | 102.9788 |

The tables show that PSO-DT has better performances in all problems compared to standard algorithm.

## 7 Conclusion

Based on the analysis of the standard PSO algorithm, the shortcoming of standard PSO has been introduced. To solve the shortcoming a disturbance term has been added to the basic velocity updating formula. Analysis indicates that the improved PSO has the same convergence conditions with standard PSO algorithm. Simulation experiments have been carried out and results show that the proposed algorithm have better performances on all benchmark functions. Then the feasibility and the advantage of the improved PSO are demonstrated.

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# Blending Scheduling Under Uncertainty Based on Particle Swarm Optimization with Hypothesis Test

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**Abstract.** Blending is an important unit operation in process industry. As a nonlinear optimization problem with constraints, it is difficult to obtain optimal solution for blending scheduling, especially under uncertainty. As a novel evolutionary computing technique, particle swarm optimization (PSO) has powerful ability to solve nonlinear optimization problems with both continuous and discrete variables. In this paper, the performance of PSO under uncertainty for blending scheduling problem is investigated, and a new hybrid approach (namely PSOHT) that combines PSO and hypothesis test (HT) is proposed. The simulation results based on an example of gasoline blending problem show that the proposed PSOHT algorithm is valid and effective for solving problem under uncertainty.

## 1 Introduction

Blending is a crucial step in process industry. The process involves the mixing of various stocks, which are the intermediate products from the refinery, along with some additives, such as antioxidants and corrosion inhibitors, to produce blends with certain qualities. It represents nonlinear programs with mass balance constraints, nonlinear blending properties and combinatorial aspects, etc. And the optimal scheduling is considered as an objective, which is very hard to achieve in process industry. In order to satisfy the economic objectives, blending scheduling is defined as the short-term manipulation of the maximization of the product profit, where the blended property is not a linear function of the inlet properties [1]. Moreover, for most optimization problems, uncertainties should be taken into account. As to scheduling problem, four types of uncertainty are mentioned: market uncertainty, process uncertainty, measurement uncertainty and model uncertainty [2].

In these days, linear programming (LP) strategies are often applied to deal with nonlinear problems, but they have some shortcomings in terms of robustness and convergence. Besides, non-linear programming (NLP) approaches do not provide a straightforward extension to handle discrete combinatorial elements in blending [2]. As a parallel search algorithm, genetic algorithm (GA) is applied to improve the fitness of a population and to discover the solution space related to a problem. It was applied to solve the task of gasoline fractions blending compounding keeping given conditions on octane numbers and amount of given types of commodity gasoline [3], but the problem of gasoline blending was simplified to linear relations.

Particle swarm optimization (PSO), as an alternative to GA, can be successfully applied in areas where GA can be applied. Compared with GA, PSO has memory, so knowledge of good solutions is retained by all particles. Whereas in GA, previous knowledge of the problem is destroyed, once the population changes. PSO has constructive cooperation between particles, particles in the swarm share information between them. Due to the simple concept, easy implementation and quick convergence, PSO algorithm shows good efficiency for many benchmark functions. And it also shows that PSO can deal with many kinds of optimization problems subject to constraints. In this paper, a hybrid PSO named PSOHT (Particle swarm optimization with hypothesis test) is proposed to solve the blending scheduling with uncertainty, where hypothesis test (HT) is used to compare solutions in uncertain environment, and to reserve good solutions for new swarm, and to maintain the diversity of the swarm.

The organization of the remaining content is as follows. In Section 2, we provide the mathematical formulation of blending scheduling problem. And in Section 3 we discuss the blending scheduling problem under uncertainty. In Section 4 we present the hybrid algorithm after briefly introducing PSO and hypothesis test. Then, in Section 5 we provide a blending scheduling problem for testing. Simulation results are provided in Section 6. Finally, we end with some conclusions.

## 2 Mathematical Formulation of Blending Scheduling

The blending scheduling problem is a nonlinear optimization problem, which can be generally formulated as follows:

$$\max_{x \in X} f(x), \quad s.t. \quad g(x) \leq 0. \quad (1)$$

where  $x = (x_c, x_d) \in R^{n_c} \times Z^{n_d}$  denotes decision variable, and  $f : R^{n_c} \times Z^{n_d} \rightarrow R$  is objective function, and  $X_c = \{x \in R^{n_c} \mid y^i \leq x^i \leq u^i, i \in \{1, 2, \dots, n_c\}\}$  denotes continuous variable, and the constraint set  $X_d = \{x \in Z^{n_d}\}$  contains the discrete non-zero integer variable, and  $g : R^{n_c} \times Z^{n_d} \rightarrow R^m$  denotes inequality constraints. The aim is to find an optimal solution  $x^* \in X$  that satisfies  $g(x^*) \leq 0$ .

Usually, constraints are taken into account as penalty functions to the objective function, which are multiplied by a positive weighting factor  $\mu$  that is monotonically increased. Penalty functions allow crossing the boundary of the feasible set and implementation of equality constraints. Penalty functions add a positive term to the objective function if a constraint is violated. To implement a penalty function for  $g(x) \leq 0$ , the objective function can be modified as [4]:

$$\tilde{f}(x, \mu) = f(x) + \sum_{i=1}^m \mu_i \cdot \min(0, g^i(x))^2. \quad (2)$$

### 3 Blending Scheduling Under Uncertainty

By adding a penalty term intended to minimize parametric sensitivity to the objective function, optimization problem of blending scheduling is developed. In addition, under uncertainty it needs to consider the feasibility of the constraints at an optimal solution for stochastic constraints. And a function penalizing violation of the constraints is enforced when constraints are not met. The penalty framework provides a mechanism for varying the feasibility requirements, ensuring operational flexibility with respect to the nonlinear constraints under uncertainty. The penalty parameter provides a trade-off between computational effort and accuracy of constraint satisfaction.

Based on Eq. (1), the optimization problem of blending scheduling under uncertainty can be formulated as follows:

$$\max_{u \in X} f(u, \theta), \quad s.t. \quad g(u, \theta) \leq 0. \quad (3)$$

where  $u \in R^n$  denotes a vector of decision variables, and  $\theta$  denotes the uncertain information in the objective function, and  $f$  denotes an objective function, and  $g$  denotes a set of constraints.

Ideally, it expects that optimization algorithm works on the expected value  $f$  while not be misled by uncertainty. Since the expected value  $f$  cannot be estimated precisely with limited evaluations, in practice multiple samplings are used to calculate the following mean sum of a number of random samples  $f(u, \theta)$  as a replacement for  $f$ .

$$J(u) = \frac{1}{n} \sum_{i=1}^n f(u, \theta_i). \quad (4)$$

where  $n$  is sample size or evaluation number.

Thus, Eq. (3) can be transformed as follows:

$$\max_{u \in X} J(u) = E[f(u, \theta)], \quad s.t. \quad g(u, \theta) \leq 0. \quad (5)$$

Taken into account the constraints by adding penalty functions as Eq. (2) under uncertainty, the problem can be described as follows:

$$\hat{J}(u, \mu, ) = \frac{1}{n} \sum_{i=1}^n [f(u, \theta_i) + \sum_{j=1}^m \mu_j \cdot \min(0, g^j(u, \theta_i))^2]. \quad (6)$$

Taking  $\hat{J}(u, \mu, )$  as a replacement for the objective function  $J(u)$  under uncertainty, we can apply PSO to the uncertain optimization problem mentioned above. Obviously, it is worthy studying the optimization performance and robustness of PSO when uncertainty with different magnitude is present and limited sampling number is allowed. Next, a hybrid PSO-based approach will be proposed to for optimization under uncertainty.



## 4 Particle Swarm Optimization with Hypothesis Test

In this section, we will propose a hybrid PSO approach named PSOHT by combining PSO with hypothesis test (HT) optimization under uncertainty. Firstly, we briefly introduce PSO and HT.

### 4.1 Particle Swarm Optimization

The theoretical framework of PSO is very simple, and PSO is easy to be coded and implemented with computer [5]. Besides, it is computationally inexpensive in terms of memory requirements and CPU times. Thus, nowadays PSO has gained much attention and wide applications in various fields [5, 6].

PSO starts with the random initialization of a swarm of particles in the search space and works on the social behavior of the particles in the swarm. Therefore, it finds the global best solution by simply adjusting the trajectory of each individual towards its own best location and towards the best particle of the swarm at each time step. However, the trajectory of each individual in the search space is adjusted by dynamically altering the velocity of each particle, according to its own flying experience and the flying experience of the other particles in the search space.

The position and the velocity of the  $i$  th particle in the  $d$ -dimensional search space can be represented as  $X_i = [x_{i,1}, x_{i,2}, \dots, x_{i,d}]$  and  $V_i = [v_{i,1}, v_{i,2}, \dots, v_{i,d}]$  respectively. Each particle has its own best position (*pbest*)  $p_i = (p_{i,1}, p_{i,2}, \dots, p_{i,d})$  corresponding to the personal best objective value obtained so far at time  $t$ . The global best particle (*gbest*) is denoted by  $p_g = (p_{g,1}, p_{g,2}, \dots, p_{g,d})$ , which represents the best particle found so far at time  $t$  in the entire swarm. The new velocity of each particle is calculated as follows:

$$v_{i,j}(t+1) = wv_{i,j}(t) + c_1r_1(p_{i,j} - x_{i,j}(t)) + c_2r_2(p_{g,j} - x_{i,j}(t)), j=1,2,\dots,d. \quad (7)$$

where  $c_1$  and  $c_2$  are constants called acceleration coefficients,  $w$  is called the inertia factor,  $r_1$  and  $r_2$  are two independent random numbers uniformly distributed in the range of  $[0, 1]$ .

The inertial weight factor  $w$  provides the necessary diversity to the swarm by changing the momentum of particles and hence avoids the stagnation of particles at local optima. Usually, it needs to define a maximum velocity for each modulus of velocity vector, which is often set as the upper limit of the each modulus of position vector. This helps to control the unnecessary excessive roaming of particles outside the predefined search space. Thus, the position of each particle is updated in each generation according to the following equation:

$$x_{i,j}(t+1) = x_{i,j}(t) + v_{i,j}(t+1), \quad j=1,2,\dots,d. \quad (8)$$

The procedure of standard PSO can be summarized as follows:

*Step 1:* Initialize a population of particles with random positions and velocities, where each particle contains  $d$  variables.

*Step 2:* Evaluate the objective values of all particles, let  $pbest$  of each particle and its objective value equal to its current position and objective value, and let  $gbest$  and its objective value equal to the position and objective value of the best initial particle.

*Step 3:* Update the velocity and position of each particle according to Eqs. (7) and (8).

*Step 4:* Evaluate the objective values of all particles.

*Step 5:* For each particle, compare its current objective value with the objective value of its  $pbest$ . If current value is better, then update  $pbest$  and its objective value with the current position and objective value. Furthermore, determine the best particle of current swarm with the best objective value. If the objective value is better than the objective value of  $gbest$ , then update  $gbest$  and its objective value with the position and objective value of the current best particle.

*Step 6:* If a predefined stopping criterion is met, then output  $gbest$  and its objective value; otherwise go back to Step 3.

## 4.2 Hypothesis Test

Hypothesis test (HT) is an important statistical technique used to make test for predefined hypothesis using experiment data [7, 8]. To perform HT for two different decision solutions when solving uncertain optimization problems, it often needs multiple independent evaluations to provide suitable performance estimations. If  $n_i$  independent simulations are carried out for solution  $X_i$ , then its unbiased estimated mean value  $\bar{J}_i$  and variance  $s_i^2$  can be calculated as follows:

$$\bar{J}_i = \bar{L}(X_i) = \sum_{j=1}^{n_i} L(X_i, \xi_j) / n_i. \quad (9)$$

$$s_i^2 = \sum_{j=1}^{n_i} [L(X_i, \xi_j) - \bar{J}_i]^2 / (n_i - 1). \quad (10)$$

Considering two different solutions  $X_1$  and  $X_2$ , whose estimated performances  $\hat{J}(X_1)$  and  $\hat{J}(X_2)$  are two independent random variables. According to the law of large number and central limit theorem, the estimation  $\hat{J}(X_i)$  subjects to  $N(\bar{J}_i, s_i^2 / n_i)$  when  $n_i$  approaches to  $\infty$ . Suppose  $\hat{J}(X_1) \sim N(\mu_1, \sigma_1^2)$  and  $\hat{J}(X_2) \sim N(\mu_2, \sigma_2^2)$ , where the unbiased estimations of  $\mu_1$ ,  $\mu_2$  and  $s_1^2$ ,  $s_2^2$  are given by Eqs. (9) and (10), and let the null hypothesis  $H_0$  be “ $\mu_1 = \mu_2$ ” and the alternative hypothesis  $H_1$  be “ $\mu_1 \neq \mu_2$ ”. If  $\sigma_1^2 = \sigma_2^2 = \sigma^2$  and  $\sigma^2$  is unknown, then the critical region of  $H_0$  is described as follows:

$$|\bar{J}_1 - \bar{J}_2| \geq t_{\alpha/2}(n_1 + n_2 - 2) \cdot \sqrt{\frac{n_1 + n_2}{n_1 n_2}} \cdot \sqrt{\frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}} = \tau. \quad (11)$$

Thus, if  $|\bar{J}_1 - \bar{J}_2| < \tau$ , i.e., the null hypothesis holds, then it can be regarded that the performances of those two solutions have no significant difference in statistical sense, otherwise they are significantly different. Furthermore, for uncertain minimization problem it is assumed that  $X_2$  is better than  $X_1$  if  $\bar{J}_1 - \bar{J}_2 \geq \tau$ , while  $X_1$  is better than  $X_2$  if  $\bar{J}_1 - \bar{J}_2 \leq -\tau$ . In addition, for a specific problem it often supposes that the theoretical performance variances of all solutions are the same [7,8], so the hypothesis test can be made according to Eq. (11). For a multi-modal stochastic optimization problem, repeated search can be avoided to some extent by applying HT to search process, but pure blind search with comparison under hypothesis test can often be trapped into local optima. Since PSO is of good performances for continuous deterministic optimization problems, it motivates us to investigate the performance of PSO by combining HT for uncertain optimization.

### 4.3 The Framework of PSOHT for Optimization Under Uncertainty

Based on the above description, we know that the population-based search mechanism of PSO can be applied for well exploration and exploitation among solution space, and HT can be used to reserve good particles for new swarm and to reduce repeated search, so as to maintain the quality and diversity of the new swarm. Thus, we propose a hybrid PSO approach named PSOHT for optimization under uncertainty, whose optimization procedure is described as follows:

- Step 1:* Initialize a population of  $N$  particles with random positions and velocities.
- Step 2:* Estimate the objective values of all particles for sampling  $n$  times. Then, determine the *pbest* of each particle and the *gbest* of the swarm.
- Step 3:* Update the velocity and position of each particle according to Eqs. (7) and (8).
- Step 4:* Estimate the objective values of new positions for sampling  $n$  times. Then, update the *pbest* of each particle.
- Step 5:* Use HT to form the new swarm:
  - Step 5.1:* Order all particles both with the old positions and with the new positions from the best to the worst, and denote them sequentially by  $\theta_1, \theta_2, \dots, \theta_{2N}$ . Let  $m = 1$ ,  $j = 2$ , and put  $\theta_1$  into the next swarm and denote it as  $\theta_m$ .
  - Step 5.2:* Perform hypothesis test for  $\theta_j$  with  $\theta_m$  which is in the next swarm. If the null hypothesis holds, i.e. Eq. (9) does not hold, then  $\theta_j$  is discarded; otherwise,  $\theta_j$  is put into the next swarm denoted as  $\theta_{m+1}$  and let  $m = m + 1$ .
  - Step 5.3:* If  $m < N$  and  $j < 2N$ , then let  $j = j + 1$  and go to Step 5.2; otherwise go to Step 5.4.

*Step 5.4:* If  $m = N$ , it means that the new swarm has been formed; otherwise, generate  $N - m$  new particles randomly and evaluate them  $n$  times to form the new swarm.

*Step 5.5:* Update the *gbest* of the swarm if necessary.

*Step 6:* If a predefined stopping criterion is met, then output the *gbest* and its estimated objective value and the expected objective value by large number of simulations; otherwise go back to Step 3 to perform the PSO-based search.

It can be seen from the above procedure that, the PSOHT inherits the fundamental population-based searching framework of PSO. Secondly, HT can reserve the best solutions and maintain the diversity of the next swarm by deleting some particles with similar performances, which is also useful to reduce repeated search to some extent. In a word, both the search element and the evaluation element are simultaneously considered in PSOHT for optimization problem under uncertainty.

## 5 Formulation of Blending Using PSO

Blending applications can also be found in several variations throughout all branches of process industry. One notable example is the important application of the gasoline blending. Gasoline is one of the most important refinery products as it can yield 60%—70% of total revenue of a typical refinery's [9]. Gasoline blending is the process of combining a number of components, produced by other refinery process units, together with small amounts of additives to make a mixture meeting certain

**Table 1.** Component data

| Component                     | Reformate | LSR naphtha | n-Butane | Catalytic gas | Alkyl ate |
|-------------------------------|-----------|-------------|----------|---------------|-----------|
| <i>RON</i>                    | 94.1      | 70.7        | 93.8     | 92.9          | 95.0      |
| <i>MON</i>                    | 80.5      | 68.7        | 90.0     | 80.8          | 91.7      |
| olefin, %                     | 1.0       | 1.8         | 0        | 48.8          | 0         |
| aromatics, %                  | 58.0      | 2.7         | 0        | 22.8          | 0         |
| <i>RVP</i> , psi              | 3.8       | 12.0        | 138.0    | 5.3           | 6.6       |
| Available, $bbl \cdot d^{-1}$ | 12000     | 6500        | 3000     | 4500          | 7000      |
| cost, $\$ \cdot bbl^{-1}$     | 34.0      | 26.0        | 10.3     | 31.3          | 37.0      |

**Table 2.** Production Requirements

|                            | regular | premium |
|----------------------------|---------|---------|
| value, $\$ \cdot bbl^{-1}$ | 33.00   | 37.00   |
| Max, $bbl \cdot d^{-1}$    | 8000    | 10000   |
| Min, $bbl \cdot d^{-1}$    | 7000    | 10000   |
| Min <i>RON</i>             | 88.5    | 91.5    |
| Min <i>MON</i>             | 77.0    | 80.0    |
| Max <i>RVP</i>             | 10.8    | 10.8    |

quality specifications. The flow sheet of gasoline blending is shown in [4]. And the component data and production requirements are extracted from the published results of gasoline blending in [10], as shown in Table 1 and Table 2.

The objective function of the blending scheduling is formulated as follows:

$$\begin{aligned}
 f(x) &= 33.0y_1 + 37.0y_2 - 34.0(x_1 + x_6) - 26.0(x_2 + x_7) \\
 &\quad - 10.3(x_3 + x_8) - 31.3(x_4 + x_9) - 37.0(x_5 + x_{10}), \\
 \text{s.t. } y_1 &= x_1 + x_2 + x_3 + x_4 + x_5, \\
 y_2 &= x_6 + x_7 + x_8 + x_9 + x_{10}, \\
 7000 &\leq y_1 \leq 8000, y_2 = 10000, x_i \geq 0, \\
 RON_1 &\geq 88.5, MON_1 \geq 77, RVP_1 \geq 10.8, \\
 RON_2 &\geq 91.5, MON_2 \geq 80, RVP_2 \geq 10.8.
 \end{aligned}
 \tag{12}$$

Specifications on gasoline qualities include Octane Number, Volatility, Sulphur Content, Aromatics Content, Reid Vapor Pressure (*RVP*) and Viscosity etc. As the most important quality index of gasoline products, Research Octane Number (*RON*), Motor Octane Number (*MON*) and *RVP* are constraints with nonlinear property correlations in the process of blending scheduling. By contrast with predictive components octane properties of other methods, the ethyl RT-70 models have higher prediction accuracy [11]. They are found to exhibit the best combination of predictive accuracy and parsimony for Octane Numbers, and therefore adopted to represent the mixing rules for Octane Numbers, namely,

$$RON_{blend} = \bar{r} + a_1(\bar{rs} - \bar{r} \cdot \bar{s}) + a_2(\bar{O}^2 - \bar{O}^2) + a_3(\bar{A}^2 - \bar{A}^2). \tag{13}$$

$$MON_{blend} = \bar{m} + a_4(\bar{ms} - \bar{m} \cdot \bar{s}) + a_5(\bar{O}^2 - \bar{O}^2) + a_6[(\bar{A}^2 - \bar{A}^2)/100]^2. \tag{14}$$

The *RVP* model adopted to represent the blending process is the blending index approach that has the following form:

$$\begin{aligned}
 RVPBI &= (RVP)^{1.25}, \\
 (RVPBI)_{blend} &= \sum_{i=1}^n (RVPBI)_i.
 \end{aligned}
 \tag{15}$$

where *r* denotes *RON*, *m* denotes *MON*, *s*=*r*-*m*, *O* denotes the olefin content, *A* denotes the aromatics content. Moreover,  $a_1 = 0.03224$ ,  $a_2 = 0.00101$ ,  $a_3 = 0$ ,  $a_4 = 0.04450$ ,  $a_5 = 0.00081$ ,  $a_6 = -0.0645$ .  $\bar{r} = \sum x_i RON_i / \sum x_i$ ,  $\bar{m} = \sum x_i MON_i / \sum x_i$ ,  $\bar{s} = \sum x_i s_i / \sum x_i$ ,  $\bar{rs} = \sum x_i s_i RON_i / \sum x_i$ ,  $\bar{ms} = \sum x_i s_i MON_i / \sum x_i$ ,  $\bar{O} = \sum x_i O_i / \sum x_i$ ,  $\bar{O}^2 = \sum x_i \cdot O_i^2 / \sum x_i$ ,  $\bar{A} = \sum x_i A_i / \sum x_i$ ,  $\bar{A}^2 = \sum x_i \cdot A_i^2 / \sum x_i$ .

## 6 Simulation Results Under Uncertainty

Since there are many parameters could be uncertain in blending scheduling, we only consider measurement uncertainty for representative. Suppose the *RVP*, *RON* or *MON* of n-Butane component is an uncertainty parameter. Then Eqs. (13), (14) and (15) are nonlinear constraints with uncertain parameters. Their uncertainty is taken as 5% of their normal distribution of expectation.

For PSOHT, PSO and GA, the parameters are all set as follows: population size is 20, the maximum generation is 500, evaluation number for each particle 10. Then Eqs. (12)-(15) and other constraints are displaced in Eqs. (6). The simulation results of gasoline blending scheduling are listed in Table 3 through Table 12.

- (1) Table 3 and Table 4 show the results of gasoline blending scheduling when only *RVP* of n-butane component has 5% of their normal distribution of expectation.
- (2) Table 5 and Table 6 show the results of gasoline blending scheduling when only *RON* of n-butane component has 5% of their normal distribution of expectation.
- (3) Table 7 and Table 8 show the results of gasoline blending scheduling when only *MON* of n-butane component has 5% of their normal distribution of expectation.
- (4) Table 9 and Table 10 show the results of gasoline blending scheduling when *RVP* and *RON* of n-butane component both have 5% of their normal distribution of expectation.
- (5) Table 11 and Table 12 show the results of gasoline blending scheduling when *RVP*, *RON* and *MON* of n-butane component all have 5% of their normal distribution of expectation. For such a case, the sample times of each particle changes to 20.

**Table 3.** Results when *RVP* of n-butane component is uncertain

| Algorithm | Reformate | LSR naphtha | n-Butane | Catalytic gas | Alkyl ate |
|-----------|-----------|-------------|----------|---------------|-----------|
| PSOHT     |           |             |          |               |           |
| regular   | 6011.43   | 1938.20     | 155.43   | 0             | 0         |
| premium   | 4200.43   | 875.94      | 207.35   | 4500          | 216.28    |
| PSO       |           |             |          |               |           |
| regular   | 6085.47   | 1914.53     | 0.01     | 0             | 0         |
| premium   | 4216.48   | 883.54      | 237.65   | 4500          | 162.32    |
| GA        |           |             |          |               |           |
| regular   | 6062.48   | 1924.23     | 13.29    | 0             | 0         |
| premium   | 4236.57   | 882.30      | 32.71    | 4500          | 348.42    |

**Table 4.** Results under uncertain *RVP*

|         | PSOHT      |            |            | PSO        |            |            | GA         |            |            |
|---------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
|         | <i>RON</i> | <i>MON</i> | <i>RVP</i> | <i>RON</i> | <i>MON</i> | <i>RVP</i> | <i>RON</i> | <i>MON</i> | <i>RVP</i> |
| regular | 90.0       | 77.0       | 10.3       | 88.5       | 77.7       | 6.0        | 88.5       | 78.1       | 6.7        |
| premium | 92.0       | 80.0       | 10.0       | 91.5       | 80.0       | 10.65      | 91.6       | 80.2       | 10.5       |
| profit  | 64507      |            |            | 61680      |            |            | 57418      |            |            |

**Table 5.** Results when *RON* of n-butane component is uncertain

| Algorithm | Reformat | LSR naphtha | n-Butane | Catalytic gas | Alkyl ate |
|-----------|----------|-------------|----------|---------------|-----------|
| PSOHT     |          |             |          |               |           |
| regular   | 5915.34  | 1930.85     | 153.81   | 0             | 0         |
| premium   | 4336.36  | 879.64      | 197.47   | 4500          | 220.34    |
| PSO       |          |             |          |               |           |
| regular   | 6740.21  | 1246.21     | 13.58    | 0             | 0         |
| premium   | 3716.16  | 1230.88     | 254.60   | 4500          | 298.36    |
| GA        |          |             |          |               |           |
| regular   | 6012.38  | 1981.64     | 5.98     | 0             | 0         |
| premium   | 4221.75  | 905.73      | 18.44    | 4500          | 354.08    |

**Table 6.** Results under uncertain *RON*

|         | PSOHT      |            |            | PSO        |            |            | GA         |            |            |
|---------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
|         | <i>RON</i> | <i>MON</i> | <i>RVP</i> | <i>RON</i> | <i>MON</i> | <i>RVP</i> | <i>RON</i> | <i>MON</i> | <i>RVP</i> |
| regular | 90.0       | 77.0       | 10.3       | 91.6       | 77.4       | 5.7        | 88.9       | 78.6       | 6.2        |
| premium | 92.7       | 80.0       | 9.7        | 92.0       | 80.0       | 10.8       | 92.6       | 80.2       | 5.9        |
| profit  | 64700      |            |            | 59428      |            |            | 56765      |            |            |

**Table 7.** Results when *MON* of n-butane component is uncertain

| Algorithm | Reformat | LSR naphtha | n-Butane | Catalytic gas | Alkyl ate |
|-----------|----------|-------------|----------|---------------|-----------|
| PSOHT     |          |             |          |               |           |
| regular   | 6266.18  | 1502.33     | 231.49   | 0             | 0         |
| premium   | 3995.49  | 938.75      | 195.26   | 4500          | 370.50    |
| PSO       |          |             |          |               |           |
| regular   | 6093.91  | 1895.30     | 10.79    | 0             | 0         |
| premium   | 4203.96  | 892.05      | 228.14   | 4500          | 175.85    |
| GA        |          |             |          |               |           |
| regular   | 5971.01  | 2011.35     | 17.64    | 0             | 0         |
| premium   | 4254.27  | 802.69      | 45.82    | 4500          | 397.22    |

**Table 8.** Results under uncertainty *MON*

|         | PSOHT      |            |            | PSO        |            |            | GA         |            |            |
|---------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
|         | <i>RON</i> | <i>MON</i> | <i>RVP</i> | <i>RON</i> | <i>MON</i> | <i>RVP</i> | <i>RON</i> | <i>MON</i> | <i>RVP</i> |
| regular | 91.0       | 77.5       | 10.5       | 90.1       | 77.0       | 6.3        | 89.8       | 77.1       | 6.6        |
| premium | 92.6       | 80.0       | 9.9        | 92.7       | 80.0       | 10.5       | 92.8       | 80.0       | 6.4        |
| profit  | 62681      |            |            | 61584      |            |            | 56975      |            |            |

**Table 9.** Results when *RVP* and *RON* of n-butane component are uncertain

| Algorithm | Reformat | LSR naphtha | n-Butane | Catalytic gas | Alkyl ate |
|-----------|----------|-------------|----------|---------------|-----------|
| PSOHT     |          |             |          |               |           |
| regular   | 6402.23  | 1487.32     | 110.45   | 0             | 0         |
| premium   | 4121.27  | 882.66      | 238.92   | 4500          | 257.15    |
| PSO       |          |             |          |               |           |
| regular   | 6257.07  | 1711.85     | 31.08    | 0             | 0         |
| premium   | 4063.03  | 988.54      | 120.39   | 4500          | 328.04    |
| GA        |          |             |          |               |           |
| regular   | 6432.31  | 1574.32     | 2.37     | 0             | 0         |
| premium   | 3789.17  | 1085.44     | 38.04    | 4500          | 587.35    |

**Table 10.** Results under uncertain *RVP* and *RON*

|         | PSOHT      |            |            | PSO        |            |            | GA         |            |            |
|---------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
|         | <i>RON</i> | <i>MON</i> | <i>RVP</i> | <i>RON</i> | <i>MON</i> | <i>RVP</i> | <i>RON</i> | <i>MON</i> | <i>RVP</i> |
| regular | 91.0       | 77.3       | 8.7        | 90.5       | 77.2       | 6.7        | 90.9       | 77.6       | 5.7        |
| premium | 92.7       | 80.1       | 10.5       | 92.5       | 80.0       | 8.3        | 92.3       | 80.0       | 6.5        |
| profit  | 60618      |            |            | 58359      |            |            | 54615      |            |            |

**Table 11.** Results when *RVP*, *RON* and *MON* of n-butane component are uncertain

| Algorithm | Reformat | LSR naphtha | n-Butane | Catalytic gas | Alkyl ate |
|-----------|----------|-------------|----------|---------------|-----------|
| PSOHT     |          |             |          |               |           |
| regular   | 6127.91  | 1857.33     | 14.76    | 0             | 0         |
| premium   | 3953.19  | 893.42      | 220.84   | 4500          | 432.55    |
| PSO       |          |             |          |               |           |
| regular   | 6588.95  | 1408.37     | 2.68     | 0             | 0         |
| premium   | 4005.85  | 785.36      | 221.59   | 4500          | 487.20    |
| GA        |          |             |          |               |           |
| regular   | 6704.55  | 1289.63     | 5.82     | 0             | 0         |
| premium   | 3963.78  | 1013.80     | 9.68     | 4500          | 512.74    |

**Table 12.** Results under three uncertainty parameters

|         | PSOHT      |            |            | PSO        |            |            | GA         |            |            |
|---------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
|         | <i>RON</i> | <i>MON</i> | <i>RVP</i> | <i>RON</i> | <i>MON</i> | <i>RVP</i> | <i>RON</i> | <i>MON</i> | <i>RVP</i> |
| regular | 90.2       | 77.0       | 6.4        | 91.2       | 78.0       | 5.5        | 91.5       | 78.3       | 5.5        |
| premium | 92.7       | 80.1       | 10.4       | 92.9       | 80.0       | 10.3       | 92.5       | 80.2       | 5.8        |
| profit  | 60442      |            |            | 55553      |            |            | 51407      |            |            |

From the above Tables, it can be seen that PSOHT is of better performance than PSO and GA. In addition, it can also be seen from the Tables that PSO is of better performance than GA for the blending scheduling under uncertainty. The merits of PSOHT lie in two aspects: it applies the population-based searching framework of PSO for exploration and exploitation in solution space; and it applies HT to reserve the best solutions and maintain the diversity of the next swarm by deleting some



particles with similar performances and to reduce repeated search to some extent. Thus, PSOHT is of good searching quality and robustness. So, the proposed PSOHT is an effective approach for function optimization under uncertainty.

## 7 Conclusion

In this paper, a new hybrid approach (namely PSOHT) combining PSO and hypothesis test (HT) was proposed and applied to blending scheduling problem under uncertainty. The simulation results based on an example of gasoline blending problem demonstrated the effectiveness of the proposed method. The future work is to study some adaptive mechanism to further improve the performance of the algorithm.

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# Fixed Parameter Estimation Method Using Gaussian Particle Filter

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**Abstract.** The degeneracy problems of general particle filtering frequently occur. Although this kind of problems can be mitigated by resampling, but the diversity characteristic between particles may be lost because the higher weighted particles will be replicated and the lower weighted particles will be discarded. For parameter-fixed application cases, the standard particle filter is invalid as no importance density function can be sampled for new particles required by the predictive distribution, and particles will quickly be exhausted. This paper proposes a new method for the parameter-fixed estimation by use of Gaussian particle filter, which can avoid making particles exhausted and can improve the estimation performance. Refer to a practical example of Direction of Arrived (DOA) estimation for coherent signals propagated in space with multi-path fading, the computer simulation has been performed. The simulation results have indicated that the performance of the new method is rather than general particle filtering.

## 1 Introduction

In the modern signal processing field, non-linear state estimation is widely applied in many cases, including robot control, computer vision, target tracking, etc.. The Extended Kalman Filter (EKF) is the classical estimation technique for non-linear state space model, which performs linear approximation by Talor-Expansion, but it required derivative for non-linear transform and Gaussian noise assumption in system model, and the algorithm used often become to divergence in case of impropriety of initial state estimation. In highly non-linear and non-Gaussian situations, it is invalid to gain a precise solution in analytical form. With the computation cost reduction, it is possible to develop a new sequential Monte Carlo particle filter based Bayesian principle. Particle filter technique can be used in any non-linear system which can be presented as state space model, and performance of asymptotic closed to MMSE can be achieved [1], [2], [3].

The iterative process of general particle filters involves three procedures, first of all, drawing particles from importance density function, next, calculating weight values related to these particles based on the system model, finally, replicating higher weighted particles and discarding lower weighted particles to obtain filtering distribution. Nevertheless, the degeneracy phenomena could frequently be encountered in general

particle filter, i.e. after some iterative processes, weights of many particles become lower and a large number of particles will be ignored in algorithm besides a few with higher weight value.

For the estimation of parameter-fixed system model, the standard particle filter algorithm will become invalid because of no importance density function to be drawn in predictive distribution and particles exhausted quickly [4]. Unfortunately, there are many applications for the estimation of fixed parameter in non-linear system, for example, the Direction Of Arrived (DOA) estimation for signals propagated in space can be expressed as basic non-linear model, and , the non-linear model becomes more complex in multi-path propagation. It is difficult to obtain satisfied result through use of analytical method, such as EKF, UKF etc.. The paper addresses problems of fixed parameter estimation based Gaussian particle filter, has overcome the drawback of degeneracy existed in the conventional particle filter, and the performance improvement are given out in simulation.

The remainder of this paper is organized as follows: the standard particle filter approach and the problems for fixed parameter estimation are simply described, in section 2. The Gaussian particle filter technique is introduced in section 3. The applications of fixed parameter model and example of DOA estimation based Gaussian particle filter for coherent signals propagated in space through multi-path is described in section 4, and simulation results present in section 5. Finally, conclusion is given in section 6.

## 2 General Particle Filter

In principle, particle filter is a posterior probabilistic density estimation approach based on Monte Carlo sample method, it is an innovation by contrast with traditional technology [5], [6], [7]. In general situation, according to Bayesian principle,

$$p(\mathbf{x} | \mathbf{z}) = \frac{p(\mathbf{z} | \mathbf{x})p(\mathbf{x})}{\int p(\mathbf{z} | \mathbf{x})p(\mathbf{x})d\mathbf{x}} . \quad (1)$$

where,  $p(\mathbf{x} | \mathbf{z})$  is the posterior probabilistic density function,  $p(\mathbf{z} | \mathbf{x})$  is the likelihood function, and  $p(\mathbf{x})$  is the prior probabilistic density function. When a set of observation are obtained, the posterior distribution of state can be computed, the expectation of arbitrary function for  $\mathbf{x}$  can be expressed as

$$E[g(\mathbf{x})] = \int g(\mathbf{x})p(\mathbf{x} | \mathbf{z})d\mathbf{x} . \quad (2)$$

If there is a large number of particles drawn from  $p(\mathbf{x} | \mathbf{z})$ , equation (2) can be approximated as

$$E[g(\mathbf{x})] \approx \frac{1}{N} \sum_{i=1}^N g(\mathbf{x}^i) .$$

where,  $\{\mathbf{x}^i, i=1, \dots, N\}$  denotes  $N$  particles drawn independently from  $p(\mathbf{x}|\mathbf{z})$ , and when  $N \rightarrow \infty$ , the above equation is accurately equal. It can be seen that the posterior probabilistic density can be expressed approximately as a set of discrete particles, the approximation relies on the value of  $N$ .

Bayesian importance sampling approach is used to estimate the posterior distribution. The detailed process is as follows, selecting an importance density function first, and then drawing particles from this distribution and obtaining a set of particles,  $\{\mathbf{x}^i, i=1, \dots, N\}$ . To approximate the posterior density  $p(\mathbf{x}|\mathbf{z})$  as weighted particles that drawn from importance density function, equation (2) can be rewritten as

$$E[g(\mathbf{x})] \approx \sum_{i=1}^N g(\mathbf{x}^i) \tilde{w}^i . \quad (3)$$

where,

$$\tilde{w}^i = \frac{w^i}{\sum_{j=1}^N w^j}, \quad w^i = \frac{p(\mathbf{z}|\mathbf{x})p(\mathbf{x})}{q(\mathbf{x}|\mathbf{z})} .$$

In order to estimate the posterior distribution sequentially, the sequential importance sampling could be considered as the transformation of the above mathematics. This new idea is described as follows. Let  $\{\mathbf{x}_{0:k}^i, i=1, 2, \dots, N\}$  denotes a set of sample particles which drawn from the importance density function,  $\mathbf{x}_{0:k} = \{\mathbf{x}_j, j=0, 1, \dots, k\}$  denotes the state set which up to time  $k$ , thus, the posterior distribution at time  $k$  can be expressed approximately as

$$p(\mathbf{x}_{0:k} | \mathbf{z}_{1:k}) \approx \sum_{i=1}^N w_k^i \delta(\mathbf{x}_{0:k} - \mathbf{x}_{0:k}^i) . \quad (4)$$

Weighting value is recursively presented as

$$w_k^i = w_{k-1}^i \cdot \frac{p(\mathbf{z}_k | \mathbf{x}_k^i) p(\mathbf{x}_k^i | \mathbf{x}_{k-1}^i)}{q(\mathbf{x}_k^i | \mathbf{x}_{k-1}^i, \mathbf{z}_k)} . \quad (5)$$

For general dynamic system model,

$$\mathbf{x}_k = f(\mathbf{x}_{k-1}, \mathbf{v}_{k-1}) . \quad (6)$$

$$\mathbf{z}_k = h(\mathbf{x}_k, \mathbf{w}_k) . \quad (7)$$

To implement particle filtering, it is required to sequentially perform following steps.

1) According to initial probabilistic density  $p(\mathbf{x}_0)$ , draw  $N$  discrete particles from this distribution based on the Monte Carlo method, and denote the result as

$$\{\mathbf{x}_{0|0}^1, \mathbf{x}_{0|0}^2, \dots, \mathbf{x}_{0|0}^N\} .$$

2) *Predictive distribution*: With respect to filtering particles at last time  $k-1$ , particles predicted in one step is obtained from system process equation (6), denote as

$$\mathbf{x}_{k|k-1}^i = f(\mathbf{x}_{k-1|k-1}^i, v_{k-1}), i = 1, \dots, N . \quad (8)$$

3) *Filtering update*: For the acceptance of a new observation, calculate the weighting value for each predictive particle, denote as,

$$b_i = \frac{p(\mathbf{z}_k | \mathbf{x}_{k|k-1}^i)}{\sum_{j=1}^N p(\mathbf{z}_k | \mathbf{x}_{k|k-1}^j)} . \quad (9)$$

Afterwards, in order to obtain filtering particles, it is required to performing  $N$  times resampling against the predictive particles set according to the above weighted value, this behavior can be formulated as

$$\Pr[\mathbf{x}_{k|k}^n = \mathbf{x}_{k|k-1}^i] = b_i, i, n = 1, 2, \dots, N .$$

where,  $\Pr[\cdot]$  denotes probability.

4) repeat step 2 and step 3 recursively.

It can obviously be shown that there is no importance density to be drawn for particles obtained in step2 when system state evolution is in fixed form, e.g. the state is a constant parameter (notice  $\mathbf{x}_k = \mathbf{x}_{k-1}$ ), therefore, the algorithm will be invalid because of particles exhausted quickly.

### 3 Gaussian Particle Filter

Gaussian particle filter (GPF) is used to approximate the predictive distribution and filtering distribution as Gaussian [8], i.e.

$$p(\mathbf{x}_k | \mathbf{z}_{1:k-1}) \approx \mathcal{N}(\mathbf{x}_k; \bar{\boldsymbol{\mu}}_k, \bar{\boldsymbol{\Sigma}}_k) .$$

$$p(\mathbf{x}_k | \mathbf{z}_{1:k}) \approx \mathcal{N}(\mathbf{x}_k; \boldsymbol{\mu}_k, \boldsymbol{\Sigma}_k) .$$

where,  $\mathcal{N}(\cdot)$  denotes normal distribution,  $\boldsymbol{\mu}_k, \boldsymbol{\Sigma}_k, \bar{\boldsymbol{\mu}}_k, \bar{\boldsymbol{\Sigma}}_k$  is filtering mean, variance and predictive mean, variance respectively. But  $\boldsymbol{\mu}_k, \boldsymbol{\Sigma}_k, \bar{\boldsymbol{\mu}}_k, \bar{\boldsymbol{\Sigma}}_k$  can not analytically be presented, and these parameters must be estimated from particles using Monte Carlo method.

Detailed procedures are described as follows,

1) Draw  $N$  particles from initial probabilistic density  $p(\mathbf{x}_0)$  based on Monte Carlo method. The result obtained can be denoted as,

$$\{\mathbf{x}_{0|0}^1, \mathbf{x}_{0|0}^2, \dots, \mathbf{x}_{0|0}^N\} .$$

2) *Predictive distribution*: From system process equation (6), a particle distribution predicted in one step is obtained

$$\mathbf{x}_{k|k-1}^{*i} = f(\mathbf{x}_{k-1|k-1}^i, \nu_{k-1}), i=1, \dots, N.$$

$$\text{Then, calculate } \begin{cases} \bar{\boldsymbol{\mu}} = \frac{1}{N} \sum_{i=1}^N \mathbf{x}_{k|k-1}^{*i} \\ \bar{\boldsymbol{\Sigma}}_k = \frac{1}{N} \sum_{i=1}^N (\mathbf{x}_{k|k-1}^{*i} - \bar{\boldsymbol{\mu}}_k)(\mathbf{x}_{k|k-1}^{*i} - \bar{\boldsymbol{\mu}}_k)^T \end{cases}. \quad (10)$$

And redraw particles from  $\mathcal{N}(\mathbf{x}_k; \bar{\boldsymbol{\mu}}_k, \bar{\boldsymbol{\Sigma}}_k)$ , then, we obtain

$$\{\mathbf{x}_{k|k-1}^1, \mathbf{x}_{k|k-1}^2, \dots, \mathbf{x}_{k|k-1}^N\}.$$

3) *Filtering distribution*: For the acceptance of a new observation, calculate the weighting value for each predictive particle according to (9), and then calculate

$$\begin{cases} \boldsymbol{\mu}_k = \frac{1}{N} \sum_{i=1}^N b_i \mathbf{x}_{k|k-1}^i \\ \boldsymbol{\Sigma}_k = \frac{1}{N} \sum_{i=1}^N b_i (\mathbf{x}_{k|k-1}^i - \boldsymbol{\mu}_k)(\mathbf{x}_{k|k-1}^i - \boldsymbol{\mu}_k)^T \end{cases}. \quad (11)$$

and redraw particles from  $\mathcal{N}(\mathbf{x}_k; \boldsymbol{\mu}_k, \boldsymbol{\Sigma}_k)$ , then, we obtain

$$\{\mathbf{x}_k^1, \mathbf{x}_k^2, \dots, \mathbf{x}_k^N\}.$$

4) repeat step 2 and step 3 recursively.

Gaussian distribution is depend on first two moment, i.e. mean and variance, so it is easy to redraw particles in each iteration for avoiding particles degeneracy.

## 4 Fixed Parameter Estimation

For parameter-fixed problems, system can be modeled in general form as

$$\begin{cases} \mathbf{x}_k = \mathbf{x}_{k-1} \\ \mathbf{z}_k = h(\mathbf{x}_k) + \mathbf{w}_k \end{cases} \quad (12)$$

where,  $\mathbf{w}_k$  is an additive Gaussian noise,  $\mathbf{x}$  is the unobserved parameter vector,  $\mathbf{z}_k$  is measurement vector at time k,  $h(\cdot)$  is the non-linear transform. Equation (12) is significant in general wireless telecommunication and other radio system, it has been

demonstrated that Bayesian posterior estimation of parameters is a Gaussian variant. In other cases if  $\mathbf{w}_k$  is not a Gaussian, it is also a favorite idea that the posterior estimation of the state is assumed to approximate to Gaussian, so that the computation complexity is reduced. DOA estimation is one of many practical examples, where it is very difficult for coherent signals propagated in space with multi-path fading. This is one of non-linear problems with highly complexity often appeared in array signal processing field, and it is very difficult to find correction solution by use of the conventional analytical method.

For an instance, let one plane wave impact to circle array sensors with N elements in figure 1, the signal arrived at the center of circle is

$$s_0(t) = A \cdot \cos[\omega_0 t + \varphi_0] .$$

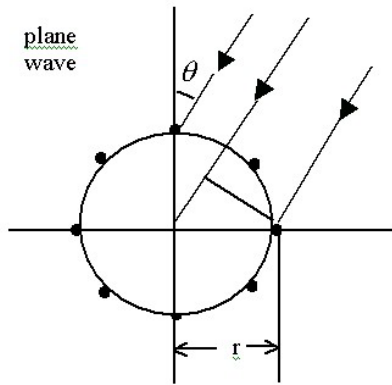


Fig. 1. Circle array sensors

The signal arrived i-th sensor can be expressed as

$$s_i(t) = A \cdot \cos[\omega_0(t + \tau_i) + \varphi_0] .$$

$$\tau_i = \frac{r}{c} \cdot \cos\left(\frac{2\pi \cdot i}{N} - \theta\right) .$$

Where,  $r$  is the radius of the circle,  $\theta$  is the incident angle,  $\tau_i$  is the time delay (or prior to) that arrived at i-th element,  $\omega_0$  is the signal frequency of incident wave,  $\varphi_0$  is the initial phase,  $c$  is the velocity of light. When there are  $M$  coherent waves which are incident to the array, the equation above can be rewritten as

$$s_i(t) = \sum_{l=1}^M A_l \cdot \cos\left\{\omega_0\left[t + \frac{r}{c} \cdot \cos\left(\frac{2\pi \cdot i}{N} - \theta_l\right)\right] + \varphi_0\right\} . \quad (13)$$

For the array output, it can be expressed as

$$\mathbf{z}(t) = \mathbf{s}(t) + \mathbf{w}(t) . \quad (14)$$

Where,  $\mathbf{w}(t) \sim \mathcal{N}(0, \sigma^2 \mathbf{I})$  is the noise vector,  $\mathbf{z}(t) = [z_1(t), z_2(t), \dots, z_N(t)]^T$  is the observation vector,  $\mathbf{s}(t) = [s_1(t), s_2(t), \dots, s_N(t)]^T$  is the array signal vector. The likelihood function is

$$p(\mathbf{z}|\boldsymbol{\theta}) = \frac{1}{(2\pi)^{N/2} |\mathbf{R}_n|^{1/2}} \exp\left[ -\frac{(\mathbf{z}-\mathbf{s})^T \mathbf{R}_n^{-1} (\mathbf{z}-\mathbf{s})}{2} \right] .$$

Here,  $\mathbf{R}_n$  is the covariance matrix of the array noise. Suppose that the posterior distribution  $p(\boldsymbol{\theta}|\mathbf{z})$  can be estimated, so according to Bayesian principle, the DOA parameter  $\boldsymbol{\theta}$  can be estimated as

$$\hat{\boldsymbol{\theta}} = E(\boldsymbol{\theta}|\mathbf{z}) = \int \boldsymbol{\theta} p(\boldsymbol{\theta}|\mathbf{z}) d\boldsymbol{\theta} .$$

and the performance is asymptotic to MMSE. Rewrite the signal model in discrete time to the state space form of the equation (12), where,

$$\mathbf{x}(k) = [A_1(k), \dots, A_M(k); \theta_1, \dots, \theta_M; \varphi_0]^T .$$

is state vector involving amplitude, DOA, and initial phase parameters related to the coherent signals, at time  $k$  respectively, and the array output signals at time  $k$  can be denoted as

$$\mathbf{z}(k) = [z_1(k), \dots, z_N(k)]^T .$$

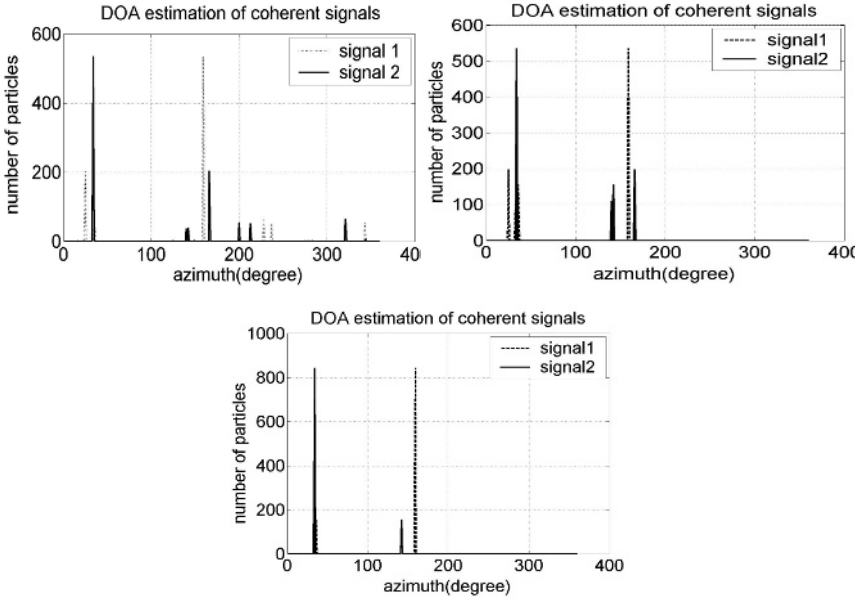
We have used Gaussian particle filter to estimate DOA for coherent signals, it is believed that the performance is asymptotic optimal when number of particles is sufficient large.

## 5 Simulation Results

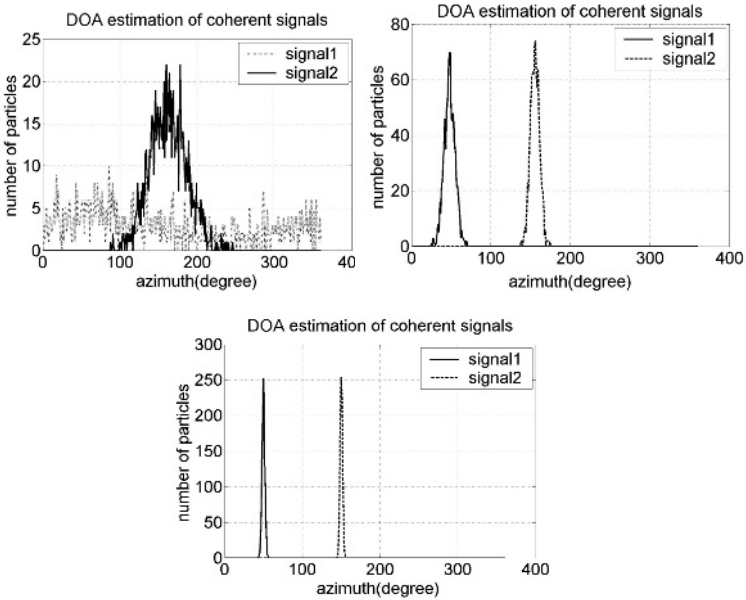
The array with 9 elements uniformly spaced in a circle of 2m diameter is used, the signal frequency is 150MHz, the number of particles equals to 1000, computer simulation is performed under some conditions, and the posterior distribution of DOA parameter  $\boldsymbol{\theta}$  is given in histogram form of particle number vs. azimuth. (Notes that the  $\theta_1, \theta_2$  characteristics are indicated in solid and dash line respectively.)

Figure 2 illustrates the DOA estimation results for coherent signals by use of the general particle filter, in these cases, there are two coherent signals to incident to the array, with azimuth of  $50^\circ, 150^\circ$ , respectively, and the signal to noise ratio (SNR) is 10dB at array output. It can be observed that the particles degeneracy phenomena occurs, and the estimation is invalid.





**Fig. 2.** DOA estimation of coherent signals by use of the general particle filter with 1 iteration (left upper case) and 2 iterations (right upper case) and >3 iterations (left bottom case), where azimuth=50°,150°, SNR=10dB



**Fig. 3.** DOA estimation of coherent signals by use of the Gaussian particle filter with 1 iteration (left upper case) and 3 iterations (right upper case) and 10 iterations (left bottom case), where azimuth=50°,150°, SNR=10dB

Figure 3 illustrates the DOA estimation results for coherent signals by use of Gaussian particle filter with the same conditions indicated in figure 2, but results are convergence to true parameter. It is obviously shown that, after a few iterations, the estimation is utilized in practice only with a few observations, and this approach is successful to be applied.

## 6 Conclusion

There are many issues for unknown parameter-fixed estimation in highly non-linear system. The conventional analytical methods such as EKF and etc. are inefficient to process these issues. The sequential Bayesian method involves predictive and filtering distribution estimation recursively, but due to degeneracy and exhaustion of particles in iterations, the standard particle filter cannot handle above problems.

Gaussian particle filter can avoid to exhausting of particles, and thus has much-improved estimation performance. This approach overcomes the drawback inherently occurred in the traditional particle filters. It is believed that the new Gaussian particle filter method will be widely applied in practice.

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# Improving Quantum-Behaved Particle Swarm Optimization by Simulated Annealing

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**Abstract.** Quantum-behaved Particle Swarm Optimization (QPSO) is a global convergence guaranteed search method, which introduced quantum theory into original Particle Swarm Optimization (PSO). While Simulated Annealing (SA) is another important stochastic optimization with the ability of probabilistic hill-climbing. In this paper, the mechanism of Simulated Annealing is introduced into the weak selection implicit in our QPSO algorithm, which effectively employs both the ability to jump out of the local minima in Simulated Annealing and the capacity of searching the global optimum in QPSO algorithm. The experimental results show that the proposed hybrid algorithm increases the diversity of the population in the search process and improves its precision in the latter period of the search.

## 1 Introduction

Particle Swarm Optimization (PSO) [1], inspired by the collective behaviors of birds, is a population based stochastic optimization technique proposed by Kennedy and Eberhart. As an emerging intelligent technology, simple and easy to realize, particle swarm has gained a lot of attention in recent years and has been investigated from various perspective. However, there are still many issues in particle swarm, such as slow convergence during the latter search, poor precision and being easy to trap in local minima. To overcome the above problems, a lot of revised PSO have emerged.

The improvement emphases of PSO algorithm mainly concentrate on combing PSO with the concepts of evolutionary computation, such as selection, recombination, breeding and so on. As articles written by Angeline [2] in 1999, the operators of selection and cross in Evolutionary computation are introduced into PSO algorithm to guarantee the convergence. And in view of breeding and cross, Lovbjerg etc. [3] further apply evolutionary mechanism into PSO algorithm to present a concrete form and the experimental results based on benchmark functions show the validity of algorithm. On the other hand, to improve the global convergence, the diversity maintenance is vital to PSO algorithm. To overcome the problem of premature convergence, the diversity measure, attractive and repulsive PSO algorithm, is applied to control the swarm by Jacques Riget [11]. In 2004, from the point of view of probability statistics, Kennedy [4] eliminated the velocity formula and sample from the Gaussian

distribution, using a random number generator and experimental results show that some remarkable degree of success can be achieved through simple collaborative probabilistic search within regions defined by particles' success. In 2004, we proposed Quantum-behaved Particle Swarm Optimization (QPSO) [5][8], which is kept to the philosophy of PSO. QPSO algorithm is depicted only with the position vector without velocity vector, which is a simpler algorithm. And the results show that QPSO performs better than standard PSO on several benchmark test functions and is a promising algorithm due to its global convergence guaranteed characteristic.

Simulated Annealing is another important stochastic optimization method based on the Monte Carlo importance-sampling, but it is very slow [9]. It starts from an initial point and takes a single point iterative strategy. And it accept not only the evolved but also the degenerated solutions with the Metropolis acceptance criterion during its annealing procedure, which makes the SA be of the potentially to find the global minimum instead of falling to local minima.

In this paper, based on our proposed Quantum-behaved Particle Swarm Optimization, Simulated Annealing, as selection operator, is introduced to improve the capacity of fine-tuning solution in the latter period of the search, which effectively employs the ability to jump from the local minima in Simulated Annealing algorithm and the capacity of global search in QPSO algorithm.

The rest of this paper is organized as follows. Section 2 briefly describes PSO and Quantum-behaved PSO algorithm. Then the mechanism of Simulated Annealing introduced into QPSO is presented in Section 3. Section 4 shows the experimental settings and the comparative results of hybrid algorithm on test functions. Finally, conclusions are made.

## 2 PSO and Quantum-Behaved PSO

### 2.1 Dynamics of Classical PSO

In a classical PSO system proposed by Kennedy and Eberhart[1], each particle flies in a D-dimensional space S according to its own historical experience and others. The velocity and location for the  $i$ th particle is represented as  $\vec{v}_i = (v_{i1}, \dots, v_{id}, \dots, v_{iD})$  and  $\vec{x}_i = (x_{i1}, \dots, x_{id}, \dots, x_{iD})$ , respectively. The particles are manipulated according to the following equation:

$$v_{id} = w \cdot v_{id} + c_1 \cdot \text{rand}() \cdot (p_{id} - x_{id}) + c_2 \cdot \text{rand}() \cdot (p_{gd} - x_{id}) \quad (1a)$$

$$x_{id} = x_{id} + v_{id} \quad (1b)$$

where  $c_1$  and  $c_2$  are acceleration constants,  $\text{rand}()$  are random values between 0 and 1. In (1a), the vector  $p_i$  is the best position (the position giving the best fitness value) of the particle  $i$ , vector  $p_g$  is the position of the best particle among all the particles in the population. Parameter  $w$  is the inertia weight [6], which does not appear in the original version of PSO [1]. In [7], M. Clerc and J. Kennedy analyze the trajectory and prove that, whichever model is employed in the PSO algorithm, each particle in

the PSO system converges to its local point  $p$ , whose coordinates are  $p_d = (\varphi_{1d}p_{id} + \varphi_{2d}p_{gd}) / (\varphi_{1d} + \varphi_{2d})$  so that the best previous position of all particles will converge to an exclusive global position with  $t \rightarrow \infty$ , where  $\varphi_{1d}, \varphi_{2d}$  are random numbers distributed uniformly on  $[0,1]$ .

## 2.2 Dynamics of Quantum-Behaved PSO

Keeping to the philosophy of PSO algorithm, we introduced the quantum theory into PSO algorithm and proposed a Quantum-behaved PSO algorithm [5][8]. In the quantum model of a PSO, the state of a particle is depicted by wave function  $\Psi(\bar{x}, t)$ , instead of position and velocity. The dynamic behavior of the particle is widely divergent from that of the particle in traditional PSO systems in that the exact values of  $x$  and  $v$  cannot be determined simultaneously. We can only learn the probability of the particle's appearing in position  $x$  from probability density function  $|\Psi(x, t)|^2$ , the form of which depends on the potential field the particle lies in.

The particles move according to the following iterative equation [5][8]:

$$x(t+1) = p \pm \beta * |mbest - x(t)| * \ln(1/u) \quad (2a)$$

Where

$$mbest = \frac{1}{M} \sum_{i=1}^M P_i = \left( \frac{1}{M} \sum_{i=1}^M P_{i1}, \frac{1}{M} \sum_{i=1}^M P_{i2}, \dots, \frac{1}{M} \sum_{i=1}^M P_{id} \right) \quad (2b)$$

$$p_{id} = \varphi * p_{id} + (1 - \varphi) * p_{gd}, \varphi = rand() \quad (2c)$$

$mbest$  (Mean Best Position) is defined as the mean value of all particles' the best position,  $\varphi$  and  $u$  are random number distributed uniformly on  $[0,1]$  respectively,  $\beta$ , called Contraction-Expansion Coefficient, is the only parameter in QPSO algorithm.

## 3 The Proposed Hybrid Algorithm

### 3.1 Simulated Annealing

Simulated annealing was essentially introduced as a Monte Carlo importance-sampling technique for doing large-dimension path integrals arising in statistical physics problem, which exploits an analogy between the way in which a metal cools and freezes into a minimum energy crystalline structure (the annealing process) and the search for a minimum in a more general system [10]. The method consists of three functions, i.e., (1)  $f(x)$ : probability density of state-space of  $D$  parameters  $x = \{x^i; i=1, D\}$ ; (2)  $p(x)$ : probability density for acceptance of new cost-function given the just previous value; (3)  $T(k)$ : schedule of annealing the temperature  $T$  in annealing-time steps  $k$ , i.e. of changing the volatility or fluctuation of the two previous probability densities.

SA's major advantage over other methods is an ability to avoid becoming trapped at local minima. The algorithm starts from an initial point and takes a single point iterative strategy, which not only accepts changes that decrease objective function  $f$ , but also some changes that increase it. The latter are accepted with a probability  $p = \exp(-\Delta f / T)$ , Where  $\Delta f$  is the increase in  $f$  and  $T$  is a control parameter, varied with the objective function involved. This allows the SA algorithm to escape from local extrema at the early stages of the search and to efficiently hill-climb as the temperature approaches zero.

### 3.2 Improving Quantum-Behaved Particle Swarm Optimization by Simulated Annealing

Although QPSO is a global convergence guaranteed optimization, there are still many inevitable issues in Quantum-behaved particle swarm algorithm as other Evolutionary Algorithm, such as poor fine-tuning solutions and premature convergence during the latter search. And it seems that QPSO lacks a hill-climbing capability to close the goal. However, SA has a stochastic hill-climbing capability and the solution state cannot stay at a fixed point for a long time. Therefore, the idea on hybridizing the QPSO with SA for performance improvement is proposed. Based on the QPSO algorithm, Simulated Annealing, as selection operator, is introduced to select those degenerated particles with Metropolis acceptance criterion in QPSO algorithm.

In QPSO algorithm, the mechanism of weak selection implicit in the search process is to select the best position of the individual particle, comparing the current fitness value of particle with its historical personal best. The selection method serves to redirect the search towards those positions in the search space that have shown a relative advantage over others recently visited. Thus, the particles with low fitness were discarded. However, those particles with low fitness may have potentially preferable evolutionary tendency and then decelerate the degeneration of the whole swarm. Therefore in our proposed hybrid algorithm, introduction the concept of Simulated Annealing into the mechanism of selection in QPSO algorithm, the particles with low fitness were also accepted with the probability to further increase the search space. Thus the particles with low fitness value but a preferable evolutionary tendency seem to be a certain probability of continuing to fly in the search space, which effectively avoid being trapped at local minima and then increase the diversity of population. Meanwhile, the proposed selection operator from SA offers QPSO a hill-climbing capability to close the optimum.

In the proposed algorithm, the probability of accepting the particles with low fitness is defined as:  $p_k = \exp(-\Delta f / T_k)$ , where  $k=1,2,3,\dots$  and  $\Delta f = f(x') - f(x)$  is the change in the objective function. The annealing operation is defined as:  $T_{k+1} = T_0 \cdot CR^k, k \leftarrow k + 1$ , where  $k$  corresponds to the number of generation.

The simulation of the proposed hybrid algorithm begins with the initial population and initial temperature. The particles then randomly search according to evolutionary equations of QPSO algorithm to generate a new population. And the new population will be compared with their best position and those particles with worse fitness will be accepted with the probability from SA. Then the results obtained will become the individuals of the next generation. The simulation is repeated until the terminal criterion is met. And the terminal criterion is always set to the maximum generations of search.

Procedure of algorithm is stated below:

Step1: Initialize of population and temperature.

Step2: Evaluate of initial population.

Step3: Annealing operation  $T_{k+1} = T_0 \cdot CR^{T_k}, k \leftarrow k + 1$

Step4: Update position of particles according to evolutionary equation Eq(2a).

Step5: If the position of particle is better than  $pbest$ , then replace  $pbest$ ;

Else accept the position of particle with probability of  $p_k = \exp(-\Delta f / T_k)$

Step6: find the global best position  $gbest$

Step7: If the stop criterion is met, then algorithm ends; else go to Step3.

### 3.3 Discussions

In theory, both QPSO algorithm and SA algorithm are optimization techniques based on probability distribution. However, SA is an optimization with the probability of which is varied with generations and finally converges to zero during the process of search, which can effectively jump out of local minima and converge to global optimum. While QPSO is a global convergence guaranteed population-based optimization algorithm, which imitates the cooperation and competition behavior of flocks. The combination of the two different optimization mechanism algorithms will enrich the search behavior greatly during the search process and increase its search capacity and efficiency in global and local area. Moreover, the redundancy and history search information in the SA algorithm is so scarce because the only solution was retained at each generation. But in QPSO algorithm, the history information of individual and the whole swarm are kept to direct the search process through cooperation and competition among the particles. The combination of these two operations with different functions improves the search structure and search space. In addition, SA, as selection mechanism with adaptive probability, increases and compliments the evolutionary capacity of QPSO. And finally, the premature is evitable in the process of search due to the loss of diversity in QPSO algorithm. The incorporation of SA is able to control the premature convergence and degeneration and then increase the diversity to jump out of the local minima. In a word, the proposed hybrid algorithm has the merits of both QPSO with mutation operator algorithm and Simulated Annealing by introducing an annealing selection operator, which ensures both search space and good solution quality.

## 4 Experimental Setting and Results

In the proposed hybrid algorithm, the only parameter  $\beta$  decreases linearly from 1.0 to 0.5. The initial parameters of algorithm are described as follows: the initial annealing temperature  $T_0 = 2$ , the annealing operation is set to  $T_{k+1} = T_0 \cdot CR^{T_k}, k \leftarrow k + 1$ , where  $CR=0.95$ . To evaluate the performance of algorithm, mean optimum and standard deviation of test functions obtained from 50 runs experiments will be recorded.

Table 1 gives the test functions: Rastrigrin, Rosenbrock and Griewank, mathematics expression, its initialization range and the corresponding limits to the search space and its function value.

**Table 1.** Test Functions

| F     | Mathematic expression                                                                                     | Initial range | $f_{\min}$ | $X_{\max}$ |
|-------|-----------------------------------------------------------------------------------------------------------|---------------|------------|------------|
| $F_1$ | $\sum_{i=1}^n (100(x_{i+1} - x_i^2)^2 + (x_i - 1)^2)$                                                     | (15,30)       | 0          | 100        |
| $F_2$ | $f(x)_3 = \sum_{i=1}^n (x_i^2 - 10 \cos(2\pi x_i) + 10)$                                                  | (2.56, 5.12)  | 0          | 10         |
| $F_3$ | $f(x)_4 = \frac{1}{4000} \sum_{i=1}^n (x_i - 100)^2 - \prod_{i=1}^n \cos(\frac{x_i - 100}{\sqrt{i}}) + 1$ | (300,600)     | 0          | 600        |

**Table 2.** Experimental Values for Rosenbrock Functions

| P  | D  | G    | SPSO    |          | QPSO    |          | QPSO-SA  |          |
|----|----|------|---------|----------|---------|----------|----------|----------|
|    |    |      | Mean    | St. Dev  | Mean    | St. Dev  | Mean     | St. Dev  |
| 20 | 10 | 1000 | 94.1276 | 194.3648 | 59.4764 | 153.0842 | 25.5521  | 58.8202  |
|    | 20 | 1500 | 204.336 | 293.4544 | 110.664 | 149.5483 | 98.9765  | 122.2852 |
|    | 30 | 2000 | 313.734 | 547.2635 | 147.609 | 210.3262 | 112.0748 | 54.0904  |
| 40 | 10 | 1000 | 71.0239 | 174.1108 | 10.4238 | 14.4799  | 10.7750  | 12.5061  |
|    | 20 | 1500 | 179.291 | 377.4305 | 46.5957 | 39.5360  | 38.1721  | 33.4951  |
|    | 30 | 2000 | 289.593 | 478.6273 | 59.0291 | 63.4940  | 47.9188  | 39.2296  |
| 80 | 10 | 1000 | 37.3747 | 57.4734  | 8.63638 | 16.6746  | 6.7566   | 6.7435   |
|    | 20 | 1500 | 83.6931 | 137.2637 | 35.8947 | 36.4702  | 59.2269  | 99.7291  |
|    | 30 | 2000 | 202.672 | 289.9728 | 51.5479 | 40.8490  | 41.6666  | 29.9889  |

**Table 3.** Experimental Values for Rastrigrin Functions

| P  | D  | G    | SPSO    |         | QPSO    |        | QPSO-SA |        |
|----|----|------|---------|---------|---------|--------|---------|--------|
|    |    |      | Mean    | St.Dev  | Mean    | St.Dev | Mean    | St.Dev |
| 20 | 10 | 1000 | 5.5382  | 3.0477  | 5.2543  | 2.8952 | 4.9388  | 2.6520 |
|    | 20 | 1500 | 23.1544 | 10.4739 | 16.2673 | 5.9771 | 13.6808 | 4.6682 |
|    | 30 | 2000 | 47.4168 | 17.1595 | 31.4576 | 7.6882 | 29.5396 | 7.6264 |
| 40 | 10 | 1000 | 3.5778  | 2.1384  | 3.5685  | 2.0678 | 2.7779  | 1.3363 |
|    | 20 | 1500 | 16.4337 | 5.4811  | 11.1351 | 3.6046 | 10.8366 | 4.5036 |
|    | 30 | 2000 | 37.2796 | 14.2838 | 22.9594 | 7.2455 | 21.1007 | 5.0758 |
| 80 | 10 | 1000 | 2.5646  | 1.5728  | 2.1245  | 1.1772 | 2.1476  | 1.3866 |
|    | 20 | 1500 | 13.3826 | 8.5137  | 10.2759 | 6.6244 | 8.5381  | 6.4073 |
|    | 30 | 2000 | 28.6293 | 10.3431 | 16.7768 | 4.4858 | 15.1721 | 3.9442 |

**Table 4.** Experimental Values for Griewank Function

| P  | D  | G    | SPSO    |         | QPSO    |         | QPSO-SA |        |
|----|----|------|---------|---------|---------|---------|---------|--------|
|    |    |      | Mean    | St.Dev  | Mean    | St.Dev  | Mean    | St.Dev |
| 20 | 10 | 1000 | 0.09217 | 0.08330 | 0.08331 | 0.06805 | 0.0858  | 0.0660 |
|    | 20 | 1500 | 0.03002 | 0.03225 | 0.02033 | 0.02257 | 0.0255  | 0.0257 |
|    | 30 | 2000 | 0.01811 | 0.02477 | 0.01119 | 0.01462 | 0.0110  | 0.0140 |
| 40 | 10 | 1000 | 0.08496 | 0.07260 | 0.06912 | 0.05093 | 0.0571  | 0.0464 |
|    | 20 | 1500 | 0.02719 | 0.02517 | 0.01666 | 0.01755 | 0.0246  | 0.0431 |
|    | 30 | 2000 | 0.01267 | 0.01479 | 0.01161 | 0.01246 | 0.0095  | 0.0104 |
| 80 | 10 | 1000 | 0.07484 | 0.07107 | 0.03508 | 0.02086 | 0.0311  | 0.0268 |
|    | 20 | 1500 | 0.02854 | 0.02680 | 0.01460 | 0.01279 | 0.0166  | 0.0124 |
|    | 30 | 2000 | 0.01258 | 0.01396 | 0.01136 | 0.01139 | 0.0092  | 0.0123 |



As in [2], for each function, three different dimension sizes, 10,20 and 30 are tested. The corresponding maximum generations are 1000, 1500 and 2000 respectively. And the population size is set to 20, 40 and 80. A total of 50 runs for each experimental setting are conducted.

Table 2-Table 4 show the mean fitness value of the best point found by the end of the trial for the 50 trials along with the standard deviation for each set of trials in the experiment. The tests showed for all functions the mean best point found by the hybrid algorithm to be statistically significantly better than pure QPSO algorithm.

## 5 Conclusions

An efficient hybrid algorithm has been proposed in this paper. As the results above demonstrate, the introduction mechanism of Simulated Annealing into the Quantum-behaved Particle Swarm Optimization improves the performance of QPSO significantly on three benchmark functions in this study. The proposed hybrid algorithm incorporates effectively the characteristics of both QPSO algorithm and SA to improve the capacity of escaping from the local minima and the ability to global search.

With the development of algorithm theory study and the spread of application field, global search algorithm have a nice prospect of research and application. And the main further research will focus on the study of hybrid algorithm.

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# Optimization of a Child Restraint System by Using a Particle Swarm Algorithm

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**Abstract.** Child restraint system (CRS) is a system in automotive vehicles for the protection of child occupants in traffic accidents. Design of appropriate CRS has been one of the major subjects for both the research community and the automotive industry. In this paper, a CRS, which includes a child booster and an adult seatbelt with load limiting function, is optimized for a ten-year child dummy. The model is built and simulated using MADYMO. Several key parameters of the system are optimized to minimize the injury to child passengers under the crash test circumstance in accordance with the ECE Regulation 44 by using a recently emerged optimization scheme, particle swarm algorithm. In order to validate this optimization approach, another optimization method, AutoDOE, a built-in subroutine of MADYMO, is also utilized for comparison. The results indicate that the particle swarm algorithm has certain advantages over the AutoDOE method in terms of the solution quality. Moreover, regarding the computational efficiency, for this particular problem the particle swarm algorithm outperforms AutoDOE.

## 1 Introduction

Child injuries occurred in road traffic accidents are gaining more and more attentions from consumers, the industry, the research community and governments. According to a census of World Health Organization in 2002 [1], in every 10 traffic accidents around the world, there is one involving the injury of child passengers. In 2002, 49,736 infants between 0~4 years old and 130,835 children between 5~14 were injured or killed while traveling as occupants in motor vehicles. The injury to children caused by traffic accidents has ranked the second place in significance among all kinds of injuries. In the recent years, the research communities and the car manufacturers have conducted extensive studies on the safety of child passengers. The child safety related regulations have been in place in the most developed countries, and most require that children using child assistant seat while traveling in ground vehicles. For child passengers between 7 to 12 years age, the existing protection means is using booster seat and 3-point adult seatbelt, aiming to make the seatbelt better fit with the child. However, the belt system is usually designed for an average sized male occupant, and therefore, in a collision accident, the belt load could reach a harmful level to

the child passenger. The safety regulations specify certain injury parameters for different body regions of the crash dummy and give maximum values for the parameters. These parameters and their values have been correlated with the severity of child injuries under crash loading. So the goal for car manufacturers and CRS producers is to design and optimize the CRS parameters such as the height of the child booster and the stiffness of the belt for the injury parameters of the dummy to meet the requirements in the standard crash tests.

Using physical tests alone to develop the CRS is costly. Therefore, computer modeling and simulation are utilized as one of the primary tools in the process. In this study, MADYMO software is selected as the simulation tool. It has shown excellence in simulating multi-body dynamics in many problems [2] [3]. A CRS model is first built in MADYMO for a concerned age group of children. The model and the parameters in the system are then converted to an optimization problem, aiming at obtaining a valid CRS scheme in the early design stage and yielding some useful guidelines for the later stages.

An AutoDOE scheme has been developed specifically for the optimization coupling with MADYMO. Its mathematical foundation refers to the principle of *design of experiments* (DOE) [4]. In [5], a genetic algorithm is implemented within MADYMO to optimize the front shape of a car in order to minimize the injury to pedestrians in collision with the car. However, due to the highly nonlinear and complex nature of vehicle collisions, it is hardly to claim that any particular optimization method is perfect, or even good enough, for all problems related to passenger safety in vehicle collisions. In this paper, a novel global optimization algorithm, particle swarm algorithm (PSA), is introduced for a CRS analysis.

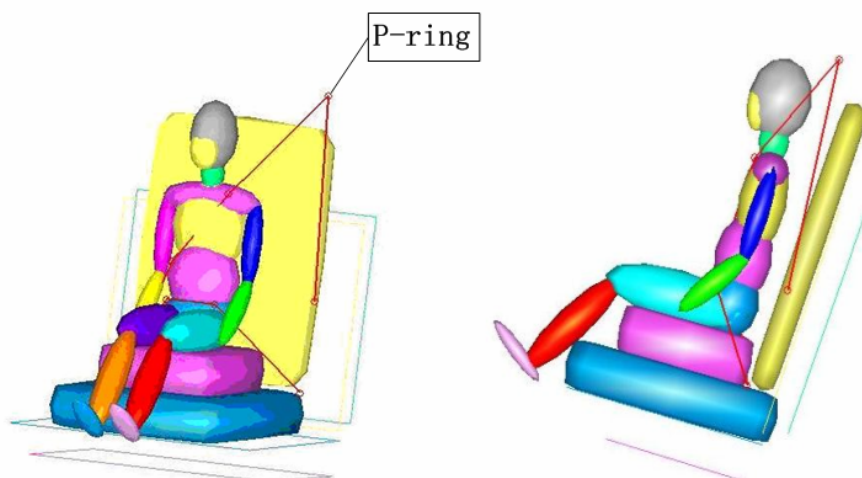
## 2 CRS Model in MADYMO

MADYMO (MAThematical DYnamic MOdel) is a program developed by TNO that simulates the dynamic behavior of physical systems emphasizing the analysis of vehicle collisions and assessing injuries sustained by passengers. It is fit for the modeling of conceptual designs in the early development phase of products. Compared with other multi-body dynamics simulators, MADYMO has its distinct properties such as easy modeling, fast computation, effective and reliable results, to list a few. These properties make it possible for designers to conduct optimization by comparing a large number of design schemes.

### 2.1 CRS Model

The CRS model is shown in Figure 1, which includes a TNO P10 child dummy that represents a 10-year-old passenger, a child booster, and a 3-point adult seatbelt. The child dummy is restrained by both the seatbelt and the booster. The booster makes the child dummy sitting in a higher position for its body to better fit with the route of the lap/shoulder belt designed for an adult passenger.

The child dummy and the seatbelt are selected from the MADYMO library, and both are modeled as a set of multiple rigid bodies. For simplicity, the booster is also modeled as a rigid body. A main reason of not modeling the booster as a deformable body is to avoid large computation load, which would result in prohibitive computing time consumption in the optimization process.



**Fig. 1.** Madymo model of child restraint system

A frontal impact test simulation is conducted in accordance with ECE regulation 44. As in the actual test, the model shown in Figure 1 is set on a sled that has an initial velocity of 50 km/h and then experiences the impact deceleration pulse specified in the regulation.

## 2.2 Optimization Model of CRS

The CRS system shown in Fig. 1 has five major parameters determining its characteristics in terms of child safety (see Table 1). All of the five parameters are selected as the design variables. In crash related optimization occupant injury parameters are usually selected as the objective and the constraints. In this case, Head Injury Criteria (HIC) of the dummy, a head injury parameter calculated from the head deceleration time history, is selected as the objective to be minimized with the maximum head displacement as the constraint. According to ECE Regulation 44, the maximum head displacement of the child should not exceed 550mm during the impact test. This value is used as the upper limit of the head displacement.

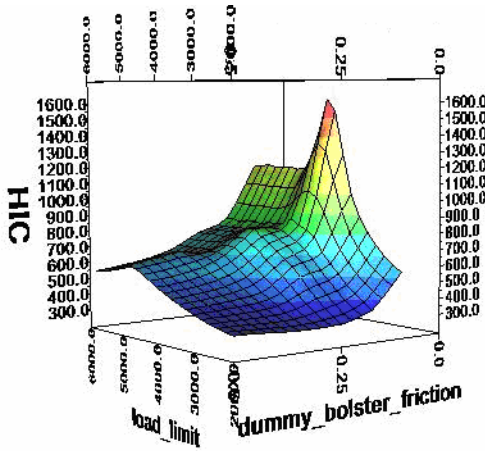
It should be noted that neither the objective nor the constraint can be expressed as an explicit function of the design variables. This is a common nature for most simulation based optimization problems. As a result, those traditional optimization techniques requiring gradient information are excluded from the set of choices. Moreover, due to the high complexity of impact and the nonlinearity of the occupant-vehicle system, the (implicit) objective function might possess multiple local optima. Fig. 2 shows the 3-D contour of HIC with two design variables, the belt load limit and the friction coefficient between the dummy and the booster. Clearly, the surface contains several local minima. Since most traditional optimization techniques only guarantee to find local optima, in such cases, it is likely to get trapped in local optima and fail to find the global one. Optimization of such a complicated occupant protection system is challenging and calls for efficient global optimization techniques.

**Table 1.** Design variables of CRS

| Subsystem                  | Optimization variable | Bounds    | Initial value |
|----------------------------|-----------------------|-----------|---------------|
| Child booster              | Stiffness Factor      | 0.5-3.0   | 1.0           |
| Seatbelt                   | Stiffness Factor      | 0.5-0.9   | 0.7           |
| Load limiter <sup>a)</sup> | Load limit (N)        | 2000-6000 | 4000          |
| P-ring <sup>b)</sup>       | Height (mm)           | 900-1200  | 1100          |
| Dummy and booster          | Friction coefficient  | 0.1-0.6   | 0.3           |

a) P-ring is labeled in Fig.1.

b) A load limiting seatbelt provides a limited belt force level (called load limiter) to the occupant in severe impact as opposed to increasing the force without any limit in traditional belt and thus inflicts injury.



**Fig. 2.** Response surface of HIC with respect to the belt load limit and the friction coefficient between the dummy and the booster

### 3 Coupling of MADYMO and Particle Swarm Optimization

#### 3.1 Particle Swarm Optimization

In 1995, Kennedy and Eberhart proposed the concept of Particle Swarm Optimization (PSO), which originated from the study of social behavior of bird flocks and fish schools [6]. It is related to genetic algorithms and falls into the framework of evolutionary optimization algorithms. In general, PSO has a very loose requirement on the optimization problem. For instance, the design variables can be either continuous or discrete, the objective function can be either explicit or implicit, and the feasible region can be either convex or concave. Due to its distinct characteristics from traditional optimization schemes and other evolutionary schemes, PSO has attracted much attention from the computational intelligence community to a wide variety of disciplines. The study of the algorithm itself as well as its application is booming in the literature.

The original PSO for unconstrained optimization can be briefly described as follows [6]. Assume the design variable is  $n$ -dimensional. At first, a set of random solutions (called particles)  $\mathbf{x}_i \in R^n$ ,  $i=1, \dots, m$ , are generated in the design space, where  $m$  denotes the population size (the number of particles). Each particle is assigned a random velocity  $\mathbf{v}_i \in R^n$ , which represents the displacement of the corresponding particle in the design space at current iteration. By evaluating the fitness (usually the objective value) of the particles, one can determine each particle's best location that it has ever visited so far, denoted by  $\mathbf{p}_i \in R^n$ ; and the entire population's best location that all the particles have ever visited so far, denoted by  $\mathbf{p}_g \in R^n$ . Then the velocity and position of each particle for the next iteration is updated as

$$\begin{aligned} v_{ij}(t+1) &= wv_{ij} + c_1r_{1j}(t)(p_{ij}(t) - x_{ij}(t)) + c_2r_{2j}(t)(p_{gj}(t) - x_{ij}(t)) \\ x_{ij}(t+1) &= x_{ij}(t) + v_{ij}(t+1) \end{aligned} \quad (1)$$

where  $i=1, \dots, m$ ,  $j=1, \dots, n$ ,  $t$  stands for the current iteration number,  $w$ ,  $c_1$ ,  $c_2$  are coefficients that can be adjusted by the user.  $r_{1j}$  and  $r_{2j}$  are two independent random functions whose values are between (0,1).

To handle constrained optimization, one usually converts the problem into an unconstrained one by adding a penalty for the violation of the constraints to the original objective function. However, the selection of an appropriate penalty function together with a set of related parameters for a particular problem requires a lot of experience and patience. Another technique is adopted in this study to handle the constraints. For each particle, its objective function value and the total violation of constraints are calculated and stored as its two properties. In assigning fitness to the entire population of particles, the following principle is adopted (assuming that the goal is to minimize the objective function, and higher fitness means better).

- Feasible particles always have higher fitness than infeasible particles.
- For feasible particles, those with smaller objectives have higher fitness than those with greater objectives.
- For infeasible particles, those with less violation of the constraints have higher fitness than those with more violation of the constraints.

### 3.2 Interface Between MADYMO and Particle Swarm Algorithm (PSA)

In addition to the GUI execution mode, MADYMO is able to run in a batch mode by defining its input file. In either mode, MADYMO produces several output files in the end. These files provide a possibility for other programs or third-party software to interact with MADYMO. Fig. 3 shows a brief flow chart regarding solving the MADYMO simulation based optimization problems by using PSA. It is observed that except the MADYMO module all tasks of the modules in Fig. 3 should be accomplished by the program that codes PSA. In other words, MADYMO can be viewed as a black-box in the process.

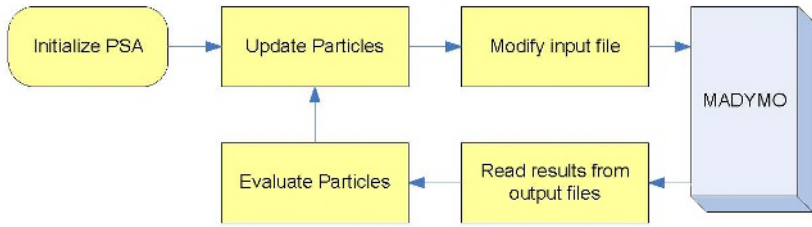


Fig. 3. MADYMO based optimization process by using PSA

### 4 Optimization Results

The population size is set to 30, and the algorithm terminates after 20 iterations. So the total number of function evaluations (MADYMO callings) is 600. In the update formula (1), set  $c_1 = c_2 = 1.9$ , and  $w = 0.7$ . Ten runs have been conducted and the statistical data are summarized in Table 2. The discrepancy of the ten HIC results is acceptable, with a standard deviation of  $10.5(\pm 4.9\%)$ , and all output solutions satisfy the head displacement constraint. The best solution found by PSA among the 10 runs is shown in Table 3. Compared with the initial design scheme, the optimal scheme has much lower HIC value without sacrifice of much head displacement. Fig. 4 shows the CRS at different time stages in the ECE Regulation 44 frontal impact test.

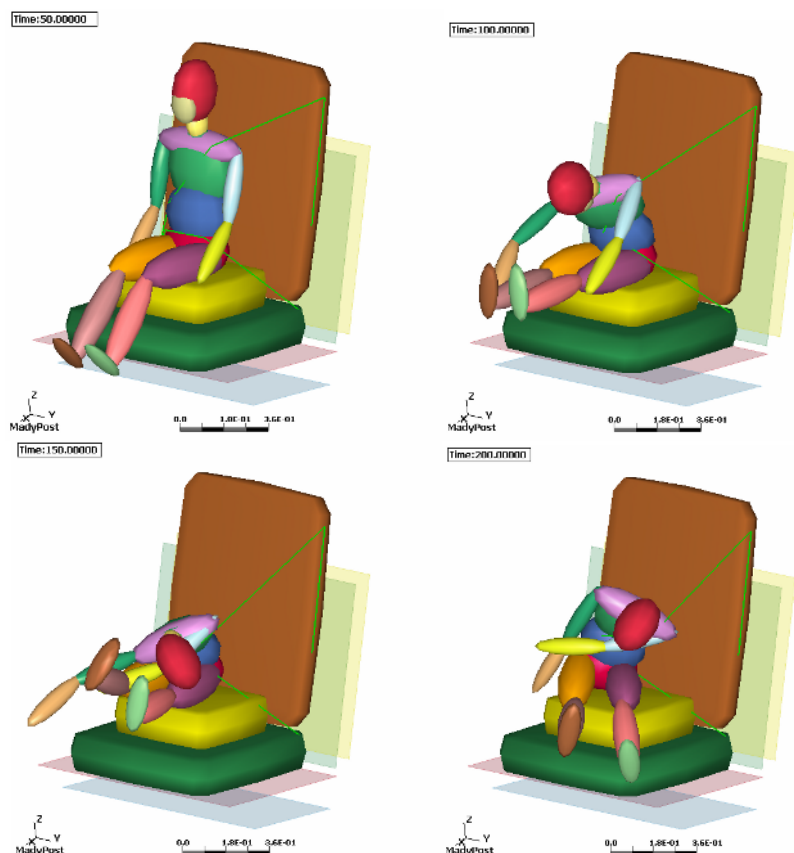
Table 2. Statistical data for 10 runs of the PSA

|                                                      | Best | Worst | Average | Standard deviation | Tolerance   |
|------------------------------------------------------|------|-------|---------|--------------------|-------------|
| <b>Optimization objective: HIC</b>                   | 192  | 228   | 213     | 10.5               | $\pm 4.9\%$ |
| optimization constraint : Head displacement < 550 mm |      |       |         |                    |             |

Table 3. Optimization results of CRS

|                | Load Limit (N) | Friction Coefficient | Belt Stiffness | Bolster Stiffness | P-ring Height (mm) | HIC | Head displacement (mm) |
|----------------|----------------|----------------------|----------------|-------------------|--------------------|-----|------------------------|
| <b>Initial</b> | 4000           | 0.3                  | 0.7            | 1                 | 1100               | 711 | 399                    |
| <b>PSA</b>     | 2123           | 0.46                 | 0.89           | 2.43              | 937                | 192 | 442                    |
| <b>AutoDOE</b> | 2000           | 0.5                  | 0.9            | 2                 | 900                | 213 | 435                    |

The last row of Table 3 lists the optimal results from AutoDOE, the scheme specifically developed for MADYMO based optimization [4]. Before the optimization, one has to discretize each variable into several levels. These discrete values of variables constitute a set of combinations of all variables. AutoDOE evaluates each



**Fig. 4.** Simulation of CRS in the frontal impact test. The corresponding times in millisecond are displayed in the top-left corner on each picture.

**Table 4.** Levels of variables for AutoDOE optimization

| Level                | 1    | 2    | 3    | 4    | 5    | 6   |
|----------------------|------|------|------|------|------|-----|
| Load Limit (N)       | 2000 | 3000 | 4000 | 5000 | 6000 | --  |
| Friction Coefficient | 0.1  | 0.2  | 0.3  | 0.4  | 0.5  | 0.6 |
| Belt Stiffness       | 0.5  | 0.6  | 0.7  | 0.8  | 0.9  | --  |
| Bolster Stiffness    | 0.5  | 0.75 | 1.0  | 2.0  | 3.0  | --  |
| P-ring Height (mm)   | 900  | 1000 | 1100 | 1200 | --   | --  |

combination of variables by calculating the corresponding objective and constraint values, and then chooses the best one as *optimum*. For this problem, the levels of variables shown in Table 4 are selected. Based on these levels AutoDOE evaluates 3000 solutions in total. The optimum is listed in Table 3.

The results listed in Tables 2 and 3 indicate that the PSA achieves the same quality solutions as AutoDOE does. But PSA calculates much fewer times of objective



functions than AutoDOE. For both methods, most of execution time is spent on the evaluation of the objective function, i.e., MADYMO executions, and each evaluation takes about 12 seconds on a 1.8 GHz personal computer. Hence, 2400 fewer evaluations result in significantly less computing time and is favored by users.

## 5 Conclusions

In this paper, the design of a child restraint system is modeled and optimized based on the multi-body dynamics simulator MADYMO. A particle swarm algorithm that adopts a novel technique for handling constraints is used to solve the problem. Compared with AutoDOE, a built-in optimization method of MADYMO that can only handle low dimensional problems, the PSA does not have this limitation, and hence is suitable for simulation based complex optimization problems. Moreover, the comparison between the proposed PSA and AutoDOE shows that the former is more computational efficient than the latter for achieving same quality solutions.

## Acknowledgement

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# Predicted-Velocity Particle Swarm Optimization Using Game-Theoretic Approach

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**Abstract.** In standard particle swarm optimization, velocity information only provides a moving direction of each particle of the swarm, though it also can be considered as one point if there is no limitation restriction. Predicted-velocity particle swarm optimization is a new modified version using velocity and position to search the domain space equality. In some cases, velocity information may be effectively, but fails in others. This paper presents a game-theoretic approach for designing particle swarm optimization with a mixed strategy. The approach is applied to design a mixed strategy using velocity and position vectors. The experimental results show the mixed strategy can obtain the better performance than the best of pure strategy.

## 1 Introduction

Inspired by the bird flocking and fish schooling, particle swarm optimization (PSO)[1][2] is proposed to simulate animal social behaviors, and has been applied many areas successfully[3][4][5][6][7][8].

Though many techniques have been proposed to enhance the computational efficiency, there still exists work to do by providing a proportional search direction selection principle. In PSO, each particle maintains two different information: position and velocity. Usually, position vector limited by constant  $v_{max}$  is used to search the optima as well as velocity provides a direction to guide the search. The empirical results[9] performed by Shi and Eberhart show that the limitation of velocity does not necessary. Furthermore, Z.H.Cui proposed a new version of PSO[10] which is using velocity and position vectors to search without any differences, and the corresponding theoretical analysis without velocity limitation  $v_{max}$  is illustrated in [11]. Since velocity information is considered as a predictor, while position information as one corrector, the algorithm is called predicted-velocity PSO (PVPSO). Though the velocity vector is used as one operator similar with position vector to making global search during the search

process. One main problem relating with effectiveness is how to select the historical best position found by each particle?

One simple way is to compute the velocity and position vectors respectively, determining the historical best position related with velocity and position vectors. There are few researches towards this direction[10][12].

In this paper, we propose a different way to design a mixed strategy. It mixed position and velocity vectors. In this way, each particle chooses one of these strategies to generate its new historical best position to a mixed distribution.

The paper is organized as follows. Section 2 gives a brief survey of particle swarm optimization. The hybrid modal using game theory is introduced in section 3. Seven benchmark functions are used to testify the new algorithm's efficiency in section 4. Finally, the useful conclusions are made.

## 2 Brief Survey of Particle Swarm Optimization

Particle swarm optimization is based on the sociological behavior associated with bird flocking[13]. Each 'bird'(called particle) flies within search space, owning two characters: position and velocity, while position vector is used to determine the situation, and velocity vector to provide a displacement value. The position and velocity update equations of standard PSO at time  $t + 1$  are presented in equation (1) and (2):

$$v_{jk}(t + 1) = wv_{jk}(t) + c_1r_1(p_{jk}(t) - x_{jk}(t)) + c_2r_2(p_{gk}(t) - x_{jk}(t)) \quad (1)$$

$$x_{jk}(t + 1) = x_{jk}(t) + v_{jk}(t + 1) \quad (2)$$

where the  $k^{th}$  dimensional variable  $v_{jk}(t + 1)$  of velocity vector  $V_j(t + 1) = (v_{j1}(t + 1), v_{j2}(t + 1), \dots, v_{jn}(t + 1))$  ( $n$  denotes the dimension of problem space) limited by

$$|v_{jk}(t + 1)| < v_{max} \quad (3)$$

where  $v_{jk}(t)$  and  $x_{jk}(t)$  are the  $k^{th}$  dimensional variables of velocity and position vectors of particle  $j$  at time  $t$ ,  $p_{jk}(t)$  and  $p_{gk}(t)$  are the  $k^{th}$  dimensional variables of historical positions found by particle  $j$  and the whole swarm at time  $t$  respectively.  $w$  is an inertia weight between 0 and 1,  $c_1$  and  $c_2$  are both constants known as accelerator coefficients, and  $r_1$  and  $r_2$  are two random numbers generated with uniform distribution within  $(0, 1)$ .

PVPSO[10][11] is a new version using velocity and position to search optima, while the difference between PVPSO and PSO is only the selection principle of historical best position. It is defined as follows for particle  $j$ :

$$p_{jk}(t + 1) = \begin{cases} p_{jk}(t), & \text{if } f(p_j(t)) = \min\{f(p_j(t)), f(x_j(t + 1)), f(v_j(t + 1))\} \\ x_{jk}(t + 1), & \text{if } f(x_j(t + 1)) = \min\{f(p_j(t)), f(x_j(t + 1)), f(v_j(t + 1))\} \\ v_{jk}(t + 1), & \text{otherwise} \end{cases} \quad (4)$$

### 3 Predicted-Velocity PSO Using Game-Theoretic Approach

In this paper, particles are regarded as players in an artificial evolutionary game, who apply different strategies (position and velocity vectors) to generate the historical best position at arbitrary time, and the distribution is adaptive adjusted.

Position vector or velocity vector of each particle can be considered as a *pure strategy* in the terms of game theory, and a *pure strategy profile* is reward of pure strategies used by particles.

At beginning, the selection probabilities of position and velocity vectors are both set to 0.5. If one pure strategy is selected and the historical best position is updated by it, suppose  $\rho_j(t)$  denotes the selection probability of this strategy of particle  $j$  at time  $t$ , then its selection probability is changed as follows.

$$\begin{cases} \rho_j(t + 1) = \rho_j(t) + (1 - \rho_j(t))\gamma \\ \rho_k(t + 1) = \rho_k(t) - \rho_k(t)\gamma, \text{ if } (k \neq j) \end{cases} \quad (5)$$

On the contrary, if one pure strategy is selected and the historical best position is not updated by it, its selection probability is changed with

$$\begin{cases} \rho_j(t + 1) = \rho_j(t) - \rho_j(t)\gamma \\ \rho_k(t + 1) = \rho_k(t) + \rho_k(t)\gamma, \text{ if } (k \neq j) \end{cases} \quad (6)$$

In this paper,  $\gamma$  is set to 0.3. The pseudocode of predicted-velocity particle swarm optimization using game-theoretic approach(PVGPSO) is as follows:

- Step1. Initiating the coefficients  $c_1, c_2, w$ , the position and velocity vectors of each particles,  $t:=0$ ;
- Step2. Updating the position and velocity vectors of each particle at time  $t + 1$ ;
- Step3. Determining one pure strategy to update the historical best position of each particle;
- Step4. Modifying selection probability of corresponding pure strategy with formula (5) and (6);
- Step5. Updating the historical best positions of the swarm,  $t=t+1$ ;
- Step6. If stop criteria is satisfied, the fitness value of historical best position of swarm is given. Otherwise, go to step 2.

### 4 Simulation Results

The benchmark functions in this section provide a balance of unimodal and multi-modal with many local minima as well as easy and difficult functions.

Sphere Modal:

$$f_1(x) = \sum_{j=1}^n x_j^2$$

where  $\min f_1(x) = f_1(0, 0, \dots, 0) = 0.0$ .

Schwefel Probleme 1.2:

$$f_2(x) = \sum_{j=1}^n \left( \sum_{i=1}^j x_i \right)^2$$

where  $\min f_2(x) = f_3(0, 0, \dots, 0) = 0.0$ .

Schwefel Problem 2.21:

$$f_3(x) = \max_j \{|x_j|, 1 \leq j \leq n\}$$

where  $\min f_3(x) = f_4(0, 0, \dots, 0) = 0.0$ .

Schwefel Problem 2.26:

$$f_4(x) = - \sum_{j=1}^n (x_j \sin(\sqrt{|x_j|}))$$

where  $\min f_4(x) = f_6(420.9687, 420.9687, \dots, 420.9687)$ .

Rastrigin Function:

$$f_5(x) = \sum_{j=1}^n [x_j^2 - 10 \cos(2\pi x_j) + 10]$$

where  $\min f_5(x) = f_8(0, 0, \dots, 0) = 0.0$ .

Ackley Function:

$$f_6(x) = -20 \exp\left(-0.2 \sqrt{\frac{1}{n} \sum_{j=1}^n x_j^2}\right) - \exp\left(\frac{1}{n} \sum_{j=1}^n \cos 2\pi x_j\right) + 20 + e$$

where  $\min f_6(x) = f_9(0, 0, \dots, 0) = 0.0$ .

Griewank Function:

$$f_7(x) = \frac{1}{4000} \sum_{j=1}^n x_j^2 - \prod_{j=1}^n \cos\left(\frac{x_j}{\sqrt{j}}\right) + 1$$

where  $\min f_7(x) = f_{10}(0, 0, \dots, 0) = 0.0$ .

**Table 1.** Comparison Results of Sphere

| Algorithm | Mean Value    | Standard Deviation |
|-----------|---------------|--------------------|
| SPSO      | 7.215190e-008 | 7.450365e-008      |
| PVPSO     | 4.172490e-011 | 1.046000e-010      |
| PVGPSO    | 2.660275e-013 | 5.973800e-013      |

**Table 2.** Comparison Results of Schwefel Problem 1.2

| Algorithm | Mean Value    | Standard Deviation |
|-----------|---------------|--------------------|
| SPSO      | 1.975425e+001 | 8.721134e+000      |
| PVPSO     | 6.489995e-016 | 2.114932e-015      |
| PVGPSO    | 5.932653e-018 | 1.614740e-017      |

**Table 3.** Comparison Results of Schwefel Problem 2.21

| Algorithm | Mean Value    | Standard Deviation |
|-----------|---------------|--------------------|
| SPSO      | 6.415644e-001 | 1.876893e-001      |
| PVPSO     | 8.403330e-007 | 1.709603e-006      |
| PVGPSO    | 4.311013e-007 | 1.101034e-006      |

**Table 4.** Comparison Results of Schwefel Problem 2.26

| Algorithm | Mean Value     | Standard Deviation |
|-----------|----------------|--------------------|
| SPSO      | -6.456704e+003 | 6.567289e+002      |
| PVPSO     | -9.037158e+003 | 4.029658e+002      |
| PVGPSO    | -8.435084e+003 | 4.392656e+002      |

**Table 5.** Comparison Results of Rastrigin

| Algorithm | Mean Value    | Standard Deviation |
|-----------|---------------|--------------------|
| SPSO      | 3.039597e+001 | 9.654424e+000      |
| PVPSO     | 1.050993e-010 | 2.228909e-010      |
| PVGPSO    | 2.762235e-014 | 7.448329e-014      |

**Table 6.** Comparison Results of Ackley

| Algorithm | Mean Value    | Standard Deviation |
|-----------|---------------|--------------------|
| SPSO      | 4.384384e-005 | 2.229432e-005      |
| PVPSO     | 2.832723e-006 | 6.603540e-006      |
| PVGPSO    | 1.463668e-007 | 3.216559e-007      |

**Table 7.** Comparison Results of Griewank

| Algorithm | Mean Value    | Standard Deviation |
|-----------|---------------|--------------------|
| SPSO      | 9.106786e-003 | 1.321899e-002      |
| PVPSO     | 2.533268e-010 | 9.538407e-010      |
| PVGPSO    | 2.291722e-012 | 4.545413e-012      |

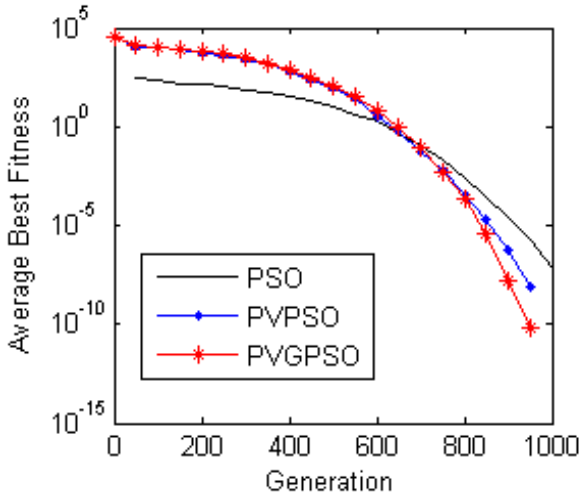


Fig. 1. Comparison Results of Sphere

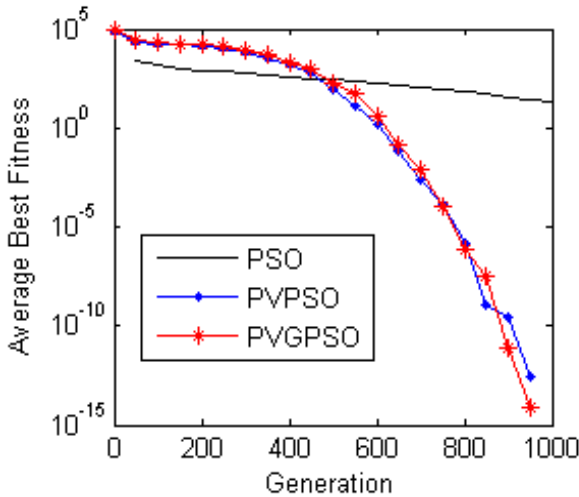


Fig. 2. Comparison Results of Schwefel Problem 1.2

Sphere, Schwefel problem 1.2 and 2.21 are n-dimensional unimodal functions while Schwefel problem 2.26, Rastrigin, Ackley and Griewank are n-dimensional multimodal functions with many local minima.

To give a more detail comparison, two different versions of PSO are used to compare: standard PSO (SPSO) and predicted-velocity PSO (PVPSO). For each experiment the simulation records the mean value and standard deviation value over all the runs. The coefficients of SPSO, PVPSO, and PVGPSO are set as

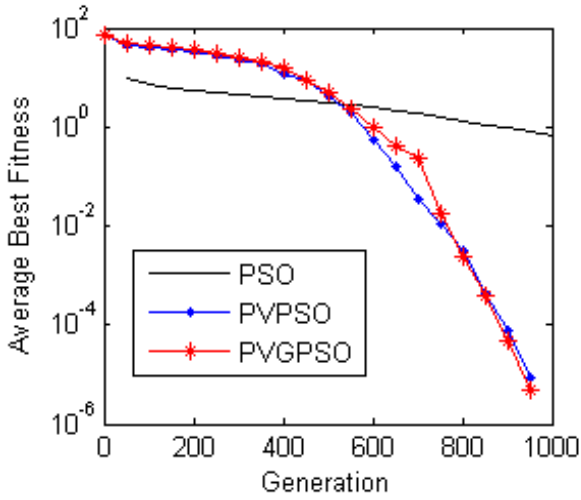


Fig. 3. Comparison Results of Schwefel Problem 2.21

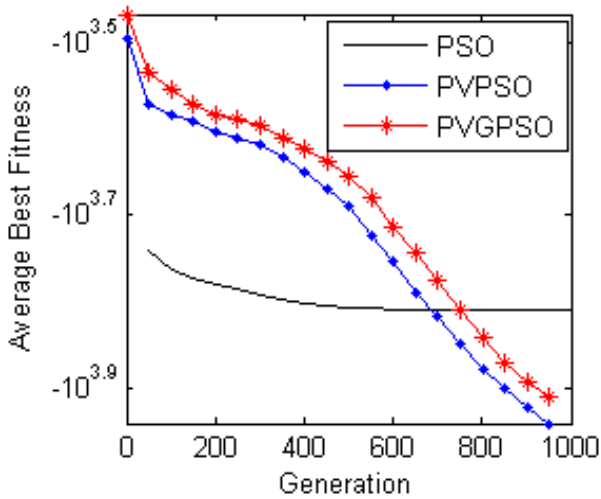


Fig. 4. Comparison Results of Schwefel Problem 2.26

follows. The inertia weight  $w$  is decreased linearly from 0.9 to 0.4 during the course, and two accelerator coefficients are set to 2.0. The dimension of each problem is 30. Total particles are 100, and  $v_{max}$  is set to 10% of the upper bound of domain in SPSO. Each experiment the simulation run 20 times while each time the largest evolutionary generation is 1000.



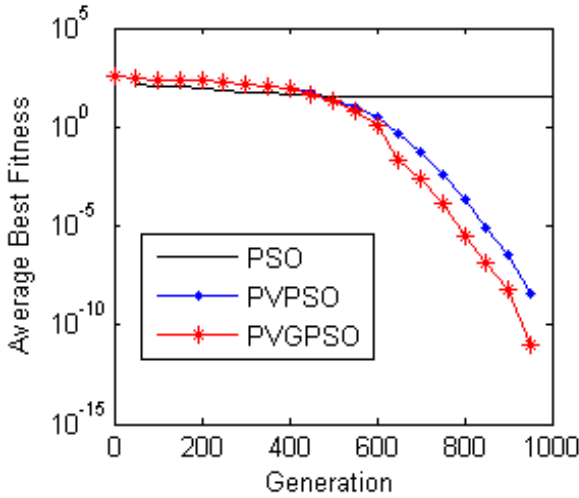


Fig. 5. Comparison Results of Rastrigin

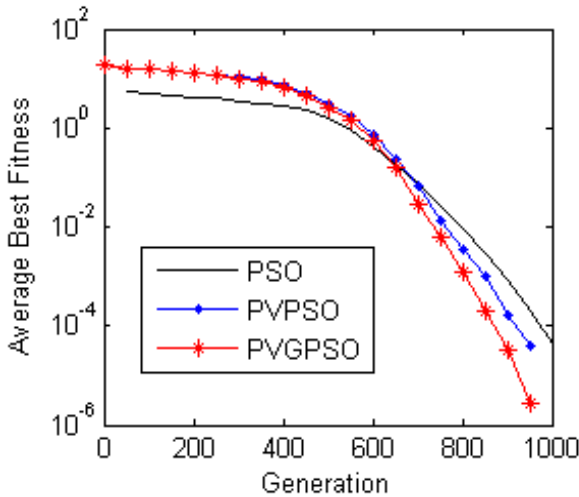


Fig. 6. Comparison Results of Ackley

Table 1 to 3 (see also Fig.1 to 3) are the comparison results of unimodal function. PVGPSO surpasses the PVPSO and SPSO in the final strategy while the SPSO is superior than PVPSO and PVGPSO at the first period.

Table 4 to 7 (see also Fig.4 to 7) are the comparison results of multi-modal functions with many local optima. PVGPSO can always find better quantity solution than PVPSO and SPSO except for Schwefel problem 2.26. In one word, PVGPSO is a better hybrid method based on game theory than single version of PVPSO and SPSO.

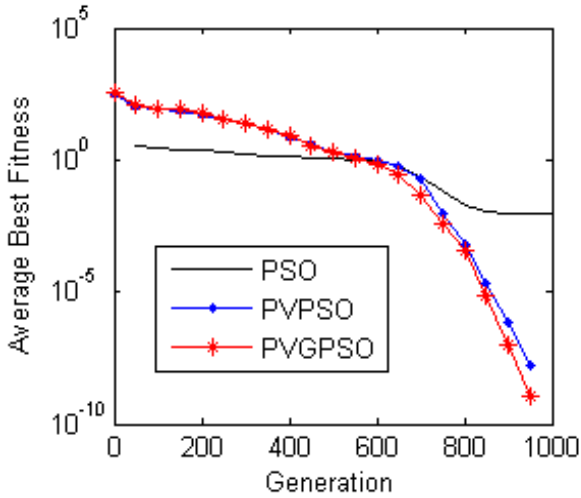


Fig. 7. Comparison Results of Griewank

## 5 Conclusion

This paper introduces a new hybrid version of particle swarm optimization using game theory. The results show that the proposed algorithm has a good performance of computational efficiency. The further research is the hybrid strategy about n-players game theory.

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# Solving the Hard Knapsack Problems with a Binary Particle Swarm Approach

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**Abstract.** Knapsack problems are important NP-Complete combinatorial optimization problems. Although nearly all the classical instances can be solved in pseudo-polynomial time nowadays, yet there are a variety of test problems which are hard to solve for the existing algorithms. In this paper we propose a new approach based upon binary particle swarm optimization algorithm (BPSO) to find solutions of these hard knapsack problems. The standard PSO iteration equations are modified to operate in discrete space. Furthermore, a heuristic operator based on the total-value greedy algorithm is employed into the BPSO approach to deal with constrains. Numerical experiments show that the proposed algorithm outperforms both the existing exact approaches and recent state-of-the-art search heuristics on most of the hard knapsack problems.

## 1 Introduction

The well-known NP-complete knapsack problem (KP) is defined as: given a set of items with corresponding unit profits  $p_j$  and unit weights  $w_j$ , along with a knapsack capacity limit  $c$ , selects a subset of the items such that the total profit is maximized with the total weight not exceeding  $c$ . It can be assumed, without loss of generality, that all profits and weights are positive, that all weights are smaller than the knapsack capacity  $c$  and that the total weight exceeds the capacity. By introducing the binary decision variable  $x_j$ , with  $x_j = 1$  if item  $j$  is selected, and  $x_j = 0$  otherwise, the classical 0/1 knapsack problem can be formulated as:

$$\begin{aligned} & \text{maximize} && \sum_{j=1}^n p_j x_j \\ & \text{subject to} && \sum_{j=1}^n w_j x_j \leq c \quad \text{with} \quad x_j \in \{0, 1\}, j = 1, \dots, n . \end{aligned}$$

In the last few decades, many exact or heuristic techniques have been proposed to solve the knapsack problems. The exact algorithms include dynamic

programming [1,2] and branch-and-bound [3,4], while the heuristic search procedures focusing on solving the problem approximately include tabu search [5], genetic algorithm (GA) [6,7] and other randomized methods. A good overview of all recent exact approaches can be seen in [8]. It is shown that although the existing algorithms are capable of solving nearly all the KP instances cited in the existing literature within reasonable time, there are two groups of new test KP problems which are hard to solve. For the first group of difficult instances with large coefficients the running times of the dynamic programming algorithms are unacceptably high, while for the other group containing six categories of structurally instances with small coefficients the branch-and-bound algorithms perform badly.

In this paper a novel BPSO algorithm is developed to solve the hard knapsack problems. A heuristic operator converting infeasible solutions into feasible solutions is applied to deal with the knapsack constrains. The procedure of the operator is based on the total-value heuristic which picks the item that contributes the highest total profit given the remaining knapsack capacity at each stage. In order to test the BPSO algorithm thoroughly, we adopt the technique in [8] to construct test instances. The experimental results of three different types of algorithms are compared with ours.

The rest of the paper is organized as follows. In Section 2, a brief introduction of PSO is given. Then a binary particle swarm algorithm for knapsack problems are proposed in Section 3. Section 4 presents the generation of the two groups of difficult instances and the performance comparison of our algorithm and the most recent algorithms on the instances. A set of conclusions are given in Section 5.

## 2 Particle Swarm Optimization

The particle swarm optimization was originally invented for the function optimization in continuous real-number spaces by Kennedy and Eberhart [9]. A review of its recent approaches to global optimization problems is presented in [10]. In a PSO model, a potential solution is represented as a particle with position  $X_{id}$  and velocity  $V_{id}$  in a D-dimensional space. Each particle maintains a record of the position with best fitness value the particle experienced so far, called personal best position or  $Pbest$ . Each particle share its  $Pbest$  with its neighborhoods, so there is a global best solution  $Gbest$ . At each search iteration, the  $i$ th particle moves according to the following equations:

$$V_{id} = V_{id} + \alpha \cdot (Pbest_{id} - X_{id}) + \beta \cdot (Gbest_d - X_{id}) \quad (1)$$

$$X_{id} = X_{id} + V_{id} \quad (2)$$

where  $\alpha$  and  $\beta$  are random numbers whose upperbounds determine the influence of  $Pbest$  and  $Gbest$ .

In order to improve the performance of the original PSO algorithm, some revised versions of PSO algorithm are proposed. One of the approaches is to introduce inertia weight  $\omega$  into (1), so (1) is substituted by

$$V_{id} = \omega \cdot V_{id} + \alpha \cdot (Pbest_{id} - X_{id}) + \beta \cdot (Gbest_d - X_{id}) . \quad (3)$$

A BPSO algorithm which operates in discrete space has been developed in [11]. But this BPSO algorithm is susceptible to function saturations, which occur when velocity values are either too large or too small. A technique using angle modulation to reduce the complexity of binary problems is proposed in [12]. Though efficient it leaves the discrete constraint satisfaction problems untouched. We will present our BPSO algorithm based on the inertia weight PSO model in the next section.

### 3 A BPSO Algorithm for KP

#### 3.1 Representation

Like GA, the first step in implementing a BPSO algorithm is to design a scheme to denote individuals. Since the decision variable  $x_j$  is binary, it is an obvious choice to represent a solution using an  $n$ -bit binary string, where  $n$  is the number of items in the KP. Thus each particle's position and velocity in our algorithm are initialized as  $n$ -bit binary-coded random vectors.

#### 3.2 Iteration Equations

Before presenting the iteration equations, we begin with introducing some new operators to be applied in our proposed BPSO.

In a binary space, a particle moves to nearer or farther corners of the hypercube (searching space) by flipping bits in its position vector. So the distance between a particle's current position and its previous best position (in (3) denoted as " $Pbest_{id} - X_{id}$ " of the  $d$ th dimension) can be stated by a vector whose bit is 1 if the alleles of  $X_i$  and  $Pbest_i$  are different and sets to 0 otherwise. For example, a particle's current position and its previous best position are:

$$\begin{aligned} X &: (10011) \\ Pbest &: (00011) \end{aligned}$$

so the distance will be (10000) since the first bits in the two vectors are different. From this simple example, it can be observed that the distance is the output of the binary *XOR* function which takes  $X$  and  $Pbest$  as its two inputs. In this way, the operation " $Pbest_{id} - X_{id}$ " in (3) will be substituted with " $Pbest_{id} \oplus X_{id}$ ". Similarly, the distance between a particle's current position and the global best position will be evaluated by " $Gbest \oplus X_i$ ".

From (3), it can be seen that a particle's velocity at iteration  $t + 1$  is primarily determined by three elements: the velocity at iteration  $t$ , the distance between  $X_i$  and  $Pbest$  and the distance between  $X_i$  and  $Gbest$ . Since the functions of the three elements (also vectors) are to reverse the corresponding bits in the position vector consistently, they can be united into one vector. Consequently,

this procedure is implemented using the *OR* operation. Here is an example: supposing the three elements are

$$\begin{aligned} A &: (10001) \\ B &: (01000) \\ C &: (00100) \end{aligned}$$

respectively, then the velocity will be  $V = A + B + C = (11101)$ .

A particle's position vector will be updated at the next step using the velocity vector. If any bit in the velocity vector is 1, the allele in the position vector will be reversed. And this operation is a equivalence of binary XOR function. This can be illustrated by going on with the previous example. With a arbitrary position vector being (10000), the updated position vector will be (01101) at next iteration.

As a result, a particle in a binary space moves according to the following equations:

$$V_{id} = \omega \cdot V_{id} + \alpha \cdot (Pbest_{id} \oplus X_{id}) + \beta \cdot (Gbest_d \oplus X_{id}) \quad (4)$$

$$X_{id} = X_{id} \oplus V_{id} \quad (5)$$

where inertia weight  $\omega$  is generally set to less than 1.0.  $\alpha$  and  $\beta$  are called acceleration coefficients used to control the convergence speed of the algorithm. Based on the previous work in [13], we have set the typical parameters for a population of 50, the inertia weight  $\omega$  of 0.729,  $\alpha$  of 1.49 and  $\beta$  of 1.49.

### 3.3 Constraints Handling

Obviously, the solutions generated by (4) may not be feasible because one of the knapsack constraints may be violated. To deal with constraints, a number of standard ways are proposed. Comparing their performance through preliminary experiments, we adopt in our BPSO the approach of using a heuristic operator to convert an infeasible solution to a feasible one.

The heuristic operator is traditionally based on a density-ordered greedy algorithm which picks the item with the highest unit profit to unit weight ratio at each stage. Instead of using the density-ordered greedy algorithm, our heuristic operator is based on a total-value greedy algorithm in which the item with highest profit will be selected if its weight does not exceed the remaining knapsack capacity at each stage. It has been shown that the total-value greedy heuristic dominates the density-ordered greedy algorithm with regard to both the worst-case performance and the average-case performance [14].

Our heuristic operator is constituted of two phases: the drop phase and the add phase. The drop phase is implemented as follows. Once a solution  $X_i = (x_1, x_2, \dots, x_n)$  generated by BPSO is infeasible, first calculate its redundancy weight  $\sum_{j=1}^n (w_j x_j - c)$  (bigger than zero obviously). Then, among the items picked in the infeasible solution, find out the subset of items with the weight of each item is smaller than the redundancy weight. Throw out the items one by one in the subset with ascent order in weight until the solution becomes feasible.

The add phase aim to improve the fitness of a feasible solution. Given the remaining knapsack capacity, the add phase continue to add the item with the largest profit among the items that are not included in the solution and whose weights are smaller than the remaining knapsack capacity until feasibility is violated.

### 3.4 Algorithm Outline

The general steps in our algorithm are described as follows:

```

initialize each particle with a random position and velocity;
initialize t_max;
while t<t_max {
 for i=1:population size {
 if a solution is infeasible {
 make the solution feasible;
 }
 calculate fitness value;
 }
 find Pbest and Gbest;
 updating each particle's position according to (4,5);
}

```

## 4 Computational Experiments

In order to test our algorithm for the knapsack problem more thoroughly, we will analyze its performance in terms of both efficiency and accuracy. Efficiency is a measure of the time required to complete the search and accuracy is what evaluates the quality of the solutions obtained. The test instances we use for measurements are some of the instances from [8], which contains a large variety of instances types. The performance for different instance types and data ranges of our approach is compared with that of the GA [6] and two well-known exact approaches, namely Expknapsack [4] and Minknapsack [1].

Two groups of difficult instances are considered in our experiments. One group consists of the traditional instances with larger coefficients; and the other group includes instances with small coefficients, but where present algorithms perform badly. The first group make the dynamic programming algorithm run slower while the second group mainly challenge the branch-and-bound algorithms.

### 4.1 Difficult Instances with Large Coefficients

Six types of traditional data instances are briefly described below. Because the traditional test instances with small data range are too easy to draw any meaningful conclusions, we choose each type with data range  $R=10^6$  and  $10^7$  for different problem sizes (i.e.  $n=100, 500, 1000, 5000$  and  $10000$ ) for testing.

*Uncorrelated instances (uncorr.):* The weights  $w_j$  and the profits  $p_j$  are chosen randomly in  $[1, R]$ .



*Weakly correlated instances (weak corr.):* The weights  $w_j$  are distributed in  $[1, R]$  and the profits  $p_j$  in  $[w_j - R/10, w_j + R/10]$  such that  $p_j \geq 1$ .

*Strongly correlated instances (str. corr.):* The weights are chosen in  $[1, R]$  and the profits are set to  $p_j = w_j + R/10$ .

*Inverse strongly correlated instances (inv. str. corr.):* The profits  $p_j$  are chosen in  $[1, R]$  and  $w_j = p_j + R/10$ .

*Almost strongly correlated instances (al. st. corr.):* The weights  $w_j$  are distributed in  $[1, R]$  and the profits in  $[w_j + R/10 - R/500, w_j + R/10 + R/500]$ .

*Subset-sum instances (sub.sum):* The weights  $w_j$  are distributed in  $[1, R]$  and  $p_j = w_j$ .

In order to eliminate the capacity-dependency of the performances, we choose the capacity in each instance as

$$c = \frac{h}{1000 + 1} \sum_{j=1}^n w_j$$

for instance number  $h = 1, 2, \dots, 1000$ . We test all the instances on an Intel Pentium 4, 2.9GHz with 256M RAM. The average execution time for each instance type, which is also the average time the BPSO takes for all the 1000 instances, is calculated. Table 1-3 gives the results for the three algorithms. For each instance type, if not all instances are solved in a time limit of 30 minutes or space limit, it is marked with a “—” in the table. “Best-so-far” values searched in 50 runs by our algorithm and GA during the same time period are compared in Table 4. A typical run for GA is set for a probability of crossover of 0.8; a probability of mutation of 0.01; and a population of 50 (same as the population in our BPSO algorithm). In each run we choose the time limit of 10 minutes as the stopping conditions for GA and our BPSO.

It is clear that our BPSO algorithm has a stable performance on all the instance types whereas the exact algorithm Expknapsack can solve only a few instances within the given time or space limit. For the dynamic programming algorithm Minknapsack, the average execution time for the strongly correlated and the inverse strongly correlated instances grow to run out of the time limit due to the rapid increasing of the computational complexity. From the results in Table 4, it can be observed that the near-optimal solutions obtained by our BPSO algorithm are more closer to the optimal solution than those obtained by GA for a majority of instances.

## 4.2 Difficult Instances with Small Coefficients

The following are some difficult instances with small coefficients. The capacity is chosen as in the previous section. The outcomes are summarized in Table 5-7. *Spanner instances( $v, m$ ):* The weights  $w_k$  of a set of  $v$  items (the spanner set) are chosen in  $[1, R]$  randomly and the profits according to the three distributions (uncorrelated, weakly correlated and strongly correlated respectively). Then the  $v$  items are normalized by setting  $p_k = \lfloor 2p_k/m \rfloor$  and  $w_k = \lfloor 2w_k/m \rfloor$ . The  $n$  items are constructed by repeatedly multiplying a random number in the interval

**Table 1.** Average execution times (ms) for instances with large coefficients, Expknap

| $n \setminus R$ | <i>uncorr.</i> |        | <i>weakcorr.</i> |        | <i>str.corr.</i> |        | <i>inv.str.corr.</i> |        | <i>al.str.corr.</i> |        | <i>sub.sum</i> |        |
|-----------------|----------------|--------|------------------|--------|------------------|--------|----------------------|--------|---------------------|--------|----------------|--------|
|                 | $10^6$         | $10^7$ | $10^6$           | $10^7$ | $10^6$           | $10^7$ | $10^6$               | $10^7$ | $10^6$              | $10^7$ | $10^6$         | $10^7$ |
| 100             | 0.1            | -      | -                | -      | -                | -      | -                    | -      | 627.1               | -      | 13.1           | 187.4  |
| 500             | 0.1            | 0.1    | -                | -      | -                | -      | -                    | -      | -                   | -      | 18.9           | -      |
| 1000            | 0.3            | -      | -                | -      | -                | -      | -                    | -      | -                   | -      | 27.6           | -      |
| 5000            | 1.1            | 1.3    | -                | -      | -                | -      | -                    | -      | -                   | -      | -              | -      |
| 10000           | 2.4            | -      | -                | -      | -                | -      | -                    | -      | -                   | -      | -              | -      |

**Table 2.** Average execution times (ms) for instances with large coefficients, Minknap

| $n \setminus R$ | <i>uncorr.</i> |        | <i>weakcorr.</i> |        | <i>str.corr.</i> |        | <i>inv.str.corr.</i> |        | <i>al.str.corr.</i> |        | <i>sub.sum</i> |        |
|-----------------|----------------|--------|------------------|--------|------------------|--------|----------------------|--------|---------------------|--------|----------------|--------|
|                 | $10^6$         | $10^7$ | $10^6$           | $10^7$ | $10^6$           | $10^7$ | $10^6$               | $10^7$ | $10^6$              | $10^7$ | $10^6$         | $10^7$ |
| 100             | 0.2            | 0.2    | 0.6              | 0.5    | 755.1            | -      | 442.3                | -      | 12.4                | 8.9    | 553.6          | -      |
| 500             | 0.2            | 0.3    | 0.5              | 0.6    | -                | -      | -                    | -      | 256.1               | 247.3  | 512.6          | -      |
| 1000            | 0.4            | 0.4    | 0.9              | 0.9    | -                | -      | -                    | -      | 636.8               | 897.1  | 681.7          | -      |
| 5000            | 1.4            | 1.4    | 7.3              | 4.8    | -                | -      | -                    | -      | 8634.7              | -      | 736.3          | -      |
| 10000           | 2.6            | 3.3    | 18.3             | 20.7   | -                | -      | -                    | -      | -                   | -      | 841.8          | -      |

**Table 3.** Average execution times (ms) for instances with large coefficients, BPSO

| $n \setminus R$ | <i>uncorr.</i> |        | <i>weakcorr.</i> |        | <i>str.corr.</i> |        | <i>inv.str.corr.</i> |        | <i>al.str.corr.</i> |        | <i>sub.sum</i> |        |
|-----------------|----------------|--------|------------------|--------|------------------|--------|----------------------|--------|---------------------|--------|----------------|--------|
|                 | $10^6$         | $10^7$ | $10^6$           | $10^7$ | $10^6$           | $10^7$ | $10^6$               | $10^7$ | $10^6$              | $10^7$ | $10^6$         | $10^7$ |
| 100             | 7.3            | 8.7    | 7.1              | 7.1    | 6.7              | 7.2    | 7.3                  | 6.8    | 6.9                 | 8.1    | 7.3            | 9.8    |
| 500             | 37.9           | 20.9   | 38.4             | 31.4   | 31.2             | 25.6   | 38.5                 | 46.2   | 35.4                | 36.3   | 51.4           | 21.2   |
| 1000            | 77.1           | 42.4   | 59.4             | 53.7   | 41.0             | 40.6   | 79.7                 | 87.5   | 41.6                | 40.9   | 52.8           | 32.8   |
| 5000            | 318.3          | 411.2  | 309.0            | 305.5  | 304.1            | 303.6  | 312.8                | 344.6  | 303.6               | 411.1  | 308.6          | 325.3  |
| 10000           | 976.2          | 963.6  | 879.4            | 1160.1 | 935.6            | 1267.3 | 1577.6               | 1960.7 | 881.9               | 923.1  | 919.5          | 939.2  |

**Table 4.** Optimal values found by GA and our BPSO,  $R = 10^6$ ,  $c = \frac{1}{2} \sum_{j=1}^n w_j$  for all the instances

| $n$   | <i>uncorr.</i> |            | <i>str.corr.</i> |            |
|-------|----------------|------------|------------------|------------|
|       | GA             | BPSO       | GA               | BPSO       |
| 100   | 39465410       | 39465410   | 32995624         | 33048651   |
| 500   | 201957104      | 202661372  | 157736230        | 157803943  |
| 1000  | 400917743      | 403053093  | 315650918        | 315789002  |
| 5000  | 2436292167     | 2446654061 | 1593860725       | 1597840513 |
| 10000 | 3751841203     | 3759039860 | 2800845121       | 2801430527 |

$[1, m]$  and any item from the spanner set. Here, we will consider uncorrelated span(2,10), weakly correlated span(2,10) and strongly correlated span(2,10).

*Multiply strongly correlated instances  $mstr(k_1, k_2, d)$ :* The weights are chosen in  $[1, R]$  randomly. If the weight can divide exactly by  $d$ , then the profit  $p_j = w_j + k_1$ , otherwise  $p_j = w_j + k_2$ . The parameters are  $k_1 = 3R/10$ ,  $k_2 = 2R/10$ ,  $d = 6$ .

**Table 5.** Average execution times (ms) for instances with small coefficients, Expknapp

| n     | span(2, 10) |             |            | mstr( $\frac{3R}{10}, \frac{2R}{10}, 6$ ) | pceil(3) | circle( $\frac{2}{3}$ ) |
|-------|-------------|-------------|------------|-------------------------------------------|----------|-------------------------|
|       | uncorr.     | weak. corr. | str. corr. |                                           |          |                         |
| 100   | -           | -           | -          | 52.1                                      | -        | 24.7                    |
| 500   | -           | -           | -          | -                                         | -        | -                       |
| 1000  | -           | -           | -          | -                                         | -        | -                       |
| 5000  | -           | -           | -          | -                                         | -        | -                       |
| 10000 | -           | -           | -          | -                                         | -        | -                       |

**Table 6.** Average execution times (ms) for instances with small coefficients, Minknap

| n     | span(2, 10) |             |            | mstr( $\frac{3R}{10}, \frac{2R}{10}, 6$ ) | pceil(3) | circle( $\frac{2}{3}$ ) |
|-------|-------------|-------------|------------|-------------------------------------------|----------|-------------------------|
|       | uncorr.     | weak. corr. | str. corr. |                                           |          |                         |
| 100   | 0.1         | 0.1         | 0.1        | 1.0                                       | 0.5      | 0.8                     |
| 500   | 1.2         | 1.3         | 2.1        | 12.4                                      | 5.4      | 37.4                    |
| 1000  | 15.6        | 23.9        | 17.9       | 40.0                                      | 39.3     | 54.9                    |
| 5000  | 363.2       | 817.4       | 803.1      | 465.0                                     | 1133.5   | 613.9                   |
| 10000 | 1142.9      | 1600.4      | 3720.4     | 1350.8                                    | 3661.2   | 1109.5                  |

**Table 7.** Average execution times (ms) for instances with small coefficients, BPSO

| n     | span(2, 10) |             |            | mstr( $\frac{3R}{10}, \frac{2R}{10}, 6$ ) | pceil(3) | circle( $\frac{2}{3}$ ) |
|-------|-------------|-------------|------------|-------------------------------------------|----------|-------------------------|
|       | uncorr.     | weak. corr. | str. corr. |                                           |          |                         |
| 100   | 7.9         | 5.7         | 7.2        | 7.3                                       | 3.9      | 3.5                     |
| 500   | 34.4        | 28.4        | 28.1       | 32.2                                      | 36.5     | 21.4                    |
| 1000  | 65.6        | 73.9        | 65.9       | 87.0                                      | 74.3     | 77.3                    |
| 5000  | 667.1       | 690.9       | 633.1      | 912.0                                     | 764.0    | 868.7                   |
| 10000 | 2595.0      | 1967.3      | 2136.6     | 1974.5                                    | 2003.1   | 1084.3                  |

**Table 8.** Optimal values found by GA and BPSO, for three types of difficult instances, R=1000

| n     | str.corr.span(2, 10) |         | mstr( $\frac{3R}{10}, \frac{2R}{10}, 6$ ) |         | pceil(3) |         |
|-------|----------------------|---------|-------------------------------------------|---------|----------|---------|
|       | GA                   | BPSO    | GA                                        | BPSO    | GA       | BPSO    |
| 100   | 13488                | 13497   | 39613                                     | 39710   | 24210    | 24210   |
| 500   | 53016                | 53035   | 199662                                    | 199673  | 126543   | 126501  |
| 1000  | 366142               | 366061  | 405512                                    | 405547  | 244767   | 244776  |
| 5000  | 1069621              | 1070096 | 2025096                                   | 2030286 | 1255665  | 1255665 |
| 10000 | 2233409              | 2233650 | 4055139                                   | 4050196 | 2515947  | 2516037 |

*Profit ceiling instances(d):* The weights are randomly distributed in [1,R] and profits  $p_j=d\lceil w_j/d \rceil$ . The parameter  $d$  is chosen as  $d=3$ .

*Circle instances(d):* The weights are randomly distributed in [1,R] and  $p = d\sqrt{4R^2 - (w - 2R)^2}$ . We choose  $d = \frac{2}{3}$ .

From these results, it is clear that Expknapp has the worst performance than any other algorithms. Although Minknap is a bit faster than our algorithm for

smaller problem size  $n$ , the solution times for both algorithm are very stable. Here again, Table 8 shows that our BPSO algorithm performs better than GA.

## 5 Conclusion

In this paper, we proposed a novel binary particle swarm approach and apply it to the hard knapsack problems. Based on the total-value greedy algorithm, a heuristic operator is designed to handle the knapsack constrains. The approach has been thoroughly evaluated with different instance types and problem sizes. The evaluation is made by comparing our algorithm with some of the best known approaches in the existing literatures. As the obtained results show, our approach exhibits an excellent level of accuracy and efficiency to the hard knapsack problems.

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# Collective Behavior of an Anisotropic Swarm Model Based on Unbounded Repulsion in Social Potential Fields

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**Abstract.** Swarm system with flexible structures adapts well to variable environment. In this article, we propose an anisotropic swarm model based on unbounded repulsion and social potential fields. The unbounded repulsion ensures the independence among autonomous agents in social potential fields, which consist of obstacles to avoid and targets to move towards. Simulation results show that the aggregating swarm can construct various formations by changing its anisotropy coefficient, and the collective behavior of mass individuals emerges from combination of the inter-individual interactions and the interaction of the individual with outer circumstances.

## 1 Introduction

In nature there are many biological swarms with collective behavior, such as colonies of bees and ants, schools of fish, flocks of birds, and herds of mammals. Living as aggregations, such swarms have more chances to avoid predators and to find food [1]. Operational principles from these systems can be applied to engineering for developing coordinated control and distributed control of multi-agent systems such as unmanned air vehicles [2] and multiple autonomous robots [3,4,5,6]. Modeling and exploring the collective dynamics has become an important issue and many investigations have been carried out [7,8,9,10,11]. The general understanding now is that the swarming behavior of mass animals is a result of an interplay between a long range attraction and a short range repulsion among individuals [12]. According to this conclusion, Gazi and Passino proposed a swarm model of engineering multi-agent systems that consists of a number of individuals with identical interaction strength and studied its cohesion stability [13]. However, the complex environment and various interaction of a practical swarm system are of importance for modeling in a common framework. The purpose of this article is to provide some results on this topic.

## 2 Anisotropic Swarm Model

Swarm model with anisotropic property can adapt well to environment by changing its structures. To achieve the variation of swarm aggregation and the

individual independence, we consider an anisotropic swarm including  $N$  individuals (members) in an  $n$ -dimensional Euclidean space, and model the individuals as points and ignore their dimensions. It is assumed that all of them move simultaneously and know the exact positions of others. The equation of motion for individual  $i$  is given by

$$\dot{x}^i = h_{x^i} + \sum_{j=1, j \neq i}^M \varepsilon_{ij} g(x^i - x^j), i = 1, \dots, M. \quad (1)$$

where  $x^i \in \mathbb{R}^n$  represents the position of member  $i$ . The equation (1) is composed of three main factors: 1)  $h_{x^i}$  stands for the effect in heading direction resting with social potential fields around individual  $i$ , 2)  $\varepsilon_{ij}$  expresses the anisotropic factor affected by the positions of individual  $i$  and  $j$ , 3)  $g(\cdot)$  is the attraction/repulsion function that governs the inter-individual original interactions. Note that the direction and magnitude of motion of each member are determined as a weighted sum of the attraction and repulsion of all the other members on this one.

In general, the form of attraction/repulsion function that we consider is

$$g(y) = -y[g_a(\|y\|) - g_r(\|y\|)]. \quad (2)$$

where  $g_a : \mathbb{R}^+ \rightarrow \mathbb{R}^+$  represents the magnitude of the attraction term, whereas  $g_r : \mathbb{R}^+ \rightarrow \mathbb{R}^+$  represents the magnitude of the repulsion term. According to the study results on smarming behavior, the effect of function  $g(\cdot)$  should be attractive for large distances and repulsive for short distances. By equating  $g(y) = 0$ , one can easily get the constant distance  $\delta$  where attraction and repulsion balance. In other words, there exists  $\delta$  such that  $g_a(\delta) = g_r(\delta)$ , and for  $\|y\| > \delta$ ,  $g_a(\|y\|) > g_r(\|y\|)$  means attraction dominates, and for  $\|y\| < \delta$ ,  $g_a(\|y\|) < g_r(\|y\|)$  means repulsion dominates.

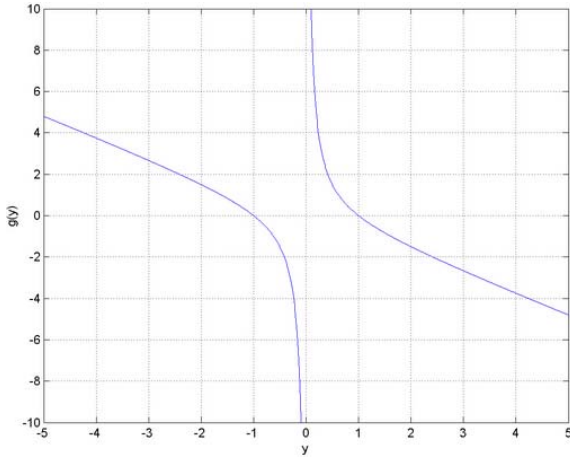
In [13], Gazi and Passino presented an inter-individual interaction function with linear attraction and bounded repulsion

$$g(y) = -y \left[ a - b \exp \left( -\frac{\|y\|^2}{c} \right) \right]. \quad (3)$$

Simulation experiments show that the bounded repulsion may cause overlap of the individual positions [14]. To ensure the independence among autonomous agents in collective motion, the anisotropic swarm model that we consider in this article is based on unbounded repulsion interaction  $g_r(\|y\|) = \frac{b}{\|y\|^2}$ , and linear attraction  $g_a(\|y\|) = a$ . The attraction/repulsion function  $g(\cdot)$  can take the form

$$g(y) = -y \left( a - \frac{b}{\|y\|^2} \right). \quad (4)$$

The  $\|y\| = \sqrt{y^\top y}$  in (4) is the Euclidean norm, and for  $\|y\| \rightarrow 0$ , we have  $g(y) \rightarrow \infty$ , which prevents individuals from collision completely. For  $y \in \mathbb{R}^1$  case and  $a = 1$   $b = 1$ , this function is shown in Fig. 1. By equating  $g(y) = 0$ , we can



**Fig. 1.** Linear attraction/Unbounded repulsion function  $g(\cdot)$

get the balance distance  $\delta = \sqrt{\frac{b}{a}} = 1$ . It can be proved that the boundary of swarm aggregation is  $\varepsilon = \sqrt{(M - 1)\frac{b}{2a}}$ , which is different from [13].

The anisotropy coefficient  $\varepsilon_{ij}$  in (1) is the main factor that affect the structures of swarm systems. Based on simple rules, many kinds of collective behavior such as swarm aggregating and formation transforming emerge from variable interactions among mass individuals. To achieve the variety of swarming structures, we present

$$\varepsilon_{ij} = \alpha \left[ \frac{h_{x^i}}{\|h_{x^i}\|} \cdot \frac{x^j - x^i}{\|x^j - x^i\|} \right], \quad \alpha > 0. \tag{5}$$

where  $\alpha$  represents the anisotropy weight of aggregation, and  $\frac{x^j - x^i}{\|x^j - x^i\|}$  is the unit direction from individual  $i$  to  $j$ . The cartesian product of  $\frac{h_{x^i}}{\|h_{x^i}\|}$  and  $\frac{x^j - x^i}{\|x^j - x^i\|}$  expresses the direction sensitivity with environment of all members in the swarm model. For  $\varepsilon_{ij} = 1$ , the swarm will converge to a hyperball with isotropic property, and for other cases, the anisotropic factor will affect the collective behavior of swarm members in the heading direction. We can also amplify the degree of anisotropy weight artificially to change swarming formation and collective motion. With this property, this swarm model can adapt well to various environment.

Note that the anisotropic interaction here is different from the interactive efficiency presented in [15], which introducing a concept of coupling matrix to reflect the interaction strength between individuals. The anisotropic interplay presented in (5) inherits from the physics researches on swarming behavior and assumes that the anisotropy originates from the effect of interaction with the environment and relative positions of individuals.

### 3 Motion in Social Potential Fields

The interactions with environment in this model are based on artificial potential functions, a concept that has been used extensively for robot navigation and control [16,17]. The environment model is built with the combination of social potential fields, in which one can take the obstacle as a high potential region and the destination as a low potential region.

The social potential fields were defined by  $\sigma(\cdot)$  which consist of artificial potential functions that model the environment containing obstacles to avoid and targets to moved toward. The negative gradient  $-\nabla\sigma(x^i)$  expresses the motion of the individuals toward regions with lower potential (analogous to destination) and away from regions with higher potential (analogous to obstacles). So the heading factor in (1) equate to  $h_{x^i} = -\nabla\sigma(x^i)$ . The artificial potential functions which are the modeling of social potential fields constructing reference circumstances [18] can take the following forms:

(1) Plane potential function

$$\sigma(x) = a_\sigma^\top x + b_\sigma, \quad a_\sigma \in \mathbb{R}^n, b_\sigma \in \mathbb{R}. \quad (6)$$

One can see that the gradient of this potential field is given by  $\nabla\sigma(x) = a_\sigma$ . This function describes an environment with constant gradient in which individuals can move along the reverse of the gradient direction.

(2) Quadratic potential function

$$\sigma(x) = \frac{A_\sigma}{2} \|x - c_\sigma\|^2 + b_\sigma, \quad A_\sigma \in \mathbb{R}, b_\sigma \in \mathbb{R}, c_\sigma \in \mathbb{R}^n. \quad (7)$$

Note that this potential field has a global extremum at  $x = c_\sigma$ . Its gradient at point  $x \in \mathbb{R}^n$  is given by  $\nabla\sigma(x) = A_\sigma(x - c_\sigma)$ . For the case  $A_\sigma > 0$  the swarm will converge to the minimum of the potential field, and for the case  $A_\sigma < 0$  the swarm will diverge from the maximum of the around region, which make swarms move forward to destination and far away from obstacles.

(3) Gaussian potential function

$$\sigma(x) = -\frac{A_\sigma}{2} \exp\left(-\frac{\|x - c_\sigma\|^2}{l_\sigma}\right) + b_\sigma, \quad A_\sigma \in \mathbb{R}, b_\sigma \in \mathbb{R}, l_\sigma \in \mathbb{R}^+, c_\sigma \in \mathbb{R}^n. \quad (8)$$

This potential field also has an extremum at  $x = c_\sigma$ . The  $l_\sigma$  and  $A_\sigma$  are coefficients which affect the scope and intensity of the potential field around the individual. The gradient of this smooth environment can be obtained by  $\nabla\sigma(x) = \frac{A_\sigma}{l_\sigma}(x - c_\sigma) \exp(-\frac{\|x - c_\sigma\|^2}{l_\sigma})$ .

(4) Multimodal Gaussian potential function

$$\sigma(x) = -\sum_{i=1}^N \frac{A_\sigma^i}{2} \exp\left(-\frac{\|x - c_\sigma^i\|^2}{l_\sigma^i}\right) + b_\sigma, \quad A_\sigma \in \mathbb{R}, b_\sigma \in \mathbb{R}, l_\sigma \in \mathbb{R}^+, c_\sigma \in \mathbb{R}^n. \quad (9)$$

It is a combination of Gaussian potential functions. Each of them has its own extremum at  $c_\sigma^i$  for individual  $i$ . Note that since the  $A_\sigma^i$  can be positive or



negative, there can be both hills and valleys leading to a complex environment.

The gradient of the environment is  $\nabla\sigma(x) = \sum_{i=1}^N \frac{A_\sigma^i}{l_\sigma^i} (x - c_\sigma^i) \exp(-\frac{\|x - c_\sigma^i\|^2}{l_\sigma^i})$ .

These artificial potential functions discussed above can compose social potential fields with which multi-agent systems interact. The combination of them can model reference environments for collective motion of swarms.

### 4 Simulation Results

As to the anisotropic swarm model based on unbounded repulsion, we chose an  $n = 2$  dimensional space to visualize the results and used the region  $[-5, 5] \times [-5, 5]$  of the space. In following simulation results the swarm has  $M = 20$  members, and parameters of the attraction/repulsion function (4) are  $a = 1$  and  $b = 1$ . We performed simulations for all the social potential fields and anisotropic property discussed above.

Fig. 2 shows the paths of all the members of a swarm moving in a plane potential field with parameter  $a_\sigma = [1, 1.2]^T$ . The circles dispersed on the top right corner represent initial random locations of individuals, and the circles arrived at the left corner are the positions of all the members in steady state. The paths composed of blank dots denote the trajectories of individuals. One can easily see that in this social potential field, as expected, the swarm moves along the negative gradient direction  $-\nabla\sigma(x) = -a_\sigma$  and congregates to an aggregation. Note that initially for this example some of the individuals move in the direction opposite the negative gradient. It is because the inter-individual attraction is stronger than the intensity of this potential field. If the potential intensity is high enough to dominate the individual motion, the convergence of swarms will need more steps to be observed.

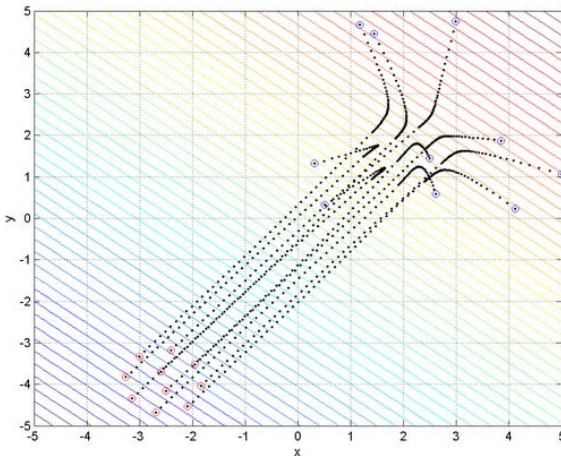
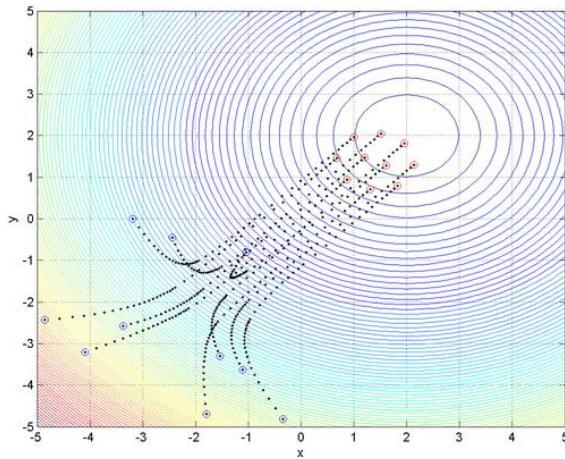


Fig. 2. Collective behavior of swarm in plane social potential field

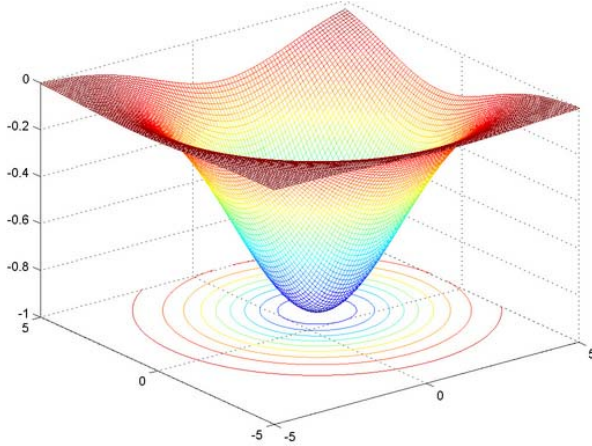
For the quadratic potential field as shown in Fig. 3, we appointed the environment with minimum at  $c_\sigma = [2, 2]^\top$  and its magnitude  $A_\sigma = 1$ . As discussed above, for  $A_\sigma > 0$ , the swarm will converge to the minimum of the potential field, and for  $A_\sigma < 0$ , the swarm will diverge from the maximum of around environment. In Fig. 3, circles dispersed on the left corner represent initial random positions of these individuals, and the circles on the top right are the positions of all the members in steady state. The individual trajectories are denoted by blank dots. This simulation result shows that swarm move towards the minimum of social potential field as aggregating at the same time for the case  $A_\sigma > 0$ . Note that the swarm size would be affected by potential environment, which can be understand easily if we consider the effect in negative gradient direction as an attraction comes from outside.



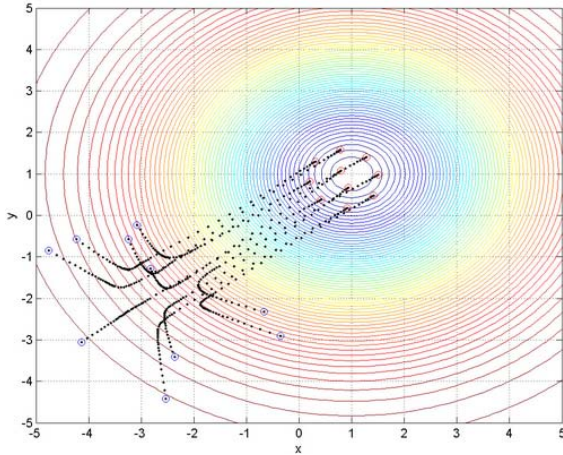
**Fig. 3.** Collective behavior of swarm in quadratic social potential field

Result from a similar nature was obtained also for the Gaussian potential field as shown in Fig. 4 and Fig. 5, in which we assumed  $c_\sigma = [1, 1]^\top$  as the minimum of the environment. The other parameters of this artificial potential function were chosen to be  $A_\sigma = 2$  and  $l_\sigma = 10$ . Fig. 4 shows the social potential field that is analogous to smooth environment for swarms. The collective behavior of individuals in this swarm is shown in Fig. 5. Note that for the case  $A_\sigma > 0$ , the swarm will converge to the minimum of the potential field along negative gradient direction as expected. This situation exists in all the simulations that we performed.

In the simulation results for the multimodal Gaussian potential field we chose the artificial environment shown in Fig. 6, which has several minima and maxima. As is shown in Fig. 6, we appointed the positions  $[2, 2]^\top, [4, 3]^\top, [8, 1]^\top$  as the minima and  $[7, 8]^\top, [5, 6]^\top, [2, 7]^\top$  as the maxima. The intensity of potential field is affected by  $l_\sigma$  and  $A_\sigma$ , which are  $[1, 3, 2, 2, 1, 2]$  and  $[-2, 6, 3, -8, 2, -4]$  respectively. Note that the region of this simulation example was chosen to be  $[0, 10] \times [0, 10]$ .



**Fig. 4.** Gaussian social potential field

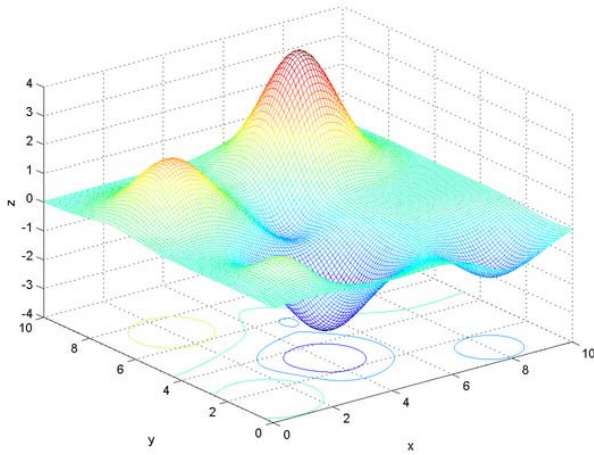


**Fig. 5.** Collective behavior of swarm in Gaussian social potential field

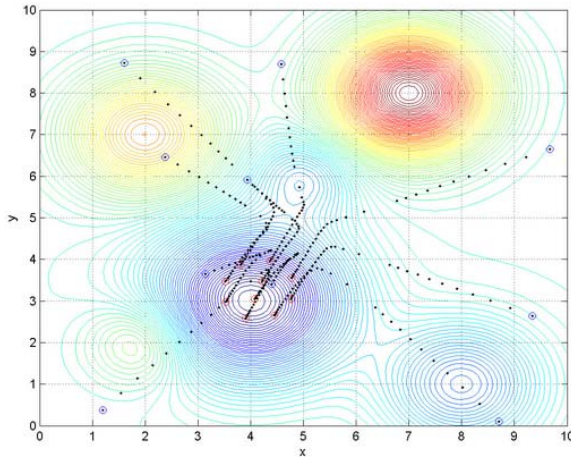
The global minimum is located at  $[4, 3]^T$ , with the magnitude  $A_\sigma = 6$  and the spread  $l_\sigma = 3$ . The plots in Fig. 7 show swarm members congregate to an aggregation and converge to the minimum of the whole region.

Due to the unbounded repulsion, the members will form a cohesive swarm without overlapping of individual positions. And the attrahen/repellent interplays between individuals ensure swarms to aggregate, with this property members will not trap into local extremum and move forward destination. Swarm will converge at the lowest potential region of the whole environment along negative gradient direction.

To observe the results of anisotropic property proposed in this model, we changed the parameter  $\alpha$  of anisotropy coefficient  $\varepsilon_{ij}$  and chose a swarm in

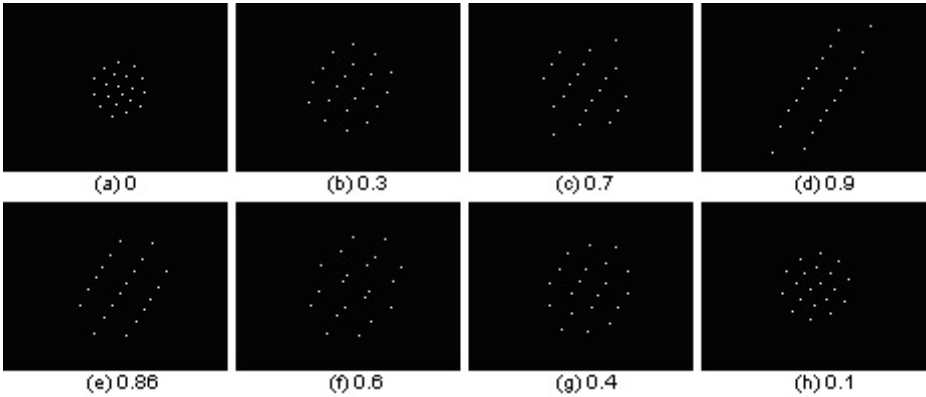


**Fig. 6.** Multimodal Gaussian social potential field



**Fig. 7.** Collective behavior of swarm in Multimodal Gaussian social potential field

which there are  $M = 20$  members. As is shown in Fig 8, the swarm can aggregate as a cluster at broad place and form line formation at narrow place. Accordingly, this swarm with variable structures adapts well to external environment. In a plane potential field with parameter  $a_\sigma = [1.1, 1]^T$ , individuals based on inter-individual attraction/repulsion can keep certain formation and move towards the target. The collective behavior of transforming formations and avoiding obstacles emerge from the interactions among mass individuals and interplay with environment, which can be seen as a reference approach for the coordinated control of multi-agent systems in engineering.



**Fig. 8.** Formation variety of anisotropic swarm as changing parameter  $\alpha$  continually

## 5 Conclusions

In this article, we propose an anisotropic swarm model based on unbounded repulsion in social potential fields, and analyze its collective behavior. To avoid overlapping of individual positions, the unbounded repulsion is introduced to constitute attraction/repulsion function  $g(\cdot)$ . The circumstances modeled by social potential fields taking the form of artificial potential functions consist of obstacles to avoid and targets to move towards in various conditions. The simulation results prove that the multi-agent system based on proposed swarm model can eventually form an aggregation of finite size around swarm center, and converge to advantaged region of the environment. By changing the parameters of anisotropy coefficient  $\varepsilon_{ij}$ , swarm can transform its formation to adapt to various environments. Based on these simple rules, many kinds of collective behavior emerge from variable interactions among mass individuals and the interaction with outer circumstances. The results obtained in this article may provide an extension to the collective motion of autonomous multi-agent systems, and the trajectories generated by this model can be used as reference trajectories for the agents to follow or track.

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# Combining Particle Swarm Optimization and Neural Network for Diagnosis of Unexplained Syncope\*

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**Abstract.** Given the relative limitations of BP and GA based learning algorithms, Particle Swarm Optimization (PSO) is proposed to train Artificial Neural Networks (ANN) for the diagnosis of unexplained syncope. Compared with BP and GA based training techniques, PSO based learning method improves the diagnosis accuracy and speeds up the convergence process. Experimental results show that PSO is a robust training algorithm and should be extended to other real-world pattern classification applications.

## 1 Introduction

In industry, economic and medicine, many real world problems such as quality control, bankruptcy prediction, pattern reorganization, and medical diagnosis can be treated as pattern classification problems. Many industrial processes exhibit nonlinear and dynamic behavior, thus nonlinear model should be developed accordingly. With the characteristics of strong self-learning, self-organization, robust error toleration and accurate nonlinear relation approximation, artificial neural network (ANN) is an appropriate tool to deal with the above-mentioned complex pattern classification problems.

Multi-layer ANN with sigmoid activation function has been shown to be able to approximate any continuous nonlinear functions [1] and is an attractive technique that can be applied to nonlinear process modeling. However, the realization of the above capability is based on sufficient training. Therefore, training techniques have much influence on the performance of the ANN for pattern classification problems.

Back-propagation (BP) training algorithm is probably the most frequently used one in practical application. However, it proved that gradient-descent based method is slow, easy to be trapped in local optimum, short of generalization and rather sensitive to initial weights [2]. Due to these drawbacks especially the local optima characteristics, ANN trained by BP cannot guarantee consistency and prediction, which will eventually reduce the reliability of its pattern classification performance.

Compared with BP, Genetic Algorithm (GA) has parallel search strategy and global optimization characteristics, which make the trained neural network have

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higher classification accuracy and faster convergence speed [3]. As a population based heuristic, GA encodes ANN architecture (weights) as chromosome and randomly generates a group of individuals. The population evolves by the “survival of fitness” principle and repeats the genetic procedure such as selection, production, crossover and mutation to explore the solution space until the terminal condition is satisfied. The best individual is decoded to correspond to the desired ANN architecture. However, the complex genetic operators make the computational expense exponentially increase with the problem scale [4]. In addition, due to the lack of effective local search mechanism, GA converged slowly and even stagnated when approaching the optimum [5].

Particle Swarm Optimization (PSO) algorithm is based on the theory of swarm intelligence. This algorithm can provide efficient solutions for optimization problems through intelligence generated from complex activities such as cooperation and competition among individuals in the biologic colony. Compared with evolutionary computation, PSO still maintains the population based global search strategy, but its velocity-displacement search model is simple and easy to implement. Also this algorithm avoids the design of complex genetic operators such as crossover and mutation. This algorithm has been applied successfully to complex nonlinear function optimization [6], task assignment [7], reactive power and voltage control [8] and so on.

The syncope is an abrupt and transient state of unconsciousness. This disease is various in pathogenesis and almost 60~70% are unexplained. Equivalently, this disease is called unexplained syncope. Due to its tremendous harm to the human health, unexplained syncope is always posing as a difficult but meaningful research topic in the medical field. However, till now, no effective methods are available to solve this compelling problem.

This paper employed PSO to train ANN and applied it to the diagnosis of unexplained syncope. Compared with BP and GA, PSO based learning algorithm can improve the diagnosis accuracy as well as accelerate the convergence process. The simulated results show that PSO is an effective ANN training method and it should be extended to other pattern classification problems.

## 2 Particle Swarm Optimization

The investigation and analysis on the biologic colony demonstrated that intelligence generated from complex activities such as cooperation and competition among individuals can provide efficient solutions for specific optimization problems [9]. Inspired by the social behavior of animals such as fish schooling and bird flocking, Kennedy and Eberhart designed the Particle Swarm Optimization (PSO) in 1995 [10]. This method is a kind of evolutionary computing technology based on swarm intelligence. The basic idea of bird flocking can be depicted as follows: In a bird colony, each bird looks for its own food and in the meantime they cooperate with each other by sharing information between them. Therefore, each bird will explore next promising area by its own experience and experience from the others. Due to these attractive characteristics, i.e. memory and cooperation, PSO is widely applied in many research area and real-world engineering fields as a powerful optimization tool.



The basic PSO model consists of a swarm of particles moving in a d-dimensional search space. The direction and distance of each particle in the hyper-dimensional space is determined by its fitness and velocity. In general, the fitness is primarily related with the optimization objective and the velocity is updated according to a sophisticated rule.

In PSO, it starts with the random initialization of a population of individuals (candidate solutions) in the search space and then simulates the social behavior of the particles in the swarm till achieves the optimum solution by iterative exploration. The position and velocity of the  $i^{\text{th}}$  particle is denoted as  $x_i = (x_{i1}, x_{i2}, \dots, x_{id})$  and  $v_i = (v_{i1}, v_{i2}, \dots, v_{id})$  respectively. At each iteration step the velocity is updated and the particle is moved to a new position. The best previously visited position of the  $i^{\text{th}}$  particle is denoted as its personal best position  $p_i = (p_{i1}, p_{i2}, \dots, p_{id})$ . Define  $g$  as the index of the best particle of the whole swarm, the position of the best individual of the whole swarm is denoted as the global best position  $p_g$ , and the new velocity of each particle is calculated as follows:

$$v_i = w \times v_i + c_1 \times \text{Rand}() \times (p_i - x_i) + c_2 \times \text{rand}() \times (p_g - x_i) \quad (1)$$

$$x_i = x_i + v_i \quad (2)$$

where  $\text{Rand}()$  and  $\text{rand}()$  are two independent random numbers uniformly distributed in the range of  $[0, 1]$ .  $c_1, c_2$  are two constants called learning factors usually  $c_1=c_2=2$  [11].  $w$  is called the inertia factor to deliver a balance between global exploration and local exploitation.

It is noticeable that three components typically contribute to the new velocity. The first part is proportional to the old velocity and is the tendency of the particle to continue in the same direction it has been traveling [12]. It can be thought of as a momentum term. The second component, which is associated with a local search, is considered as the cognitive part representing the private thinking. The third term, which is associated with a global search, is considered as the social part representing the social-psychological adaptation of knowledge. In addition, studies of inertia weight  $w$  yield the conclusion that starting with a high value and lowering it throughout the iterations will help enhance the possibility of converging globally and save the computational expense in the local search procedure.

### 3 PSO for Neural Networks

An artificial neural network is composed of a series of interconnected nodes and the corresponding weights between them. It aims at simulating the complex mapping between the input and output. A 3-layer feed-forward ANN basically consists of input units, hidden units and output units. Let  $w_{ih}$  denotes the weight between the input node and the hidden one. Likewise,  $w_{ho}$  denotes the weight between the hidden node and output one. ANN is characterized by the ability of self-learning and error toleration. With the appropriate activation functions and trained weights, ANN can

approximate any smooth, nonlinear function or relationship between the input and output. The training process is carried out on a set of data including input and output parameters. Usually, the data are split into two parts namely training samples and testing samples. The learning procedure is based on the training samples and the testing samples are used to verify the performance of the trained network. During the training, the weights in the network are adjusted iteratively till a desired error depicted as equation (3) is obtained.

$$E = \sum_{i=1}^m \sum_{k=1}^{n_o} (t_i^k - y_i^k)^2 / 2 \quad (3)$$

where,  $t_i^k$  and  $y_i^k$  represents the actual and the predicted function values respectively,  $m$  is the number of training samples, and  $n_o$  is the number of output nodes.

The neural network is trained by minimizing the above error function in a search space based on weights. PSO generates possible solutions and measure their quality by using a forward propagation through the neural network to obtain the value of the error function. This error value is used as the particle's fitness function to direct it toward the more promising solution. The global best particle is corresponded to the desired trained network after adequate iterations.

PSO based training algorithm can be summarized in the following steps:

Step1. Define the network structure, parameters of PSO and the fitness function.

Step2. Encode the candidate weight solution as  $x = \{w_{ih}, w_{ho}\}$ .

Step3. Initialize the position (weights) and velocity of each particle (change of weights in a single iteration) randomly in the predefined range. Evaluate the fitness of each particle according to the previously defined error function.

Step4. Identify the personal best fitness value and update the corresponding position for each particle; Identify the global best fitness value and update its position.

Step5. Update the velocity and the position for the whole particle swarm according to equation (1) and (2).

Step6. If the stopping condition is not satisfied, go to step 4. Otherwise, terminate the iteration and obtain the best weight setting from the global best solution.

## 4 Experimental Results and Analysis

The upright tilt table test is a commonly used diagnostic technique for unexplained syncope [13]. Basic upright tilt table test, as well as isoproterenol tilt table test, is a quite effective diagnostic technique for unexplained syncope. The diagnostic parameters used in the test can be listed and classified as follows:

1. General diagnostic parameters: sex and age.
2. Subjective diagnostic parameters: nausea, fatigue, swelling in the legs, dizziness, sweating, pallor, palpitations, chest pain, shortness of breath, muscle cramps, numbness, fainting, unconsciousness.
3. Auxiliary diagnostic parameters: heart rate (HR) and blood pressure (BP).

The diagnostic results yielded by the above parameters approximately fall into two categories: negative response and positive response. The latter can be further

classified into three categories: heart restraint class, blood vessels restraint class and the syndrome class.

The data of unexplained syncope are obtained from the Biomedical Department at Wuhan University. From the total samples, 177 samples are specified as training set, while the remaining 59 are specified as testing set. The input nodes represent the diagnostic parameters in the upright tilt table test. The output nodes mean the classes of the diagnostic results. All the source data should be preprocessed and normalized as follows:

1. Sex: male (1), female (0).
2. Age: 15-30 (0), 30-40 (0.5), and 40-70 (1).
3. Symptoms: presence (1), absence (0).
4. BP/HR: presence (1), absence (0).
5. Diagnostic results: negative (1000), heart restraint (0100), blood vessels restraint (0010), and syndrome (0001).

The data before the bracket present the practical diagnostic data and the inside present the normalized ones which will be served as actual parameters for the input nodes of the neural network.

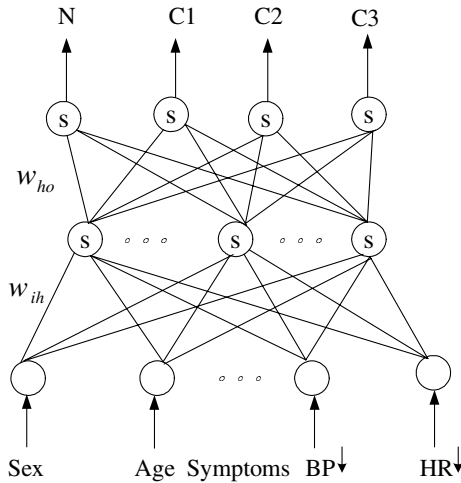
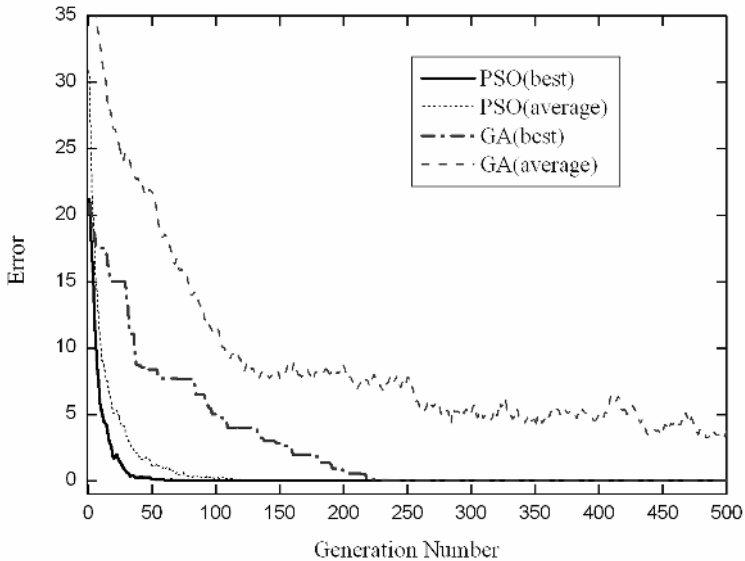


Fig. 1. The ANN model for diagnosis of unexplained syncope

The structure of the neural network model for the diagnosis of unexplained syncope is constructed as Figure 1. The 18 input nodes of the 3-layer feed-forward ANN represent the diagnostic parameters. The 4 output nodes represent the diagnostic results. The number of the hidden nodes is specified by the empirical equation. Sigmoid function is selected as activation function.

Before the training process, we should set the parameters of the training algorithm. In this paper, for PSO, we set population size  $n=80$ ,  $w=0.5$ ,  $c_1=c_2=2$ . The inertial weight decreases from 0.9 to 0.4 linearly. The initial weights are randomly generated between [0, 1]. The termination condition is defined as follows: (1) The predefined

maximum iteration number  $Itermax$  is reached or (2) the training error is smaller than the threshold  $e$ . To validate the performance of PSO, BP and GA were also adopted as the training algorithms. In BP, the learning rate is 0.3 and momentum factor is 0.8. In GA, the crossover probability  $P_c$  is 0.9 and the mutation probability  $P_m$  is 0.1. Also, roulette wheel selection, binary encoding scheme and elite strategy are used. The population size is the same as that in PSO. It should be pointed out that each experiment was randomly carried out for 20 times, the typical results (medium performance) were recorded in the tables and figures.



**Fig. 2.** Training error curves of PSO and GA

The simulation experiment is carried out in two steps:

Firstly, set  $Itermax=500, 1000$  as the termination condition (1) to compare the training error and diagnosis accuracy of neural network trained by PSO, GA and BP. The experimental results are presented in Table 1 and Table 2. The comparison of convergence between the two population based algorithms is illustrated in Figure 2. Several conclusions can be drawn from the results: (a) When the maximum iteration is reached, all the particles in PSO converged to the optimum region whereas the individuals in GA distributed more diversely, which demonstrated that PSO is obviously superior in terms of convergence consistency. (b) Compared with BP and GA, PSO not only guaranteed high diagnostic accuracy but also performed better regarding error precision, which in turn improved the diagnostic reliability. (c) GA suffered from the intrinsic slow convergence flaw although it could also get promising weight solution. (d) With the relative small iteration scale, BP converged much faster and the training performance was even better than GA to some extent, but it would trap into local optimum with the increasing of the iteration scale.

**Table 1.** Comparison of different performance (Itermax=500)

| Training algorithms | Error   |         |         | Diagnostic accuracy |
|---------------------|---------|---------|---------|---------------------|
|                     | Worst   | Average | Best    |                     |
| PSO                 | 7.2E-20 | 7.2E-20 | 7.2E-20 | 98.6 %              |
| GA                  | 16.5    | 1.6     | 1.0E-10 | 89.4 %              |
| BP                  | –       | 7.4E-03 | –       | 98.4 %              |

**Table 2.** Comparison of different performance (Itermax=1000)

| Training algorithms | Error   |         |         | Diagnostic accuracy |
|---------------------|---------|---------|---------|---------------------|
|                     | Worst   | Average | Best    |                     |
| PSO                 | 5.3E-30 | 5.3E-30 | 5.3E-30 | 99.2 %              |
| GA                  | 11.2    | 0.7     | 2.1E-18 | 97.6 %              |
| BP                  | –       | 3.6E-03 | –       | 98.6 %              |

**Table 3.** Comparison of different computational expense (e=0.001)

| Training algorithm | Iteration number | CPU time (s) |
|--------------------|------------------|--------------|
| PSO                | 76               | 8.2          |
| GA                 | 522              | 42.1         |
| BP                 | 3538             | 169.2        |

**Table 4.** Comparison of different computational expense (e=0.0001)

| Training algorithm | Iteration number | CPU time (s) |
|--------------------|------------------|--------------|
| PSO                | 144              | 15.762       |
| GA                 | 702              | 56.476       |
| BP                 | 32798            | 845.824      |

Secondly, set training error less or equal to 0.001, 0.0001 as the termination condition. This trial aimed at comparing the computational expense between BP, GA and PSO with equivalent training precision. As can be seen from Table 3 and Table 4, although GA can obtain the desired convergence, PSO performed much better in terms of computational expense without the loss of convergence quality. In addition, BP suffered severe stagnation in achieving the desired precision.

## 5 Conclusion

PSO is an optimization algorithm based on swarm intelligence. It directs the search through the intelligence generated from cooperation and competition among the individuals. The merits of this novel algorithm can be summarized as follows: Firstly, with the parallel search strategy, it can locate the global optimum consistently.

Secondly, its velocity-displacement search model is simple and easy to implement. Thirdly, few parameters should be considered and set up. Moreover, the information flow with single direction can absolutely speed up the convergence process. Finally, variable inertial weight can effectively guarantee the compromise between global search and local search.

In this paper, a neural network based on PSO is proposed for the diagnosis of unexplained syncope. Compared with BP and GA, PSO can improve the diagnosis accuracy and speed up the convergence simultaneously. The experimental results reveal that PSO is a promising training algorithm and we should explore its potential in other optimization areas.

Further research could be done in the future. In the algorithm itself, several pre-defined parameters such as the inertial weight and learning factors can be adjusted dynamically by tracking the current process. Also analysis on the trained network can generate different patterns of input parameters, which could be used to conduct the rule acquisition. In addition, improved model is desired for other real-world problems with larger amount of source data and more complicated mapping relationship.

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# Parameter Estimation Approach in Groundwater Hydrology Using Hybrid Ant Colony System

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**Abstract.** A new approach to parameter estimation in groundwater hydrology is developed using hybrid ant colony system with simulated annealing. Based on the information from the observed water heads and calculated water heads, an objective function for inverse problem is proposed. The inverse problem of parameter identification is formulated as an optimization problem. Simulated annealing has the ability of probabilistic hill-climbing and is combined with ant colony system to produce an adaptive algorithm. A hybrid ant colony optimization is presented to identify the transmissivity and storage coefficient for a two-dimensional, unsteady state groundwater flow model. The ill-posedness of the inverse problem as characterized by instability and non-uniqueness is overcome by using computational intelligence. Compared with gradient-based optimization methods, hybrid ant colony system is a global search algorithm and can find parameter set in a stable manner. A numerical example is used to demonstrate the efficiency of hybrid ant colony system.

## 1 Introduction

Parameter identification, or model calibration, is a critical step in the application of mathematical models in hydrologic sciences. Unfortunately, parameter identification is an inherently difficult process and, as an inverse problem, it is plagued by the well-documented problems of nonuniqueness, nonidentifiability and instability [1]. Numerous optimization techniques have been used to solve groundwater remediation design and parameter identification problems. In a parameter identification problem, the objective function can be the weighted difference between the observed and calculated values at certain observation points in the aquifer. The identified parameters can be hydraulic conductivity or other aquifer parameters, such as storage coefficient [2]. In recent years, global optimization methods are being increasingly used to solve groundwater remediation design and parameter identification problems. These methods include simulated annealing, genetic algorithm, tabu search and ant colony system. Compared with gradient based local search methods, global optimization methods do not require the objective function to be continuous, convex, or differentiable. They have also shown other attractive features such as robustness, ease of implementation, and the ability to solve many types of highly complex, nonlinear problems. One common drawback of these global optimization methods is

that many objective function evaluations are typically required to obtain optimal or near-optimal solutions [3]. The ant colony system is a kind of natural algorithm inspired by behavior or processes presented in nature. Ant colony system has been widely used in the traveling salesman problem, job-shop scheduling problem and quadratic assignment problem. When compared with traditional first-order methods, the ant colony system is recognized to have a better capability to find the global optimum solution. The objective of this paper is to present a new method based on hybrid ant colony system for obtaining the parameters of a linear groundwater flow model.

## 2 Classical Ant Colony System

Ant colonies have always fascinated human beings. Social insects, such as ants, bees, termites and wasps, often exhibit a collective problem-solving ability[4].The ant colony system is first applied to the traveling salesman problem. In Ant System, the traveling salesman problem is expressed as a graph (N, E), where N is the set of towns and E is the set of edges between towns. The objective of the traveling salesman problem is to find the minimal length closed tour that visits each town once. Each ant is a simple agent to fulfill the task. It obeys the following rules: 1) It chooses the next town with a probability which is a function of the town distance and of the amount of trail present on the connecting edge; 2) before a tour is completed, it can not choose the already visited towns; 3) when it completes a tour, it lays a substance called trail on each edge (i, j ) visited; 4) it lives in an environment where time is discrete. It must choose the next town at time t, and be there at time t+1. Let m, n be the total number of ants and towns. An iteration of the Ant system is called, as the m ants all carry their next moves during time interval (t, t+1). The n iterations constitute a cycle. In one cycle, each ant has completed a tour. Let  $\tau_{ij}(t)$  denote the intensity of trail on edge (i, j ). After a cycle, the trail intensity is updated as[5]:

$$\tau_{ij}(t+1) = \rho\tau_{ij}(t) + \Delta\tau_{ij} \tag{1}$$

Where  $\rho$  is a coefficient, and (1- $\rho$ ) represents the evaporation of trail between times t and t+1

$$\Delta\tau_{ij} = \sum_{k=1}^Z \Delta\tau_{ij}^k \tag{2}$$

Where  $\Delta\tau_{ij}$  is the quantity per unit of length of trail substance placed on path(i,j) by the kth ant between times t and t+1[6]

$$\Delta\tau_{ij}^k = \begin{cases} Q/J_k & \text{path}(i, j) \text{ is selected} \\ 0 & \text{otherwise} \end{cases} \tag{3}$$



Where  $Q$  is a constant related to the quantity of trail laid by ants. Ants build solutions using a probabilistic transition rule. The probability  $p_{ij}^k(t)$  with which ant  $k$  in town  $i$  at iteration  $t$  chooses the next town  $j$  to move to is a function of the heuristic function of the desirability  $\eta_{ij}$  and the artificial pheromone trail  $\tau_{ij}(t)$ :

$$p_{ij}^k(t) = \frac{[\tau_{ij}]^\alpha [\eta_{ij}]^\beta}{\sum_{i=1}^L [\tau_{ij}]^\alpha [\eta_{ij}]^\beta} \quad (4)$$

Where  $\alpha$ ,  $\beta$  are adjustable constants, which can weigh the relative importance of pheromone trail and of objective function,  $L$  is the number of states that will be visited. A reasonable heuristic function is written as follows:

$$\eta_{ij} = \frac{1}{J_k} \quad (5)$$

Where  $J_k$  is the objective function of  $k$ th ant path. Ant colony system could not perform well without pheromone evaporation. From Eq. (4), it is obvious that the transition probability is proportional to the visibility and the trail intensity at time  $t$ . The visibility shows that the closer towns have a higher probability of being chosen. The mechanism behind this is a greedy constructive heuristic. While the trail intensity shows that the more trail on edge  $(i, j)$ , the more attractive it is. The process can be characterized by a positive feedback loop, in which an ant chooses a path thus reinforces it. In order to constrain the ants not to visit a previous visited town, a data structure called the tabu list is associated with each ant. All the visited towns are saved in it. When an ant finishes a cycle, the tabu list is then emptied and the ant is free again to choose. Let  $\text{tabu}_k$  denote the tabu list of the  $k$ th ant.

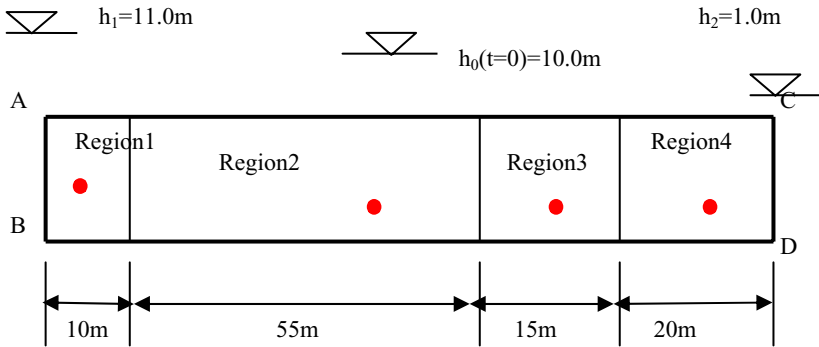
### 3 Parameter Estimation Approach in Groundwater Hydrology Using Hybrid Ant Colony System

#### 3.1 Solution Definition of Inverse Problem and Its Ill-Posedness

The parameter identification problem can be formulated to find the model parameters by adjusting  $m$  until the measured data match the corresponding data computed from the parameter set in a least-squares fashion. The objective function is defined as follows [7]

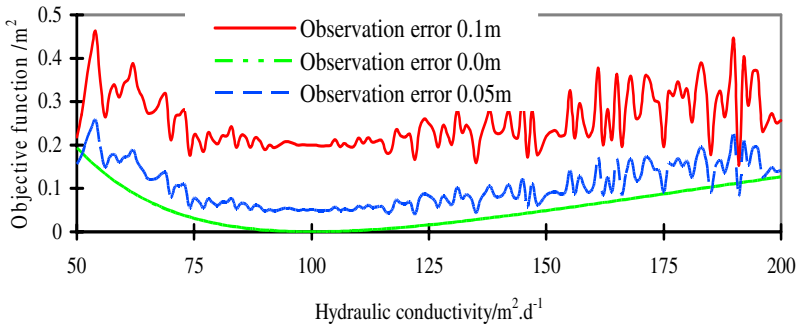
$$J(m) = (h_m - h_c(m))^T w (h_m - h_c(m)) \quad (6)$$

Where  $h_m$  is the measured displacement vector;  $h_c$  is the computing displacement vector, which is related to the identified parameter vector  $m$ .  $w$  is weighting matrix in order to take into account the different observed equipments for the water head measurements [8,9]. This objective function clearly depends on the measured data and the parameters of model.



**Fig. 1.** Configuration of the two-dimensional groundwater flow model

Fig. 1 shows the groundwater flow model, in which the four observing points for water heads are set in order to get measurement data and to identify the aquifer parameters. The objective function can become complex as shown as Fig.2, such as non-convex, or even multi-modal if errors contained in the model equation or /and errors in the measurement data are large. The multi local minima can be found from Fig.2. In such a case, the solution may vibrate or diverge when conventional gradient-based optimization methods are used, which gives rise to the necessary for a robust optimization method such that a stable convergence is always achieved.



**Fig. 2.** Objective functions of the different measurement errors

### 3.2 Simulated Annealing Algorithm for Neighborhood Search

Simulated annealing is another important algorithm which is powerful in optimization and high-order problems. It uses random processes to help guide the form of its search for minimal energy states. Simulated annealing is a generalization of a Monte Carlo method for examining the equations of state and frozen states of n-body systems. The concept is based on the manner in which liquids freeze or metals recrystallize in the

process of annealing[10]. In an annealing process a melt, initially at high temperature and disordered, is slowly cooled so that the system at any time is approximately in thermodynamic equilibrium. As cooling proceeds, the system becomes more ordered and approaches a "frozen" ground state at  $T=0$ . Hence the process can be thought of as an adiabatic approach to the lowest energy state. If the initial temperature of the system is too low or cooling is done insufficiently slowly the system may become quenched forming defects or freezing out in meta-stable states, that is, trapped in a local minimum energy state. Simulated annealing is a very general optimization method which stochastically simulates the slow cooling of a physical system. The idea is that there is a objective function  $F$ , which associates a objective function with a state of the system, a temperature  $T$ , and various ways to change the state of the system. The algorithm works by iteratively proposing change and either accepting or rejecting each change. Having proposed a change we may evaluate the change  $\delta F$  in  $F$ . The proposed change may be accepted or rejected by the Metropolis criterion; if the objective function decreases ( $\delta J < 0$ ), the change is accepted unconditionally; otherwise it is accepted but only with probability  $\exp(-\delta J/T)$ . For given old solution, a new solution can be created as following [11]:

$$m_{new} = m_{old} + \Delta m \quad (7)$$

Where  $\Delta m$  is a random perturbation of solution. The accepted probability of the new solution,  $p_{new}$ , will be expressed:

$$p_{new} = \begin{cases} 1 & J_{old} \geq J_{new} \\ \exp[-\delta J / T_k] & J_{old} < J_{new} \end{cases} \quad (8)$$

Where  $\delta J = J_{new} - J_{old}$ . Three parameters essential for implementation of the simulated annealing algorithm are as follows: 1) initial value of the control parameter,  $T_i$ , 2) the number of perturbations generated at each  $T$ , and 3) the decrement of the control parameter  $T$ . These parameters affect the speed of the algorithm and the quality of the final solution. A simple approach is to choose a value for  $T_i$  that allows a large percentage of non-improving solutions to be accepted [10]. The number of solutions generated at each  $T$  is selected to allow equilibrium to take place before decreasing  $T$ . The decrement of  $T$  is chosen such that it allows only small changes in the value of  $T$ . The equation used for decreasing  $T$  is expressed as follows:

$$T_{k+1} = \xi T_k \quad (9)$$

Where  $\xi=0.9$  is a typical selection. A crucial requirement for the proposed changes is reachability or ergodicity-that there be a sufficient variety of possible changes that one can always find a sequence of changes so that any system state may be reached from any other. When the temperature is zero, changes are accepted only if  $F$  decreases, an algorithm also known as hill-climbing, or more generally, the greedy algorithm. The initial temperature can be determined as [12]

$$T_i = \frac{-1}{\ln p_i} \quad (10)$$

Where  $p_i$  is the desired initial acceptable probability. It is usually between 0.7 and 0.9. Similarly, the final temperature can be determined as

$$T_f = \frac{-1}{\ln p_f} \quad (11)$$

Where  $p_f$  is the desired final acceptable probability. It is usually very close to zero. The system soon reaches a state in which none of the proposed changes can decrease the objective function, but this is usually a poor optimum. In real life, we might be trying to achieve the highest point of a mountain range by simply walking upwards; we soon arrive at the peak of a small foothill and can go no further. On the contrary, if the temperature is very large, all changes are accepted, and we simply move at random ignoring the cost function. Because of the reachability property of the set of changes, we explore all states of the system, including the global optimum. The system evolves until a stop criterion is reached. Very fast simulated annealing scheme proposed by Ingber is applied to produce new solution [13]

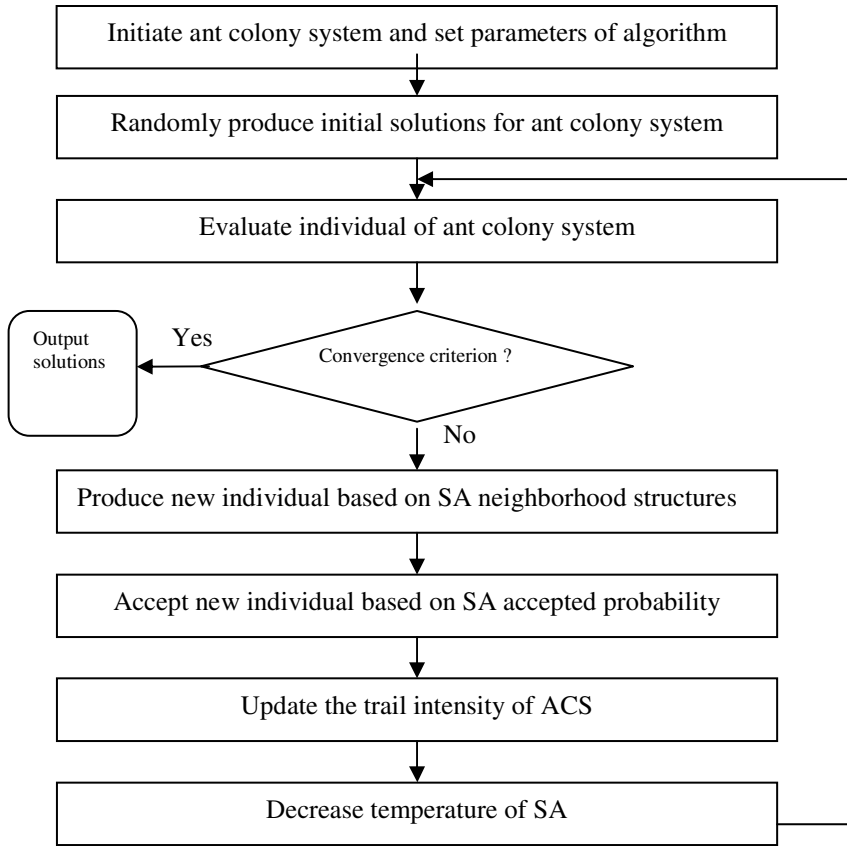
$$\Delta m_i = \eta_i (m_{i_{\max}} - m_{i_{\min}}) \quad (12)$$

$$\eta_i = \text{sign}(u_i - 0.5) T_i \left[ \left(1 + \frac{1}{T_i}\right)^{2|u_i - 0.5|} - 1 \right] \quad (13)$$

Where  $m_{\max}$  and  $m_{\min}$  represent up and down bounds for parameters respectively;  $u_i$  is a random value in  $[-1, 1]$  domain, the value of  $\eta_i$  is just located in  $[-1, 1]$ . The whole process for parameter identification using simulated annealing is shown as follows: Step 1: Initial parameters (initial  $T$  and temperature descent rate  $\alpha$ ) are fixed. Step 2: Initial solution is generated and the corresponding  $J$  is calculated. Step 3: The system solution is updated according to the mechanism designed. Step 4: Parameter  $T$  is modified according to the descent rate established. Step 5: One comes back to the step 3 to calculate the next solution from the current one up to  $T$  or  $\varepsilon$  reaches a value fixed beforehand. Step 6: The best solution visited is written as last solution of inverse problem.

### 3.3 Hybrid Ant Colony System for Parameter Identification

Ant colony system is global search techniques for optimization. However, it is poor at hill-climbing. Simulated annealing has the ability of probabilistic hill-climbing. Therefore, the two techniques are combined here to produce a new algorithm that has the merits of both ant colony system and simulated annealing, by introducing a local search. A new hybridization of ant colony system with simulated annealing is proposed. Fig 3 shows the fundamental structure of hybrid ant colony system with simulated annealing.



**Fig. 3.** Fundamental structure of hybrid ant colony system with simulated annealing

The main concept of inverse problem of parameter identification with the hybrid ant colony system can be summarized in the following steps: Step 1: depict each unknown parameter by an interval based on available prior information; Step 2: discretize each interval into a number of strata, let the middle of each stratum represent that stratum; Step 3: run the simulation model of choice for all, or a randomly selected subset of all the possible parameter combinations; Step 4: evaluate each stratum on the bases of the smallest of the value of the objective function in such a way that small values of the objective function receive higher scores; Step 5: Produce new individual based on SA neighborhood structures; Step 6: Accept new individual based on SA accepted probability. Step 7: on the basis of the value of the objective function, place a certain amount of trail(pheromone in the case of real ants) on each stratum visited along its pathway. Step 8: Decrease temperature of SA according to decreasing scheme; Step 9: repeat step 4 to step 8 until the some convergence criterion is satisfied.

## 4 Experiment

To test the applicability and efficiency of the hybrid ant colony system, a two dimensional flow problem is considered, as shown as Fig.1. The aquifer is bound by two constant-head boundaries with the initial heads both at 11m at  $t > 0$ , the head at right boundary is instantaneously lowered to 10m. The transient head distribution is simulated using finite element method with a time step of 0.1 day. Hydraulic conductivity and specific storage coefficient are listed in Table 1. Table 2 records measured water head data at different points at different times.

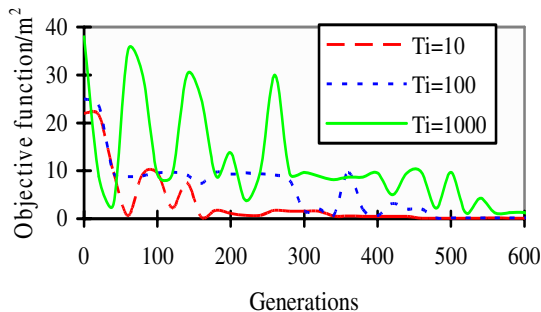
**Table 1.** Hydraulic conductivity and specific storage coefficient

| Parameters | $k_1 / \text{m}^2 \cdot \text{d}^{-1}$ | $k_2 / \text{m}^2 \cdot \text{d}^{-1}$ | $k_3 / \text{m}^2 \cdot \text{d}^{-1}$ | $k_4 / \text{m}^2 \cdot \text{d}^{-1}$ | $S_s$ |
|------------|----------------------------------------|----------------------------------------|----------------------------------------|----------------------------------------|-------|
| Values     | 2000.0                                 | 100.0                                  | 10.0                                   | 1000.0                                 | 0.02  |

**Table 2.** Measured water head data at different points at different times

| Observation time/d | Observation point 1#/m | Observation point 2#/m | Observation point 3#/m | Observation point 4#/m |
|--------------------|------------------------|------------------------|------------------------|------------------------|
| 0.1                | 10.68716               | 9.979836               | 9.170668               | 3.640028               |
| 0.2                | 10.72888               | 9.807406               | 8.396107               | 3.374715               |
| 0.3                | 10.69714               | 9.537611               | 7.756343               | 3.121658               |
| 0.4                | 10.63557               | 9.198385               | 7.028817               | 1.584894               |
| 0.5                | 10.56086               | 8.835012               | 6.398876               | 1.423336               |

According to the flow mathematical model with finite element method and measured water-head data, the aquifer parameters are identified with hybrid ant colony system with simulated annealing. Fig. 4 shows the influence of initial temperature of simulated annealing algorithm to convergence process.



**Fig. 4.** Influence of initial temperatures to convergence process

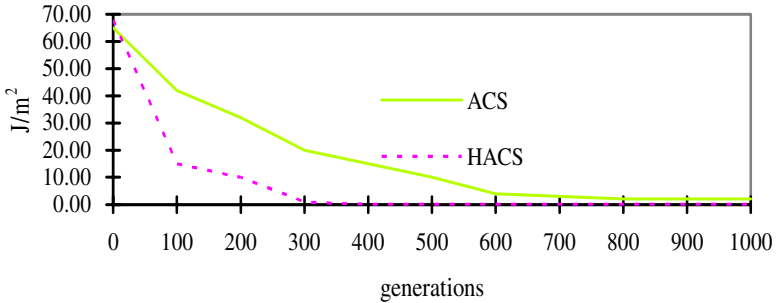
In order to simulate observation errors, the measured water heads can be simulated by adding a random error to the theoretical values

$$h_m^* = h_m + \text{sign}(R - 0.5) \times \Delta h \tag{14}$$

Where  $h_m^*$  are the measured data with observation errors,  $h_m$  are the measured data without observation errors. *Sign* is the sign function, and  $R$  is a random variable in the interval  $[0,1]$ ,  $\Delta h$  is observation error. Comparison of identified hydraulic conductivity and specific storage coefficient with theoretical values is listed in Table 3. Fig. 5 shows the convergence process of objective function with classical ant colony system and hybrid ant colony system.

**Table 3.** Comparison of identified hydraulic conductivity and specific storage coefficient with theoretical values

| Model parameters          | $k_1 / \text{m}^2 \cdot \text{d}^{-1}$ | $k_2 / \text{m}^2 \cdot \text{d}^{-1}$ | $k_3 / \text{m}^2 \cdot \text{d}^{-1}$ | $k_4 / \text{m}^2 \cdot \text{d}^{-1}$ | $S_s$ |
|---------------------------|----------------------------------------|----------------------------------------|----------------------------------------|----------------------------------------|-------|
| Theoretical Values        | 2000.0                                 | 100.0                                  | 10.0                                   | 1000.0                                 | 0.02  |
| Identified values by HACS | 2010.3                                 | 99.7                                   | 10.2                                   | 1009.0                                 | 0.018 |
| Identified values by ACS  | 2022.7                                 | 110.2                                  | 9.95                                   | 1012.5                                 | 0.025 |



**Fig. 5.** Convergence process of objective function with different searching method

## 5 Conclusion

Hybrid ant colony system for solving the parameter identification problem is proposed. The three characteristics of the ant colony system, such as positive feedback process, greedy constructive heuristic and distributed computation, work together to find the solution to the inverse problems fast and efficiently. However, classical ant colony system is poor at hill-climbing. Simulated annealing has the ability of probabilistic hill-climbing. Therefore, the two techniques are combined here to produce a new algorithm that has the merits of both ant colony system and simulated annealing, by introducing a local search. A new hybridization of ant colony system with simulated annealing is proposed. Modern heuristic search techniques,

such as genetic algorithm, simulated annealing and ant colony system, are well suited for solving the parameter identification problem in groundwater flow model. The gradient based methods are not applicable for this type of inverse problem because of the difficulty in evaluating the function derivatives and the presence of many local minimum points in the objective function. One of the advantages of ant colony system over other optimization methods is that it is easy to implement complex inverse problem.

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# Route-Exchange Algorithm for Combinatorial Optimization Based on Swarm Intelligence\*

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**Abstract.** Inspired by the information interaction of individuals in swarm intelligence, a new algorithm for combinatorial optimization is proposed, which is called as Route-Exchange Algorithm (REA). This is a heuristic approach, in which the individuals of the swarm search the state space independently and simultaneously. When one encounters another in the process, they would interact with each other, exchange the information of routes toured, and utilize the more valuable experiences to improve their own search efficiency. An elite strategy is designed to avoid vibrations. The algorithm has been applied to Traveling Salesman Problem (TSP) and assignment problem in this paper. Some benchmark functions are tested in the experiments. The results indicate the algorithm can quickly converge to the optimal solution with quite low cost.

## 1 Introduction

Since the social insects have evolved to fit the ever-changing environments for millions of years, it is believed that their behaviors are most effective in the collective way. Therefore, scientists have been returning to social insects for heuristics recently, such as ants, bees etc. In 1991, Marco Dorigo was inspired by the forage behaviors of ants, and proposed Ant Colony Optimizer (ACO) [1] for distributed optimization problems. After that, J. Kennedy and R. C. Eberhart were inspired by the forage behaviors of birds and fish, and proposed Particle Swarm Optimizer (PSO) [2] for continuous optimization problems. These methods have been applied to many problems and proved successful. Since then, there have been many analogous methods [3], [4], [5] reported.

Social insects are usually characterized by self-organization. Complex collective behavior emerges from the interactions of individuals who exhibit simple behaviors by themselves. In social insects, central control is not necessarily needed. Every individual is self-autonomous. They can only obtain local information, and interact with their geographical neighbors. They can also change the local environment or mark in the local environment to interact with the remote individuals indirectly, namely stigmergy. These features all characterize swarm intelligence. Swarm intelligence is

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defined as any attempt to design algorithms or distributed problem-solving devices inspired by the collective behaviors of the social insect colonies and other animal societies [6]. Generally speaking, swarm intelligence denotes that more complex intelligence emerges from the interactions of individuals who behave as a swarm [1], [6].

In the swarm systems, environment, individual and behavior rule are all sufficiently considered by researchers as three elementary factors [7]. Based on them, however, systematical and general theory still cannot be established. In fact, the information interaction of the individuals is very important. All methods mentioned above imply the information interactions, and it plays a key role for solving problems. In this paper we focused on the information interactions, and proposed a novel algorithm for combinatorial optimization. It is called as Route-Exchange Algorithm (REA), in which each individual put the better experiences in its memory by interacting with others, and behaves according to the best experiences in the next repetition.

The new approach is applied to solve traveling salesman problem (TSP) and assignment problem firstly. Since they are classical combinatorial optimization problems, various approaches for them have been reported [8], [9], [10]. Though REA is just a new computational method, it has shown its efficiency in the solving process. This paper is organized as follows. Section 2 describes REA. It is applied to TSP in section 3 and assignment problem in section 4. Section 5 gives some conclusions and remarks.

## 2 Route-Exchange Algorithm

Assuming a finite state space of a problem, each state can be denoted by a node. If individual can transit between state  $c_i$  and state  $c_j$ , then node  $c_i$  and  $c_j$  is connected. Meanwhile, the cost of the transition is denoted by  $d_{ij}$ . Solving the problem implies finding the shortest route to the given state with some constraint conditions.

The REA is a heuristic approach inspired by the information interactions of population, in which every individual searches the state space independently and simultaneously. As far as people are concerned, if a number of them are asked to fulfill the same task independently, they would interact with each other, and learn from each other to improve their own performances. This mechanism is applied in the route-exchange algorithm.

### 2.1 Search Process of Individuals

Given a complete graph of  $n$  nodes,  $m$  individuals are required to find the shortest Hamiltonian cycle independently from different starting nodes with the same velocity  $v$ , where  $m \leq n$ . They could encounter the fellows somewhere in the process, which enable them to interact information. Each individual has two storages: one is for the permutation of nodes  $(c_{\pi(1)}, c_{\pi(2)}, \dots, c_{\pi(r)})$  visited by itself in the current iteration, another is for the best permutation  $(c_{\pi^*(1)}, c_{\pi^*(2)}, \dots, c_{\pi^*(q)})$  visited by itself

or others ever encountered in the current repetition. For the convenience of depiction, we denote the former with *route-storage-A*,  $RS\_A$  for short, and the latter with  $RS\_B$ . When two individuals encounter, they would compare the quality of the two routes visited in the current repetition with each other, put the better one into  $RS\_B$ , and continue to tour. In the next repetition, the individual would prefer  $RS\_B$  of previous repetition and follow it first, then previous  $RS\_A$ .

### 2.2 State Transition Function

As for the  $k$ th individual, if he is at node  $i$  sometime, then the probability that he selects the node  $j$  as his next node is as follows:

$$p_{ij}^k = \begin{cases} \frac{(\eta_{ij})^\alpha \cdot \rho_B}{\sum_{r \in allowed_k} (\eta_{ir})^\alpha}, l_{ij} \in RS\_B \\ \frac{(\eta_{ij})^\alpha \cdot \rho_A}{\sum_{r \in allowed_k} (\eta_{ir})^\alpha}, (l_{ij} \in RS\_A) \wedge (l_{ij} \notin RS\_B) \\ \frac{(\eta_{ij})^\alpha \cdot \rho_C}{\sum_{r \in allowed_k} (\eta_{ir})^\alpha}, else \end{cases} \quad (1)$$

where  $\eta_{ij} = 1/d_{ij}$ ,  $l_{ij}$  denotes the edge  $(i, j)$ ,  $allowed_k$  denotes the set of all candidate nodes when the  $k$ th individual is at node  $i$ ,  $\rho_A$ ,  $\rho_B$  and  $\rho_C$  are selection parameters,  $\rho_C < \rho_A < \rho_B$ , and  $\alpha$  is a control parameter.

### 2.3 Encounter Operation

Given that the  $k$ th individual reaches the node  $i$  at time  $T_k$ , and the  $l$ th individual reaches the same node at time  $T_l$ . If the inequality (2) is satisfied, then the two individuals are judged encountered.

$$|T_k - T_l| \leq \frac{\bar{d}_{ij}}{\beta v}, \quad j \in Neighbor_i \quad (2)$$

where  $Neighbor_i$  is the set of nodes connected directly with node  $i$ , and  $\beta$  is a control parameter.

In order to evaluate the quality of the route  $(c_{\pi(1)}, \dots, c_{\pi(q)})$ , we have  $G$  that

$$G = \left(\frac{1}{q}\right)^\delta \cdot \frac{\sum_{i=1}^{q-1} d_{i,i+1}}{q} \quad (3)$$

where  $\delta$  is a control parameter. The smaller the value of  $G$  is, the better the quality of the route is.

## 2.4 Elite Strategy

We have designed an elite strategy to avoid vibrations. After each repetition, the individual who has the best results in the current repetition is required to save his experience, and take the same tour in the next repetition. In this way, the best individual can keep his capability of influence on others, and accelerate others to improve their fitness.

## 2.5 Step by Step Procedure of REA

Step1: Initialize

Put all individuals on different nodes randomly,  $NC=1$ .

Step 2: Search the State Space

For each individual, tour the nodes by Formula (1) with velocity  $v$ .

Step 3: Encounter Judgment and Operations

For each node, calculate the time  $T$  that every individual reaches it, determine whether two individuals encounter with each other according to Equality (2). If yes, compare their routes with  $G$  in Formula (3) and put the better routes into  $RS\_B$ .

Step 4: Elite Strategy

Find the individual who has the best results in the current repetition, put the route of  $RS\_A$  into  $RS\_B$ .

Step 5: Stop Criterion

If  $NC=NC_{max}$ , stop the program and return the results, otherwise,  $NC=NC+1$ , select the first node of  $RS\_B$  as the starting node and return to the next repetition. If  $RS\_B$  is empty, take the first node of  $RS\_A$  instead.

## 3 REA for TSP

Traveling salesman problem (TSP) is probably the most well-known NP-hard combinatorial optimization problem. The task of the traveling salesman problem is to find the shortest route for a traveling salesman to visit all the cities once and only once, and return to the starting city, which is also known as a Hamiltonian cycle. The problem can be described as follows.

Given a set of cities  $C = \{c_1, c_2, \dots, c_n\}$ , for each pair  $(c_i, c_j)$ ,  $i \neq j$ , let  $d(c_i, c_j)$  be the distance between city  $c_i$  and  $c_j$ . Solving the TSP entails finding a permutation  $\pi^*$  of the cities  $(c_{\pi^*(1)}, \dots, c_{\pi^*(n)})$ , such that

$$\sum_{i=1}^n d(c_{\pi^*(i)}, c_{\pi^*(i+1)}) \leq \sum_{i=1}^n d(c_{\pi(i)}, c_{\pi(i+1)}), \forall \pi \neq \pi^*, (n+1) \equiv 1 \quad (4)$$

In the symmetric TSP  $d(c_i, c_j) = d(c_j, c_i), \forall i, j$ , while in the asymmetric TSP this condition is not satisfied. In this work we consider the symmetric TSP.

REA is designed for TSP. It can be easily coded into program. We tested it on some TSP instances defined in the TSPLIB [11]. The experiments were conducted on several Windows XP Pentium IV 1.60 GHz PCs with 256 Mbytes of memory. The results of the instances are summarized in Table 1. The first column stands for the names of the test instances, the second for exact optimal tour length for each problem given in the TSPLIB. The third column stands for the best results we have obtained, the fourth to the sixth for the results in each run time, the seventh for the average results, and the eighth for the relative error (Err), respectively, where the relative error is calculated as

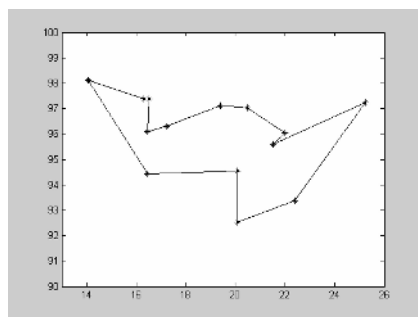
$$Err = \frac{Ave - Opt}{Opt} \times 100\% \quad (5)$$

The ninth column denotes the repetition times required, and the last denotes the number of individuals employed in the program.

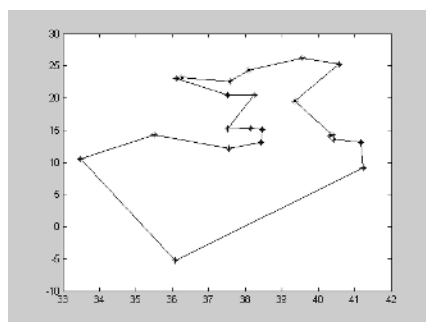
Table 1 indicates that the proposed route-exchange algorithm can be used to solve symmetric TSP effectively. It can be seen that among 8 test problems, the maximum relative error is 6.81% (of the test problem Eil51) and the average relative error of all is easily calculated to be 3.23%. While the number of nodes increases, the repetition times required doesn't increase remarkably. In other words, the results can converge quickly to good solutions, and the complexity of the computation can be kept quite low. Fortunately, we have obtained better solutions than that given in the TSPLIB for

**Table 1.** Summary of the experiment results

| Problem    | Opt   | Best Result | Run1  | Run2  | Run3  | Ave.  | Err(%) | NC <sub>max</sub> | Ind |
|------------|-------|-------------|-------|-------|-------|-------|--------|-------------------|-----|
| Burma14    | 33.23 | 31.88       | 33.23 | 31.88 | 33.21 | 32.77 | -1.38  | 10                | 10  |
| Ulys-ses22 | 75.67 | 75.67       | 76.06 | 76.63 | 75.67 | 76.12 | 0.59   | 30                | 20  |
| Bayg29     | 9074  | 9336        | 9399  | 9336  | 9433  | 9389  | 3.47   | 30                | 20  |
| Bays29     | 2020  | 2097        | 2097  | 2097  | 2107  | 2067  | 2.33   | 30                | 28  |
| Swiss42    | 1273  | 1303        | 1325  | 1329  | 1303  | 1319  | 3.61   | 30                | 30  |
| Att48      | 33524 | 34707       | 35073 | 34707 | 36458 | 35413 | 5.63   | 30                | 40  |
| Eil51      | 426   | 451         | 451   | 454   | 459   | 455   | 6.81   | 30                | 40  |
| Berlin52   | 7542  | 7870        | 7870  | 7918  | 7931  | 7900  | 4.75   | 30                | 40  |



(a) Burma14, length=31.88



(b) Ulysses22, length=75.67

**Fig. 1.** The best tours we obtained in the experiments

Burma14. Fig. 1 illustrates the best tours of two instances we tested. Obviously the results are very well.

#### 4 REA for Assignment Problem

There are  $n$  jobs can be done by  $n$  workers. The cost of job  $i$  done by worker  $j$  is  $c_{ij}$ . Assuming one worker can only do one job, the objective is to assign jobs to right workers to minimize the total cost.

Since the famous Hungarian method for the assignment problem was proposed in 1955 [12], various approaches for assignment, quadratic assignment have been proposed in past five decades. Although there are many special topics in this area [13], such as multi-dimensional assignment, dynamic assignment and constrained assignment [14], the foundation of all assignment problems is the basic assignment problem and Quadratic Assignment Problem (QAP).

We denote the jobs and workers as two types of node sets  $J$  and  $W$ . The distance of node  $c_i$  ( $c_i \in J$ ) and  $c_j$  ( $c_j \in W$ ) is denoted with  $d_{ij}$ , which is the cost of job

$i$  done by worker  $j$ . When applying REA to the assignment, individuals cannot select more than one node in the same type of node set continuously. In addition, if there are  $u$  nodes in the individual's  $RS\_A$ , we set  $\eta_{ij}$  that

$$\eta_{ij} = \begin{cases} d_{ij}, (u + 1) / 2 = 0 \\ 1 / d_{ij}, else \end{cases} \tag{6}$$

If the length of the route in  $RS\_A$  is denoted with  $len$ , and the individual will go to node  $c_j$  from  $c_i$ , then the increase of length is

$$len_{u+1} = \begin{cases} len_u, (u + 1) / 2 = 0 \\ len_u + d_{ij}, else \end{cases} \tag{7}$$

**Table 2.** The cost matrix of 10 jobs and 10 workers

| $i \setminus j$ | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 |
|-----------------|----|----|----|----|----|----|----|----|----|----|
| 1               | 7  | 33 | 91 | 96 | 5  | 7  | 73 | 46 | 20 | 79 |
| 2               | 19 | 57 | 4  | 4  | 80 | 66 | 53 | 24 | 91 | 23 |
| 3               | 40 | 47 | 16 | 73 | 81 | 40 | 65 | 35 | 84 | 16 |
| 4               | 87 | 76 | 40 | 99 | 1  | 90 | 76 | 51 | 47 | 24 |
| 5               | 98 | 47 | 67 | 56 | 88 | 49 | 63 | 34 | 86 | 42 |
| 6               | 44 | 7  | 35 | 50 | 46 | 57 | 89 | 50 | 83 | 30 |
| 7               | 63 | 44 | 76 | 37 | 15 | 80 | 17 | 42 | 77 | 85 |
| 8               | 41 | 34 | 88 | 90 | 39 | 60 | 52 | 52 | 93 | 1  |
| 9               | 56 | 85 | 46 | 53 | 37 | 10 | 73 | 14 | 16 | 93 |
| 10              | 91 | 55 | 95 | 68 | 44 | 13 | 78 | 31 | 50 | 77 |

**Table 3.** The best solution for the assignment problem

| Job $i$       | 1 | 2 | 3  | 4 | 5  | 6 | 7  | 8  | 9  | 10 |
|---------------|---|---|----|---|----|---|----|----|----|----|
| Worker $j$    | 1 | 4 | 3  | 5 | 8  | 2 | 7  | 10 | 9  | 6  |
| Cost $C_{ij}$ | 7 | 4 | 16 | 1 | 34 | 7 | 17 | 1  | 16 | 13 |

**Table 4.** The performance of REA for examples of different size

| Example   | 1   | 2   | 3      | 4   | 5      |
|-----------|-----|-----|--------|-----|--------|
| Size      | 20  | 30  | 40     | 50  | 60     |
| Best Val. | 154 | 189 | 191    | 174 | 169    |
| Mean Val. | 154 | 189 | 192.45 | 174 | 173.33 |
| Max Val.  | 154 | 189 | 198    | 174 | 182    |
| Best Rate | 1   | 1   | 0.64   | 1   | 0.84   |

For an example of 10 jobs, its cost matrix was generated via a random number generator as shown in Table 2. After 20 repetitions, the best solution achieved is shown in Table 3.

The optimal value is 116. By Hungarian method, we can confirm that the achieved solution is optimal.

To test the performance of REA, we run it on several randomly generated examples of different size. For each example, we run the program of REA for 50 times by starting from different random nodes. The achieved best values, maximum values, mean values and the rate to achieve the best solution are shown in Table 4.

From Table 4 we can see that REA can be applied to solving assignment problem successfully. We noticed that the lowest “best rate” occurred in problem 3 instead of problem 4 and problem 5 with larger size, because the best rate depends not only on the size but also on the structure of cost matrix of the problem.

## 5 Conclusions

In REA, individuals achieve their goals by exchanging information with each other. In this way, the better routes have more chances to be taken. Because the exchange of route information is the most important idea in the algorithm, it is called as route-exchange algorithm. As can be seen in the experiments and results, this algorithm can converge quickly to a good solution with quite low computing complexity. The stagnancy in local optimum, which is generally existent as a defect in the analogous other algorithms, can be effectively avoided. Also, the elite strategy we designed plays a very important role in this algorithm, which helps to attract other individuals to the global optimum step by step.

On the other hand, it can be seen that the information interaction based on swarm intelligence is worth well exploring in the context of solving optimization problems. Interaction rule is the most important rule in a swarm system, which has showed its great powers. There may be a lot of algorithms inspired by it emerging in the near future.

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# Stability Analysis of Swarm Based on Double Integrator Model\*

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**Abstract.** In this paper, we consider an  $M$ -member individual-based continuous-time double integrator swarm model in an  $n$ -dimensional space. The swarm model based on the Newton's law is more suitable to describe the swarm aggregation and has wide practical applications. We present stability analysis for the case of linear attraction and bounded repulsion to characterize swarm cohesiveness, size and ultimate motions while in a cohesive group. Finally, some numerical examples and simulation results are presented to illustrate the effectiveness of the swarm model.

## 1 Introduction

In recent years, the problem of coordination and control of multiple agents is becoming one of the hotspots. This is partly due to broad applications of multi-agent systems in many areas including cooperative control of unmanned air vehicles, flocking of birds, schooling for underwater vehicles, distributed sensor networks, etc. Although the application backgrounds are different, the fundamental principles are very similar, that is, coordinating multiple agents to achieve a goal of the whole system.

Aggregating behavior of multi-member, such as flocks of birds, schools of fish, herds of animals, and colonies of bacteria [4,7,8,9], draws many scientists' attention, which mainly lines in the researching value of the swarms' inner operational mechanism of self-organization. From the principle we can use it to the areas of unmanned air vehicles, attitude alignment for cluster of satellites, formation control of multi-robot teams [2,12,13]. The aggregating model used to simulate flock behavior has been presented in [3]. That paper explored an approach based on simulation as an alternative to scripting the paths of each bird individually. The aggregate motion of the simulated flock is created by a distributed behavioral birds choose their own course.

In the early days biologists worked on understanding and modeling of swarming behavior, they brought forward swarm models supposed of attractin/repulsion functions [5,6]. Recently [1,10,11] continued the topic, authors all had

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proved the swarm could converge to a bounded region, and used the Lyapunov method to show their stability. [11] extended the results in [1] by specifying a class of general attraction/repulsion functions. It is very significant to introduce the “safety area ”to the engineering, for example, it can decrease the friction between machines, increase the safe coefficient of operation and so on. The drawback is that the center of the model is stillness, which is inconsistent with biology since any creature is moving. In this paper, we establish a double integrator swarm model which considers the motion of the swarm.

The paper is organized as follows. In section 2, we establish a double integrator model of the swarm. The swarm size after aggregating is discussed in section 3, and the stability analysis of swarm is given in section 4. We also provide numerical simulations to reify our theories in section 5.

## 2 Model of an Aggregation Swarm

As is known to us, the derivative of position is velocity, and the second derivative of position is acceleration. So if the model is an integrator such as ones in [1,10,11], it is equal to use force to control velocity, but we know the change of velocity needs a process, during the period the acceleration plays an important part, so it is quite necessary to consider the double integrator model, meanwhile it expresses the relation between the force and the acceleration. [11] pointed out that the swarm model should be generalized to a double integrator model based on the Newton’s law  $F = ma$ . The double integrator model is more practical and has more applications. When a swarm arrives to the state of balance, it requires not only the member of the swarm not scattered, but also velocity matching. Thus, we assume the expectant velocity of the swarm member is  $v_d$ .

Consider a swarm of  $M$  individuals (members) in an  $n$ -dimensional Euclidean space. We assume synchronous motion and no time delays, i.e., all the members move simultaneously and know the exact positions of all the other members. Thus, we propose a swarm model in which each agent is expressed in the form of a double integrator:

$$\begin{cases} \dot{x}_i = v_i \\ \dot{v}_i = \sum_{j=1, j \neq i}^M g(x_i - x_j) - k(v_i - v_d), \end{cases} \quad i = 1, 2, \dots, M \quad (1)$$

where  $x_i \in \mathcal{R}^n$  represents the position of individual  $i$ ,  $v_i \in \mathcal{R}^n$  represents the velocity of individual  $i$ ,  $g : \mathcal{R}^n \rightarrow \mathcal{R}^n$  represents the function of attraction and repulsion between individuals,  $k \in \mathcal{R}^+$  is a constant.

Consider functions  $g(\cdot)$  of type

$$g(y) = -y[g_a(\|y\|) - g_r(\|y\|)]$$

where  $g_a : \mathcal{R}^+ \rightarrow \mathcal{R}^+$  represents the magnitude of the attraction term, whereas  $g_r : \mathcal{R}^+ \rightarrow \mathcal{R}^+$  represents the magnitude of the repulsion term, the vector  $y$  determines the alignment, so the actual attraction and repulsion are  $-yg_a(\|y\|)$ ,

and  $yg_r(\|y\|)$  respectively, where  $\|y\| = \sqrt{y^T y}$  is the Euclidean norm. Assume that  $g(\cdot)$  satisfies the following Assumptions.

(A1)  $g(\cdot)$  is an odd function that have terms for attraction and repulsion acting in opposite direction, i.e.,  $g(y) = -g(-y)$ .

(A2) There exists a unique distance  $\delta$  at which we have  $g_a(\delta) = g_r(\delta)$ . Moreover, we have  $g_a(\|y\|) > g_r(\|y\|)$  for  $\|y\| > \delta$  and  $g_r(\|y\|) > g_a(\|y\|)$  for  $\|y\| < \delta$ .

(A3) There exist corresponding functions  $J_a : \mathcal{R}^+ \rightarrow \mathcal{R}^+$  and  $J_r : \mathcal{R}^+ \rightarrow \mathcal{R}^+$  such that

$$\nabla_y J_a(\|y\|) = yg_a(\|y\|) \quad \text{and} \quad \nabla_y J_r(\|y\|) = yg_r(\|y\|) .$$

$J_a(\cdot), J_r(\cdot)$  are the artificial social potential functions of the attraction and repulsion between the individuals, respectively.

Assumptions (A1),(A2) and (A3) were introduced by [11]. We denote  $\mathcal{G}(\cdot)$  as the set of  $g(\cdot)$  which satisfies (A1-A3).

The inter-individual attraction/repulsion is based on an interplay between attraction and repulsion forces with the attraction dominating on large distances, and the repulsion dominating on short distances, and there is a unique constant distance where attraction and repulsion balance. It has been observed that the individuals in swarms desire neither too close (avoiding crowding) nor too far (avoiding dispersion) from other individuals. Too close the distance between two individuals is, they will disperse; too far the distance between two individuals is, they will close. Therefore, the dependence on this kind of functions makes intuitive sense, the size of the swarm is finite.

For simplicity, we use a variable substitution  $x'_i = x_i - v_d t, v'_i = v_i - v_d$  to the model (1). Then, we can rewrite the model (1) as follows

$$\begin{cases} \dot{x}'_i = \dot{x}_i - v_d = v_i - v_d = v'_i \\ \dot{v}'_i = \dot{v}_i = \sum_{j=1, j \neq i}^M g(x_i - x_j) - k(v_i - v_d) \\ \quad = \sum_{j=1, j \neq i}^M g(x'_i - x'_j) - kv'_i, \quad i = 1, 2, \dots, M \end{cases} \quad (2)$$

Using  $x_i, v_i$  instead of  $x'_i, v'_i$  for convenience, the model (2) can be rewritten as

$$\begin{cases} \dot{x}_i = v_i \\ \dot{v}_i = \sum_{j=1, j \neq i}^M g(x_i - x_j) - kv_i, \quad i = 1, 2, \dots, M \end{cases} \quad (3)$$

The properties of the swarm model (1) can be obtained by analyzing the swarm model (3). So we analyze the model (3) in this paper for convenience.

It is clear that the center of the swarm should be defined as  $\bar{x} = \frac{1}{M} \sum_{i=1}^M x_i$ .

Thus, the velocity of the center is obtained as  $\bar{v} = \dot{\bar{x}} = \frac{1}{M} \sum_{i=1}^M \dot{x}_i = \frac{1}{M} \sum_{i=1}^M v_i$ .

**Theorem 1.** *The center  $\bar{x}$  of the swarm described by model (3) with an attraction/repulsion function  $g(\cdot) \in \mathcal{G}(\cdot)$  converges to a fixed point.*

*Proof.* Consider the model (3), the time derivative of center is given by

$$\begin{aligned} \dot{\bar{x}} &= \frac{1}{M} \sum_{i=1}^M \dot{x}_i = \frac{1}{M} \sum_{i=1}^M v_i = \bar{v} \\ \dot{\bar{v}} &= \frac{1}{M} \sum_{i=1}^M \dot{v}_i = \frac{1}{M} \sum_{i=1}^M \left[ \sum_{j=1, j \neq i}^M g(x_i - x_j) - kv_i \right] \\ &= \frac{1}{M} \sum_{i=1}^M \left\{ \sum_{j=1, j \neq i}^M - [g_a(\|x_i - x_j\|) - g_r(\|x_i - x_j\|)] (x_i - x_j) - kv_i \right\} \\ &= -\frac{1}{M} \sum_{i=1}^{M-1} \sum_{j=i+1}^M \{ [g_a(\|x_i - x_j\|) - g_r(\|x_i - x_j\|)] (x_i - x_j) + \\ &\quad [g_a(\|x_j - x_i\|) - g_r(\|x_j - x_i\|)] (x_j - x_i) \} - \frac{1}{M} \sum_{i=1}^M kv_i \\ &= -k\bar{v} \end{aligned}$$

So the center of the swarm satisfies

$$\begin{cases} \dot{\bar{x}} = \bar{v} \\ \dot{\bar{v}} = -k\bar{v} \end{cases} \tag{4}$$

From (4), we can get  $\bar{v} = \bar{v}(0)e^{-kt}$ ,  $\bar{x} = \bar{x}(0) + \frac{\bar{v}(0)}{k} - \frac{\bar{v}(0)}{k}e^{-kt}$  which means that as  $t \rightarrow \infty$ ,  $\bar{v} \rightarrow 0$ , and  $\bar{x} \rightarrow \bar{x}(0) + \frac{\bar{v}(0)}{k} \triangleq \xi$  (a constant). ■

Thus, it is clear that as  $t \rightarrow \infty$ , the velocity of the center of the swarm model (1) will tend to  $v_d$ , and the center will tend to  $v_d t + \xi$ , i.e., the center will begin with the initial position and move at the expectant speed  $v_d$ .

### 3 Analysis of Swarm Cohesion

The position difference between the individual  $i$  and the center of the swarm is defined as  $e_i = x_i - \bar{x}$ , and the velocity difference between the individual  $i$  and the center of the swarm is defined as  $p_i = v_i - \bar{v}$ .

In [1,10], the following attraction/repulsion function is considered

$$g(y) = -y \left[ a - b \exp \left( -\frac{\|y\|^2}{c} \right) \right] \tag{5}$$

The attraction term is linear and the repulsion term is bounded for (5). In this paper, we extend the function to a kind of  $g(\cdot) (\in \mathcal{G}(\cdot))$  which is composed of linear attraction terms and bounded repulsion terms, i.e.,

$$\begin{cases} g_a(\|y\|) = a \\ g_r(\|y\|) \|y\| \leq b \end{cases} \tag{6}$$

where  $a > 0, b > 0$  are finite positive constants. The swarm model (1) or (3) using more general attraction/repulsion functions  $g(\cdot) (\in \mathcal{G}(\cdot))$  can also be analyzed similarly by using the method given in this paper.  $g_a(\|y\|) = a$  means that  $g_a(\|y\|)$  is invariant, but it is compatible with the Assumption A2 because  $g_r(\|y\|)$  has relation with the distance  $\|y\|$ .

From (2), we have

$$\dot{e}_i = \dot{x}_i - \dot{\bar{x}} = v_i - \bar{v} = p_i \tag{7}$$

and

$$\begin{aligned} \dot{p}_i &= \dot{v}_i - \dot{\bar{v}} \\ &= \sum_{j=1, j \neq i}^M -[g_a(\|x_i - x_j\|) - g_r(\|x_i - x_j\|)](x_i - x_j) - kv_i + k\bar{v} \\ &= -aMe_i + \sum_{j=1, j \neq i}^M g_r(\|x_i - x_j\|)(x_i - x_j) - kp_i \end{aligned} \tag{8}$$

Let  $\epsilon_i = \text{col}(e_i, p_i), i = 1, \dots, M$ . Then we have

$$\dot{\epsilon}_i = \begin{pmatrix} \dot{e}_i \\ \dot{p}_i \end{pmatrix} = \left[ \begin{pmatrix} 0 & 1 \\ -aM & -k \end{pmatrix} \otimes I_n \right] \epsilon_i + \begin{pmatrix} 0 \\ \sum_{j=1, j \neq i}^M g_r(\|x_i - x_j\|)(x_i - x_j) \end{pmatrix}.$$

Let  $F = \begin{pmatrix} 0 & 1 \\ -aM & -k \end{pmatrix}$  and  $f = \begin{pmatrix} 0 \\ \sum_{j=1, j \neq i}^M g_r(\|x_i - x_j\|)(x_i - x_j) \end{pmatrix}$ . Then we can obtain eigenvalues of the matrix  $F$  as follows

$$\lambda(F) = \frac{-k \pm \sqrt{k^2 - 4aM}}{2}$$

if  $\sqrt{k^2 - 4aM} \geq 0$  then  $\lambda(F) < 0$ , which implies that  $F$  is a stable matrix; if  $\sqrt{k^2 - 4aM} < 0$ , then the real part of  $\lambda(F)$  is negative, which also implies that  $F$  is a stable matrix. Thus, for any given symmetric positive definite matrix  $Q$ , the Lyapunov equation  $F^T P + PF = -Q$  has a symmetric positive definite solution matrix  $P$ .

The maximum and minimum eigenvalues of any symmetric positive definite matrix  $S$  are denoted as  $\lambda_{max}(S)$  and  $\lambda_{min}(S)$  respectively. Note that for any symmetric positive definite matrix  $S$  with fit dimensions the following inequalities are satisfied

$$\lambda_{min}(S) \| \epsilon_i \|^2 \leq \epsilon_i^T S \epsilon_i \leq \lambda_{max}(S) \| \epsilon_i \|^2. \tag{9}$$

Then we establish the following theorem.

**Theorem 2.** Consider the swarm described by model (3) with an attraction/repulsion function  $g(\cdot) (\in \mathcal{G}(\cdot))$  given in (6). As time progresses, all the members of the swarm will converge to a hyperball

$$B(\bar{x}) = \left\{ x : \|x - \bar{x}\| \leq \frac{2\lambda_{max}(P)[(M - 1)b]}{\lambda_{min}(Q)} \right\}.$$

*Proof.* Choose the Lyapunov function  $V_i = \epsilon_i^T(P \otimes I_n)\epsilon_i$  for each individual. Then, we have

$$\begin{aligned} \dot{V}_i &= \dot{\epsilon}_i^T(P \otimes I_n)\epsilon_i + \epsilon_i^T(P \otimes I_n)\dot{\epsilon}_i \\ &= ((F \otimes I_n)\epsilon_i + f)^T(P \otimes I_n)\epsilon_i + \epsilon_i^T(P \otimes I_n)((F \otimes I_n)\epsilon_i + f) \\ &= -\epsilon_i^T(Q \otimes I_n)\epsilon_i + 2\epsilon_i^T(P \otimes I_n)f, \end{aligned} \tag{10}$$

from which we can obtain

$$\begin{aligned} \dot{V}_i &\leq -\epsilon_i^T(Q \otimes I_n)\epsilon_i + 2 \|\epsilon_i\| \lambda_{max}(P)(M-1)b \\ &= -\lambda_{min}(Q) \|\epsilon_i\|^2 + 2 \|\epsilon_i\| \lambda_{max}(P)(M-1)b \\ &= -\|\epsilon_i\| (\lambda_{min}(Q) \|\epsilon_i\| - 2\lambda_{max}(P)(M-1)b). \end{aligned} \tag{11}$$

If  $\|\epsilon_i\| > \frac{2\lambda_{max}(P)}{\lambda_{min}(Q)}(M-1)b$ , then  $\dot{V}_i < 0$ . This implies that as  $t \rightarrow \infty$ ,  $\epsilon_i$  will converge into the ball around  $col(\bar{x}, \bar{v})$  defined by  $\|\epsilon_i\| \leq \frac{2\lambda_{max}(P)}{\lambda_{min}(Q)}(M-1)b$ , and  $\|x_i - \bar{x}\| \leq \|\epsilon_i\| \leq \frac{2\lambda_{max}(P)}{\lambda_{min}(Q)}(M-1)b, i = 1, 2, \dots, M$ . This proves the theorem. ■

*Remark 1.* Note that  $\|v_i - \bar{v}\| \leq \|\epsilon_i\| \leq \frac{2\lambda_{max}(P)}{\lambda_{min}(Q)}(M-1)b$ , it expresses that the velocity of agent  $i$  can not exceed  $\frac{2\lambda_{max}(P)}{\lambda_{min}(Q)}(M-1)b$  relative to the velocity of the center; once  $\|v_i - \bar{v}\|$  or  $\|x_i - \bar{x}\|$  exceeds the bound, the agent will run towards to minimize its potential. Finally, the distance and speed relative to the center will not exceed  $\frac{2\lambda_{max}(P)}{\lambda_{min}(Q)}(M-1)b$ .

*Remark 2.* The above result is an asymptotic result, i.e.,  $x_i(t) \rightarrow B(\bar{x})$  as  $t \rightarrow \infty$ . However, from stability theory we can show that the swarm of any size a little larger than  $\frac{2\lambda_{max}(P)}{\lambda_{min}(Q)}(M-1)b$  will be formed in a finite time.

From (9),(10) and  $g_r(\|y\|) \|y\| \leq b$ , we have

$$\dot{V}_i \leq -\frac{\lambda_{min}(Q)}{\lambda_{max}(P)}V_i + 2\frac{1}{\sqrt{\lambda_{min}(P)}}\sqrt{V_i}\lambda_{max}(P)(M-1)b \tag{12}$$

Set  $\beta = \frac{\lambda_{min}(Q)}{2\lambda_{max}(P)}$ . From (12) we have

$$\begin{aligned} \dot{V}_i &\leq -2\beta V_i + 2\frac{1}{\sqrt{\lambda_{min}(P)}}\sqrt{V_i}\lambda_{max}(P)(M-1)b \\ &= -\beta V_i - \left[ \sqrt{\beta V_i} - \frac{\lambda_{max}(P)(M-1)b}{\sqrt{\lambda_{min}(P)\beta}} \right]^2 + \frac{[\lambda_{max}(P)(M-1)b]^2}{\lambda_{min}(P)\beta} \\ &\leq -\beta V_i + \frac{[\lambda_{max}(P)(M-1)b]^2}{\lambda_{min}(P)\beta} \end{aligned} \tag{13}$$

Then we obtain

$$V_i \leq V_i(0)e^{-\beta t} + \frac{[\lambda_{max}(P)(M-1)b]^2}{\lambda_{min}(P)\beta^2}(1 - e^{-\beta t}) \tag{14}$$

where  $V_i(0)$  is the value when the time  $t = 0$ , the above function implies that the swarm will congregate with a convergence exponent no less than  $\beta$ .

*Remark 3.* The right hand of Equation (14) will tend to  $\frac{[\lambda_{max}(P)(M-1)b]^2}{\lambda_{min}(P)\beta^2}$  as  $t$  tends to infinity, then  $V_i \leq \frac{[\lambda_{max}(P)(M-1)b]^2}{\lambda_{min}(P)\beta^2}$ . From (9)  $\|\epsilon_i\| \leq \frac{1}{\sqrt{\lambda_{min}(P)}}\sqrt{V_i} \leq \frac{\lambda_{max}(P)(M-1)b}{\lambda_{min}(P)\beta} = \frac{\lambda_{max}(P)}{\lambda_{min}(P)} \frac{2\lambda_{max}(P)(M-1)b}{\lambda_{min}(Q)}$ , the bound is  $\frac{\lambda_{max}(P)}{\lambda_{min}(P)}$  times bigger than the primary bound, the reason consists in Equation (12) which magnifies relative to Equation (11). Comparatively, the former bound is better than the latter, but from the latter we can get the boundary about the convergent rate of swarm.

### 4 Stability Analysis of a Cohesive Swarm

Section 3 shows the swarm members described with model (3) will converge into a bounded region. It does not mention anything about how the swarm members move. This issue is investigated in this section. We first define the state  $x = col(x_1, x_2, \dots, x_M)$  as the vector of the swarm members' positions and the state  $v = col(v_1, v_2, \dots, v_M)$  as the vector of their velocities. We will prove that  $v(t) \rightarrow 0$  as  $t \rightarrow \infty$  in the next theorem for swarm model (3), which means that the swarm will converge to a constant configuration. Moreover, we conclude that the configuration to which the swarm members converge move at the velocity of  $v_d$  for model (1).

**Theorem 3.** Consider the swarm described by model (3) with an attraction/repulsion function  $g(\cdot) (\in \mathcal{G}(\cdot))$  given in (6). As  $t \rightarrow \infty$ ,  $v(t) \rightarrow 0$ .

*Proof.* Choose the (generalized) Lyapunov function  $J : \mathcal{R}^{nM} \times \mathcal{R}^{nM} \rightarrow \mathcal{R}$  defined as

$$J(x, v) = \sum_{i=1}^{M-1} \sum_{j=i+1}^M [J_a(\|x_i - x_j\|) - J_r(\|x_i - x_j\|)] + \frac{1}{2} v_i^T v_i$$

Calculating the gradient of  $J(x, v)$  with respect of  $x_i$  yields

$$\begin{aligned} \nabla_{x_i} J(x, v) &= \sum_{j=1, j \neq i}^M [\nabla_{x_i} J_a(\|x_i - x_j\|) - \nabla_{x_i} J_r(\|x_i - x_j\|)] \\ &= \sum_{j=1, j \neq i}^M [(x_i - x_j)g_a(\|x_i - x_j\|) - (x_i - x_j)g_r(\|x_i - x_j\|)] \\ &= -\dot{v}_i - kv_i \end{aligned} \tag{15}$$

Now, taking the time derivative of the Lyapunov function along the motion of the system we obtain

$$\begin{aligned} \dot{J}(x, v) &= [\nabla_x J(x, v)]^T \dot{x} + \sum_{i=1}^M \dot{v}_i^T v_i = \sum_{i=1}^M [\nabla_{x_i} J(x, v)]^T \dot{x}_i + \sum_{i=1}^M \dot{v}_i^T v_i \\ &= \sum_{i=1}^M (-\dot{v}_i - kv_i)^T v_i + \sum_{i=1}^M \dot{v}_i^T v_i = -k \sum_{i=1}^M \|v_i\|^2 \leq 0 \end{aligned} \tag{16}$$



for all  $t \geq 0$ . From theorem 2, the swarm members move in a bounded region. Then, using the LaSalle’s Invariance Principle we conclude that as  $t \rightarrow \infty$ , the swarm will converge to the largest invariant subset of the set defined as

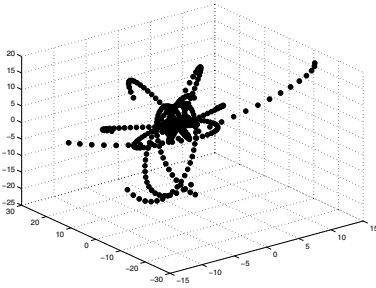
$$\Omega = \{(x, v) : \dot{J}(x, v) = 0\} = \{(x, v) : \dot{v} = 0\}$$

which implies that as  $t \rightarrow \infty$ ,  $v(t) \rightarrow 0$ . ■

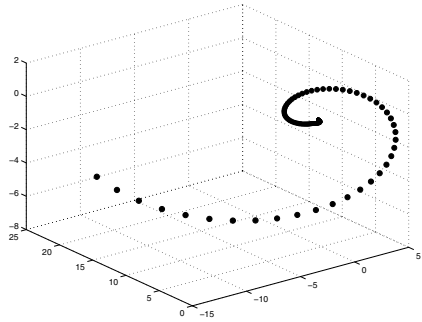
Note that  $v(t) \rightarrow 0$  implies  $x(t) \rightarrow C$ (a constant), meanwhile it implies the distance between any two individuals is fixed, i.e., the configuration of the swarm is fixed. Relative to model (1), the results above provides us information that the swarm with a fixed configuration runs with a constant velocity  $v_d$  as  $v(t) \rightarrow 0$ .

### 5 Simulation Examples

In this section we will provide some simulation examples in order to illustrate the results of this paper. We choose  $n = 3$  for the simulation for easy visualization. However, note that the results hold for any  $n$ . The swarm model considered in this section is model (3), and the attraction/repulsion function  $g(\cdot) (\in \mathcal{G}(\cdot))$  is given in (6) with the parameters  $a = b = 0.2$ .



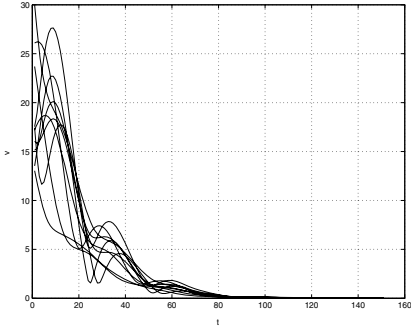
**Fig. 1.** The paths of swarm members



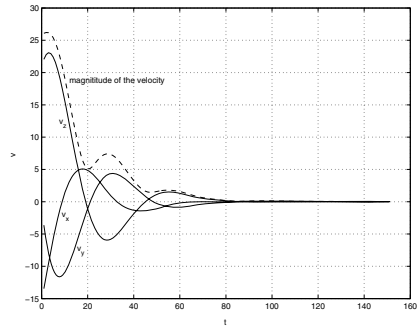
**Fig. 2.** The path of a member

The plot in Fig. 1 shows the behavior of  $M = 10$  swarm members with initial positions and velocities brought at random. As one can see, the individuals form a cohesive cluster as predicted by the theory. The center of the swarm will be fixed, in fact, it will run with a constant velocity  $v_d$  in model (1). One member’s path is depicted in Fig. 2. As the figure depicts, the member’s path is gyroidal, which accords with practicality, all the swarm’s members can not aggregate in a direct way since every member has its initial velocity, besides, the direction of its velocity is stochastic.

As to the velocity, see Fig. 3 and Fig. 4. Here all the figures are simulated with the model (3), so the velocity will tend to zero. Of course the velocity will tend to  $v_d$  if we use the model (1).



**Fig. 3.** The speed of swarm members



**Fig. 4.** The speed of a member,  $v_x, v_y, v_z$  are the components of the velocity

## 6 Conclusion

In this paper we consider a double integrator model of aggregating for multi-agent system, using Lyapunov function to analyze swarms' stability. Actually, the swarm model discussed here can be viewed as performing distributed optimization using a distributed gradient method. The attraction/repulsion functions considered here are not limited to only the swarm model, they can be used to describe anisotropic swarms with reciprocal and nonreciprocal interactions [10] (one integrator model), or swarms moving in a noisy environment [15]. We get our inspiration from biology, otherwise, aggregating has important relations to control and automation. we believe that our work is helpful to the multi-agent coordination and control literature.

Our model is a kinematic model, it is fit for individuals which move basing on the Newton's law in an environment. In our model the initial positions and initial velocities are known, and all the individuals know the exact relative positions of all the other individuals, it is a model's advantage. In biological swarms, the ranges of individuals' senses are limited, i.e., each individual usually can see (or sense) only the individuals in its neighborhood. Therefore, the final behavior of the swarms described by our model may not be in harmony with real biological swarms very well. Nevertheless, the analysis about the swarm's behavior is a first step toward developing the stability theory for aggregating of swarms. Moreover, in engineering applications the sensing limitations of the agents can be overcome with technologies such as global positioning system (GPS).

By observing the model, we know that the model is global basing on the definition of the attraction/repulsion function over the entire domain, and holds for any dimension  $n$ . In the future, we can extend the work to the local information problem, communication or sensing delay problem, time varying attraction/repulsion problem and so on.

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# Interest Based Negotiation Automation

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**Abstract.** The negotiation in general sense, as one of the most fundamental and powerful interaction of human beings, represents the dynamic process of exchanging information and perspectives towards mutual understanding and agreements. Interest based negotiation allows negotiators to discuss the concerns behind the negotiation issues so that a mutually acceptable win-win solution is more likely to be reached. This paper, for the first time, proposes a computational model for interest based negotiation automation which enables the automation of the fundamental elements of negotiation. Based on the model, algorithms are designated to automate the fundamental elements with practical computational complexity. This model provides not only a theoretical foundation for software agent based negotiation automation, but also a practical approach.

## 1 Interest Based Negotiation

Negotiation, as one of the most fundamental and powerful interaction, represents comprehensive human interactive activities, varying from simple information interchanges, to cooperation and coordination, in wide areas including education, business process, entertainment and other social activities. Similar as Information Systems which free people from the repeated or routine works, negotiation automation is able to free people from tedious interactions including both trivial actions, e.g. selection of a new laptop computer for purchase, and complex tasks, e.g. supply chain management, learning path selection and composition of interactive movies.

The traditional negotiation is Position Based Negotiation (PBN). In a PBN, the involved parties are firmly committed to their bargaining positions. They exchange proposals and counter proposals in the anticipation that one or more parties will compromise to achieve a settlement of the dispute. It is also known as win-lose negotiation. A position of a negotiation party tells others what he/she wants, and reflects his/her

point of view on a certain issue. It does not tell others about the complex decision making process that lead to the position; nor does it provide others the opportunity to take his/her interests into account. In position based negotiation, the involved parties argue only their positions. Their underlying interests may never be explicitly mentioned. If no agreement on the positions, the negotiation fails.

Interest Based Negotiation (IBN) <sup>[1]</sup> is a process that seeks to discover and satisfy the underlying interests of parties rather than to meet the stated positions or demands that they bring to negotiation. It is also known as win-win negotiation. Interests of a negotiation party tell others why he/she wants something. They reflect his/her underlying concern, needs or desire behind an issue. In interest based negotiation, the interests of participants are identified and explored, which helps them to understand the others' perspectives instead of simply reacting to the positions. By discussing the reasons behind the positions, mutually acceptable agreement is more likely to be reached. Interest based negotiation is therefore not only a much more powerful tool for conflict resolution, but also a good tool for coordination and cooperation.

For example, both party A and party B want to buy a same land. The position of each party is to have the land. There is no settlement in PBN unless one party gives in. Though, the underlying reason for having the land could be that, party A, as an international company, wants to have a local office in that location, and party B, as a real estate developer, wants to generate income by building something on the land for sale. Using IBN, the agreement could be that, B builds an office block and sells to A.

Software (intelligent) agent, as a new type of autonomous components for construction of open, complex and dynamic systems, is one of the most suitable software entities to carry out negotiation automation. In fact, software agent based negotiation automation has gained increasing prominence. On the other hand, agent community also takes negotiation as a core part of agent interactions. Some negotiation definitions are even presented in software agent context. For example, Jennings et al.<sup>[2]</sup> defined negotiation as the process by which a group of agents try to come to a mutually acceptable agreement on some matter. Negotiation underpins attempts to cooperate and coordinate and is required both when the agents are self interested and when they are cooperative. However, these pioneer work limits at introducing negotiation into computer science or software agent literature. They remain at a high level of abstraction, which lack of theoretical foundation for turning this opportunity into reality.

The research of negotiation automation in software agent community can be categorized into three main approaches: game theoretic approach <sup>[3][4]</sup>, heuristic approach <sup>[5][6]</sup> and argumentation-based approach <sup>[7][8]</sup>. The game theoretic approach models a negotiation situation as a game, and attempts to find dominant strategies for each participant by applying game theory techniques. The heuristic-based approach models agents' decision making heuristically during the course of the negotiation. In both of the approaches, negotiators are not allowed to exchange additional information other than the proposal. This is a restriction on supporting general negotiations especially when the participants have limited information about the environment, or when their decisions depend on those of the others.

The Argumentation-Based approach allows agents to exchange additional information such as justifications, critiques, and other forms of persuasive information within the interactions. It enables agents to gain a wider understanding of their counterparts,

thereby make it easier to resolve certain conflicts, for an instance, conflicts due to incomplete knowledge. This approach has been advocated as a promising means of resolving conflicts within agent societies. For example, Rahwan et al <sup>[9]</sup> tried to equip intelligent agents with the ability to conduct interest based negotiation using argumentation based approach. They studied the relationships between agent's goals and the types of arguments that may influence other agents' decision, as well as defined a set of locutions that can be used in the negotiation procedure.

Overall, the existing literature in argumentation based negotiation automation remains at a high level discussion. Theoretical foundation has not yet been reported towards the realization of negotiation automation. For example, there is no research to automatically generate the arguments for the process of interest based negotiation. This paper proposes a general computational model for negotiation automation, based on which, algorithms are proposed to automate the process. The rest of the paper is organized as follows. Section 2 proposes the general computational model for interest based negotiation automation. Section 3 are the algorithms to automate the negotiation. Section 4 illustrates the approach with a case study and Section 5 concludes the paper.

## 2 Computational Model of Interest Based Negotiation

The Computational Model of Interest Based Negotiation (CMIBN) proposed in this section is a generic conceptual model representing the core parts of negotiation in a form that can be feasibly realized by computing techniques. It includes belief base, plan base, reasoning engine and negotiation engine. The CMIBN is defined as

$$\text{CMIBN} = \langle B_b, P_b, R_e, N_e \rangle,$$

$$N_e = \langle \text{PJG}, \text{CD}, \text{R}, \text{A} \rangle,$$

where  $B_b$  is the belief base,  $P_b$  is the plan base,  $R_e$  is the reasoning engine and  $N_e$  is the negotiation engine.

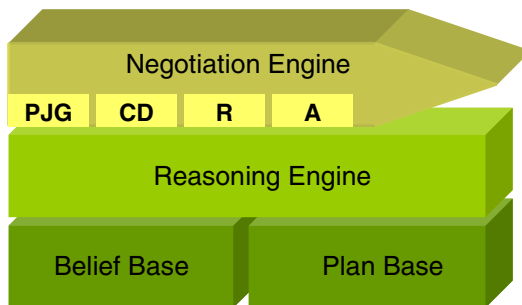


Fig. 2.1. Computational model of interest based negotiation

In the CMIBN, each party negotiates according to the reasoning over his/her belief and plan. Fig. 2.1 illustrates the architecture of the CMIBN, followed by details.

*Belief base* is the knowledge base of the negotiator. It can be defined by a set of rules.

*Plan Base* keeps the knowledge about how to achieve each position. In the Plan Base, each plan is defined by a set of organized actions to be performed towards a position. Plan base and the corresponding negotiation will be covered by a separate paper.

*Reasoning Engine*, based on the needs of the negotiation and the Belief Base, generates negotiation positions and makes selections among different positions to pursue.

*Negotiation Engine*, with the support of the Reasoning Engine, manages the negotiation process and generates the negotiation related arguments automatically. It has four components, namely, PJG – Proposal and Justification Generation; CD- Conflict Discovery; R – Recommendation; A – Adjustment.

- <1> PJG, *proposal and justification generation*: To make proposal and provide justifications (reasons) for the proposal.
- <2> CD, *conflict discovery*: To find the conflicts between the participants. By questioning the justifications behind the proposal (such as giving proof of incorrect information used), one party can persuade the other party to change the decision.
- <3> R, *recommendation*: To recommend alternative solutions and provide justifications for a new solution. If the alternative option is more attractive to the counterparties, the counterparties may change the original decision.
- <4> A, *adjustment*: To revise its knowledge base to incorporate new information obtained from the counterparties during the negotiation process. The negotiation process is also the process for the participants to gain more complete information about the environment.

For example, the PJG of a personal agent (A1) can make a proposal “Book a next Monday ticket of Air China from Melbourne to Shanghai” to a travel agency’s agent (A2), with the justification “I would travel to Shanghai on Monday. Air China has directly flight from Melbourne to Shanghai”. The CD of A2, for an instance, provides information that “Air China does not have direct flight from Melbourne to Shanghai on next Monday”. This can persuade A1 to change proposal. Alternatively, component R of A2, for an instance, makes recommendation “Book a ticket of Qantas Airline from Melbourne to Shanghai on next Monday” with the justification “Qantas Airline flies from Melbourne to Shanghai on Monday”. In the negotiation process, A1 acquires new information that Qantas Airline flies from Melbourne to Shanghai on Monday while Air China does not. The component A of A1 may adjust its belief base accordingly.

### 3 Interest Based Negotiation Automation

Interest based negotiation is to solve conflicts by discussing the underlying reasons behind the positions and seek alternative solutions. The conflicts may be due to some conflicting belief or contention on the resources while perusing the position. It can be therefore categorized into two types of negotiation: belief negotiation and plan negotiation, to address the different types of conflicts. For example, the father of a kid believes that the happiness of his child relies on the success of his career, which leads to a high requirement on the kid’s school performance. The mother of the kid how-

ever, believes that the happiness of her child comes from the freely growth with little pressure. This is a belief conflict. On the other hand, if there is no belief conflict. Both of the father and mother believe that they should spend a good amount of time with their kid. They can still have conflicts for example how to arrange their time. This becomes a plan conflict. This paper focuses on the belief negotiation and leaves plan negotiation to another report.

The belief conflicts are normally due to the incomplete or incorrect knowledge of the environment. Through argumentation, negotiation parties may form a more complete and accurate understanding of the environment. Agreement between negotiators could be possibly reached through the decision making on the new belief.

To automate interest based negotiation, a key issue is to automate the arguments generation for the basic components of the negotiation engine, namely, proposal generation, conflict discovery, recommendation and adjustment.

The rest of the paper considers belief base as a set of rules in propositional logic. Namely, given a language  $L$  of propositional logic with finite variable set  $U$ , a belief base is a finite set of propositional formulas in  $L$ . Every  $u \in U$  is an atom, and any atom or negated atom is a literal. We use “ $\sim$ ” to denote negation. We consider the case that all formulas are disjunction of two literals, i.e. in the form of  $x \vee y$  (or  $\sim x \rightarrow y$ ), where  $x, y$  are literals (If a formula is a fact  $x$ , it can be represented in the form of  $x \vee x$  for consistency). Usually the belief of negotiators can be represented as the “IF ... THEN ...” format. For example, a young man believes that to become a software engineer, he needs to have a software engineering degree, hence he should enter a university. His belief can be modeled as: become a software engineer  $\rightarrow$  have a software engineering degree, have a software engineering degree  $\rightarrow$  enter a university.

### 3.1 Conflict Discovery

In the interest based negotiation process, if the participants have conflicts in their positions, they may exchange the justifications (set of rules used in the reasoning process) leading to the position. One party may start the conflict discovery process, trying to break the logic flow in other parties’ justifications. Obviously, a computational model of conflict discovery is fundamental to automate interest based negotiation.

Identifying the apparent conflict, e.g. party A believes “Pre-school children can study math” while party B believes “pre-school children cannot study math”, is easy. However, it is not easy to discover the implied conflicts caused by steps of deduction over a large amount of rules among the negotiation parties. This sub-section presents the Conflict Discovery Algorithm, as a fundamental enabling component, to discover conflicts of two parties automatically.

The Conflict Discovery Algorithm of a negotiation party takes one rule from the opposing party’s justification, generates a *proof* (knowledge subset) of the negation of that rule automatically. If such a proof exists, the arguments of proof can be passed to the counterpart as a challenge to its justification.



**Definition 3.1. Graph Representation of a Formula Set:** For a formula set  $S=\{x_1\vee y_1, x_2\vee y_2, \dots, x_n\vee y_n\}$ , let  $U=\{ u_1, u_2, \dots, u_m\}$  be the atom set of  $S$ . A graph  $G=(V, E)$  is defined as the graph representation of  $S$ , where

$$V=\{ u_i, \sim u_i \mid 1\leq i\leq m\},$$

$$E=\{(\sim x_i, y_i), (\sim y_i, x_i) \mid x_i \vee y_i \in S, 1\leq i\leq n\}.$$

**Algorithm 3.1. Conflict Discovery Algorithm (CDA)**

Input: Formula  $p=x_0\vee y_0$  // a rule from the opposing party  
 Formula set  $S=\{ x_1\vee y_1, x_2\vee y_2, \dots, x_n\vee y_n\}$   
 // belief base of the negotiator, or the subset of the belief base relevant to  $p$ .  
 Let  $U=\{ u_1, u_2, \dots, u_m\}$  be the atom set of  $S\cup\{p\}$

Output: If there is formula subset  $S'\subset S$  such that  $S' \Rightarrow \sim p$ , output  $S'$ .  
 Otherwise output “no proof”.

- (1) Construct a graph  $G=(V, E)$  corresponding to  $S\cup\{p\}$ , where,  
 $V=\{ u_i, \sim u_i \mid 1\leq i\leq m\}$   
 $E=\{(\sim x_i, y_i), (\sim y_i, x_i) \mid x_i \vee y_i \in S\cup\{p\}, 0\leq i\leq n\}$
- (2) If there is no  $u_i \in U$  such that there are directed paths from  $u_i$  to  $\sim u_i$  and from  $\sim u_i$  to  $u_i$  (directed closed walks containing  $u_i$  and  $\sim u_i$ ), return “no proof”.
- (3) Let  $E'$  be the directed closed walk containing  $u_i$  and  $\sim u_i$  found in (2)  
 Let  $S'=\{(x \vee y) \mid (\sim x, y) \in E'\} - \{x_0\vee y_0\}$ , return  $S'$  // the proof for  $\sim p$

**Computational Complexity Analysis of Conflict Discovery Algorithm**

In the CDA algorithm, step (1) has complexity of  $O(m+n)$ . In step (2), the directed path from one vertex to another can be found using DFS algorithm in time  $O(m+n)$ . At most  $m$  atoms in  $U$  are tested, which gives the complexity of  $O(m(m+n))$ . Step (3) has complexity of  $O(n)$ . So the algorithm can be implemented in an order of  $O(m(m+n))$ .

**Theorem 3.1** *There are conflicts between a rule and a belief base if and only if the algorithm CDA presents a proof for the negation of the rule.*

**Proof**

According to CDA, if the  $u_i$  exists, there are directed paths from  $u_i$  to  $\sim u_i$  and vice versa, each of these directed closed walks provides evidence that  $S\cup\{p\}$  is unsatisfiable<sup>[10]</sup>, which is a resolution refutation for  $S\cup\{p\}$ <sup>[11]</sup>. If  $S$  is consistent and there is a resolution refutation for  $S\cup\{p\}$ ,  $S \Rightarrow \sim p$ <sup>[12]</sup>. In other words,  $S' \Rightarrow \sim p$ ,  $S'$  is the proof for  $\sim p$ . If there is no such  $u_i$  exists,  $S\cup\{p\}$  is consistent<sup>[10]</sup> and no proof for  $\sim p$ . ■

**3.2 Recommendation**

The belief bases regulate the behavior of the involved parties in an automated negotiation process. Based on the belief base, each party makes proposals to others. If they cannot reach an agreement, one party may try to persuade the other parties to change their minds by recommending alternative solutions. If the alternative solution is more attractive, the opposing party may change the original position. This process is a fundamental component of interest based negotiation: recommendation. The following result is to enable the automation of recommendation.

**Definition 3.2.1. Transitive Closure:** Let  $G$  be a directed graph with  $n$  vertices. The transitive closure of the adjacency matrix of  $G$  is an  $n \times n$  matrix  $A$ , where

$$A[i, j] = \begin{cases} 1, & i = j \text{ or there exists a directed path from vertex } i \text{ to } j \\ 0, & \text{otherwise} \end{cases}$$

**Definition 3.2.2. Matrix Representation of a Formula Set:** Suppose  $G$  is the graph representation of a formula set  $S$ ,  $A$  is the transitive closure of the adjacency matrix of graph  $G$ .  $A$  is called the Matrix Representation of  $S$ .

The computational model of recommendation automation proposed in this paper is called Belief Base Matrix (BBM). The idea behind BBM is as follows. If  $A[i, j] = 1$ , there exists a path from  $i$  to  $j$ . That is,  $j$  can be derived from  $i$  by applying the formulas following the order they appear in the path. So the matrix representation can be used as a model for the reasoning process of recommendation. It can be stored and reused until the belief base is revised.

In the follows, the Belief Base Matrix Algorithm is to compute the matrix representation of a belief base. The recommendation automation is then modeled by the Recommendation Algorithm. Given one interest from the other party, the algorithm will automatically generate the recommendation and the justification based on its knowledge (the belief base matrix).

### Algorithm 3.2.1. Belief Base Matrix Algorithm (BBMA)

Input: Formula set  $S = \{x_1 \vee y_1, x_2 \vee y_2, \dots, x_n \vee y_n\}$  //  $S$  is consistent

Let  $U = \{u_1, u_2, \dots, u_m\}$  be the atom set of  $S$

Output: The matrix representation of  $S$ .

- (1) Construct a graph  $G = (V, E)$  corresponding to  $S$ , where,
  - $V = \{u_i, \sim u_i \mid 1 \leq i \leq m\}$  also noted as  $V = \{v_1, v_2, \dots, v_{2m}\}$
  - $E = \{(\sim x_i, y_i), (\sim y_i, x_i) \mid x_i \vee y_i \in S, 1 \leq i \leq n\}$
- (2) // Construct the transitive closure of the adjacency matrix of graph  $G$ .
  - For each  $v_i, v_j \in V$  do
    - If  $(v_i, v_j) \in E$  or  $v_i = v_j$  then  $A_0[v_i, v_j] = 1$
    - Else  $A_0[v_i, v_j] = 0$
  - End For
  - For  $k \leftarrow 1$  to  $2m$  do
    - For each  $v_i, v_j \in V$  do
      - $A_k[v_i, v_j] = A_{k-1}[v_i, v_j] + A_{k-1}[v_i, v_k] \cdot A_{k-1}[v_k, v_j]$
      - // “ $\cdot$ ” and “ $+$ ” are logic multiplication and logic addition
    - End For
  - End For
  - Return  $A_{2m}$  //  $A_{2m}$  is the matrix representation of  $S$ .

### Computational Complexity Analysis of BBMA

In the algorithm BBMA, step (1) can be finished in  $O(m+n)$  time and the complexity order of step (2) is  $O(m^3)$ . So the complexity of the algorithm is  $O(m^3+n)$ .

**Algorithm 3.2.2. Recommendation Algorithm (RA)**

Input: Literal  $v$  // *interest of the opposing party*  
 Formula set  $S = \{x_1 \vee y_1, x_2 \vee y_2, \dots, x_n \vee y_n\}$  // *belief base, consistent*  
 Let  $U = \{u_1, u_2, \dots, u_m\}$  be the atom set of  $S$   
 Matrix  $A$  // *matrix representation of  $S$*   
 Graph  $G$  // *graph representation of  $S$*

Output: Recommendation  $v_r$ , formula set  $S' \subset S$  if  $S' \cup \{v\} \Rightarrow v_r$  and  $v_r$  is preferable for itself. Otherwise output “no recommendation”.

- (1) If  $v \notin U$  and  $\sim v \notin U$  Then return “no recommendation”.  
 // *no relevant information about  $v$  according to its knowledge*
- (2) Let  $R = \{v' \mid A[v, v'] = 1, v' \neq v\}$   
 If  $R = \{\}$  then return “no recommendation”.
- (3) Select  $v_r \in R$  as recommendation  
 //  *$R$  is the set of results can be derived from  $v$ , i.e. the set of recommendation*  
 // *the designation of selection strategy is not a focus of this paper*  
 Find a path  $E'$  from  $v$  to  $v_r$  in  $G$   
 Let  $J = \{(\sim v_i \vee v_j) \mid (v_i, v_j) \in E'\}$ , //  *$J$  is the justification of  $v_r$*   
 Return “recommendation:” +  $v_r$  + “, its justification:” +  $J$

**Computational Complexity Analysis of RA**

In the algorithm, step (1) and step (2) can be finished in  $O(m)$  time. In step (3) the path can be found using DFS algorithm in  $O(m+n)$  time,  $J$  can be constructed in  $O(n)$  time, thus step (3) can be finished in  $O(m+n)$  time. So the complexity of the algorithm is  $O(m+n)$ .

**3.3 Proposal and Justification Generation**

As proposal generation is a similar process as recommendation, it is omitted in this paper.

**3.4 Adjustment**

Upon receiving the new knowledge from other parties (for example, new knowledge comes from the proof of a conflict, or the justification of a recommendation), a negotiator will exam the new knowledge and adjust its belief, i.e revise its belief base to incorporate the new knowledge. From the adjusted belief base, he/she may make new decision (new positions).

To revise the belief base, the negotiator needs to add new knowledge, remove or modify the old knowledge in the belief base, and keep the consistency at the same time. The relationship among knowledge could be very complicated, which makes the detecting and eliminating inconsistency difficult. Similar to conflict discovery, all the apparent and *implied* inconsistency are to be addressed. In general, revising a knowledge base to incorporate new knowledge is not tractable<sup>[13]</sup>.

Most of the time, different rules in a knowledge base are of different importance. For instance, if the new formula is more certain than others, the least certain

inconsistent knowledge can be dropped. Alternatively, formulas may also be ordered according to their arrival time in the knowledge base. Then the oldest inconsistent knowledge might be rejected in order to restore consistency.

Based on prioritized knowledge base, it is possible to automate the adjustment process with polynomial complexity algorithms<sup>[14]</sup>. The detailed result will be reported separately.

## 4 Case Study

Suppose X is a company in the manufacturing industry. It has strong intention to improve its competency in the global market. X believes that developing new products and increasing productivity are the steps to improve competency. To increase productivity, X believes it needs to extend working hours, thus needs to update product line hardware. The belief base of company X can be represented as:

$$B_b^{(X)} = \{ a_1, a_1 \rightarrow a_2, a_1 \rightarrow a_3, a_3 \rightarrow a_4, a_4 \rightarrow a_5, a_6 \rightarrow a_7 \}, \text{ where}$$

$a_1$ : improve competency  
 $a_2$ : develop new products  
 $a_3$ : increase productivity  
 $a_4$ : extend working hours  
 $a_5$ : update product line hardware  
 $a_6$ : improve efficiency  
 $a_7$ : update product line software

The belief base can also be represented as

$$B_b^{(X)} = \{ a_1 \vee a_1, \sim a_1 \vee a_2, \sim a_1 \vee a_3, \sim a_3 \vee a_4, \sim a_4 \vee a_5, \sim a_6 \vee a_7 \},$$

which is a rule set where negotiation automation algorithms proposed in Section 3 apply.

Suppose Y is a computer company specialized in manufacturing software. Y believes that encouraging organizational learning through knowledge management systems is an excellent way to improve the competency of an organisation. It is currently promoting its knowledge management products. The belief base of Y can be represented as:

$$B_b^{(Y)} = \{ a_1, a_1 \rightarrow a_2, a_1 \rightarrow a_3, a_1 \rightarrow a_8, a_8 \rightarrow a_9, a_3 \rightarrow a_6, a_4 \rightarrow \sim a_6 \}.$$

Or

$$B_b^{(Y)} = \{ a_1 \vee a_1, \sim a_1 \vee a_2, \sim a_1 \vee a_3, \sim a_1 \vee a_8, \sim a_8 \vee a_9, \sim a_3 \vee a_6, \sim a_4 \vee \sim a_6 \},$$

where

$a_8$ : encourage organizational learning  
 $a_9$ : adopt knowledge management systems

### 4.1 Making Proposal

X wants to improve the competency, based on its belief  $\{ a_1, a_1 \rightarrow a_3, a_3 \rightarrow a_4, a_4 \rightarrow a_5 \}$ , it makes a proposal  $a_5$ , that is to buy new product line hardware. Proposal generation is similar to recommendation generation, the detailed procedure is omitted here.

### 4.2 Conflict Discovery

Company Y does not have the product line hardware X wants. No agreement can be reached upon this position. After knowing the reason behind X’s position, Y can generate recommendation to X, or provide proof to challenge X’s justification. The automation of generating a proof to challenge  $a_3 \rightarrow a_4$  in  $B_b^{(X)}$  is illustrated here. The recommendation will be covered in Section 4.3.

The graph representation of  $B_b^{(Y)} \cup \{a_3 \rightarrow a_4\}$  is

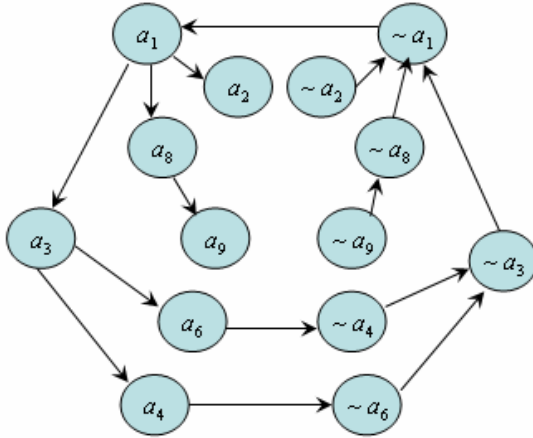


Fig. 4.2.1. Graph representation of  $B_b^{(Y)} \cup \{a_3 \rightarrow a_4\}$

There is a directed closed walk containing  $a_3$  and  $\sim a_3$ :

$$a_3 \rightarrow a_4 \rightarrow \sim a_6 \rightarrow \sim a_3 \rightarrow \sim a_1 \rightarrow a_1 \rightarrow a_3$$

The logic proof for  $\sim (a_3 \rightarrow a_4)$  is  $\{a_4 \rightarrow \sim a_6, a_3 \rightarrow a_6, a_1 \rightarrow a_3, a_1\}$ . The interpretation is that:

- increase productivity  $\rightarrow$  improve efficiency ( $a_3 \rightarrow a_6$ ),
- improve efficiency  $\rightarrow$   $\sim$  extend working hours ( $a_4 \rightarrow \sim a_6$  i.e.  $a_6 \rightarrow \sim a_4$ ),

It tells that productivity can not be increased by extending working hours. This provides a proof to challenge X’s justification  $a_3 \rightarrow a_4$  for the position to purchase product line hardware.

### 4.3 Recommendation

Algorithm BBMA automatically creates the matrix representation of Y’s belief base. The matrix is omitted here due to the restriction of length. Based on the matrix, algorithm RA finds all the results that can be derived from the interest  $a_1$  (to improve competency). Among them  $a_9$  (adopt knowledge management system) is what Y is promoting.

The path  $a_1 \rightarrow a_8 \rightarrow a_9$  tells that adopting knowledge management systems can also improve the competency, so Y recommends X to buy the knowledge management system products. If X is satisfied with the recommendation and persuaded by the justification, it will accept the recommendation. Then agreement is reached.

#### 4.4 Adjustment

X receives the new knowledge during the recommendation or conflict discovery process from Y, for example,  $a_1 \rightarrow a_8, a_8 \rightarrow a_9, a_3 \rightarrow a_6, a_4 \rightarrow \sim a_6$ . It may store them in a temporary place. If some knowledge appears repeatedly or come from a trust party, X may initiate the adjustment process. Suppose X is going to add  $\{a_3 \rightarrow a_6, a_4 \rightarrow \sim a_6\}$  to its belief base, and give them the highest priority. The challenged knowledge  $a_3 \rightarrow a_4$  is given the lowest priority. After the adjustment the belief base becomes<sup>1</sup>:

$$B_b^{(X)} = \{a_3 \rightarrow a_6, a_4 \rightarrow \sim a_6, a_1, a_1 \rightarrow a_2, a_1 \rightarrow a_3, a_4 \rightarrow a_5, a_6 \rightarrow a_7\}$$

In a later stage, if X wants to improve its competency, probably it will make a new proposal  $a_7$  (update product line software) based on the belief  $\{a_1, a_1 \rightarrow a_3, a_3 \rightarrow a_6, a_6 \rightarrow a_7\}$ .

### 5 Conclusion and Future Work

This paper proposed a computational model for interest based negotiation automation. The negotiation studied in this paper is in general sense, which includes general processes of exchanging information and perspectives towards mutual understanding and agreements. It represents wide range of activities in most areas that involves dynamic interactions, including education, organisation management, cooperation, commerce and business.

As interest based negotiation allows involved parties to dig into the reasons behind their positions, it is much more powerful and constructive than position based negotiation. It therefore has raised significant attention in various communities including researchers. However, the existing literature is largely limited at high level discussions. This paper addresses the challenge by proposing a computational model of interest based negotiation, including algorithms for the main negotiation automation elements, namely proposal generation, conflict discovery and recommendation for belief negotiation. A case study has illustrated how interest based negotiation automation can be feasibly carried out by computational entities, e.g. software agents. Due to the limitation of length, plan negotiation will be reported in a separate paper.

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<sup>1</sup> The justification automation will be covered by a separate report.

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# Phase Transition of a Skeleton Model for Surfaces

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**Abstract.** A spherical model of skeleton with junctions is investigated by Monte Carlo simulations. The model is governed by one-dimensional bending energy. The results indicate that the model undergoes a first-order transition, which separates the smooth phase from the crumpled phase. The existence of phase transition indicates that junctions play a non-trivial role in the transition.

## 1 Introduction

Surface model of Helfrich, Polyakov and Kleinert (HPK) [1,2,3] has long been investigated for a model of biological membranes [4,5,6,7,8,9]. A curvature energy called the bending energy is assumed in the Hamiltonian, which is discretized on triangulated surfaces in numerical studies [10]. It was reported that the model undergoes a first-order transition between the smooth phase and a crumpled (or wrinkled) phase [11,12,13]. Experimentally, a similar transition was recently observed in an artificial membrane [14].

The curvature energy in HPK model is a two-dimensional one, and it reflects a homogeneous structure of membranes as a two-dimensional surface. In fact, the conventional picture of biological membranes is connected to such homogeneity, and moreover many artificial membranes are known as homogeneous.

However, membrane skeleton, called the cytoskeleton in biological membranes, has been considered to play a crucial role in maintaining shape and motion. Recent experimental studies reveal that free diffusion of lipids suffers from the existence of cytoskeletons: the so-called hop-diffusion was actually observed [15]. The artificial membrane, in the above-mentioned experimental study, is considered not to be a homogeneous surface, because it is partly polymerized [14].

Therefore, it is interesting to study whether the phase transition occurs in a skeleton model, which is obviously different from the conventional surface model such as HPK model. The skeleton model is significantly simplified as a model for surfaces; it contains only skeletons and the junctions. Consequently, we consider that the simplified model enable us to focus on whether skeletons play a crucial role on the phase transition in biological and artificial membranes.

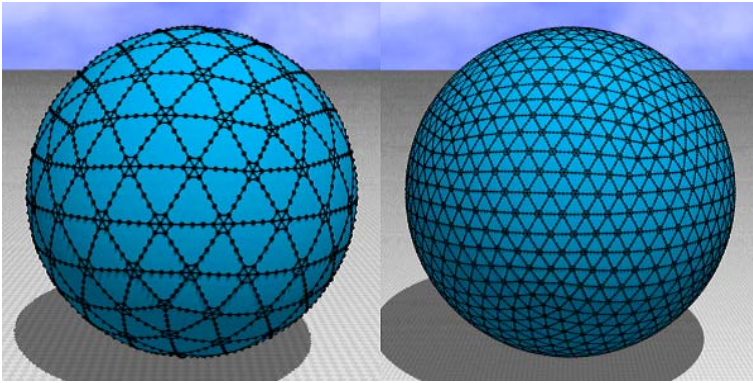
In this paper, we report numerical evidence that a phase transition occurs in a skeleton model, which is governed by one-dimensional bending energy. This result is remarkable, because no phase transition can be observed in one-dimensional object described by Hamiltonian of local interactions.



## 2 Model and Monte Carlo Technique

By dividing every edge of the icosahedron into some pieces of the uniform length, we have a triangulated surface. The compartment structure is built on the surface by eliminating the vertices inside the compartment. The boundary of the compartment forms the skeletons with junctions. We denote by  $(N, N_S, N_J, L)$  the total number of vertices (including those in the junctions and their neighboring vertices), the total number of vertices in the skeletons (excluding both vertices in the junctions and their neighboring vertices), the total number of junctions, and the number of bonds between two neighboring junctions in a compartment, respectively. Note that  $L - 1$  is the number of vertices in the skeleton between the junctions.

A starting configuration of Monte Carlo (MC) simulation is shown in Fig. 1(a), 1(b), where  $(N, N_S, N_J, L) = (2562, 1440, 162, 4)$  and  $(N, N_S, N_J, L) = (19362, 10890, 1212, 4)$ . The dots are clearly seen in (a) and unclear in (b) because the size of (b) is relatively large. The surface of the sphere is shown in the snapshot for clarity. The hexagon and the pentagon (which are clearly seen in (a)) correspond to the junctions. Total number of the pentagon is 12, and the remaining junctions are hexagonal.

(a)  $(2562, 1440, 162, 4)$ (b)  $(19362, 10890, 1212, 4)$ 

**Fig. 1.** Starting configuration of surfaces of (a)  $(N, N_S, N_J, L) = (2562, 1440, 162, 4)$  and (b)  $(N, N_S, N_J, L) = (19362, 10890, 1212, 4)$ . Thick lines denote the skeletons and the junctions, and small dots the vertices. The dots are clearly seen in (a) and unclear in (b) because the surface size is relatively large. The surface of the sphere is shown for clarity in both (a) and (b).

Henceforth, we use terminology *junction* for the hexagonal (or pentagonal) objects or for the central vertices of these objects, *skeleton* for linear object between junctions, and *surface* for junction + skeleton.

The Gaussian bond potential  $S_1$ , the one-dimensional bending energy  $S_2^{(1)}$  for skeletons, and the two-dimensional bending energy  $S_2^{(2)}$  for junctions, are given by

$$S_1 = \sum_{\langle ij \rangle} (X_i - X_j)^2, \quad S_2^{(1)} = \sum_{[ij]} (1 - \mathbf{t}_i \cdot \mathbf{t}_j), \quad S_2^{(2)} = \sum_{\langle ij \rangle} (1 - \mathbf{n}_i \cdot \mathbf{n}_j), \quad (1)$$

where  $\sum_{\langle ij \rangle}$  in  $S_1$  is the sum over bonds  $(ij)$  connecting all the vertices  $i$  and  $j$  (including those at the junctions and their neighboring vertices),  $\sum_{[ij]}$  in  $S_2^{(1)}$  is the sum over nearest neighbor bonds  $i$  and  $j$  on the skeletons between junctions,  $\sum_{\langle ij \rangle}$  in  $S_2^{(2)}$  is the sum over bonds  $\langle ij \rangle$  connecting the central point of the junction  $i$  and the nearest neighbor vertex  $j$ . The symbol  $\mathbf{t}_i$  in  $S_2^{(1)}$  is the unit tangential vector of the bond  $i$ . The symbol  $\mathbf{n}_i$  in  $S_2^{(2)}$  is the unit normal vector of the triangle  $i$ .

$S_2^{(2)}$  is defined only at the junctions. Note also that the bond  $[ij]$  in  $S_2^{(1)}$  includes the bonds connected to the central point of the junction.  $S_1$  includes bonds that connect the vertices nearest neighbor to the junctions. The reason of this is for the sake of the in-plane elasticity at the junctions. When  $S_1$  excludes such bonds, skeletons at the junctions freely move into the in-plane directions. The potential  $S_1$  describes a one-dimensional interaction between vertices in the skeletons and a two-dimensional interaction only at the junctions.

The partition function of the model is defined by

$$Z = \int' \prod_{i=1}^N dX_i \exp(-S), \quad S = S_1 + b_1 S_2^{(1)} + b_2 S_2^{(2)}, \quad (2)$$

where  $b_1$ ,  $b_2$  are the one-dimensional bending rigidity and the two-dimensional bending rigidity. In this paper,  $b_2$  is fixed to  $b_2 = 5$ , and  $b_1$  is varied in the MC simulations. The center of the surface is fixed in the MC simulations, and this is denoted by  $\prime$  in  $\int' \prod_{i=1}^N dX_i$ .

The canonical Metropolis MC technique is used to obtain the mean value of physical quantities. The vertices  $X$  of the skeleton are sequentially shifted so that  $X' = X + \delta X$ , where  $\delta X$  is randomly chosen in a small sphere. The new position  $X'$  is accepted with the probability  $\text{Min}[1, \exp(-\Delta S)]$ , where  $\Delta S = S(\text{new}) - S(\text{old})$ . The vertices of junctions (hexagons and pentagons) are shifted in two steps. Firstly 7 (or 6) vertices at one junction are shifted simultaneously at random, and the second step is a random translation and a random rotation of the hexagon (or the pentagon) as a rigid object. Those shifts are controlled by small numbers given at the beginning of the simulations to maintain about 50% acceptance rates.

Four different sizes are assumed for surfaces in the MC simulations. The surface size  $(N, N_S, N_J, L)$  are (19362, 10890, 1212, 4), (10242, 5760, 642, 4), (5762,

3240, 362, 4), and (2562, 1440, 162, 4). In the simulations, two parameters are fixed: the total number of vertices  $L$  in the skeleton between junctions and the two-dimensional bending rigidity  $b_2$  are fixed to

$$L = 5, \quad b_2 = 5. \quad (3)$$

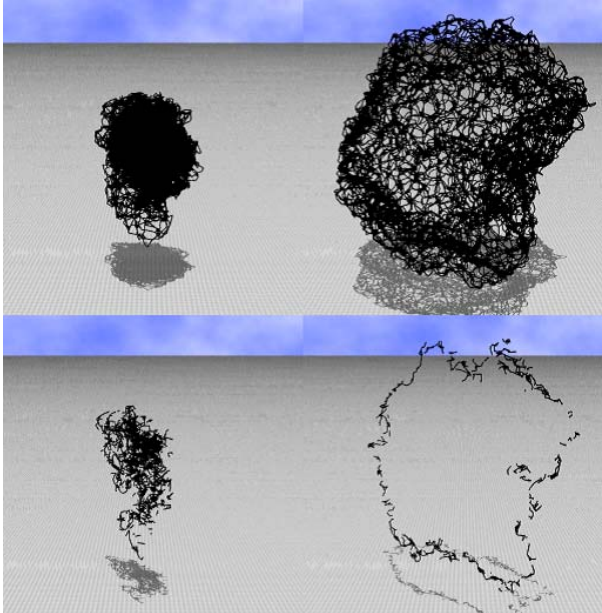
### 3 Results

First, we show snapshots of surface obtained at  $b_1 = 2.9$  (crumpled phase) and  $b_1 = 2.93$  (smooth phase) in Figs.2(a) and 2(b), respectively. The size of surface is  $(N, N_S, N_J, L) = (19362, 10890, 1212, 4)$ . The surface sections are shown in Figs.2(c),2(d). We clearly find that the surface is crumpled (smooth) at  $b_1 = 2.9$  ( $b_1 = 2.93$ ).

Figure 3(a) is plots of  $S_1/N$  against  $b_1$  obtained on the surfaces of size  $(19362, 10890, 1212, 4)$ ,  $(5762, 3240, 362, 4)$ , and  $(2562, 1440, 162, 4)$ . Because of the scale invariant property of the partition function  $Z$  in Eq.(2),  $S_1/N$  is predicted to be  $S_1/N = 3N/2(N-1) \simeq 1.5$ . We find from the figure that the predicted relation for  $S_1/N$  is satisfied. The line connecting the data was obtained by multi-histogram reweighting technique.

(a)  $b_1 = 2.9$ , crumpled

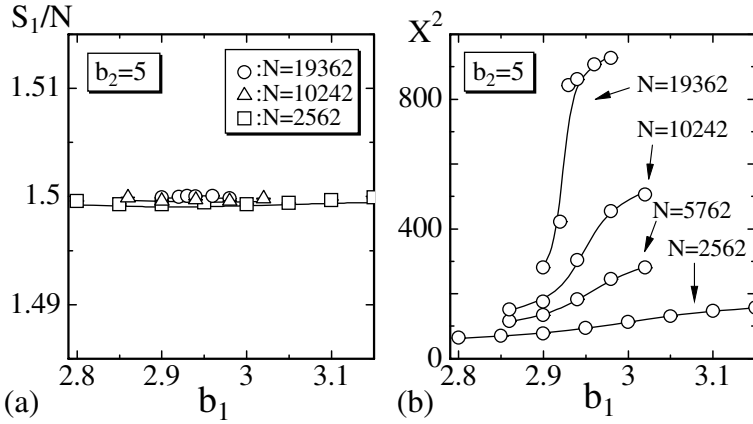
(b)  $b_1 = 2.93$ , smooth



(c) the surface section of (a)

(d) the surface section of (b)

**Fig. 2.** Snapshots of surfaces of size  $(N, N_S, N_J, L) = (19362, 10890, 1212, 4)$  obtained at (a)  $b_1 = 2.9$  (crumpled) and (b)  $b_1 = 2.93$  (smooth). (c) The surface section of (a), and (d) the surface section of (b).



**Fig. 3.** (a)  $S_1/N$  against  $b_1$ , and (b)  $X^2$  against  $b_1$ .  $b_2$  is fixed to  $b_2 = 5$ . The curves are drawn by multi-histogram reweighting technique.

Figure 3(b) is the mean square size  $X^2$  defined by

$$X^2 = \frac{1}{N} \sum_i (X_i - \bar{X})^2, \quad \bar{X} = \frac{1}{N} \sum_i X_i, \quad (4)$$

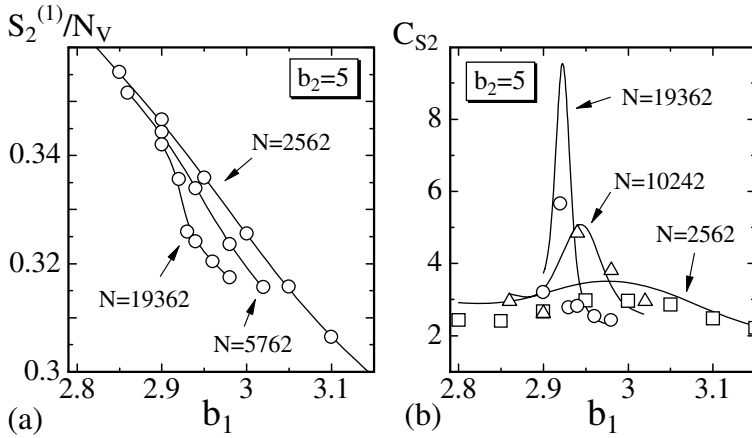
where  $\bar{X}$  is the center of the surface. The size  $X^2$  of surfaces increases with increasing  $b_1$  and varies rapidly at intermediate  $b_1$  on the surface of (19362, 10890, 1212, 4). This indicates the existence of the crumpling transition.

The bending energy  $S_2^{(1)}/N_V$  against  $b_1$  is plotted in Fig. 4(a), where  $N_V = N - N_J$  is the total number of vertices where  $S_2^{(1)}$  is defined. We find again a rapid varying of  $S_2^{(1)}/N_V$  against  $b_1$  as the surface size increases.

Figure 4(b) shows the specific heat  $C_{S_2^{(1)}}$  defined by

$$C_{S_2^{(1)}} = \frac{b^2}{N_V} \langle (S_2^{(1)} - \langle S_2^{(1)} \rangle)^2 \rangle. \quad (5)$$

The curves drawn by multi-histogram reweighting technique indicate an anomalous behavior of  $C_{S_2^{(1)}}$ . This can be considered as a sign of the phase transition. We expect that the transition is of first-order because of the sharp peak in  $C_{S_2^{(1)}}$  at the surface of  $(N, N_S, N_J, L) = (19362, 10890, 1212, 4)$ . The junctions play a nontrivial role in the phase transition, because we know that one-dimensional linear skeleton such as an elastic circle has no phase transition. The finite-size scaling analysis can be done with more extensive MC simulations including larger surfaces rather than those in this paper, and the first-order transition will be confirmed.



**Fig. 4.** (a)  $S_2^{(1)}/N_V$  against  $b_1$ , and (b)  $C_{S_2^{(1)}}$  against  $b_1$ .  $N_V = N - N_J$  is the total number of vertices where  $S_2^{(1)}$  is defined.  $b_2$  is fixed to  $b_2 = 5$ . The curves are drawn by multi-histogram reweighting technique.

## 4 Summary and Conclusion

We have investigated the phase structure of a skeleton model for membranes by using Monte Carlo simulation technique. Linear skeletons are joined with junctions and form a surface, which covers a sphere. Hamiltonian is a linear combination of the Gaussian bond potential, one-dimensional bending energy  $S_2^{(1)}$ , and the two-dimensional bending energy  $S_2^{(2)}$ , which is defined only at the junctions. Four different sized surfaces were used in the simulation. The length  $L$  of skeleton between junctions was fixed to  $L = 5$  in those surfaces, and the two-dimensional bending rigidity  $b_2$  was also fixed to  $b_2 = 5$ .

We found that there are two distinct phases in the model; the smooth phase and the crumpled phase, which are characterized by small  $S_2^{(1)}$  and large  $S_2^{(1)}$ , respectively, and also by small  $X^2$  and large  $X^2$ . Moreover, these two phases are separated by a phase transition, which was predicted to be of first-order on account of the anomalous behavior of the specific heat for  $S_2^{(1)}$ .

Although we have obtained a sign of first-order transition in the skeleton model, more extensive MC simulations are necessary to confirm the result. The junctions are expected to play a non-trivial role in the phase transition, because we know that one-dimensional linear skeleton such as an elastic circle has no phase transition. Then, it is interesting to study the dependence of junction elasticity on the phase transition. A rigid junction model is also interesting. Rigid junction has an infinite in-plane and bending resistance against force, while the junction in this paper has finite elastic resistance. Phase structure of skeleton models can be clarified by further numerical studies.

## Acknowledgement

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# A Novel Approach Model for Chinese Postman Problem

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**Abstract.** Molecular programming(MP) has been proposed as an evolutionary computation algorithm at the molecular level. MP is different from other evolutionary algorithms in its representation of solutions using DNA molecular structures and its use of bio-lab techniques for recombination of partial solution. In this paper, Chinese Postman Problem(CPP) has been solved by means of molecular programming. We make use of the encoding scheme of S.Y.Shin for encoding real values. The new method is biologically plausible and has a fixed code length.

## 1 Introduction

Aldeman who showed the potential of using biomolecules for solving computational problem pioneered the field of DNA computing [1]. He solved the hamiltonian path problem using DNA molecules, and Lipton came up with a method to solve the satisfiability(SAT) problem [2]. In 1997, Q.ouyan et al presented a molecular biology based experimental solution to the maximal clique problem [3]. In 2000, liu et al designed DNA model system, a multi-based encoding strategy is used in a one word approach to surface-based DNA computation [4]. In 2001, wu analyzed and improved their surface-based method [5]. In 2005, Shi et al proposed a scheme of 3-states programmable automaton by DNA computing [6]. All their works use the tools of molecular biology and all demonstrate the feasibility of carrying out computations at the molecular level. One of the formal frameworks for molecular computations is Tom Head's splicing system, which gives a theoretical foundation for computing based on DNA recombination [7]. DNA computing represents the problem with DNA molecules and solves them by biological laboratory techniques.

DNA is a double-helix structure, the main characteristics of which are: (1) DNA molecule are convoluted by two single parallel deoxynucleotide chain; (2) the deoxyribose and phosphoric, which link to each other alternately, array in outer side; (3) the base group of two single chain can complement under the process that A complements T and C complements G, which is called base-pairing. After found the structure of DNA, many experimental methods have been invented including hybridization, annealing, amplifying, melting, separating, cutting, ligation, polymerase chain reaction(PCR), affinity column, gel electrophoresis and so on, which conduce to solving the information output and information storage. One advantage of DNA computing is

massive parallelism. Another benefit is its enormous information storage capacity. 1 $\mu$ mol DNA contains approximately 1020 molecules which allow a big problem space can be searched in almost constant time. Despite significant progress, several problems remain and need to be resolved. Firstly, for a complex issue, a large amount of DNA is need in coding, which is hard to be achieved. Secondly, DNA computing is inaccurate, which can be caused by inaccurate hybridization, the effect of secondary structure of DNA molecule, the inaccuracy of experiment and large cost for biological lab experiments, all of these affecting the result of DNA computing. These problems can be alleviated by a software tool, which simulates DNA computing in advance to optimize DNA codes and experimental conditions [8]. Molecular programming (MP) has been proposed for this purpose. MP is a tool for programming DNA computers by means of artificial evolution [9]. On the other hand, MP can be regarded as a new evolutionary computation method that represents problem in DNA double strands and uses bio-lab techniques as search operators. In 2002, Yin et al. solved the Chinese postman problem with DNA computing, but this method is based on the fact that all weights are integer [10]. In that paper, we used molecular programming to solve Chinese Postman Problem. Most of the problems solved by DNA computing are non-weighted graph, such as Hamilton path problem [1] and maximal clique problem [2]. In contrast, the Chinese Postman Problem has weight (usually real valued) associated with edges. Shine proposed a method to represent weights in DNA codes to solve travelling salesman problem [9]. This method is based on the fact that hybridization between G/C pairs occurs more frequently those those between A/T pairs. It is because there are 3 hydrogen bonds between G and C, whereas 2 hydrogen bonds between A and T. Similar to the method, we can solve Chinese Postman Problem. For terminologies and notations not defined in this paper, the readers are referred to Ref. [12], [13].

## 2 Chinese Postman Problem

All graphs considered in the paper are finite, undirected and connected graphs. Let  $G$  be a connected graph and  $e_{ij}$  a edge of  $G$ . Let  $w_{ij}$  be a weight of  $e_{ij}$ . We call a sequence constructed from vertex and edge with alternating is closed walk, if its Starting vertex is the same as finishing vertex; Call a tour is generalized Euler tour if it contains all of the edges of graph  $G$  at least once. Let  $G$  be a connected weighted graph, Chinese Postman Problem is to find a generalized Euler tour that satisfy the sum of weight of all edges is minimum and starting vertex is fixed. We designed the following algorithm to solve it:

- Step 1: Generate random closed walk through the graph.
- Step 2: Keep only those closed walk that begin with fixed vertex and end with fixed vertex (keep only all closed walk passing through the fixed vertex).
- Step 3: Keep only those closed walk that enter all of the edge of the graph at least once. (namely, keep only those generalized Euler tour).
- Step 4: Find the shortest closed walk, it will be our solution.
- Step 5: Determine postman path.



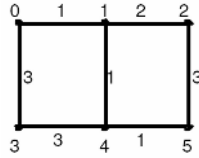
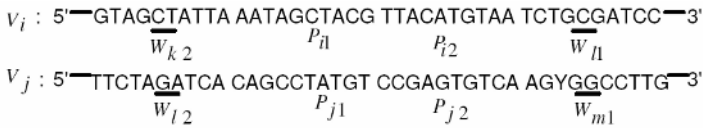


Fig. 1. Shows an instance of a graph that has 6 vertices. Let the fix vertex be 0, then the generalized Euler tour is 0-1-2-3-4-1-4-5-0 and the sum of weight is 14.

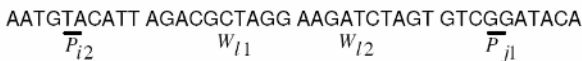
### 3 Coding Scheme on Chinese Postman Problem

Most existing DNA computing methods follow the Adleman's coding scheme to solve NP-complete problems. Here, the vertex codes are generated at random and then the edge codes, which link the vertices, are produced using the vertex codes.

Ouyang et al proposed a new coding scheme in which the edges have binary values coded in sequences. Recently, Zhang et al proposed an improved DNA algorithm to solve travelling salesman problem [9], coding scheme of the method can overcome the difficult brought by real valued weights. According to the coding scheme, we represent edge sequences in two components: link sequences and weight sequences, represent the weight of edges by varying the amount of A/T pairs and G/C pairs in weight sequences. Generally, DNA length and the G/C contents influence the ligation among DNA sequences. The longer the sequences the more often they get hybridized, thus leading to longer sequences of ligations. Similarly, the more G/C pairs the sequences have, the more probable they get hybridized. The reason is that the hybridizations between the G/C pairs are preferred to those between A/T pairs, since there are 2 hydrogen bonds formed between A and T and 3 hydrogen bonds between G and C. We encode the vertex with 4 components: 10bp weight sequence (W2), 10bp position sequence (P1), 10bp position sequence (P2), and 10bp weight sequence (W1), where the vertex position sequence for all the randomly generated.



a: Vertex Sequences



b: Edge Sequences ( $V_i \rightarrow V_j$ )

Fig. 2. The fixed length coding scheme. Vertex sequence  $V_i$ ,  $V_j$ , with their the edge sequence ( $V_i \rightarrow V_j$ ).

We also encode edge sequences with 4 components: 10-bp link sequence ( $P_{i2}$ ), 10-bp weight sequence ( $W_1$ ), 10-bp weight sequence ( $W_2$ ), and 10-bp link sequence ( $P_{j1}$ ) (see Fig.2 and Fig.3). The polarity of edge codes is the opposite (3'-5') to vertex codes. The position sequences represent a specific vertex; the weight sequence denotes a weight value in an edge. The weight sequences describe the proportion of edge weights, so the coding scheme can express the real value weights. The way to describe the edge weights is explained in the fitness function [9].

We use Fig1 detailed to illustrate the coding scheme. In step 1, the vertex position sequences  $P_{i1}$  and  $P_{i2}$  for all  $i$  is randomly generated. In step 2 and 3, the whole edge sequences are designed. For the case of  $V_i-V_j$ , We design link sequences  $P_{i2}$ ,  $P_{j1}$ , weight sequence  $W=(W_1, W_2)$  and then they are combined. In Step 4, the vertex weight sequence is designed in a similar way; vertex weight sequences are generated by the edge weight sequences, and then are combined position sequences and weight sequences. In Step 5, the amount of G/C contents in edge sequences is optimized by a genetic algorithm [9]. This is done so that the edges with smaller weights have more G/C contents and thus have higher probability of being contained in the final solution. Encode to Fig.1 is presented Table 1.

**Table 1.** Coding scheme of Fig.1

(a). Vertex sequence: weight and position sequence

1 → 0 → 1: 5'-CTAATGACTGCAACCCAAAACCTGGTAGAGATCTATGATA-3'  
 1 → 0 → 5: 5'-CTAATGACTGCAACCCAAAACCTGGTAGAGGCACGTGCAT-3'  
 5 → 0 → 1: 5'-CGACTACCGTCAACCCAAAACCTGGTAGAGATCTATGATA-3'  
 5 → 1 → 5: 5'-CGACTACCGTCAACCCAAAACCTGGTAGAGGCACGTGCAT-3'  
 0 → 1 → 2: 5'-CTAATGACTGATATCGCGGGTTCAACGTGCCACATGCGTC-3'  
 2 → 1 → 0: 5'-CGAGTACCGTATATCGCGGGTTCAACGTGCATCTATGATA-3'  
 0 → 1 → 0: 5'-CTAATGACTGATATCGCGGGTTCAACGTGCATCTATGATA-3'  
 2 → 1 → 2: 5'-CGAGTACCGTATATCGCGGGTTCAACGTGCCACATGCGTC-3'  
 0 → 1 → 4: 5'-CTAATGACTGATATCGCGGGTTCAACGTGCTATAACATGAT-3'  
 4 → 1 → 4: 5'-CTAGAACTTGATATCGCGGGTTCAACGTGCTATAACATGAT-3'  
 4 → 1 → 0: 5'-CTAGAACTTGATATCGCGGGTTCAACGTGCTCTATGATA-3'  
 4 → 1 → 2: 5'-CTAGAACTTGATATCGCGGGTTCAACGTGCCACATGCGTC-3'  
 2 → 2 → 4: 5'-CGAGTACCGATATCGCGGGTTCAACGTGCTATAACATGAT-3'  
 1 → 2 → 3: 5'-CGAGTACCGTCAGTTGACATGCAGGATCGAGCCGCGCCGCG-3'  
 1 → 2 → 1: 5'-CGAGTACCGTCAGTTGACATGCAGGATCGACACATGCGTC-3'  
 3 → 2 → 3: 5'-GGCCGCGCCGACAGTTGACATGCAGGATCGAGCCGCGCCGCG-3'  
 3 → 3 → 1: 5'-GGCCGCGCCGACAGTTGACATGCAGGATCGACACATGCGTC-3'  
 2 → 3 → 2: 5'-GGCCGCGCCGAACCTGGTACCAAGCTTGACGCGCCGCGCG-3'  
 4 → 3 → 4: 5'-GTATACTACAAACCTGGTACCAAGCTTGACGAATTCATCT-3'

2 → 3 → 4: 5'-GGCCGCGCCGAACCTGGTACCAAGCTTGACGAATTCATCT-3'  
 4 → 4 → 2: 5'-GTATACTACAAACCTGGTACCAAGCTTGACGCCGGCCGCG-3'  
 3 → 4 → 5: 5'-GTATACTACATGGTTTGGACTGGTCAAGTTGGCCCCGGCGC-3'  
 5 → 4 → 3: 5'-GGCCCGGCCGTGGTTTGGACTGGTCAAGTTGAATTCATCT-3'  
 3 → 4 → 3: 5'-GTATACTACATGGTTTGGACTGGTCAAGTTGAATTCATCT-3'  
 5 → 4 → 5: 5'-GGCCCGGCCGTGGTTTGGACTGGTCAAGTTGGCCCCGGCGC-3'  
 1 → 4 → 1: 5'-CTAGAACTTGTGGTTTGGACTGGTCAAGTTTATAACATGAT-3'  
 3 → 4 → 1: 5'-GTATACTACATGGTTTGGACTGGTCAAGTTTATAACATGAT-3'  
 1 → 4 → 3: 5'-CTAGAACTTGTGGTTTGGACTGGTCAAGTTGAATTCATCT-3'  
 1 → 4 → 5: 5'-CTAGAACTTGTGGTTTGGACTGGTCAAGTTGGCCCCGGCGC-3'  
 5 → 5 → 1: 5'-GGCCCGGCCGTGGTTTGGACTGGTCAAGTTTATAACATGAT-3'  
 0 → 5 → 0: 5'-CGTAGCTCGATATAGCGCATGCAGGATCGAGCACGTGCAT-3'  
 4 → 5 → 4: 5'-GGCCCGGCCGTATAGCGCATGCAGGATCGAGGCCCGGCGC-3'  
 4 → 5 → 0: 5'-GGCCCGGCCGTATAGCGCATGCAGGATCGAGCACGTGCAT-3'  
 0 → 5 → 4: 5'-CGTAGCTCGATATAGCGCATGCAGGATCGAGGCCCGGCGC-3'

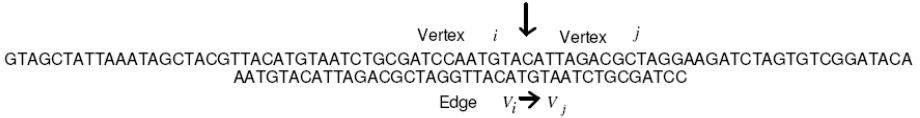
(b). Edge sequence: Link and weight sequence

0 → 1: 3'-GGACCATCTCTAGATACTATGATTACTGACTATAGCGCCC-5'  
 1 → 0: 3'-AAGTTGCACGTAGATACTATGATTACTGACGTTGGGTTTT-5'  
 1 → 2: 3'-AAGTTGCACCGTGTACGCAGGCTCATGGCAGTCAACTGTA-5'  
 2 → 1: 3'-CGTCCTAGCTGTGTACGCAGGCTCATGGCATATAGCGCCC-5'  
 2 → 3: 3'-CGTCCTAGCTCGGCCGGCGCCCGGCGCGGCTTGGACCATC-5'  
 3 → 2: 3'-GTTCGAACTGCGGCCGGCGCCCGGCGCGGCGTCAACTGTA-5'  
 3 → 4: 3'-GTTCGAACTGCTTAAGTAGACATATGATGTACCAAACCTG-5'  
 4 → 3: 3'-ACCAGTTCAACTTAAGTAGACATATGATGTTTGGACCATG-5'  
 4 → 5: 3'-ACCAGTTCAACCGGGCCGCGCCGGGCCGGCATATCGCGTA-5'  
 5 → 4: 3'-CGTCCTAGCTCCGGGCCGCGCCGGGCCGGCACCAAACCTG-5'  
 5 → 0: 3'-CGTCCTAGCTCGTGCACGTAGCATCGAGCTGTTGGGTTTT-5'  
 0 → 5: 3'-GGACCATCTCCGTGCACGTAGCATCGAGCTATATCGCGTA-5'  
 1 → 4: 3'-AAGTTGCACCATATGTACTAGATCTTGAACACCAAACCTG-5'  
 4 → 1: 3'-ACCAGTTCAAATATGTACTAGATCTTGAACATATAGCGCCC-5'

The notation  $0 \rightarrow 1 \rightarrow 2$  in Table1(a) means that vertex 1 has in-edge from vertex 0 ( $0 \rightarrow 1$ ) and out-edge to vertex 2 ( $0 \rightarrow 2$ ). Note that the edge sequences with high weights have more G/C pairs than A/T pairs. Similarly, the edge sequences with low weights have more A/T pairs than A/T pairs. The link sequences contain the same number of A/T pairs and G/C. Thus, the weight sequences control the edge weight, and the link sequences have little effect on representing weight values.

## 4 Molecular Algorithm on Chinese Postman Problem

To implement Step 1 of algorithm, for each vertex  $i$  in the graph and for each edge  $i \rightarrow j$  in the graph, 50pmol of oligonucleotide strand "i" and 50pmol of oligonucleotide strand "i  $\rightarrow$  j", respectively, were mixed together in a single ligation reaction, the oligonucleotides "i  $\rightarrow$  j" served as splints to bring oligonucleotides associated with compatible edges together for ligation (Fig.3).



**Fig. 3.** Ligation procedure

Hence the ligation reaction resulted in the formation of DNA molecules encoding random closed walk through the graph. The scale of this ligation reaction far exceeded what was necessary for the graph under consideration. For each edge in the graph, approximately  $6 \times 10^{13}$  copies of the associated oligonucleotide were added to the ligation reaction. Hence it is likely that many DNA molecules encoding the closed walk were created. In fact, the creation of a single such molecule would be sufficient. As a result, for this graph quantities of oligonucleotides less than an attomole would be sufficient. Alternatively, a much larger graph could have been processed with the picomole quantities used here. To implement Step 2 of the algorithm, the product of Step 1 was amplified by polymerase chain reaction (PCR) using rear 10bp of position sequence oligonucleotide "0" and former 10bp of position sequence oligonucleotide "0" as primer. Thus only those molecules encoding generalized Euler tour that begin with vertex 0 and end with vertex 0 were amplified. To implement Step 3 of the algorithm, the product of Step 2 was affinity-purified with a biotin-avidin magnetic beads system. First generating single-stranded DNA from the double-stranded DNA product of Step 2 and then incubating the single-stranded DNA with corresponding complement sequence of TAGATACTATGATTACTGAC conjugated to magnetic beads accomplished this. Only those single-stranded DNA molecules that contained the sequence TAGATACTATGATTACTGAC and hence encoded closed walk that through edge  $0 \rightarrow 1$  or  $1 \rightarrow 0$  edge at least once, denaturalize to the bound complement sequence of ATGTCGTCTG and were retained.

This process was repeated successively with corresponding complement sequence of GTGTACGCAGGCTCATGGCA, CGGCCGGCGCCCGCGCGGC, CTTAAGTAGACATATGATGT, CCGGGCCGCGCCGGGCCGGC, CGTGCACGTAGCATCGAGCT and ATATGTACTAGATCTTGAAC. Only those single-stranded DNA molecules that contained the sequences GTGTACGCAGGCTCATGGCA, CGGCCGGCGCCCGCGCGGC, CTTAAGTAGACATATGATGT, CCGGGCCGCGCCGGGCCGGC, CGTGCACGTAGCATCGAGCT and ATATGTACTAGATCTTGAAC.

Hence encoded closed walk that through edge  $0 \rightarrow 1$  or edge  $1 \rightarrow 0$ , edge  $1 \rightarrow 2$  or edge  $2 \rightarrow 1$ , edge  $2 \rightarrow 3$  or edge  $3 \rightarrow 2$ , edge  $3 \rightarrow 4$  or edge  $4 \rightarrow 3$ , edge  $4 \rightarrow 5$  or edge  $5 \rightarrow 4$ , edge  $5 \rightarrow 0$  or edge  $0 \rightarrow 5$ , edge  $1 \rightarrow 4$  or edge  $4 \rightarrow 1$  at least once. Namely, we can find out all generalized Euler tour of Fig 1. To implement Step 4 of algorithm, we observed the number of hydrogen bonds Of products of Step 3. It is for us to find the shortest DNA strand (for the graph Fig 1, the number of hydrogen bonds Of the shortest DNA sequences must be Minimum). Extract the DNA stand, afterwards, this product was PCR-amplified and gelpurified several times to enhance its purity. To implement Step 5 of algorithm, we carry through sequencing to products of Step 4. Thereby, we can find out the solution of Chinese Postman Problem. Similarly S.Y.Shin's experimentation, we can all accomplish bio-experiment Step 1, Step 2, Step 3 and Step 4. Moreover, sequencing to implement Step 5, we must purified products after each operation, it brings us convenience to sequencing by Sanger's method, we can also use the method of SBH(sequencing by hybridization)<sup>13</sup>. Consequently, we may read out postman paths of Chinese Postman Problem.

## 5 Conclusion

The potential of molecular computation is impressive, what is not clear is whether such massive numbers of inexpensive operation can be productively used to solve real computational problems. We presented a weight encode scheme for molecular programming and demonstrated its performance on Chinese postman problem. In this encoding, the relative values of G/C contents against A/T contents are taken into account to represent real-valued weight of the edge in the graph. Since G/C pairs have 3 hydrogen bonds and A/T pairs 2, we can represent real-valued  $x$  by according to G/C contents. We have shown that the method is effective for reliable DNA computing applied to Chinese postman problem. The method can easily be modified to use in other graph problem in which edges are associated with real-valued costs. Nonetheless, for certain intrinsically complex problem, such as Chinese Postman Problem where existing electronic computers are very inefficient and where massively parallel searches can be organized to take advantage of the operations that molecular biology currently provides, it is conceivable that molecular computation might compete with electronic computation to our problem. We encode a graph with  $n$  vertices, only encode position sequences of the  $n$  vertices and weight sequences of all edges oligonucleotide sequences of all vertices and edge will be determined. Thus, difficulty of encoding will be debased. Approach in the paper may be solving Chinese Postman problem and it is very convenience. We can also solve the shortest path problem, TSP problem with the method in the paper.

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# DNA Computing Model of the Integer Linear Programming Problem Based on Molecular Beacon

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**Abstract.** Biological chip technology and DNA computing are new research areas in biology science and information science separately. The essential characteristic of both is the massive parallel of obtaining and managing information. The integer linear programming problem is an important problem in opsearch and it is an NP-complete problem. But up to now, there does not exist any good algorithm yet. A new DNA computing model is provided to solve a integer linear programming problem based on Molecular Beacon chip. In the method, the integer linear programming problem is solved with molecular beacon by fluorescing upon hybridization to their complementary DNA targets. The method has some significant advantages such as simple encoding, excellent sensitivity, high selectivity, low cost, low error, short operating time, reusable surface and simple experimental steps. The result suggest s the potential of Molecular Beacon used as a DNA computer chip.

## 1 Introduction

In 1961, Feynman gave a visionary talk describing the possibility of building computers that were sub-microscopic [1]. Despite remarkable progress in computer miniaturization, this goal has yet to be achieved. Computer scientists rank computational problems in three classes: easy, hard and incomputable [2]. About thirty years ago there was developed a conception designating a hierarchy of complexity classes for problems on finite sets. And so long as we use digital computers with finite memory storing discrete objects to resolve computational problems, it is relevant for any non-trivial algorithm designing. With the current state-of-the-art the most important complexity classes are P (problems solvable in polynomial time) and NP (problems whose solution certificate can be verified in polynomial time). The most fruitful result of the conception is that complexity classes have so-called complete problems. A problem of a class is complete if you can solve any other problem of this class in polynomial time having a polynomial time algorithm for the first one. Hence complete problems are hardest in their own classes and as they exist we may choose any of them to advance solving techniques for the entire class. The concept of complete problems for a class is generalized to hard problems for the class by inclusion of all other problems, whose polynomial time algorithm gives polynomial time solvability for the class. So, there are NP-complete

and NP-hard problems [3,4]. One of the major achievements of computer science in the last two decades is the understanding that many important computational search problems are NP-complete and thus are unlikely to have efficient algorithms that solve the problem exactly. Adleman (1994) showed that DNA can be used to solve a computationally hard problem, the directed hamiltonian path problem (DHPP), and demonstrated the potential power of parallel, high-density computation by molecules in solution [5]. This parallelism allows DNA computers to solve larger hard problems such as NP-complete problems in linearly increasing time, in contrast to the exponentially increasing time required by an electronically computer. After Adleman initiated the field of DNA computing, Lipton (1995) proposed DNA experiments to solve the satisfiability (SAT) problem [6]. In 1997, Ouyang et al presented a molecular biology based experimental solution to the "maximal clique" problem<sup>[2]</sup>. In 2000, Liu et al designed DNA model system; a multi-based encoding strategy is used in a one-word approach to surface-based DNA computation [7]. In 2001, Wu analyzed and improved their surface-based method [8]. In 2002, Yin et al gave a Chinese postman problem based on DNA computing [9]. All of these efforts made use of molecular biology and demonstrated the feasibility of carrying out computation at the molecular level. One of the formal frameworks for molecular computations is Tom Head's splicing system, which gives a theoretical foundation for computing based on DNA recombination [10]. 0-1 programming problem and the satisfiability problem are closely related, and 0-1 programming problem is a generalization of the satisfiability problem. Up to now, there have been many results for solving the satisfiability problem [6,7,11,12]. In 2002, Braich et al solved a 20-variable instance of the NP-Complete three-satisfiability problem on a simple DNA computer, and proposed this computational problem may be largest yet solved by non-electronic means<sup>[13]</sup>. A molecular beacon (MB) is a synthetic short hairpin oligonucleotide molecule that consists of a loop and a stem structure. The loop portion of a MB is a probe sequence complementary to a target molecule. In the absence of target, the self-complementary domains anneal to form a stem-loop hairpin structure in a unimolecular reaction that serves to bring the fluorescence reporter group into close proximity with the quencher group and results in quenching of the reporter. In the presence of target, the central loop domain will hybridize with the complementary target DNA in a bimolecular reaction, forcing the molecule to unfold: reporter and quencher are now physically separated and the fluorescence of the reporter dye will be restored upon excitation. In 2004, Yin et al proposed DNA computing model for 0-1 programming problem [14]. In 2005, Wang et al proposed DNA algorithm for integer linear programming problem [15]. It is regret biological operation method hasn't given in their paper. In the paper, we solved the integer linear programming problem with molecular beacon by fluorescing upon hybridization to their complementary DNA targets, and presented detail biological operation method.

For terminologies and notations not defined in this paper, the readers are referred to Ref. [16].

## 2 Basic Theory of Integer Linear Programming Problem

Let us consider the integer linear programming problem (ILP):



$$\begin{aligned}
 & \max(\min) C^T x \\
 & Ax = b \\
 & x \geq 0, x \text{ is integer}
 \end{aligned} \tag{1}$$

Where the entries of  $A = \{a_{ij}\}_{m \times n}$ ,  $b = \{b_i\}_{m \times 1}$  and  $c = \{c_i\}_{n \times 1}$  are integer. Let  $a_1 = \max_{i,j} \{|a_{ij}|\}$ ,  $a_2 = \max_i \{|b_i|\}$  and  $a_3 = \max(\{a_1, a_2\} \cup \{c_j : j = 1, 2, \dots, n\})$ .

**Theorem 1[17].** If the above ILP has a finite optimum, then it has an optimal solution  $x$  such that  $|x_j| \leq n^3 [(m + 2)a_3]^{4m+2}$ ,  $j = 1, 2, \dots, n$ .

**Theorem 2[15].** Every ILP is equivalent to a 0-1 linear programming (ZOLP).

**Theorem 3[17].** ILP is NP-complete problem.

By Theorem 2 and 3, we have the following theorem:

**Theorem 4[15].** ZOLP is NP-complete problem.

Let  $a_j = \max_i \{a_{ij}, c_j\}$ . We replace each term  $a_{ij}x_j$  of the ZOLP by  $\sum_{k=1}^{a_j} a_{ij}^k x_{jk}$  and

each term  $c_j x_j$  by  $\sum_{k=1}^{a_j} c_j^k x_{jk}$ , where:

- (1)  $x_{jk}$  are 0-1 variables;
- (2)  $a_{ij}^k = 1 (1 \leq k \leq a_{ij}), a_{ij}^k = 0 (a_{ij} \leq k \leq a_j)$  when  $a_{ij} > 0$ ;
- (3)  $a_{ij}^k = -1 (1 \leq k \leq |a_{ij}|), a_{ij}^k = 0 (|a_{ij}| \leq k \leq a_j)$  when  $a_{ij} < 0$ ;
- (4)  $a_{ij}^k = 0 (1 \leq k \leq a_j)$ , when  $a_{ij} = 0$ ;
- (5)  $c_j^k = 1 (1 \leq k \leq c_j), c_j^k = 0 (c_j < k \leq a_j)$ , when  $c_j > 0$ ;
- (6)  $c_j^k = -1 (1 \leq k \leq |c_j|), c_j^k = 0 (|c_j| < k \leq a_j)$ , when  $c_j < 0$ ;
- (7)  $c_j^k = 0 (1 \leq k \leq a_j)$  when  $c_j = 0$ ;
- (8)  $\sum_{k=1}^{a_j} x_{jk} = a_j$  or  $0 (1 \leq j \leq n)$ .

The resulting ZOLP is denoted by ZZOLP.

**Theorem 5[15].** Every ZOLP is equivalent to a ZZOLP, and their optimums are the same.

By Theorem 4 and 5, we have the following.

**Theorem 6.** ZZOLP is NP-complete problem.

### 3 The Model System of ZZOLP

Let  $\{A_i | i \in I\}$  be a family of sets indexed by a nonempty set  $I$ . The Cartesian product of the sets  $A_i$  is the set of all functions  $f: I \rightarrow \bigcup_{i \in I} A_i$  such that  $f(i) \in A_i$  for all  $i \in I$ . It is denoted  $\prod_{i \in I} A_i$ . If  $I = \{1, 2, \dots, t\}$ , the product  $\prod_{i \in I} A_i$  is often denoted by  $A_1 \times A_2 \times \dots \times A_t$  and is identified with the set of all ordered  $t$ -tuples  $(a_1, a_2, \dots, a_t)$ , where  $a_i \in A_i$  for  $i = 1, 2, \dots, t$ . Let  $m$  be a minimum integer such that  $4^m \geq n$ , set  $\langle n \rangle = 0, 1, 2, \dots, 2^n - 1$  and  $A_i = \{A, G, C, T\}$ .

#### 3.1 DNA Algorithm of ZZOLP

Let us consider the ZZOLP

$$\begin{aligned} \max C^T x \\ Ax = b \\ x = 0 \text{ or } 1 \end{aligned} \quad (2)$$

where the entries of  $b = \{b_i\}_{m \times 1}$  are integer and the entries of  $A = \{a_{ij}\}_{m \times n}$  and  $c = \{c_i\}_{m \times 1}$  are -1, 0, 1. We will use the set  $x = (x_1, x_2, \dots, x_n)^T$  instead of  $\langle n \rangle$ . Then there exists an injection  $f$  from  $x$  to  $\prod_{i=1}^m A_i$ . For example,  $f: x_1 \rightarrow \text{AACCTGGTTGGT}$  when  $x_1 = 1$ ,  $x_1 \rightarrow \text{AGGCCTGACTGA}$  when  $x_1 = 0$ ;  $x_2 \rightarrow \text{ACCATAGCTAGC}$  when  $x_2 = 1$ ,  $x_2 \rightarrow \text{ACCGATTCATTC}$  when  $x_2 = 0$ ;  $x_3 \rightarrow \text{AGAGTCTCAGAG}$  when  $x_3 = 1$ ,  $x_3 \rightarrow \text{AAGGCCTGCCTG}$  when  $x_3 = 0$ . where  $x = (x_1, x_2, x_3)^T = (\text{AACCTGGTTGGT}, \text{ACCATAGCTAGC}, \text{AGAGTCTCAGAG})^T$  instead of 7,  $x = (x_1, x_2, x_3)^T = (\text{AGGCCTGACTGA}, \text{ACCATAGCTAGC}, \text{AGAGTCTCAGAG})^T$  instead of 3.

Set  $X = (M(f(x_1)), M(f(x_2)), \dots, M(f(x_n)))^T$ , where  $M(f(x_i))$  is a molecular beacon with loop  $f(x_i)$ ,  $\bar{X} = (\overline{f(x_1)}, \overline{f(x_2)}, \dots, \overline{f(x_n)})$  and  $\bar{X}^* = (\overline{f(x_1)}^*, \overline{f(x_2)}^*, \dots, \overline{f(x_n)}^*)$ , where  $\overline{f(x_i)}$  is complementary stands of  $f(x_i)$  and  $*$  is a color fluorescent tag. Immobilize the  $2^n$  same columns  $\xi = (X, X, \dots, X)$  on the surface.

We designed the following algorithm to solve ZZOLP:

Step 1.  $i := 1$

Step 2. If  $i = m + 1$ , then return step 7.

Step 3. Cover every  $\overline{f(x_i)}$  when the coefficients of  $x_i$  are -1 and every  $\overline{f(x_2)^*}$  when the coefficients of  $x_i$  are 1 in the  $i$ th equality constraint.

Step 4. Hybridizing, choose the columns whose  $S^+ - S^- = b_i$  (where  $S^+$  is the number of the components which have two color fluorescent tags and  $S^-$  is number which only have one color fluorescent tags in the column vector).

Step 5. Delete the above surplus columns and uncover the covered  $\overline{f(x_i)}$  and  $\overline{f(x_2)^*}$ .

Step 6. Let  $i:=i+1$  and return step 2

Step 7. Cover every  $\overline{f(x_i)}$  when the coefficients of  $x_i$  are -1 and every  $\overline{f(x_2)^*}$  when the coefficients of  $x_i$  are 1 in the object function.

Step 8. Hybridizing, choose the columns whose  $S^+ - S^-$  is Maximum.

Step 9. Record the above columns and  $S^+ - S^-$

Step 10. End

### 3.2 Biological Operation for DNA Algorithm of ZZOLP

For a system of equations that contains  $n$  variables  $x_1, x_2, \dots, x_n$  and  $m$  equations, in order to implement biological operation of algorithm mentioned above, the progress can be separated into the following steps.

Step1: Synthesis  $3n$  oligonucleotides divided into 3 groups, which include  $n$  oligonucleotides in each group. The oligonucleotides in the first group represent variable  $x_1, x_2, \dots, x_n$  respectively and written as  $x_1, x_2, \dots, x_n$ ; the second represent variable  $\bar{x}_1, \bar{x}_2, \dots, \bar{x}_n$  respectively ( $x_i = 1$  if and only if  $\bar{x}_i = 0$  and written as  $\bar{x}_1, \bar{x}_2, \dots, \bar{x}_n$ ; the third group represent complementary strands of the first group respectively, individual written as  $x'_1, x'_2, \dots, x'_n$ . (pay attention to oligonucleotide  $x_i$  represents variable  $x_i = 1$  and oligonucleotide  $\bar{x}_i$  represents variable  $\bar{x}_i = 0, i = 1, 2, \dots, n$ ).

Step2: Constructing  $2^n$  molecular beacons with loop  $x_1, x_2, \dots, x_n, \bar{x}_1, \bar{x}_2, \dots, \bar{x}_n$  as probes and tagging oligonucleotides  $x'_1, x'_2, \dots, x'_n$  with fluorescent green ABI, written their as  $x_1^*, x_2^*, \dots, x_n^*$ . Our molecular beacon has total of 22 bases, of which 12 bases corresponding to  $x_1, x_2, \dots, x_n, \bar{x}_1, \bar{x}_2, \dots, \bar{x}_n$  are the sequence of interest and 5 base pairs form stem, Texas Red is used as fluorophore and DABCYL as the quencher. Fix the  $2^n$  molecular beacons on the surface and where the molecular beacons are arranged in  $2^n$  rows representing all variables of the given computational problem (fixed method can be seen [18]).

Step3: Add  $x'_i$  to the surface when the coefficients of  $x_i$  are -1 and add  $x_i^*$  to the surface when the coefficients of  $x_i$  are 1 in the  $i$ th equality constraint. Any solution

that satisfies this equality will be the columns whose  $S^+ - S^- = b_i$  (where  $S^+$  is the number of the components which have two color fluorescent tags and  $S^-$  is number which only have one color fluorescent tags in the column vector). Further, we can determine the solution for satisfying (dissatisfying) the constraint equation by a method of fluorescence image, and observe their color and record.

Step4: The temperature is raised to separate all double-stranded DNA into single-strands by thermal denaturation. After washing with the certain buffer, the surface is returned to the initial state.

Step5: we can remove all infeasible solution and obtain feasible solution of the problem by repeating step3 and step4. Add  $x'_i$  to the surface when the coefficients of  $x_i$  are -1 and add  $x_i^*$  to the surface when the coefficients of  $x_i$  are 1 in the object function and choose the satisfied constraint equation columns whose  $S^+ - S^-$  is Maximum, the variable value of the columns are optimum solutions.

### 4 The Discussion of the Simple ZZOLP

We discuss in detail simple 0-1 programming problem as below:

$$\begin{aligned} \max u &= x - y + z \\ \begin{cases} x + y - z = 1 \\ x + y + z = 1 \\ x, y, z = 0,1 \end{cases} \end{aligned} \tag{3}$$

To discuss the 0-1 programming problem, the progress was separated into six steps:

Step1: Synthesis 9 oligonucleotides divided into 3 groups, which include 3 oligonucleotides in each group. The oligonucleotides in the first group represent variable  $x, y, z$  respectively and written as  $x, y, z$ ; the second represent variable  $\bar{x}, \bar{y}, \bar{z}$  respectively ( $x = 1$  if and only if  $\bar{x} = 0$ , such as  $y, z$ ) and written as  $\bar{x}, \bar{y}, \bar{z}$ ; the third group represent complementary strands of the first group respectively and written as  $x', y', z'$  (see Fig.1). (pay attention to oligonucleotide  $x$  represents variable  $x = 1$  and oligonucleotide  $\bar{x}$  represents variable  $\bar{x} = 0$ ,  $y$  and  $z$  are also so).

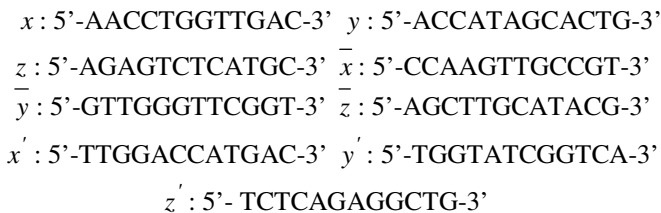


Fig. 1. Detailed encoding of all variables

Step2: Constructing 6 molecular beacons with loop  $x, y, z, \bar{x}, \bar{y}, \bar{z}$  as probes and tagging oligonucleotides  $x', y', z'$  with fluorescent green ABI, written their as  $x^*, y^*, z^*$ . Our molecular beacon has total of 22 bases, of which 12 bases corresponding to  $x, y, z, \bar{x}, \bar{y}, \bar{z}$  are the sequence of interest and 5 base pairs form stem, Texas Red is used as fluorophore and DABCYL as the quencher. Fix the 6 molecular beacons on the surface and where the molecular beacons are arranged in 8 rows representing all variables of the given computational problem (see Fig.2).

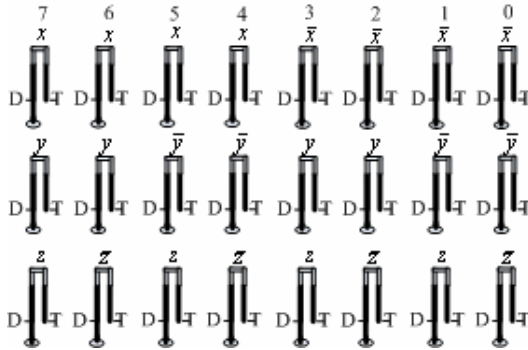


Fig. 2. Fixed molecular beacons on the surface

Step3: For the first constraint equation, we add the complementary strands tagged fluorescent green ABI  $x^*, y^*$  and complementary strands untagged fluorescent green ABI  $z'$  to the surface. Any solution that satisfies this equality will be the columns whose  $S^+ - S^- = 1$  (where  $S^+$  is the number of the components which have two color fluorescents tags and  $S^-$  is number which only have one color fluorescent tags in the column vector). Further, we can determine the solution for satisfying (dissatisfying) the constraint equation by a method of fluorescence image, and observe their color and record. (the feasible solution of the problem is “2,4,7”, see Fig.3).

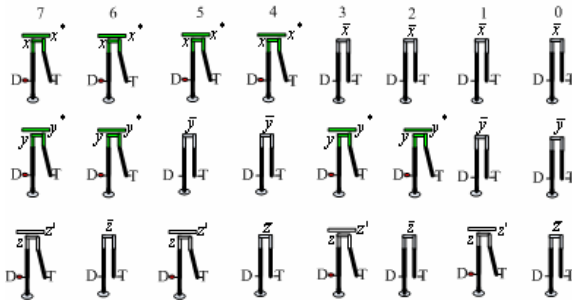


Fig. 3. Hybridize figure of the first constraint equation

Step4: The temperature is raised to separate all double-stranded DNA into single-strands by thermal denaturation. The surface is returned to the initial state by washing in buffer (without regard for infeasible solution determined above). For the second constraint equation, similar to step3 above by adding the complementary strands tagged fluorescent green ABI  $x^*$ ,  $y^*$ ,  $z^*$  to the surface, we can determine the solution of satisfying constraint equation by a method of fluorescence-image, and observe their color and record, Any solution satisfied this equality will be will be the columns whose  $S^+ - S^- = 1$  (the feasible solution of the problem is “1,2,4”, see Fig.4).

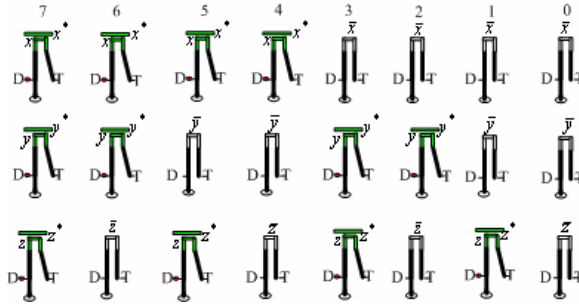


Fig. 4. Hybridize figure of the second constraint equation

Step5: For the object function, we add the complementary strands tagged fluorescent green ABI  $x^*$ ,  $z^*$  and complementary strands untagged fluorescent green ABI  $y'$  to the surface and choose the satisfied constraint equation columns whose  $S^+ - S^-$  is Maximum, the variable value of the columns are optimum solutions (we only care the two columns of “2”, “4”, the optimum solution is “4”, it shows that variable value is (1,0,0), see Fig.5). We can obtain optimum solution (1,0,0), and the maximum value of objective function is 1 .

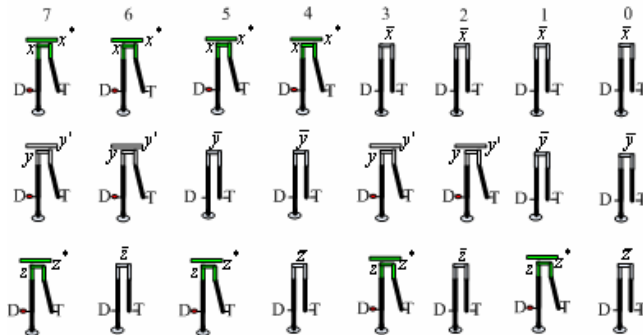


Fig. 5. Hybridize figure of the objective function

The experiment is not complicated and we can accomplish a result that is similar to the experiment performed by Fang [19].

## 5 Analysis Conclusions

Because computers have obvious limits in storage, speed, intelligence and miniaturization, recently, concerns regarding the methods of DNA computation have arisen, especially their efficient parallelism. In order to solve a practical issue, there are still some problems that need a farther study in biologic technology. In this article, we highlight a DNA computing model to solve an integer linear programming problem based molecular beacon. The model we proposed has a potential to solve linear programming problem, which is an important issue in operational research. With the advance of the biologic technology and the molecule biology, the general linear programming problem will be solved. In our method, we adopt fluorescence marking technique, laser focus technique and molecular beacon technique, and read solution by viewing fluorescence, the method of which has some significant advantages such as simple encoding, excellent sensitivity, high selectivity, low cost, low error, short operating time, reusable surface and simple experimental steps. The result suggest s the potential of Molecular Beacon used as a DNA computer chip.

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# DNA Computing Processor: An Integrated Scheme Based on Biochip Technology for Performing DNA Computing

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**Abstract.** An integrated scheme based on biochip technology for performing DNA computing is proposed here. This work is motivated by the goal of integrating all the steps of DNA computing into one machine called DNA computing processor. The basic structure of processor consists of making DNA micro-arrays unit, encoding DNA sequences unit, micro-reaction unit, solution extraction unit and micro-control unit. The functions of each unit are discussed in detail, especially for the solution extraction unit, where the optimal solution spaces are extracted. Finally, conclusions are drawn and future studies are discussed.

## 1 Introduction

Since Adleman's seminal publication [1], there have already been many interesting and exciting results about DNA computing. These works have led to hope of a DNA computer that can outperform the fastest realizable super computers at NP-complete combinatorial problems. Although the models, algorithms and biological operations of each successful instance may be different, the fundamental ideas of DNA computing are same. Namely, first, the extra complex structure of organism is resulted from a series of simple manipulations of the original information expressed by DNA strands. Second, the computable function can be obtained by a series of elementary and simple computing. DNA computing is just based on the both similarities, [2].

Three kinds of approaches for performing DNA computing, which are test tube-based, surface-based and biochip-based, respectively. Test tube-based model is the primary grade of DNA computing, and always used to verify whether the algorithm is feasible or not. Surface-based model is the bridge between test tube-based and biochip-based. Biochip-based model is the only way to realize the real DNA computer.

In this paper, we propose an integrated scheme based on biochip technology for performing DNA computing to try integrating all the steps of DNA computing into one machine called DNA computing processor, and making DNA computing is

hands-free and reliable. The rest of this contribution is organized as follows. In section 2, we present a simple description of DNA computing principle and biochip technologies. In section 3, we then propose the integrated scheme based on biochip technologies for performing DNA computing. Section 4 introduces the functions of each unit in detail. Finally, we conclude in section 5 by present some problems to be further considered in the future.

## 2 Backgrounds

### 2.1 The Steps of DNA Computing

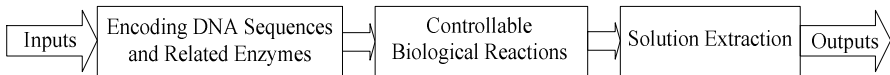
In general, DNA computing may be considered as consisting of a concatenation of three major stages:

**Encoding DNA Sequences Stage.** This stage can be considered as mapping the instances of an algorithmic problem in a systematic manner onto DNA molecules;

**Biological Reactions Stage.** Intrinsic molecular interactions of DNA molecules are exploited and generate a very large space of solution candidates;

**Solution Extraction Stage.** All the generated molecules representing solution candidates are subjected to a series of mechanical manipulations and other physical processes to identify and extract specify molecules, if available, that are regarded as the exact encodings of the optimal solutions of the original computational problem.

Thus, the steps of DNA computing can be illustrated in Figure 1. The double-lines are data lines.



**Fig. 1.** The steps of DNA computing

### 2.2 Biochip Technology

Biochip is a small solid platform made of plastic materials, membrane, or glass, upon which biological information can be stored, retracted, and analyzed. Biochip technology incorporates elements of micro-fluidics, micromachining, synthetic chemistry, separation technology, and detection technology of biological molecules. Biochip technology is moving towards the following directions, [3]:

**Miniaturization.** Tiny apparatus to handle tiny amount of samples;

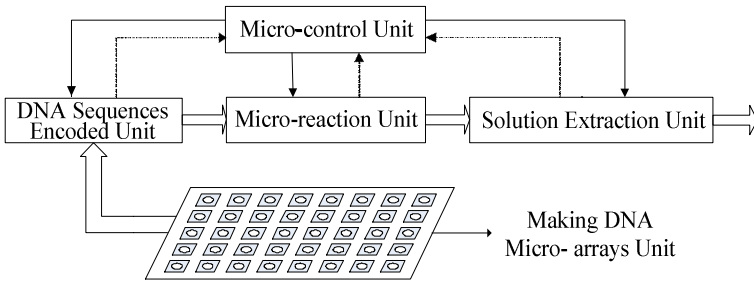
**Integration.** A small apparatus to perform multiple functions;

**Parallelism.** Biological reactions and information are analyzed in parallel.

With the rapid progress in biochip technologies, it is possible that lab-on-a-chip will come true. Thus, the ideas discussed here may realize in the future.

### 3 DNA Computing Processor

As discussed above, the basic structure of DNA computing processor may consist of making DNA micro-arrays unit, encoding DNA sequences unit, micro-reaction unit, solution extraction unit and micro-control unit. The structure of DNA computing processor is shown in Figure 2. The real lines, broken lines and double-lines represent control lines, feedback lines and data lines, respectively.



**Fig. 2.** DNA computing processor organization

The functions of each unit are as follows.

## 4 The Functions of Each Unit

### 4.1 Making DNA Micro-arrays Unit

This unit performs DNA micro-arrays preparation from original micro-structure and micro-systems under the control of micro-control unit. There exist two variants of the chips: cDNA micro-arrays and oligonucleotide arrays. Two commonly used types of chips differ in the size of the arrayed nucleic acids. In cDNA micro-arrays, relatively long DNA molecules (longer than 100nt) are immobilized by high-speed robots on a solid surface. The oligonucleotide arrays, relatively short nucleic acids are fabricated either in-situ light-directed chemical synthesis or by conventional synthesis followed by immobilization on a glass substrate. Since nucleic acid sequences utilized in DNA computing are always short, here, we only introduce in-situ synthesis.

Usually oligos are built up base-by-base on the surface of the array. This takes place by covalent reaction between the 5' hydroxyl group of the sugar of the last nucleotide to be attached and the phosphate group of the next nucleotide. Each nucleotide added to the oligonucleotide on the glass has a protective group on its 5' position to prevent the addition of more than one base during each round of synthesis. The protective group is then converted to a hydroxyl group either with acid or with light before the next round of synthesis. The different methods for deprotection lead to the

three main technologies for making in-situ synthesized arrays: photodeprotection using masks, photodeprotection without masks and chemical deprotection with synthesis via inkjet technology. For knowing more, see [4] please.

## 4.2 Encoding DNA Sequences Unit

This unit is mainly made up of making DNA micro-arrays biochips. In this unit, the design and selection of encoding DNA sequences set is crucial. The encoding design problem for DNA computing consists of mapping the instances of an algorithmic problem in a systematic manner onto specific molecules so that the underlying chemical reactions avoid all these sources of error, and the resulting products contain, with a high degree of reliability, enough molecules encoding the answers to the problem's instances to enable a successful extraction, [5].

In fact, for each successful instance of DNA computing, in any case, how ingenious the designing algorithms are, the basic biological manipulations are absolutely necessarily, which are separating, fusing, lengthening, shortening, cutting, linking, modifying, and multiplying etc. all the manipulations on DNA sequences can be regarded as operators of DNA computing and must ensure these manipulations have no errors. Thus, encoding problem come down to DNA sequences design at last. That is to say, encoding problem can be regarded as DNA sequences design for making sure the underlying chemical reactions controllable.

To ensure biological reactions controllable, some constraints should be considered according to the definition of encoding problem, thus, many approaches for encoding problem have been proposed in the last decade, [6-19]. All of which focus on the design of DNA sequences to reduce the possibility for undesirable reactions.

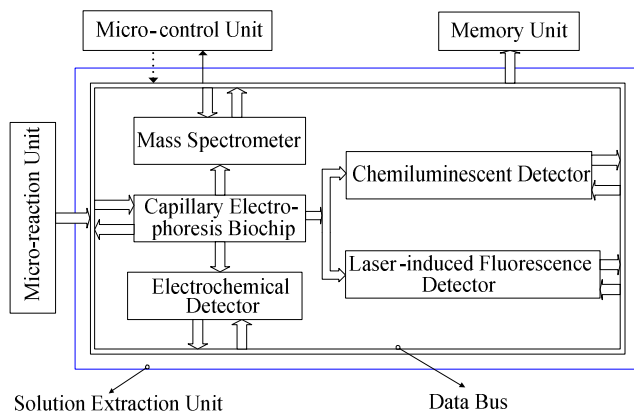
## 4.3 Micro-reaction Unit

In this unit, intrinsic molecular interactions of DNA molecules are exploited in parallel and generate a very large space of solution candidates. To extract few desirable solutions, the polymer chain reaction (PCR) is absolutely necessarily before solution extraction stage. PCR allows the production of more than 10 million copies of a target DNA sequence from only a few molecules. The sensitivity of this technique means that the sample should not be contaminated with any other DNA or previously amplified products that may reside on chip. The efficiency and specificity of amplification in PCR is always highly dependent on the nature of the template DNA and primers. Therefore optimization of reaction conditions is often necessary. The common method is to design a Kit to simplify optimization and contains ready-to-use reaction buffers covering a wide range of possible values for all components, [20].

## 4.4 Solution Extraction Unit

Based on the several successful applications have been demonstrated in the last decade, [21-24], we can draw the following conclusion: In DNA computing, solutions either are separated by electrophoresis, then extracted by biological detection device, or extraction followed reactions tightly. On the other hand, it is considered that there

does not exist a universal detection method due to the variety and complexity of samples, in addition, in order to control and transfer special analysis software stored in memory unit more easily, here we give a modularized design method for detection. Besides, bus topology is utilized for data transfer to extend and maintain modules.



**Fig. 3.** The modularized scheme for solution extraction

The functions of each module are as follows.

**Microchip Capillary Electrophoresis.** Microchip capillary electrophoresis that integrates sequential method process steps such as sample handling, staining, destaining, detection and analysis into a single process that creates a complete laboratory on a chip, has been demonstrated that it can significantly improve the quality of data for nucleic acid fragment analysis when compared to classical gel techniques. Specifically, the new technology provides enhanced resolution and better reproducibility. The main operations of this technology are as follows.

- i) Samples are loaded into the chip's micro-channels and are connected with electrodes when placed in the instrument. Voltage drives the sample from the sample well through the micro-channels and into the separation channel, where a polymer sieves the DNA fragments by size.
- ii) Intercalating dye binds to DNA fragments, which fluoresce when excited by a laser.
- iii) Software plots fluorescence intensity versus time and produces an electropherogram for each sample. The data can also be displayed in tabular format or in a gel-like image, simulating traditional gel electrophoresis.
- iv) The Bioanalyzer software quantitates approximate concentration and accurately sizes each protein or DNA/RNA fragment in a digital format, [25].

**Chemiluminescent Detector.** Chemiluminescent detector has become a competitive device due to no light required and smaller volume. The interface between capillary electrophoresis units and chemiluminescent detector is complex. Besides, dead volume and overflow phenomena may be introduced, and then reduce separation

efficiency. Making zero-dead volume column reactor using micro processing technique can solve these problems.

Electronic systems based on charge-coupled device (CCD) detectors are a way of visualizing various types of gel media, the systems generate digital images that can be archived, reproduced, and analyzed. Chemiluminescent samples emit light at extremely low levels, and the inherent electronic noise of CCD chips and limitations of much of the associated hardware have resulted in the majority of so called chemiluminescent-ready systems being incapable of producing accurate, reproducible results.

The requirement is for a system that combines high levels of accuracy and automation, leaving the user to concentrate on applications and results. The second requirement for high-quality chemiluminescent imaging is automation, [26].

**Laser-induced Fluorescence Detector.** Laser-induced fluorescence (LIF) is a spectroscopic method. The preferred specie is excited with help of a laser. The wavelength is often selected to be the one at which the specie has its largest cross section. The excited specie will after some time, usually in the order of few nanoseconds to microseconds, deexcite and emit light at a wavelength larger than the excitation wavelength. This light, fluorescence, is measured.

Two different kinds of spectra exists, LIF-spectra and excitation scans. The LIF-spectra are performed with a fixed lasing wavelength, as above and the fluorescence spectrum is analyzed. Excitation scans on the other hand collects all fluorescent light, without measuring the wavelength.

Instead the lasing wavelength is changed. The advantage over absorption spectroscopy is that it is possible to get two- and three-dimensional images since fluorescence takes place in all directions. The signal-to-noise ratio of fluorescence signals to very high, providing a good sensitivity to the process. It is also possible to distinguish between more species, since both the lasing wavelength can be tuned to a particular excitation of given specie, [27].

**Mass Spectrometer.** Mass spectrometers use the difference in mass-to-charge ratio of molecules to separate them from each other. Mass spectrometry is therefore useful for quantization of molecules and also for determining chemical and structural information about molecules. Molecules have distinctive fragmentation patterns that provide structural information to identify structural components.

The general operation of a mass spectrometer is:

- i) Create gas-phase ions;
- ii) Separate the ions in space or time based on their mass-to-charge ratio;
- iii) Measure the quantity of ions of each mass-to-charge ratio.

In general a mass spectrometer consists of an ion source, a mass-selective analyzer, and an ion detector. Since mass spectrometers create and manipulate gas-phase ions, they operate in a high-vacuum system. The magnetic-sector, quadrupole, and time-of-flight designs also require extraction and acceleration ion optics to transfer ions from the source region into the mass analyzer. The details of mass analyzer designs are discussed in the individual documents listed below. Basic descriptions of sample introduction/ionization and ion detection are discussed in separate documents on ionization methods and ion detectors, respectively, [28].

**Electrochemical Detector.** The Electrochemical Detector can operate in three different detection modes:

- i) In the Conductivity mode, current conducted by ions in solution in an electric field is measured;
- ii) In DC Amperometry, a constant voltage is applied to the working electrode in the amperometry cell and the resulting current is the detector output;
- iii) Integrated Amperometry is similar to DC Amperometry in that the same cell and associated circuitry are used. After the initial stages of signal processing, the cell current is integrated and the resulting charge is the detector output reported for each integration period. A user-programmed waveform, or repetitive series of potentials, is applied to the cell, and the same waveform program sets the start and finish of the integration period. The program is entered from the waveform screen.

An important distinction between conductivity and amperometric detection is that no electron transfer reactions occur during conductivity detection. During DC and integrated amperometric detection, electrons are actually transferred between the electrode and the analyte molecules. Although, in theory, all three detection modes could employ the same detector cell, a cell optimized for conductivity is not appropriate for amperometry, and vice versa, [29].

#### 4.5 Micro-control Unit

The main functions of micro-control unit are to control and direct the above four units to perform the physical and biological operations in order. The main control steps are as follows.

As making DNA micro-arrays unit, micro-control unit mainly performs building the oligonucleotides on the glass array one base at a time, at each step, adding the base via the reaction between the hydroxyl group 5' of the terminal base and the phosphate group of the next base. Note, there is a protective group on the 5' of the base being added, which prevents the addition of more than one base at each step. Following addition, there is a deprotection step at which the protective group is converted to a hydroxyl group to allow addition of the next base.

As encoding DNA sequences unit, micro-control unit mainly performs extracting DNA polymerase chain and controlling its length in terms of the need of micro-reactions. Besides, combining DNA and the correlative enzymes automatically, labeling the digestion sites, and making it available for the following micro-reactions and biological detection.

As micro-reaction unit, micro-control unit mainly performs controlling the PCR conditions, the main controls parameters are as follows.

**Initial Denaturation Stage.** The initial denaturation should be performed over an interval of 1-3min at 95°C if the GC content is 50% or less. For GC-rich templates the denaturation interval should be prolonged up to 10min.

**Denaturation Stage.** Usually denaturation for 0.5-2min at 94-95°C is sufficient. The GC content should be taken into consideration. Denaturation time can be optimized empirically.

**Primer Annealing Stage.** Usually the optimal annealing temperature is 5°C lower than the melting temperature of primer-template DNA duplex. Incubation for 0.5-2min is usually sufficient. However, if non-specific PCR products are obtained in addition to the expected product, the annealing temperature should be optimized by increasing it stepwise by 1-2°C.

**Extending Stage.** Usually the extending step is performed at 70-75°C.

**Number of Cycles.** The number of PCR cycles depends on the amount of template DNA in the reaction mix and on the expected yield of the PCR product. In most cases, 25-35 cycles are sufficient.

**Final Extending Stage.** After the last cycle, the samples are incubated at 72°C for 5-15min to fill-in the protruding ends of newly synthesized PCR products, [30].

As solution extraction results unit, micro-control unit mainly performs controlling the following operations, such as exciting and controlling applicator, transforming optical signal into digital signal (using image manipulation technology), transforming related data into relevant digital signal, and sending it to memory subsystem, then using special analysis software to analyze data quantitatively, at last, the digital computer performs processing data and readout results.

## 5 Discussion

In the previous sections, we show the DNA computing processor which integrates all the steps of DNA computing into one machine. Besides, the functions of each unit also are discussed in detail, especially for the detection and analysis unit, where the optimal solution spaces are extracted.

It should be mentioned that the DNA computing processor proposed here is only a virtual machine. To realize real DNA computer, At least, the following research subjects should be emphasized: designing DNA computing model and arithmetic, organizing biochemical units, data storage technology, interface and communication, micro flow control, performance tuning etc. The technical problems need to be solved are as follows. How to realize the operation automatically? How to realize the communication between processor or EMS memory and computer interior? How to evaluate its performance?

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# General DNA Automaton Model with R/W Tape

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**Abstract.** Since Turing machine is consisted of R/W Tape head and Turing Tape, that means a DNA based Turing machine must realize the read and write processes on Turing Tape with DNA molecules, and make the head move in two directions either. Based on our previous works on DNA computing, especially on DNA automaton and the relationship between enzymes and their computation ability with DNA automaton model. We combined different enzymes together to modify the cut and recognition sites with a programmable Tape head to embody the read and write symbol procedure on Turing tape. And this article will describe how the programmable Tape head moves in two direction and read/write procedure of Turing Tape in details.

## 1 Introduction

One of the main goals of the research on DNA Computing is to realize a Turing machine by DNA molecules. A Turing machine is a kind of state machine. At any time the machine is in any one of a finite number of states. Instructions for a Turing machine consist in specified conditions under which the machine will transition between one state and another. A Turing machine has an infinite one-dimensional tape divided into cells. Traditionally we think of the tape as being horizontal with the cells arranged in a left-right orientation. The tape has one end, at the left say, and stretches infinitely far to the right. Each cell is able to contain one symbol. The machine has a read-write head, which at any time scanning a single cell on the tape. This read-write head can move left and right along the tape to scan successive cells.

Some schemes of realization Turing computations through DNA computing have been proposed. The pioneer conceiving of DNA automaton is the DNA Turing model proposed by C. Bennett [1] in 1973, but a feasible model of DNA automaton is constructed by Rothmund [2] using restriction enzymes in 1995. In this DNA computing model, the Turing tape is encoded by DNA sequence, the restriction enzyme recognizes the specific sequence of DNA sequence which acts as the tape head of automaton, cuts correspondence sites to make the tape head move forward and therefore the transition of automaton status achieved. This model is quite perfect in theory, and makes a great contribution to the research of DNA automatons. In fact, the succeed models of DNA automatons are based on this model in which DNA sequence encoded tape symbols and restriction enzyme trigger the automaton. The drawback of this model is that it is too idealized to realize by experiment. Therefore, Smith and Schweitzer [3] make effort to use DNA and standard laboratory technique to realize the DNA Turing model. Whereafter, Beaver [4] proposed a DNA Turing machine to operate single molecule. In 1995, winfree [5] proposed a cellular automata model of

DNA computing, and realize a programmable self-assembly DNA model in 1998 by experiment [6].

In order to explore the feasibility of autonomous molecular computing, kensaku sakamoto [7] proposed a DNA computing model use the hairpin formation by single-stranded DNA molecules to solve a famous NP problem, the so-called  $\square$ satisfiability $\square$  problem (SAT) in 2000. The problem is elaborately encoded with DNA hairpin structure, and the selected DNA hairpin structure is well-designed to contain a recognition site of given restriction enzyme to cut off them. This model approves the feasibility of DNA automatons, but it is so well-designed to extend.

Till 2001, Yaakov benenson[8] proposed a programmable molecule automaton model based on DNA computing, and the restriction enzyme in this DNA automaton is *FokI*. The main merit of this DNA automaton model is that it is programmable. In this model, the distribution between states and symbols depends on the length of the spacer between the recognition site and the restriction site of the particular restriction enzyme employed. Benensons automaton realized the basic features and processes of a finite automaton with two internal states using enzyme *FokI* with DNA computing. This automaton has an alphabet comprising two input symbols therefore can have eight possible transition rules, 255 possible transition-rule selections and 3 possible selections of accepting states, resulting in 765 syntactically distinct programs. In 2004 Yaakov benenson applied his DNA automaton in cancer diagnosing [9].

We have some DNA based automaton models already. In formal works on DNA automaton, we have studied the computation ability of finite DNA automaton with different enzymes and gives out the formula to calculate probable maximum states directly from the features of restriction enzyme. With further discussions, we proposed a DNA finite automaton with three internal states which is more powerful than the finite automaton [10].

In this paper, we give out the scheme of DNA automaton model with its tape head moves in two directions, and how symbols can be read from and write into the tape, which will surly lead to the realization of DNA Turing machine.

Since Turing machine is consisted of R/W Tape head and Turing Tape, that means a DNA based Turing machine must realize read and write processes on Turing Tape by DNA molecules, and make the head move in two directions either. Based on our previous works on DNA computing, especially on DNA automaton and the relationship between enzyme and its computation ability, we combined different enzymes together to modify the cut and recognition sites with a programmable Tape head to embody the read and write symbol procedure on Turing tape. And this article will describe the programmable Tape head move in two direction and read/write procedure of Turing Tape in details.

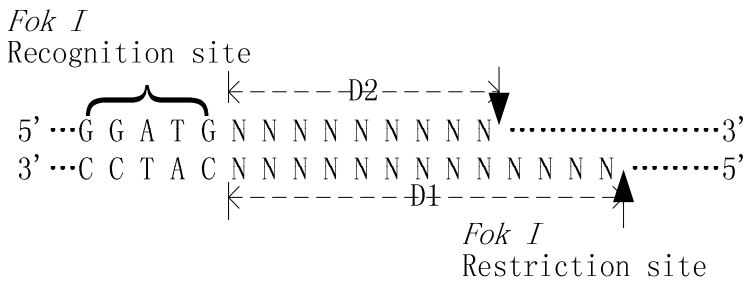
## 2 Programmable Tape Head Move in Two Directions

The symbol-read procedure of a finite DNA automaton using *Fok I* is implement by the stick process of the sticky ends of the Turing tape and the state-transfer molecular, so that the virtual Tape head of a finite DNA automaton is located on the sticky end of the Turing tape made by *Fok I*. From the state change procedure of finite state DNA automaton we can see, whatever two states or three states finite DNA automaton of

Benenson type using *Fok I*, the length of the encoded DNA Tape will become shorter by the state change procedure, thus the position of the virtual Tape head will move forward to the next symbol correspondingly and the move direction of the virtual head can move only in one direction in the same way. If we can make the Turing tape longer after state changed, likewise we can make the virtual Tape head move backward, that is to say, the manner of state-change procedure should be changed.

Typically a DNA automaton consists with three molecular units: software unit, double-stranded DNA encodes input and output information with programming amounts; regulation unit, which regulate software molecule concentrations, and hence make automaton transit according to a definite procedure; Hardware unit, Restriction Enzyme which provide state change method. The key point of a DNA automaton is Restriction Enzyme that makes automaton transition possible, while the cutting site and recognizing site of Restriction Enzyme determined the computation ability of a DNA automaton. In order to make the virtual Tape head move in two directions as program, new state-change method should be added into the scheme of DNA automaton. Since the state-change procedure is determined by Restriction Enzyme the hardware unit of DNA automaton, new enzyme must be introduced and combined with previous enzyme to make possible a programmable virtual tape head move in two directions.

Let's compare the two kinds of enzymes with different features: one is cut site beside the only recognition site and the other is cut site between two recognition sites. Restriction enzymes with a recognition site and a cut site beside have some wonderful features, and have been successfully used in DAN computing. These enzymes act on DNA sequence as follows (*Fok I* in this example):

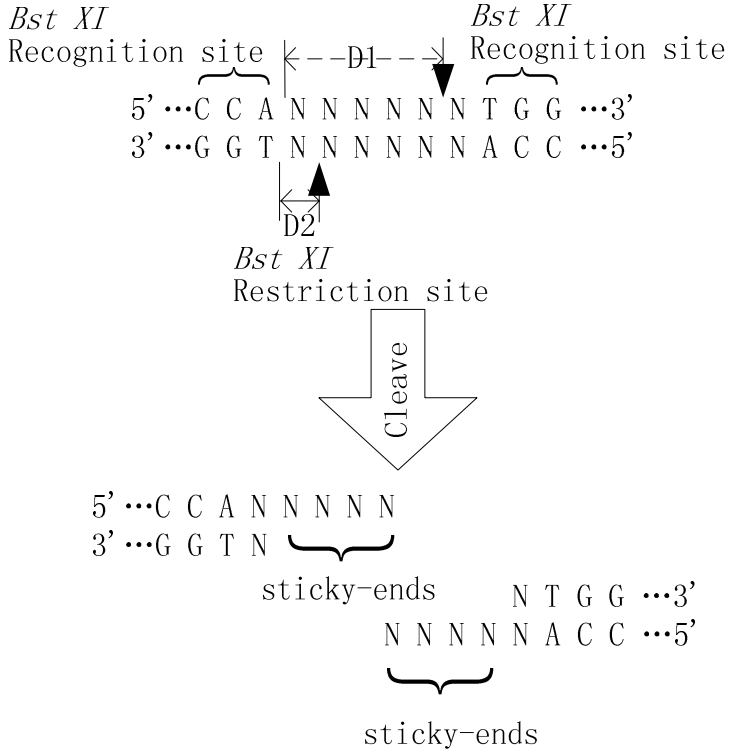


**Fig. 1.** N denotes any base that can be encoded. The distance between recognition site and restriction site of the restriction enzyme provides the encoding space for states and symbols.  $D_1$  and  $D_2$  determine the state transition mode the restriction enzyme can provide for DNA automaton. The restriction enzyme used in programmable DNA automaton model is of this kind<sup>1</sup>.

Given a restriction enzyme with one recognition site and a cut site beside, the distances between recognition site and restriction site are  $D_1$  and  $D_2$  (Fig. 2.), and  $D_1 > D_2$ . We can calculate probable maximum states directly from the features of this kind of restriction enzyme.

Because the cut site of this kind of enzyme is located on the right side of recognition site, the Turing tape will become shorter as state changes. And using this type of enzyme the virtual tape head of DNA automaton can only move forward.

As to the Restriction enzyme with two recognition sites and a cut site between them, the situation became different. This kind of restriction enzyme has two recognition sites, thus gives more restriction to encoding process of DNA automaton, the action of these restriction enzymes can be demonstrate as (*BstXI* in this example):

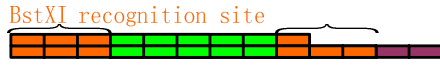


**Fig. 2.** *Bst XI* has two recognition site, D1 and D2 provide the encoding space for DNA automaton. Since  $D1 > D2$ , the separated pieces have single stranded "sticky-ends," which allow the complementary pieces to combine. Therefore, this kind of restriction enzyme can also provide several state transition modes due to  $D1 + D2$  is not zero. In fact, *Bst XI* has been successfully applied in DNA automaton of hairpin model to solve SAT problem<sup>10</sup>.

A restriction enzyme with two recognition sites and a cut site between them can provide some new state transition scheme for DNA automaton. With this feature, we can make tape head moves not only forward but also backward, which should cooperate with a felicitous coding scheme of DNA sequence.

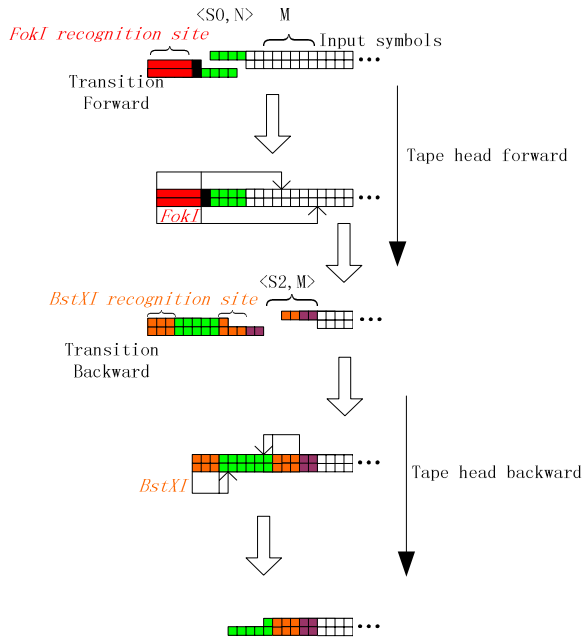
**2.1 Forward to Backward Transition**

We introduce restriction enzyme *BstXI* to provide a forward to backward procedure, the transition unit for change the direction of Turing tape from Forward to backward is as follows:



**Fig. 3.** Tape head direction Transition unit, forward to backward. Orange cells represent the recognition sites of *Bst XI*, green cells represent the encoding DNA sequence that will add to the Turing tape, purple cells represent the encoding sticky end.

This transition unit can change the move direction of current Turing tape from forward to backward, the direction changing procedure of the virtual tape head is demonstrated as follows:

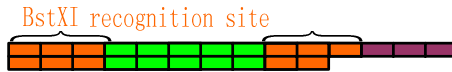


**Fig. 4.** Tape head direction changing procedure from forward to backward. Red cells represent the recognition sites of *FokI*, Orange cells represent the recognition sites of *Bst XI*, green cells represent the encoding DNA sequence, purple cells represent the encoding sticky end.  $M$  is the programmed command symbol indication the direction changing procedure from forward to backward, when the virtual tape head read symbol  $M$ , with correspond direction transition unit from forward to backward present, the exposure sticky end of Turing tape with stick with the direction transition unit, the offspring sequence contains the recognition site of *Bst XI*, after cleave action by *Bst XI*, the sticky end of Turing tape is upside down when virtual tape head change its direction, and the move direction of virtual Tape head changed.

The length of DNA sequence encoded input symbols increased as *Bst XI* cleaves it, thus makes the tape head move backward. Since the sticky end is upside down when tape head change its direction, the state transition molecule must change accordingly.

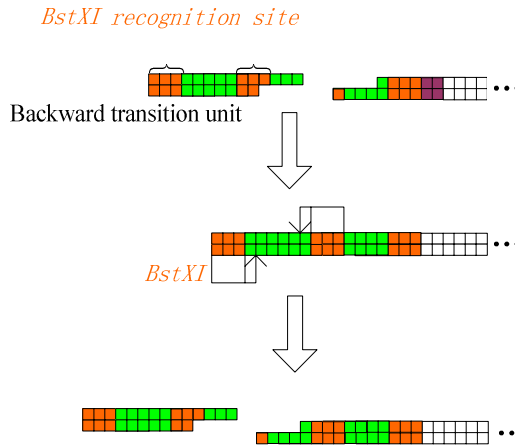
### 2.2 Backward Transition Procedure

After the direction of virtual Turing tape head changed, the exposure sticky end of Turing tape changed upside down as fig. 4, therefore absolutely forbid the Turing tape to react with any forward transition unit as previous finite state DNA automaton, which will reduce the constraint condition of encoding of DNA automaton. In order to make the two direction virtual Turing tape really sound, the tape head should be able to continue the backward movement after direction changes, that is to say, a new type of transition unit so called backward transition unit should make the continue backward movement possible. The backward transition unit is designed as follows, which is based on the feature of restriction enzyme *BstXI*:



**Fig. 5.** Backward transition unit. Orange cells represent the recognition sites of *Bst XI*, green cells represent the encoding DNA sequence that will add to the Turing tape, purple cells represent the encoding sticky end.

The backward transition unit enables the virtual tape head to continue the backward movement. And the backward transition procedure is demonstrated as follows:



**Fig. 6.** Backward transition procedure. Orange cells represent the recognition sites of *Bst XI*, green cells represent the encoding DNA sequence that will add to the Turing tape, purple cells represent the encoding sticky end.

Each time a transition procedure finished, the Turing tape increase in 7bp(Bp is the unit of the Count of the cells which represent oligonucleotides), in which 3bp is the recognition site that can not be coded, 4bp is encoding DNA sequence.

The move speed of virtual tape head(in bp per transition bp/T) is programmable, which is determined by the scheme of backward transition unit. With enzyme *Bst XI*,



we can provide three mode of backward transition with different speed 7bp/T, 6bp/T and 5bp/T.

### 2.3 Backward to Forward Transition

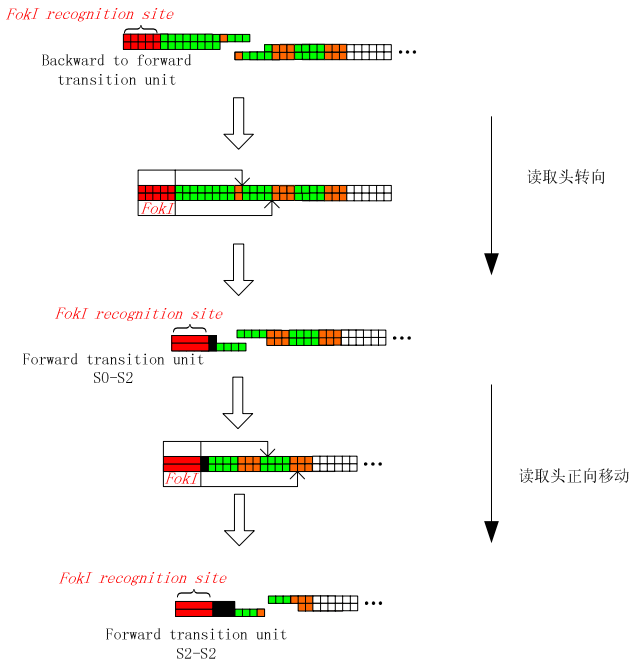
Consider the automaton is running in a backward transition mode, if the automaton could not return back to a forward transition mode in some condition, we can't say this automaton has a free programmable tape head.

We used the feature of enzyme *FokI* to realize the backward to forward transition unit. The scheme of this unit is designed as follows:



**Fig. 7.** Backward to forward transition unit. Red cells represent the recognition sites of *FokI*, Orange cells represent the recognition sites of *Bst XI*, green cells represent the free coding space of DNA sequence.

With the backward to forward transition unit, the backward to forward transition procedure is as follows:



**Fig. 8.** Backward to forward transition procedure. Red cells represent the recognition sites of *FokI*, Orange cells represent the recognition sites of *Bst XI*, green cells represent the free coding space of DNA sequence.

As the tape head of DNA automaton moves backward, we can give a command to change its direction to forward movement. When the exposed sticky end of backward movement Turing tape matches the sticky end of backward to forward transition unit, the DNA automaton enters the backward to forward transition procedure.

The offspring of backward to forward transition unit and Turing tape contains recognition site of enzyme *FokI*, after cleaved by *FokI*, the exposed sticky end is same as its forward movement sticky end as formal finite DNA automaton, thus accomplish the backward to forward transition procedure. After the procedure, the virtual tape head of DNA automaton can continue its forward movement with programmed transition units and enzyme *FokI*.

### 3 Symbol Write Procedure of DNA Automaton

Another problem from finite automaton to the Turing machine is that a tape head of Turing machine can write symbols to Turing tape.

Write symbol procedure can be realized by add new symbols to current tape, but add new symbol encoded DNA sequences directly to current tape is not a feasible way, because the new symbols that will directly add to the tape couldn't contain any more sticky end that can react with any other transition unit, or else the new symbols sequence will be destroyed by with the transition unit presents, thus the offspring of the new symbols and tape couldn't keep the sticky end of formal tape, and the DNA automaton can't react with any other transition units, that is to say the DNA automaton will stop if any new symbols is added to its tape directly.

In fact, we can use the backward transition procedure as Fig. 6 to write symbols to the Turing tape. Since the tape of DNA automaton increase with backward transition procedure, and the added sequence contain free coding space (green cells in Fig. 6), together with the forward to backward transition procedure in Fig. 4, backward to forward transition procedure in Fig. 8, the entire programmable symbol read and write procedure is totally settled.

### 4 Conclusion

Based on the previous works on finite state DNA automaton, by combined two enzymes *FokI* and *Bst* together, we provide a feasible way to realize a DNA automaton with programmable free virtual tape head, which can read and write symbols. These works will lead to the prospective realization of a DNA Turing machine will further experimentation and application validation.

### Acknowledgments

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# Interpolated Hidden Markov Models Estimated Using Conditional ML for Eukaryotic Gene Annotation

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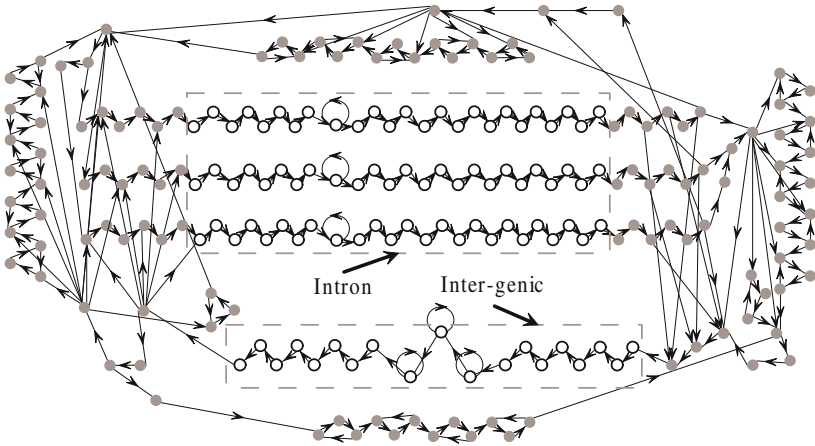
**Abstract.** To improve the performance of computational gene annotation programs, we introduced the well known interpolated Markov Chain (IMC) technology to the class Hidden Markov models (CHMM). CHMM was applied in one of the best eukaryotic gene prediction systems: HMMgene. The conditional Maximum Likelihood estimation (CMLE) algorithm was used to estimate the interpolation parameters. The resulting gene prediction program improves exon level sensitivity by 3% and specificity by about 1% compared to HMMgene as trained and tested on some standard human DNA sequence dataset.

## 1 Introduction

In the field of computational biology, eukaryotic gene annotation methods are used to annotate the exon-intron structures of genes scattered in genome sequence. Although methods based on the comparison of two or more genomes have greater accuracy, there are still several good reasons to develop improved single-genome predictors [1].

Rogic et al. did a comprehensive evaluation of popular gene annotation programs based on single-genome using the human, mouse and rat genome sequences as test dataset, among which HMMgene [2] had the highest prediction accuracy [3]. The model of HMMgene is totally a class hidden Markov model (CHMM) [4] and it can be estimated in one go from scratch by using conditional maximum likelihood estimation (CMLE). We introduced the well known Interpolated Markov chain (IMC) technology to this CHMM, and estimated the interpolation parameters by CMLE. The interpolation scheme has been successfully applied in microbial gene identification [5] and gene annotation for small eukaryotes [6]. But it hasn't been applied in any class hidden Markov models for high eukaryotic gene annotation yet. And no estimation algorithms were devised to estimate the interpolation parameters under this model. Our gene prediction program improves exon level sensitivity by 3% and specificity by about 1% compared to HMMgene as trained and tested on standard human DNA sequence dataset.





**Fig. 2.** The CHMM structure of HMMgene. The circles denote the states in CHMM. "Gray" states emit nucleotides in the coding regions, and "white" states in the intron region or inter-genic region as showed by the boxes with dashed frames. This picture was produced with the Java software BioLayout [7].

Krogh, A. used a discriminative approach, conditional ML:

$$\theta^{CML} = \arg \max_{\theta} P(c|s, \theta) \quad (2)$$

This probability can be rewritten as

$$P(c|s, \theta) = P(s, c|\theta) / P(s|\theta) \quad (3)$$

Probability  $P(s|\theta)$  was calculated by the forward algorithm disregarding labels.

To be able to discover genes, we need a Markov model that satisfies the grammar of genes. The structure of HMMgene was shown in Fig. 2. For both model training and gene predicting, we align observation sequences with the model. Each observation symbol corresponds to a state. So the observation sequence leads to some state sequences after the alignment, and every state sequence produce a label sequence which gives annotation for the observation sequence.

## 2.2 Interpolated Markov Chains (IMC)

$N$ th order Markov chain is also called an  $(N + 1)$ -mer sequence model. In order to fully exploit the information represented in the lower order models, we can use a linear interpolation scheme:

$$P(s_t|s_{t-2}s_{t-1}) = \lambda_1 \tilde{P}(s_t) + \lambda_2 \tilde{P}(s_t|s_{t-1}) + \lambda_3 \tilde{P}(s_t|s_{t-2}s_{t-1}) \quad (4)$$

In this example, the model order is 2.

To facilitate the following description, we rewritten (4) as:

$$\bar{\theta}_t^2 = \lambda_0 \cdot \tilde{\theta}_t^0 + \lambda_1 \cdot \tilde{\theta}_t^1 + \lambda_2 \cdot \tilde{\theta}_t^2 \quad (5)$$

Here  $\lambda_k$  denotes the interpolation parameters,  $\tilde{\theta}_t^k$  denotes the conditional probability of seeing  $s_t$  given  $k$  previous symbols in a fixed order model of order  $k$ , and  $\theta_t^k$  denotes the conditional probability of seeing  $s_t$  given  $k$  previous symbols in an interpolated model with order  $k$ .

So far interpolation scheme hasn't been applied in any class hidden Markov models for eukaryotic gene annotation. And no estimation algorithms were devised to estimate the interpolation parameters under this model.

### 3 ICHMM and Parameter Estimation

#### 3.1 Interpolated Class Hidden Markov Models (ICHMM)

In a standard HMM, each state is with fixed order. And there're two kinds parameters: the probability of going from one state to another (transition parameter) and the conditional probability of seeing a base in a state (emission parameter). After the interpolation technology is introduced to HMM, some or all of the states are not with fixed order. The transition parameters remain the same and the emission parameters of interpolated states take the form of (5).

In principle, using higher order is always preferable to using lower order, but only if sufficient data is available to produce reliable probability estimates. By using the interpolation scheme we try to take advantage of multiple fixed order models and give precise and reliable estimation.

#### 3.2 Parameter Estimation for ICHMM by Using CMLE

CMLE was used to estimate ICHMM parameters: transition, emission and interpolation parameters. After interpolation is used, we re-separate transition and emission into two groups: emission parameters associated with interpolated states (denoted by  $\hat{\theta}$ ), and the other emission and transition parameters (denoted by  $\tilde{\theta}$ ).  $\bar{\theta}$  has the form of (5). In the following  $\theta$  is still used to denote both groups sometimes for concision. And (2) is rewritten as

$$\theta^{CMLE} = \arg \max_{\hat{\theta}, \tilde{\theta}, \lambda} P(c, s | \hat{\theta}, \tilde{\theta}, \lambda) / P(c | s, \hat{\theta}, \tilde{\theta}, \lambda) \quad (6)$$

To do the optimization in (6), first it is converted to logarithms. Define

$$L_f = -\log P(s|\theta) \quad (7)$$

$$L_c = -\log P(c, s|\theta) \quad (8)$$

Then to estimate  $\hat{\theta}$ ,  $\tilde{\theta}$  and  $\lambda$ , we need to maximize

$$L = \log P(c, s|\theta)/P(s|\theta) = L_f - L_c \tag{9}$$

Here the maximization approach is based on the gradient of  $L$ .

**Calculation of the Gradient.** First we give two more denotations. Since a fixed order conditional probability  $\hat{\theta}^k$  ( $k$  is the order) may contribute to more than one interpolated conditional probabilities  $\bar{\theta}$  with order  $K \geq k$ . We use  $\Theta$  to denote an interpolated probability set, in which all the probabilities are associated with certain  $\hat{\theta}^k$ . And we use  $\pi$  to denote a path by which a sequence goes through the model.

The probability  $P(s|\theta)$  is written as a sum over all possible paths through the model,

$$P(s|\theta) = \sum_{\pi} P(s, \pi|\theta) \tag{10}$$

And the probability for a given path is

$$P(s, \pi|\theta) = \prod_{i=1}^N \theta_i^{n_i(s, \pi)} \tag{11}$$

where  $n_i(s, \pi)$  is the number of times the parameter  $\theta_i$  is used in the path  $\pi$  for sequence  $s$ . The derivative calculation of (7) with respect to parameter  $\theta_j$  can be found in [4] :

$$\partial L_f / \partial \theta_j = -n_j(s) / \theta_j \tag{12}$$

Here  $n_j(s)$  is the expected number of times  $\theta_j$  is used by the sequence  $s$ , *i.e.*, the average of  $n_j(s, \pi)$  over all possible paths, and is calculated by standard forward-backward algorithm.

Now we calculate the gradient of the log likelihood  $L_f$  with respect to  $\hat{\theta}$ ,  $\tilde{\theta}$  and  $\lambda$ . The gradient with respect to  $\hat{\theta}$  is the same as (12). The gradient of the log likelihood  $L_f$  with respect to  $\tilde{\theta}$  is written as

$$\frac{\partial L_f}{\partial \tilde{\theta}_q^k} = \sum_{\bar{\theta}_j \in \Theta} \frac{\partial L_f}{\partial \bar{\theta}_j} \frac{\partial \bar{\theta}_j}{\partial \tilde{\theta}_q^k} = - \sum_{\bar{\theta}_j \in \Theta} \lambda_{j,k} \cdot \frac{n_j(s)}{\bar{\theta}_j} \tag{13}$$

Here  $\lambda_{j,k}$  is the  $(k + 1)$ th interpolation parameter of  $\bar{\theta}_j$  (see (5)), and  $q$  and  $j$  denote index of probability parameters in the model. And the gradient of the log likelihood  $L_f$  with respect to  $\lambda$  is written as

$$\frac{\partial L_f}{\partial \lambda_{j,k}} = \frac{\partial L_f}{\partial \bar{\theta}_j} \frac{\partial \bar{\theta}_j}{\partial \lambda_{j,k}} = -\tilde{\theta}_q^k \cdot \frac{n_j(s)}{\bar{\theta}_j} \tag{14}$$

where  $\tilde{\theta}_q^k$  contributes to  $\bar{\theta}_j$  as a  $k$ th order member.

The gradients of the other log likelihood  $L_c$  can be calculated in a similar manner. For example the gradient of  $L_c$  respect to  $\lambda$  is

$$\partial L_c / \partial \lambda_{j,k} = -\tilde{\theta}_q^k \cdot m_j(c, s) / \bar{\theta}_j \tag{15}$$



Here  $m_j(c, s)$  is the expected number of times  $\theta_j$  is used by the sequence  $s$  and giving the correct labeling  $c$ . This number can be calculated by a trivial modification of the standard forward-backward algorithm, which makes each observation only go with the model states with the same label.

**Parameter Updating Algorithm.** Here the extended Baum-Welch algorithm (EBW) [8] is used. First we define another kind of set  $\Omega$ : all values in this set sum up 1. EBW re-estimates parameters for each iteration. The updating formula is given as following using  $\lambda$  as an example:

$$\lambda_{i,j}^* = \frac{\lambda_{i,j} \left( \frac{\partial L}{\partial \lambda_{i,j}} + D \right)}{\sum_{\lambda_{i,k} \in \Omega} \lambda_{i,k} \left( \frac{\partial L}{\partial \lambda_{i,k}} + D \right)} \quad (16)$$

After some iterations,  $L$  will converge to a local optimum for a sufficiently large value of the constant  $D$ .

## 4 Application and Discussion

### 4.1 Training and Testing Datasets

Both HMMgene and our ICHMM program are trained on Genie96 dataset collected by Martin Reese ([http://www.fruitfly.org/seq\\_tools/datasets/Human](http://www.fruitfly.org/seq_tools/datasets/Human)). The dataset HMR195 by Sanja Rogic [3] is used as test dataset. It contains 195 human, mouse and rat sequences entering GenBank after Genie96 was produced.

### 4.2 Application of ICHMM for Gene Annotation

**Order of States.** In HMMgene, the coding regions were modeled by 2th order states, the inter-genic and the internal intron regions by 3th order states and the splice signal regions mostly by 1th order states. These orders gave the best estimation and generalization ability with this model structure. The structure of our ICHMM is the same as that of HMMgene. In our ICHMM, 3th order interpolated states were used for coding regions, 4th order for inter-genic and internal intron regions, and 1th order for most of exon part of splice signal regions. All the other states remain the same as fixed order states in HMMgene.

**Parameter Initiation.** First we set part of the interpolation parameters to zero so that the ICHMM was actually CHMM just the same as HMMgene. The standard Baum-Welch algorithm was used to do the optimization in (1).

After this ML estimation, we used the ad-hoc weighting approach based on  $\chi^2$  test [5] to initiate the interpolation parameters. Then interpolated states with these interpolation parameters were used to replace fixed order states in this ML trained model, which was used as our initial model for CML training.

**Procedure of CML Iteration.** During the iteration of the extended Baum-Welch algorithm the model accuracy on the test set was monitored and after

20 iterations, the model with the highest accuracy was chosen. After both our ICHMM program and the re-implemented HMMgene were trained like this, we compared their highest accuracy.

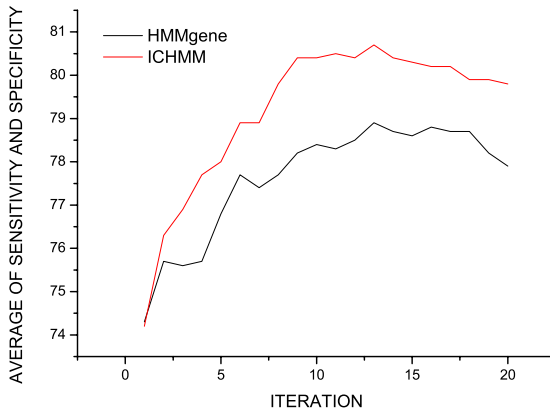
**Accuracy Comparison.** At the exon level, predicted exons (PE) are compared to annotated exons (AE). True exons (TE) is the number of predicted exons which are exactly identical to an annotated exon (i.e. both endpoints correct). Three numbers were calculated:

1. Exon sensitivity:  $S_n = TE/AE$ .
2. Exon specificity:  $S_p = TE/PE$ .
3. Average of exon sensitivity and specificity.

Table 1 shows the highest predicting accuracy on the test set of both programs. We can see our ICHMM program improves exon level sensitivity by 3% and specificity by about 1% compared to HMMgene as trained/tested on human DNA sequence dataset described above.

**Table 1.** Gene annotation accuracy comparison

| Program | Exon sensitivity | Exon specificity |
|---------|------------------|------------------|
| ICHMM   | 79.9%(757/948)   | 81.5%(757/929)   |
| HMMgene | 77.0%(730/948)   | 80.7%(730/905)   |



**Fig. 3.** The average of exon sensitivity and specificity on test set during training

The performance of HMMgene here was comparative to that presented in [3], which indicates our re-implementation of HMMgene was successful. Since HMMgene had the highest prediction accuracy from Rogic's evaluation using the same test dataset as in this work. Since then no comprehensive evaluation of ab initio gene prediction programs for human genome was published, we didn't elaborate the comparison between ICHMM and other popular predictors.

To achieve a more comprehensive comparison between the predicting ability of these two programs, we plotted the average of exon sensitivity and specificity as a function of training iterations (Fig. 3). Fig. 3 indicates that both performance lines are mono-modal during the first 20 iterations. After the performance reaches the peak value, it drops gradually because the models are getting over-fitting to the training data. In general ICHMM outperforms HMMgene in a reliable way.

### 4.3 Discussion

From the design and application detail of ICHMM, we can see the interpolation scheme here was not used to smooth the “specific probabilities” with the “general probabilities”, but to make the “good probabilities” contribute more to the interpolated probabilities. The “good probabilities” are both reliable and precise. The CMLE algorithm estimated the interpolation parameters automatically.

## 5 Conclusion

The linear interpolation scheme was introduced to the class hidden Markov models, which resulted in our interpolated class hidden Markov models. The CHMM was used in one of the best eukaryotic gene annotation systems: HMMgene. The conditional Maximum Likelihood estimation algorithm was used to estimate the interpolation parameters. Finally we applied this ICHMM for gene annotation, the final program compares favorably to HMMgene as trained and tested on Human DNA sequences. Exon level sensitivity was improved by 3% and specificity by about 1%.

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# Predicting Melting Temperature ( $T_m$ ) of DNA Duplex Based on Neural Network

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**Abstract.** In DNA computing, similar thermodynamic stability of the encoding DNA sequences is conducted to improve the reliability and precision of the computing process. The melting temperature is a suitable parameter used to evaluating the stability of DNA duplex. Traditional method to predict  $T_m$  in biological engineering may exist larger error for a few sequences. Thus it misfits the larger amount of DNA sequences in DNA computing. In this paper, we introduced artificial neural network to predict the  $T_m$  based on Next-Nearest-Neighbor model. Our result shows that the methods have a higher precision than TP methods based on nearest-neighbor model.

## 1 Introduction

The concept of DNA computing first proposed by Adleman in 1994[1]. The potential power of massive parallelism and high information density of bio-molecules offers a novel method to solve complex computational problems. Subsequently, many scientists devoted themselves to this new research area, and presented a lot of DNA computing models about combinatorial NP-complete problems.

In DNA computing, information is encoded in DNA sequences, its processing is accomplished through a series of biochemical reactions, and the retrieval of information is mainly implemented through specific hybridization between DNA sequences. Therefore, the result of DNA computing heavily depends on the biochemical reactions, which will be greatly influenced by the thermodynamic stability of DNA duplex. And melting temperature ( $T_m$ ) determination is the easiest and fastest method to evaluate the stability of a DNA duplex. So accurate prediction of DNA melting temperature is important for DNA computing.

With the primary aim of predicting DNA stability from sequence alone, one widely used method for predicting nucleic acid duplex stability uses a Nearest-Neighbor model. Several nearest-neighbor parameter sets for predicting DNA duplex stability are available in literature [2-7]. These methods can work while the number of sequences is less. According to the augment of problem scale, the number of DNA code increased

rapidly. Artificial neural network have been widely applied in performing function approximation, pattern association, and pattern classification. A study of prediction of the  $T_m$  of RNA/DNA duplexes using neural networks based on the nearest-neighbor model has been reported [8]. In order to improve the predicting precision of  $T_m$ , we established a neural network model to predict the  $T_m$  of DNA duplex based on the Next-Nearest-Neighbor parameter. And a method to obtain the eigenvector of the DNA sequences have been developed, which will be regarded as the input of neural networks.

## 2 Materials and Methods

### 2.1 Melting Temperature ( $T_m$ )

Generally,  $T_m$  is the temperature at which half of the heated DNA molecules have denatured. It is affected by the purification of DNA, the concentration of buffer solutions and the pH.  $T_m$  can be calculated according to

$$T_m = \Delta H^\circ / (\Delta S^\circ + R \ln C_t) \tag{1}$$

In which  $\Delta H^\circ$  and  $\Delta S^\circ$  is the changes enthalpy and entropy, and R is the gas constant [1.987cal/(K mol)].  $C_t$  is the mol concentration of DNA, which is replaced by  $C_t/4$  for non-self-complementary molecules.

### 2.2 Nearest-Neighbor (N-N) Model

The Nearest-Neighbor model pioneered by Borer et al in 1974[2]. In the Nearest-Neighbor model, the thermodynamic stability of a base pair is dependent on the identity of the adjacent base pairs. In duplex DNA there are 10 such unique doublets.. Table 1 listed the Nearest-Neighbor thermodynamic parameters [7].

To illustrate the calculation procedure for 5' -GCTAGC-3' next.  $C_t$  is 01.mM.

|    |    |    |    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|----|----|----|
| AA | AT | TA | CA | GT | CT | GA | CG | GC | GG |
| TT | TA | AT | GT | CA | GA | CT | GC | CG | CC |
| 0  | 0  | 1  | 0  | 0  | 2  | 0  | 0  | 2  | 0  |

Fig. 1. The number of base pairs

$$\Delta H^\circ(\text{predicted}) = \Delta H^\circ(\text{gc/cg}) + 2\Delta H^\circ(\text{ct/ga}) + \Delta H^\circ(\text{ta/at}) + \Delta H^\circ(\text{Init}) + \Delta H^\circ(\text{Sym}) = -40.7\text{kcal/mol} \tag{2}$$

$$\Delta S^\circ(\text{predict}) = 2\Delta S^\circ(\text{gc/cg}) + 2\Delta S^\circ(\text{ct/ga}) + \Delta S^\circ(\text{ta/at}) + \Delta S^\circ(\text{Init}) + \Delta S^\circ(\text{Sym}) = 114.8\text{eu} \tag{3}$$

$$T_m = \Delta H^\circ / (\Delta S^\circ + R \ln C_t) = 305.8\text{K} \tag{4}$$

**Table 1.** Thermodynamic Parameters for DNA ([Na<sup>+</sup>]=1M,pH=7) [7]

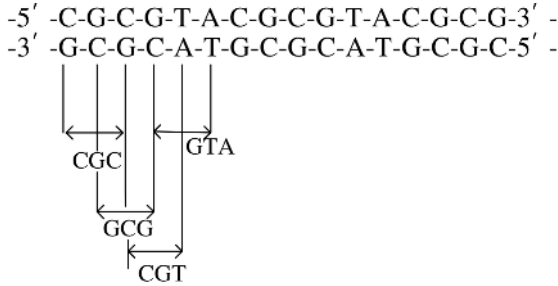
| Propagation sequence | $\Delta H(\text{kcal/mol})$ | $\Delta S(\text{eu})$ |
|----------------------|-----------------------------|-----------------------|
| AA/TT                | $-8.4 \pm 0.7$              | $-23.6 \pm 1.8$       |
| AT/TA                | $-6.5 \pm 0.8$              | $-18.8 \pm 2.3$       |
| TA/AT                | $-6.3 \pm 1.0$              | $-18.5 \pm 2.6$       |
| CA/GT                | $-7.4 \pm 1.1$              | $-19.3 \pm 2.9$       |
| GT/CA                | $-8.6 \pm 0.7$              | $-23.0 \pm 2.0$       |
| CT/GA                | $-6.1 \pm 1.2$              | $-16.1 \pm 3.3$       |
| GA/CT                | $-7.7 \pm 0.7$              | $-20.3 \pm 1.9$       |
| CG/GC                | $-10.1 \pm 0.9$             | $-25.5 \pm 2.3$       |
| GC/CG                | $-11.1 \pm 1.0$             | $-28.4 \pm 2.6$       |
| GG/CC                | $-6.7 \pm 0.6$              | $-15.6 \pm 1.5$       |
| Initiation at G-C    | 0                           | $-5.9 \pm 0.8$        |
| Initiation at A-T    | 0                           | $-9.0 \pm 3.2$        |
| Symmetry correction  | 0                           | -1.4                  |
| 5'-terminal T·A bp   | 0.4                         | 0                     |

### 2.3 Next-Nearest-Neighbor (N-N-N) Model

The different duplex sequences containing the same number of nearest-neighbors have differences in T<sub>m</sub>'s up to 5.3°C. For instance, the DNA duplexes TCTATAGA and TAGATCTA (the number of nearest-neighbors all is 0120022000, based on Scheme 1) in 1 M Na<sup>+</sup> have melting temperatures of 28.1 and 33.4°C, respectively, at the same total single strand concentration of C<sub>T</sub>=0.1 mM. Thermodynamic properties of such duplexes are not distinguishable in the N-N model, because the calculation procedure of the N-N model is based solely on the numbers of nearest-neighbors. Thus, the N-N model predicts the same T<sub>m</sub> for such duplexes and more accurate prediction cannot be obtained with the N-N model. Logical extension to possibly account for these observations would be to formulate a Next-Nearest-Neighbor model that also takes into account interactions in next-nearest-neighbor base pairs (triplets) [10].

Actually the consecutive next-nearest-neighbor subunits partially overlay each other and share the same doublet. This treatment is possible because the shorter range. Because each triplet consists of two successive N-N doublets, the N-N-N interactions are evaluated as a deviation from the average N-N interactions. For instance, triplet 5'-CGC-3' can be considered as the combination of 5'-CG-3' and 5'-GC-3' stacks. Thus, the N-N-N interaction in 5'-CGC-3' is a deviation from the average of the 5'-CG-3' and 5'-GC-3' N-N interactions. This approach to the N-N-N model is an extension of the single formalism of the N-N model.

In the N-N-N model, there are 32 possible triplets in DNA duplex. The calculating procedure for N-N-N model is illustrated at Fig.2. The DNA is 18 base pairs long. The first four triplets from the left side are marked, CGC/GCG, GCG/CGC, CGT/GCA, GTA/CAT.



**Fig. 2.** Structure and central sequences of the DNA duplex used in evaluation of next-nearest-neighbor parameters

If  $F$  denotes the times of triplet, the numbers of the 32 possible triplets in the DNA are,

|                   |                   |                   |                   |
|-------------------|-------------------|-------------------|-------------------|
| $F_{AAA/TTT} = 0$ | $F_{AAG/CTT} = 0$ | $F_{AAT/ATT} = 0$ | $F_{AAC/GTT} = 0$ |
| $F_{AGA/TCT} = 0$ | $F_{AGG/CCT} = 0$ | $F_{AGT/ACT} = 0$ | $F_{AGC/GCT} = 0$ |
| $F_{ATA/TAT} = 0$ | $F_{ATG/CAT} = 0$ | $F_{ATC/GAT} = 0$ | $F_{ACA/TGT} = 0$ |
| $F_{ACG/CGT} = 4$ | $F_{ACC/GGT} = 0$ | $F_{GAA/TTC} = 0$ | $F_{GAG/CTC} = 0$ |
| $F_{GAC/GTC} = 0$ | $F_{GGA/TCC} = 0$ | $F_{GGG/CCC} = 0$ | $F_{GGC/GCC} = 0$ |
| $F_{GTA/TAC} = 4$ | $F_{GTG/CAC} = 0$ | $F_{GCA/TGC} = 0$ | $F_{GCG/CGC} = 6$ |
| $F_{TAA/TTA} = 0$ | $F_{TAG/CTA} = 0$ | $F_{TGA/TCA} = 0$ | $F_{TGG/CCA} = 0$ |
| $F_{TTG/CAA} = 0$ | $F_{TCG/CGA} = 0$ | $F_{CAG/CTG} = 0$ | $F_{CGG/CCG} = 0$ |

The frequencies of next-nearest-neighbor triplet for a given sequence were used as the input data of the network. In order to reduce the size of the input vectors and improve the generalization of the neural network, we presented a method to obtain the eigenvector of the DNA sequences.

When sequences are synthetic and melt in a single cooperative transition, the melting temperature  $T_m$  is calculated simply as  $\Delta H^\circ / \Delta S^\circ$  [9]. Base on the N-N model, we calculated the  $\Delta H^\circ$ ,  $\Delta S^\circ$  and  $\Delta H^\circ / \Delta S^\circ$  of 32 possible next-nearest-neighbor triplets. It is showed in Table 2. The data is sorted by the values of  $\Delta H^\circ / \Delta S^\circ$  in ascending order.

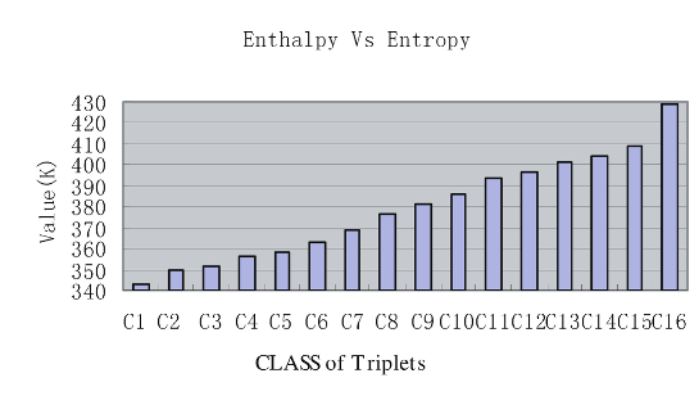
The dimension of the input vector is large to the problem. Therefore, we united the approximately data. If the difference of  $\Delta H^\circ / \Delta S^\circ$  between two adjacent triplets is less than 2, we think they should belong in one. So we divided the possible 32 triplets into 16 groups. The composition in each group is listed in Table 2.

**Table 2.** The enthalpy ( $\Delta H^\circ$ ) and entropy ( $\Delta S^\circ$ ),  $\Delta H^\circ/\Delta S^\circ$  of 30 possible next-nearest-neighbor triplets [7]\*

| G  | Triplet | $\Delta H^\circ$<br>(kcal/<br>mol) | $\Delta S^\circ$<br>(eu) | $\Delta H^\circ/\Delta S^\circ$<br>S <sup>o</sup> (k) | G   | Triplet | $\Delta H^\circ$<br>(kcal/<br>mol) | $\Delta S^\circ$<br>(eu) | $\Delta H^\circ/\Delta S^\circ$<br>S <sup>o</sup> (k) |
|----|---------|------------------------------------|--------------------------|-------------------------------------------------------|-----|---------|------------------------------------|--------------------------|-------------------------------------------------------|
| C1 | ATA/TA  | -12.8                              | -0.0373                  | 343.2                                                 | C8  | AGA/TCT | -13.8                              | -0.0364                  | 379.1                                                 |
| C2 | TAA/TT  | -14.7                              | -0.0421                  | 349.2                                                 | C8  | GAG/CTC | -13.8                              | -0.0364                  | 379.1                                                 |
| C3 | AAT/AT  | -14.9                              | -0.0424                  | 351.4                                                 | C9  | TGA/TCA | -15.1                              | -0.0396                  | 381.3                                                 |
| C4 | AAA/TT  | -16.8                              | -0.0472                  | 355.9                                                 | C9  | CAG/CTG | -13.5                              | -0.0354                  | 381.4                                                 |
| C5 | TAG/CT  | -12.4                              | -0.0346                  | 358.4                                                 | C10 | ACG/CGT | -18.7                              | -0.0485                  | 385.6                                                 |
| C5 | GTA/TA  | -14.9                              | -0.0415                  | 359                                                   | C10 | AGC/GCT | -17.2                              | -0.0445                  | 386.5                                                 |
| C6 | ATC/GA  | -14.2                              | -0.0391                  | 363.2                                                 | C10 | GCA/TGC | -18.5                              | -0.0477                  | 387.8                                                 |
| C6 | AAC/GT  | -17                                | -0.0466                  | 364.8                                                 | C10 | TCG/CGA | -17.8                              | -0.0458                  | 388.6                                                 |
| C6 | ATG/CA  | -13.9                              | -0.0381                  | 364.8                                                 | C11 | GCG/CGC | -21.2                              | -0.0539                  | 393.3                                                 |
| C6 | AAG/CT  | -14.5                              | -0.0397                  | 365.2                                                 | C12 | ACC/GGT | -15.3                              | -0.0386                  | 396.4                                                 |
| C6 | GAA/TT  | -16.1                              | -0.0439                  | 366.7                                                 | C13 | GGA/TCC | -14.4                              | -0.0359                  | 401.1                                                 |
| C7 | TTG/CA  | -15.8                              | -0.0429                  | 368.3                                                 | C14 | AGG/CCT | -12.8                              | -0.0317                  | 403.8                                                 |
| C8 | AGT/AC  | -14.7                              | -0.0391                  | 375.9                                                 | C14 | TGG/CCA | -14.1                              | -0.0349                  | 404                                                   |
| C8 | GAC/GT  | -16.3                              | -0.0433                  | 376.4                                                 | C14 | GGC/GCC | -17.8                              | -0.044                   | 404.5                                                 |
| C8 | ACA/TG  | -16                                | -0.0423                  | 378.3                                                 | C15 | CGG/CCG | -16.8                              | -0.0411                  | 408.8                                                 |
| C8 | GTG/CA  | -16                                | -0.0423                  | 378.3                                                 | C16 | GGG/CCC | -13.4                              | -0.0312                  | 429.5                                                 |

\*Solutions are 1 M NaCl sodium cacodylate, and 0.5 mM Na<sub>2</sub>EDTA, pH 7. The units for  $\Delta S^\circ$ (eu) are cal/K per mol of interaction. TAA/TTA means 5'-TAA-3' Watson-Crick base paired with 5'-TTA- 3'.

The 16 patters in Fig.3 correspond to the 16 groups of triplets. Then we calculated the frequencies of 16 patters to a DNA duplex. In this calculation, each base pair in the middle of the sequence is used three times, but each base pair at the end is used only once and each base pair next to the end is used twice. Therefore we propose the



**Fig. 3.** Class of possible triplets based on enthalpy VS entropy



two end parameters initiation C • G and initiation A • T as a correction. Initiation A • T parameter for duplexes that contain only A•T base pairs [7], then C17=1,C18=0. Initiation G • C parameter for duplexes contain at least one G • C base pair, then C17=0 and C18=1. In the Fig.3 the frequencies of the end parameters are C17=0 and C18=1. In our method the symmetry effect and the 3`-terminal phosphate present on some oligomers are ignored.

### 2.4 Back-Propagation (BP) Method

The back-propagation algorithm [11] is a generalization of the least mean squares algorithm that modifies network weights to minimize the mean square error between the desired and actual outputs of the network. The input and target vectors are used to train a network until it can approximate a function, associate input vectors with specific output vectors, or classify input vectors in an appropriate way as defined by you. Networks with biases, a sigmoid layer, and a linear output layer are capable of approximating any function with a finite number of discontinuities. The appropriate notation used in the two-layer logsig/purelin network is showed next.

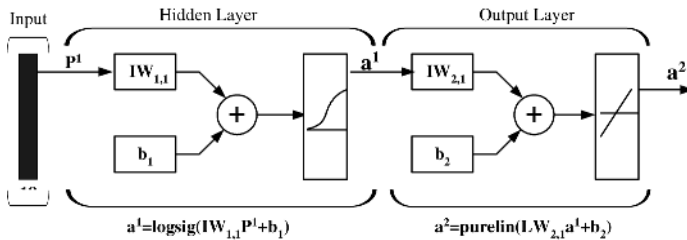


Fig. 4. Three-layer network

We constructed three-layer traditional BP neural networks with 18 neurons in the input layer, one neuron in the output layer. And we have tried six, five, four or three neurons in the hidden layer. But we found the network with four neurons in the hidden layer have the best result.

### 3 Results and Discussion

In the process of training these neural networks, the train set and test set are set as random from 84 sequences [7,12]. And there are 72 sequences in train set and 12 sequences in test set. The initial weight values are set as random real numbers and the BP method is utilized to optimize the final weights, while the supervisor is the measured Tm data. We predicted the Tm based on nearest-neighbor thermodynamic parameter (TP) [7] for comparison. To test the repeatability of neural network, we repeated the learning and testing processes using different random real numbers as initial weights and obtained very similar results.

The predicted results based on neural networks (NN) and nearest-neighbor thermodynamic parameter (TP) for the training and test sets are listed in Table 3 respectively. And the comparison of NN and TP methods is also illustrated in Fig. 5 and Fig.6.

**Table 3.** Predictions of Tm (K) by NN and TP methods for training and test set\*

| No.       | Sequences    | Experiment<br>Tm (k) | Predicted<br>Tm by NN of<br>(k) | Error<br>NN Tm<br>(k)** | Predicted<br>Tm by TP<br>(k)** | Error<br>of TP (K) |
|-----------|--------------|----------------------|---------------------------------|-------------------------|--------------------------------|--------------------|
| Train Set |              |                      |                                 |                         |                                |                    |
| 1         | ccgg         | 289.75               | 290.30                          | -0.55                   | 285.54                         | 4.21               |
| 2         | tgatca       | 294.05               | 295.35                          | -1.30                   | 289.66                         | 4.39               |
| 3         | tcatga       | 295.95               | 295.35                          | 0.60                    | 289.66                         | 6.29               |
| 4         | gcgc         | 300.65               | 301.51                          | -0.86                   | 299.35                         | 1.3                |
| 5         | tctataga     | 301.25               | 300.42                          | 0.83                    | 296.88                         | 4.37               |
| 6         | cgtgc        | 303.25               | 304.57                          | -1.32                   | 308.97                         | -5.72              |
| 7         | aataccg      | 303.45               | 303.69                          | -0.24                   | 312.33                         | -8.88              |
| 8         | ggattga      | 303.55               | 303.88                          | -0.33                   | 312.46                         | -8.91              |
| 9         | aaaaaaaa     | 304.35               | 304.53                          | -0.18                   | 305.45                         | -1.1               |
| 10        | caaaaag      | 304.65               | 304.25                          | 0.40                    | 305.84                         | -1.19              |
| 11        | agccg        | 304.75               | 305.48                          | -0.73                   | 309.65                         | -4.9               |
| 12        | gcgagc       | 306.35               | 313.05                          | -6.70                   | 322.6                          | -16.25             |
| 13        | gtgaac       | 306.35               | 302.80                          | 3.55                    | 305.1                          | 1.25               |
| 14        | tagatcta     | 306.55               | 304.88                          | 1.67                    | 296.88                         | 9.67               |
| 15        | agcttca      | 306.95               | 310.60                          | -3.65                   | 309.73                         | -2.78              |
| 16        | cgatcg       | 307.45               | 308.59                          | -1.14                   | 309.56                         | -2.11              |
| 17        | cgtacg       | 308.15               | 308.59                          | -0.44                   | 309.71                         | -1.56              |
| 18        | ggtatacc     | 309.15               | 307.54                          | 1.61                    | 313.37                         | -4.22              |
| 19        | gacgtc       | 309.25               | 310.40                          | -1.15                   | 310.09                         | -0.84              |
| 20        | ttttataataaa | 309.45               | 309.29                          | 0.16                    | 314.12                         | -4.67              |
| 21        | caaaaaag     | 310.05               | 310.89                          | -0.84                   | 312.5                          | -2.45              |
| 22        | acctagtc     | 310.45               | 312.38                          | -1.93                   | 319.52                         | -9.07              |
| 23        | accgca       | 311.15               | 310.03                          | 1.12                    | 315.6                          | -4.45              |
| 24        | aatccagt     | 311.55               | 311.88                          | -0.33                   | 313.41                         | -1.86              |
| 25        | cgggtgc      | 312.55               | 313.55                          | -1.00                   | 322.79                         | -10.24             |
| 26        | ctagtgga     | 313.45               | 314.01                          | -0.56                   | 319.4                          | -5.95              |
| 27        | caaataaag    | 314.55               | 312.44                          | 2.11                    | 313.12                         | 1.43               |
| 28        | agcgtaag     | 315.55               | 314.92                          | 0.63                    | 323.26                         | -7.71              |
| 29        | agtctga      | 315.85               | 316.56                          | -0.71                   | 318.35                         | -2.5               |
| 30        | cccggg       | 316.15               | 315.01                          | 1.14                    | 325.11                         | -8.96              |
| 31        | cgctgtaa     | 316.35               | 313.37                          | 2.98                    | 324.75                         | -8.4               |
| 32        | ggaattcc     | 316.95               | 316.73                          | 0.22                    | 318.85                         | -1.9               |
| 33        | cgatatcg     | 317.25               | 314.77                          | 2.48                    | 316.79                         | 0.46               |
| 34        | caaaaaaag    | 317.35               | 317.01                          | 0.34                    | 317.59                         | -0.24              |
| 35        | caagcttg     | 317.75               | 318.22                          | -0.47                   | 319.19                         | -1.44              |
| 36        | gggacc       | 318.05               | 317.34                          | 0.71                    | 318.46                         | -0.41              |

**Table 3.** (continued)

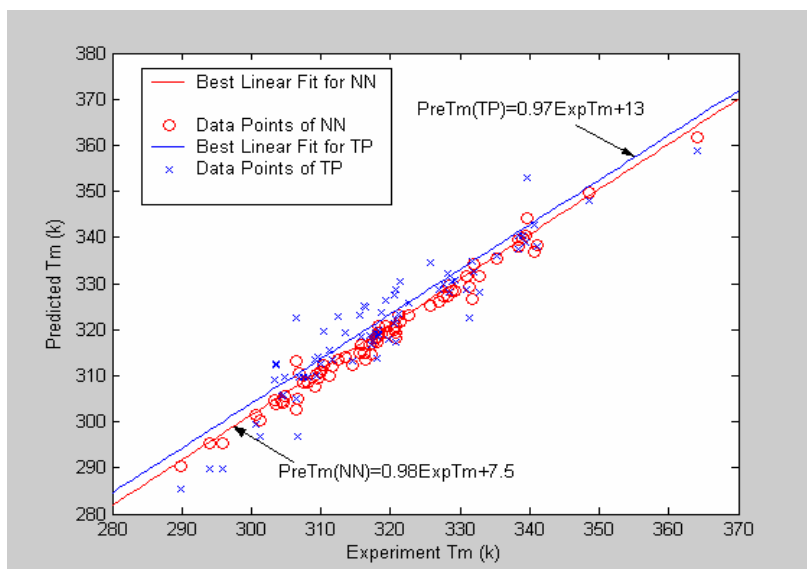
|    |                  |        |        |       |        |        |
|----|------------------|--------|--------|-------|--------|--------|
| 37 | gtagctac         | 318.05 | 318.46 | -0.41 | 313.83 | 4.22   |
| 38 | gaagcttc         | 318.35 | 319.30 | -0.95 | 318.97 | -0.62  |
| 39 | caaagaaa         | 318.35 | 320.79 | -2.44 | 319.85 | -1.5   |
| 40 | gccagtta         | 318.65 | 319.17 | -0.52 | 323.65 | -5     |
| 41 | gtcgaaca         | 319.35 | 320.67 | -1.32 | 326.45 | -7.1   |
| 42 | gatgcac          | 319.65 | 319.30 | 0.35  | 317.92 | 1.73   |
| 43 | caaacaaag        | 320.45 | 319.89 | 0.56  | 321.45 | -1     |
| 44 | gccagttaa        | 320.55 | 320.56 | -0.01 | 327.61 | -7.06  |
| 45 | gatcgatc         | 320.75 | 319.30 | 1.45  | 317.25 | 3.5    |
| 46 | gttgcaac         | 320.85 | 318.22 | 2.63  | 322.39 | -1.54  |
| 47 | agccgtg          | 320.85 | 320.93 | -0.08 | 328.73 | -7.88  |
| 48 | atctatccg        | 321.15 | 323.23 | -2.08 | 323.41 | -2.26  |
| 49 | acgacctc         | 321.35 | 321.63 | -0.28 | 330.36 | -9.01  |
| 50 | gccagttaa        | 322.55 | 323.21 | -0.66 | 325.87 | -3.32  |
| 51 | ctcacggc         | 325.65 | 325.19 | 0.46  | 334.67 | -9.02  |
| 52 | ggcgcc           | 327.05 | 325.91 | 1.14  | 328.54 | -1.49  |
| 53 | ggagctcc         | 327.55 | 327.09 | 0.46  | 329.75 | -2.2   |
| 54 | ggacgtcc         | 328.25 | 327.09 | 1.16  | 332.15 | -3.9   |
| 55 | ccgegg           | 328.35 | 329.65 | -1.30 | 328.19 | 0.16   |
| 56 | cgcgcg           | 328.85 | 328.53 | 0.32  | 330.4  | -1.55  |
| 57 | gcgcgc           | 329.25 | 328.53 | 0.72  | 330.66 | -1.41  |
| 58 | gccggc           | 330.85 | 331.60 | -0.75 | 328.54 | 2.31   |
| 59 | atgagctcat       | 331.25 | 329.35 | 1.90  | 322.66 | 8.59   |
| 60 | cacggctc         | 331.65 | 326.55 | 5.10  | 334.69 | -3.04  |
| 61 | caactgatattatta  | 331.95 | 334.17 | -2.22 | 332.42 | -0.47  |
| 62 | cggccg           | 332.75 | 331.60 | 1.15  | 328.19 | 4.56   |
| 63 | gtataccggtatac   | 335.35 | 335.36 | -0.01 | 336.13 | -0.78  |
| 64 | gcgaaaagcg       | 338.35 | 339.52 | -1.17 | 340.3  | -1.95  |
| 65 | catatggccatag    | 338.45 | 338.14 | 0.31  | 337.58 | 0.87   |
| 66 | catattggccaatag  | 339.05 | 339.87 | -0.82 | 340.27 | -1.22  |
| 67 | gtataaccggtatac  | 339.45 | 340.50 | -1.05 | 338.94 | 0.51   |
| 68 | cgcattgggtacgc   | 339.65 | 344.12 | -4.47 | 352.86 | -13.21 |
| 69 | ccatcgctacc      | 340.75 | 336.88 | 3.87  | 342.65 | -1.9   |
| 70 | gcgaattcgc       | 341.05 | 338.28 | 2.77  | 337.92 | 3.13   |
| 71 | cgcgaattcgcg     | 348.55 | 349.72 | -1.17 | 348.11 | 0.44   |
| 72 | cgcgtacgcgtacgcg | 364.15 | 361.86 | 2.29  | 358.71 | 5.44   |
|    | AME              |        |        | 1.30  |        | 3.59   |
|    | RMSE             |        |        | 1.80  |        | 4.81   |
|    | $\rho$           |        | 0.99   |       | 0.94   |        |

**Table 3.** (continued)

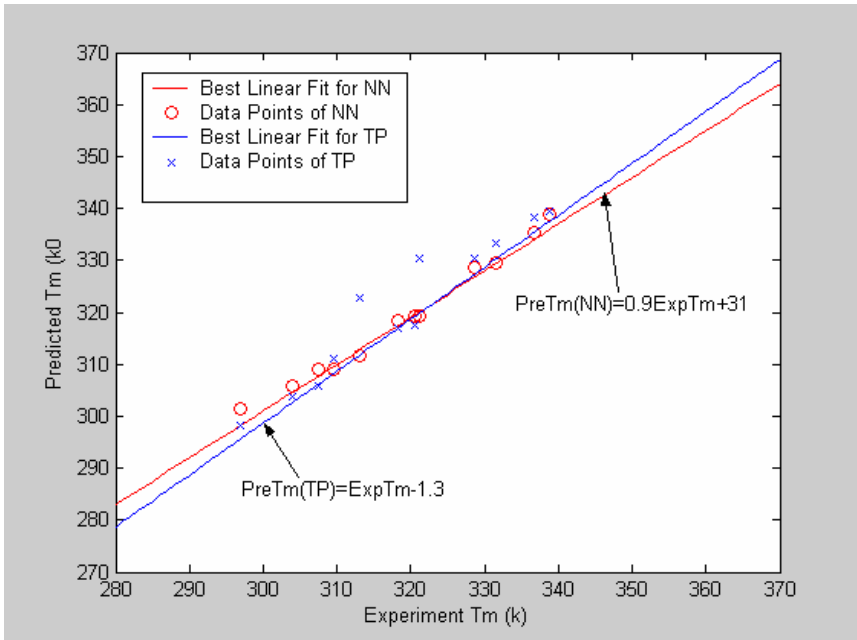
| Test Set |              |        |        |       |        |       |
|----------|--------------|--------|--------|-------|--------|-------|
| 1        | cgcg         | 296.85 | 301.51 | -4.66 | 298.1  | -1.25 |
| 2        | ggatcc       | 303.95 | 305.95 | -2.00 | 303.79 | 0.16  |
| 3        | gctagc       | 307.45 | 309.01 | -1.56 | 305.79 | 1.66  |
| 4        | gcatgc       | 309.65 | 309.01 | 0.64  | 311.16 | -1.51 |
| 5        | cacggc       | 313.15 | 311.77 | 1.38  | 322.79 | -9.64 |
| 6        | gtacgtac     | 318.25 | 318.46 | -0.21 | 317.05 | 1.2   |
| 7        | catcgatg     | 320.55 | 319.30 | 1.25  | 317.45 | 3.1   |
| 8        | cccaggg      | 321.25 | 319.36 | 1.89  | 330.33 | -9.08 |
| 9        | gcataatcgt   | 328.65 | 328.74 | -0.09 | 330.3  | -1.65 |
| 10       | cgtcgacg     | 331.45 | 329.54 | 1.91  | 333.33 | -1.88 |
| 11       | ccattgctacc  | 336.65 | 335.38 | 1.27  | 338.13 | -1.48 |
| 12       | ctgacaagtgtc | 338.85 | 338.88 | -0.03 | 339.39 | -0.54 |
|          | AME          |        |        | 1.41  |        | 2.56  |
|          | RMSE         |        |        | 1.85  |        | 3.71  |
|          | $\rho$       |        | 0.99   |       | 0.96   |       |

\* AME, absolute mean error;  $\rho$ , relation coefficient; The sequences for train and test are from [7] and [12]; RMSE, root mean square error,  $RMSE = [\sum_{i=1}^N (Xi - Yi)^2 / (N - 1)]^{1/2}$ ;

\*\*The Tm was predicted based on nearest-neighbor thermodynamic parameter (TP) [7].



**Fig. 5.** Comparison of NN and TP methods for training set



**Fig. 6.** Comparison of NN and TP methods for test set

As seen above, the predicted  $T_m$  of the train and test sets by NN methods (AME=1.3K, RMSE=1.8K,  $\rho=0.99$  for Train Set and AME=1.41K, RMSE=1.85K,  $\rho=0.99$  for Test Set) agree with the experimental data better than TP method (AME=3.59K, RMSE=4.81K,  $\rho=0.94$  for Train Set and AME=2.56K, RMSE=3.71K,  $\rho=0.96$  for Test Set). The best linear fit for NN is better than TP. The RMSE and best linear fit results of NN illuminated that most predicting  $T_m$  approached the experiment  $T_m$  well. It is possible for us to apply the methods into predicting  $T_m$  of a number of coding sequences in DNA computing.

From the sequences TCTATAGA (Exp $T_m$ =301.25k, Pre $T_m$ (NN) =300.42k, Pre $T_m$ (TP)=296.88k) and TAGATCTA (Exp $T_m$ =306.55k, Pre $T_m$ (NN)=304.88k, Pre $T_m$ (TP)=296.88k), it is showed that the methods based on next-nearest-neighbor model and neural networks distinguish the sequences have the same number of nearest-neighbors well. It can not be distinguish in the nearest-neighbor thermodynamic parameter methods (the two sequences have the same  $T_m$  296.88K).

## 4 Conclusion

Thus we can conclude that the neural network method is a reliable way to predict melting temperatures of DNA duplexes. The interactions in next-nearest-neighbor base pairs (triplets) being taken into account, we obtain higher precision in predicting the  $T_m$  than nearest-neighbor TP methods. It can be applied in the complex code designing of DNA computing, such as designing the code scheme of DNA automaton

[13]. And certainly it can be used to predict T<sub>m</sub> of DNA duplex in commonly experiment designing.

However, the methods didn't solve the problem that the sequences have the same number of nearest-neighbors but different T<sub>m</sub> completely, which is only great reduced. We hope we can discuss it in the next work.

## Acknowledgments

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# Programmable Pushdown Store Base on DNA Computing

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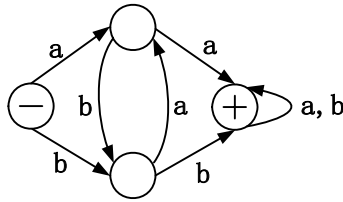
**Abstract.** DNA computing aims at using nucleic acids for computing. Micromolar DNA solutions can act as billions of parallel nanoprocessors with few consume. Finite automata is a general compute model. Now, A programmable finite automata based on DNA computing is available[1]. It's act as a basic features and processes of a finite automaton with two internal states and an alphabet comprising two input symbols. Here we describe a new finite automata made of biomolecules, which can be used as a programmable pushdown store.

## 1 Introduction

DNA computing aims at using nucleic acids for computing. The concept of the DNA computing was given by T.Head in 1987[2], Adleman's successful solution of a seven-vertex instance of the NP-complete Hamiltonian directed path problem by a DNA algorithm initiated the field of biomolecule computing in 1994[3]. In the past ten years, Both the theory and the experiment method of DNA computing was improved greatly [4-9]. The DNA computing model include: sticker system[10], splicing system[11-12] etc, the hairpin formation[13] and the plasmids[14] can be used for DNA computing too.

A DNA solution can act as billions of parallel nanoprocessors with few consume. But a particular method must be given to solve a special problem by the original DNA computing model (such as splicing system, stick model). There is no generally way to dispose all of them now. In the other hand, electronic computer can solve problem in a universal way (base Turing machine), although it's need vast time and consume. An automata made of biomolecules can combine the strongpoint of the two ways for computation.

A finite automaton  $A$  over  $\Sigma$ , where  $\hat{a} = \{s_1, s_2, \dots, s_n\}$ , is a finite directed graph in which every vertex has  $n$  arrows leading out from it, with each arrow labeled by a distinct  $s_i$  ( $1 \leq i \leq n$ ). There is one vertex, labeled by a '-' sign, called the initial vertex, and a (possibly empty) set of vertices, labeled by a '+' sign, called the final vertices. Fig 1. shows a graph which describe a certain finite automaton.



**Fig. 1.** All words over  $\Sigma$  containing two consecutive a's or two consecutive b's

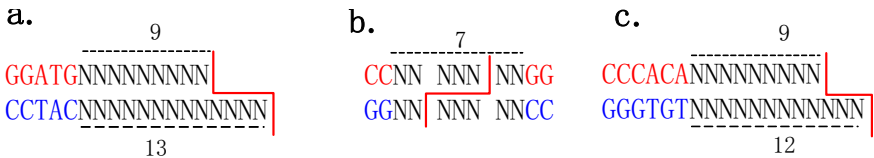
Now, the realization of computing devices operating autonomously on the molecular scale is available [15]. It's a programmable finite automaton comprising DNA and DNA-manipulating enzymes that solves computational problems autonomously. The automaton's hardware consists of a restriction nuclease and ligase, the software and input are encoded by double-stranded DNA, and programming amounts to choosing appropriate software molecules. Upon mixing solutions containing these components, the automaton processes the input molecule via a cascade of restriction, hybridization and ligation cycles, producing a detectable output molecule that encodes the automaton's final state, and thus the computational result. It's act as a basic features and processes of a finite automaton with two internal states and an alphabet comprising two input symbols.

Here we describe a new finite automata made of biomolecules, which can be used as a programmable pushdown store. A new kind of restriction nuclease is used as hardware to manipulate it.

## 2 A Simple Pushdown Store

DNA chain is combined with four kinds of base, which is A, G, C and T. If the bases were coded compatibly, then the DNA chain can considered as a data chain which can store some information.

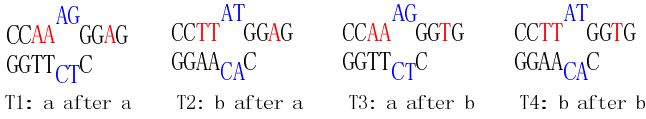
A biomolecule pushdown store have two actions, the one is “push” (write the data) and the other is “pop” (read the data). The data can be read/write by straightly get/set the DNA sequence, but this way not suitable for automata because of some extra electric instruments is needed. A new way should be find to realize the two actions of the pushdown store.



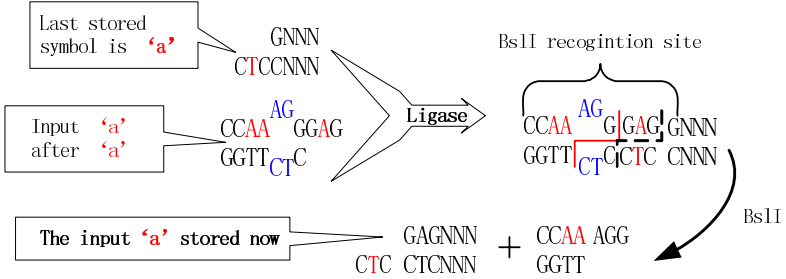
**Fig. 2.** Show the enzyme's recognition site. N for any type of base. a for FokI, b for BslI and c for RleAI.



**a. Transition molecules for push data**



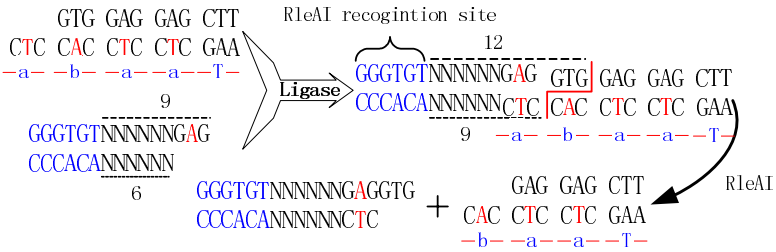
**b. mechanism of ‘push’ data**



**c. Transition molecules for pop data**



**d. mechanism of ‘pop’ data**



**Fig. 3.** **a**, the encode of the transition molecules for input, each for input an ‘a’ after an ‘a’, a ‘b’ after an ‘a’, an ‘a’ after a ‘b’ and a ‘b’ after a ‘b’. Each of the four transition molecules is encoded with two bp mismatch (the blue part), which can’t prevent the two terminal product ligate again. **b**, an example to illustrate the mechanism for ‘push’ data action of the pushdown store. One of the two terminal product of one transition is the lengthened pushdown store molecular (the left one of the ‘+’), and the other is useless now (the right one of the ‘+’). **c**, the encode of the transition molecules for pop data. T5 for pop an ‘a’ from the pushdown store, while T6 for pop a ‘b’. **d**, an example fro illustrate the mechanism for ‘pop’ data, the Terminal state is encoded with ‘GAA’(the last three bp). The data pop will not stop till the ruin of the transition data or the terminal state of pushdown is exposed.

In fact, each action of the pushdown store is similar to the state transition of a programmable automation. A model of programmable and autonomous computing machine made of biomolecules was proposed in 2001[1]. Because of the input/output DNA was cut when this computing machine complete a state transition, the input/output DNA will be shorter and shorter when the machine running. So the path of the state transition can't be save under this mechanics, neither any information can be stored.

In Benenson's automata, the restriction nuclease FokI was used to cut the DNA strain as a part of the hardware. Its recognition site can be pictured by the Fig. 2a. We can see it's hardly to increase the length of the DNA strain.

BsII (recognition site show in Fig. 2b) will be used as the part of the hardware of the new type of automata to push the data, and RleAI (recognition site show in Fig. 2c) will be used to pop the data instead of FokI.

A simple pushdown store can be constructing now. Its hardware consists of a mixture of the restriction nucleases BsII and RleAI, T4 DNA ligase and ATP.

## 2.1 Push the Data to the Store

For push the data to the pushdown store, the 'transition molecules' should be designed properly (One of the schemes show in Fig.3a), which encode the four possible transition rules and the input.

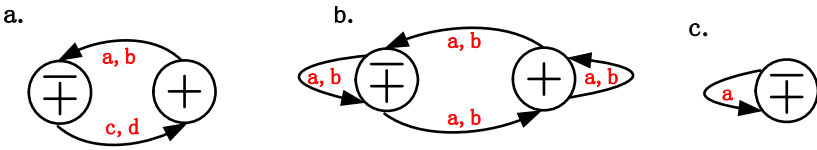
An example was given to illustrate the "push" (write the data) mechanism of the pushdown store in Fig.3b. First, add some input to the solution, in this example the input symbol is 'a'. The sticky end of the inputted transition molecule ligates to the pushdown store molecule. The product will be cleaved by BsII inside the current symbol encoding, the pushdown store molecule get a new sticky end, coded as current symbol. To prevent the leftover of the transition molecules and the store molecules ligates together again, the transition molecules is encoded with two bp mismatch. More transition molecular can be put into the solution to save the data to the pushdown store.

## 2.2 Pop the Data from the Store

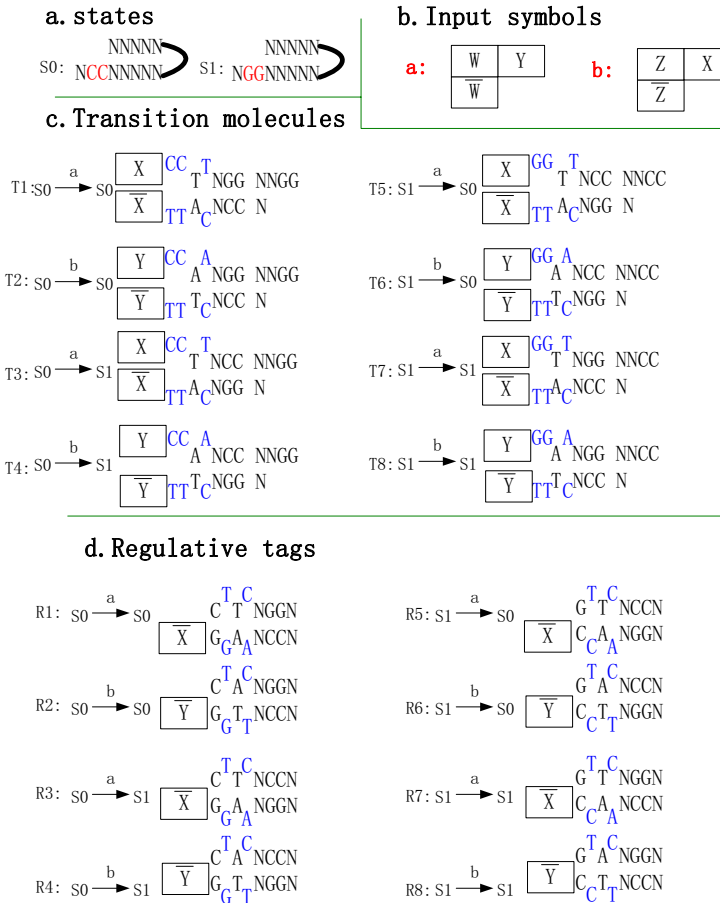
To pop the data from the pushdown store, two extra 'transition molecules' are needed (Fig.3c). The "pop" action of the pushdown store is illustrated in Fig.3d. When pop the data. First add transition molecules (T5 and T6) to the solution, one type of the transition molecules (in the example is T5) will ligates to the pushdown store molecule. The product will be cleaved by RleAI, and the cleave position between the current data's and the next data's encoding, exposing a new three-nucleotide sticky end. The "pop" action will continuous till the pushdown store reach its 'Terminal State', if the 'transition molecules are enough.

## 3 Programmable Finite Automata Based on the Pushdown Store

The simple pushdown store aforementioned can also be treated as a finite automaton. It act as a finite automaton with two internal states and an alphabet comprising for



**Fig. 4.** The states transition graph for pushdown store. **a.** the states transition graph for pushdown store when pushing data, **b.** the stats transition graph for pushdown store when popping data. **c.** The stats transition graph for pushdown store when popping data if use only one state transition molecular.



**Fig. 5.** Design detail of the molecular finite automaton. **a.** the two states of the automaton: S0 and S1. These hairpin formations are the computing molecules too. **b.** Two symbols of the input. The sticky end of one symbol can match the sticky end of the Regulative tags (Fig.5d) for another input symbol. In simple words, a match with the R2, 4, 6, 8 and b match the R1, 3, 5, 7. **c.** Eight transition molecules. The blue bp is mismatched to prevent the transition before the adding of the input symbol. Each of them will match with its Regulative tags (T1 v R1, T2 v R2... T8 v R8) and the states of the automaton. (T1, 2, 3, and 4 matched with S0, T5, 6, 7 and 8 matched with S1). **d.** Eight regulative tags.

input symbols when pushing data (Fig4.a); On the other hand, it process as a finite automaton with two internal states and an alphabet comprising two input symbols when popping data (Fig4.b). Both of the finite automata can't be programmed.

The pushdown store described before can be improve to a programmable finite automata which has two internal states (Fig. 5a) and an alphabet comprising two input symbols(Fig. 5b). Its hardware consists of a mixture of the restriction nuclease BslI, T4 DNA ligase, ATP and the computing molecules (Fig. 5a); while the software comprises eight transition molecular (Fig. 5d) and eight regulative tags (Fig.5e). The computation starts when the hardware, software and input are mixed together, one and only one type of the input molecular needed be put into the solution for one state transition.

This automaton is programmable obviously. It can be programmed by use different software, in another word choose different transition molecules and regulative tags. A selection of such programs is shown in Fig. 6a

The automaton process the input as shown in Fig. 6c. First, put one type of the input molecules into the solution ('a' in this example). Then let the double stranded software molecular to be single stranded. The input molecules will regulate the tags, in this example, the input molecules will match all regulative tags for 'b', only the

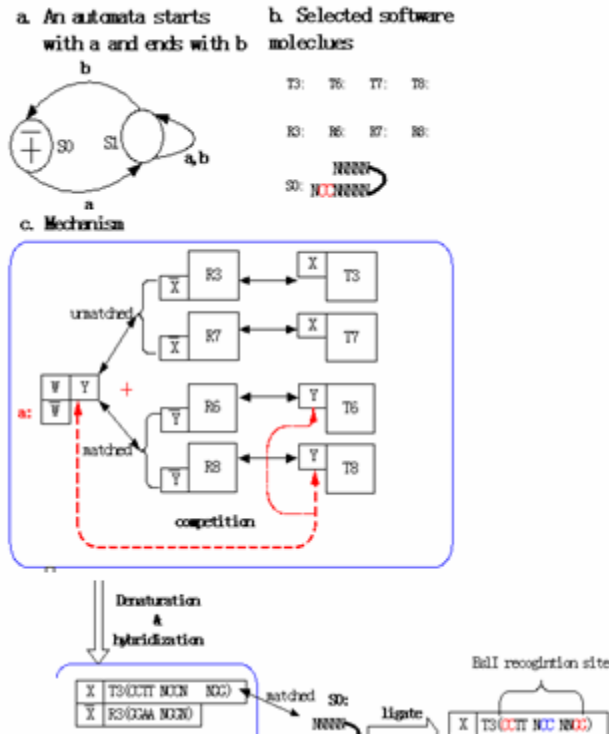


Fig. 6. Mechanism of the Molecular Automata

regulative tags for ‘a’ are active now. These tags will match with exist transition molecules, and the transition molecules match the initial states will ligate to the computing molecules. The product will be cleaved by BslI, and exposed a new sticky end which can express the new states of the automaton. The computation proceeds until no transition molecule matches the input and the states. To prevent the transition start before the input molecules adding, some base pair of the transition molecules are mismatched. (Especially the recognition site of the BslI).

The computing molecules will be lengthen when the automaton processing, and the transition history is stored in it. In this sense this automaton is a pushdown store too

## 4 Conclusion and Discussion

A simple pushdown store was described first, which can push(write, lengthen the sequence) and pop(read, shorten the sequence) data by two kinds of nucleases and exact environment. But this pushdown store can’t be programmable. An improved pushdown store was given as a finite automaton which has two internal stats (S0,S1) and an alphabet comprising two input symbols(a,b). It can not only store the transition history in the automaton computing molecules, but also be programmed by change the selection of its software molecules base on the transition map, which can used in more complex computing.

The Programmable finite automaton can be improved further. The ‘N’ in the software molecules can coded for store more information, then the Programmable finite automaton can be improved to a more powerful programmable Biomolecule pushdown store. For this, sixteen transition molecules and the corresponding regulation tags must be encoded for sixteen situations as shown in Table 1. This programmable pushdown store can be treated as a finite automation too, which have 4 internal states and 4 input symbols. For it too inconvenient to describe, this automaton will not illustrate here, and will be studied in future.

**Table 1.** The columns classify the software molecules by states transition, and the row classify it by input symbol

|           | S0 to S0 | S0 to S1 | S1 to S0 | S1 to S1 |
|-----------|----------|----------|----------|----------|
| a after a | T1       | T5       | T9       | T13      |
| b after b | T2       | T6       | T10      | T14      |
| b after a | T3       | T7       | T11      | T15      |
| a after b | T4       | T8       | T12      | T16      |

The sequence of the new automata is not shorter and shorter but longer and longer in the processing, which is the most import difference between the new automata and the Benenson’s. The added sequence can use too store some information, it can be read it one by one through the reverse procession or using some special tools. A general DNA computing model is useful for solve routine problems. And a finite automaton was realized now. But it less power than the Turing computer model. More powerful increase the state of the automaton [16]. It’s can be shown that the class of finite machines with two pushdown stores has exactly the same power as the class of Turing machines and

more pushdown stores can't strength its power. Then a pushdown stores should be designed for construct a finite automaton which as powerful as Turing machines.

Of course, all of the automation described below is more complex than before and more difficult too get a perfect result. New technical should be used in the experiment such as molecular beacon etc.

## Acknowledgment

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# Research on the Counting Problem Based on Linear Constructions for DNA Coding

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**Abstract.** This article advances linear coding construction method for DNA codes based on three-letter alphabets. Further more it also advances the new conception of Constrain Strength and algorithm of Construction and Search. We use the former to evaluate the coding amount of combinatorial constraints and use the latter to validate the evaluated results. Experiments show that experiment result accords with the theoretically evaluated value very well.

## 1 Introduction

In 1994, Adleman introduced a feasible way to solve Hamiltonian Path Problem (HPP)[1] by utilizing the biochemical experiments underlying DNA recombination and separation, thus inaugurated a new era of DNA computation. Up to this day, the encoding still is an important and difficult problem in DNA computation, because the errors of biochemical response are beyond control in DNA computation. For this reason, people hope to make up for them through appropriate DNA sequences codes. When DNA strands incompletely match, the hybridization (annealing) which performs the basic core processing may happen, thereby DNA strands form unwanted secondary structure. This is a very problematic source of errors.

In order to reduce the possibility that DNA strands form unwanted secondary structure, many researchers put forward various kinds of encoding method for DNA computing. Garzon defines DNA coding problem in computation [2]. Baum proposes a hypothesis to reduce degree of similarity with sequences of DNA [3]. Feldkamp advance another method to define similarity of DNA sequences [4]. Suyama present DNA coding number based on gene expression and analysis[5]. Frutos gives a strategy for DNA sequence designing using template [6]. Arita give another single template method for DNA computing encode[7,8]. Wenbin Liu describes a constructing method that produces more coding sequences based on template strategy[9]. Braich presents constraints for DNA sequence designing over three-letter alphabets, which is already applied in DNA computing experiment and got satisfactory result [10].

Two important factors in the DNA computing encoding are coding quality and coding amount. The higher coding quality, the more stringent the coding constraints,

and the less coding amount. In order to increase the reliability of DNA computing, we must set the strictest constraint according to codes amount, so codes amount is a very important problem in DNA sequence designing. Now articles in this aspect are very scarce, what's more, most of them only focus on single-constraint counting problem which mainly deals with the Hamming distance constraint and the length of minimal subsequences constraint[3,4]. The literature[2,11,12,13] presents codes counting expressions about the minimal Hamming distance constraint. But there are few articles about codes counting that satisfy combinatorial constraints for DNA computing.

Based on the three-letter alphabets coding strategy and linear coding theory[14], this paper successfully solve the coding counting problem for the combinatorial constraints which are the Hamming constraint for a minimal distance  $d$ , the length of minimal subsequences constraint and the fixed  $GC$ -content constraint.

## 2 DNA Codes Construction Method Based on Linear Codes

### 2.1 DNA Coding Problem

The three-letter alphabets strategy which was introduced by Braich is simple and effective. Its codes sequences contain only three bases of nucleotide  $\{A,T,C\}$  without base  $G$ , and its advantages are following. Firstly the secondary structures of DNA molecule that only contain three bases are far less than contain four bases, so it can improve biological specificity of DNA molecule very much. In the second it can decrease difficulty of biological operation, because the base  $G$  is most difficult in composed DNA molecule. But the disadvantage is that the amount of fundamental codes decrease drastically.

The DNA codes problem over three-letter alphabets may be formulated as following. For an alphabet  $\Sigma=\{A,T,C\}$ , there exists a fundamental set  $Z$  of codewords length of which is  $l$ ,  $Z=\Sigma^l=\{<b_1,b_2,\dots,b_l>|b_i \in \Sigma, i=1,2,\dots,l\}$ , obviously  $|Z|=3^l$ . Seeking a subset  $W$  of  $Z$ , which satisfy

$$\forall x_i, x_j \in W \quad \tau(x_i, x_j) \geq k$$

Where  $k$  is a positive integer,  $\tau$  is evaluation criterion of DNA codewords, such as the minimal Hamming distance, the fixed  $GC$ -content and the length of minimal subsequences. On one hand, we have to consider the size of set  $W$ (e.g.  $|W|$ ) in the DNA coding problem.

In [2,6,3,4,13], three different constraints on DNA codes are considered: the minimal Hamming distance constraint, the length of minimal subsequences constraint and the fixed  $GC$ -content constraint. The purpose of the first two constraints is to make nondesirable hybridizations between different DNA strands less likely to happen, they influence the change in the Gibb's free-energy[15] when DNA molecules hybridize, so they are important indication among biological specificity of encoded DNA molecules. The fixed  $GC$ -content constraint is used to obtain similar melting temperatures.

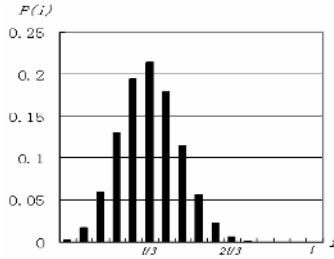


## 2.2 Constraints on DNA Coding

### 2.2.1 Fixed GC-Content Constraint

The GC-content constraint is that for each codewords  $x \in W$  there is the same GC-weight when the  $l$  length of codewords is fixed. In the fundamental codewords, eq(1) is  $C$ -weight  $i$  distribution over three-letter alphabets.

$$P_c(i) = C^i \times 2^{(l-i)} / 3^l, \quad i=0,1,2,\dots,l \tag{1}$$



**Fig. 1.** This is GC-content distribution over three-letter alphabets when  $l=15$ , values of codewords at 4,5,6 base  $C$  are largest. Without effort, the GC-content constraint is about  $1/3$ , it can preserve fundamental codewords to greatest degree.

### 2.2.2 Minimal Hamming Distance Constraint

The Hamming distance is the number of digits by which two blocks of the same length differ, the distance of words  $x_1$  and  $x_2$  marked as  $H(x_1, x_2)$ . The Minimal Hamming distance  $d$  for a DNA code  $W$  is that  $H(x_1, x_2) \geq d$  for all  $x_1, x_2 \in W$  with  $x_1 \neq x_2$ . This constraint will be enforced in all of the codes we consider, it has been proposed as a necessary criterion for reliable DNA-based computation, in a general way  $d \geq l/2$ . The bigger value of  $d$ , the more reliable computation is.

Now the question is how to construct codewords that satisfy the minimal Hamming distance constraint. We might as well denote three bases  $A, T, C$  with number  $0, 1, 2$ , so that DNA codes sequences is turned into ternary number sequences. Experiment shows that constructing DNA codes using linear system codes is an excellent method.

$$H = \begin{bmatrix} p_{11} & p_{12} & \dots & p_{1k} & 1 & 0 & \dots & 0 \\ p_{21} & p_{22} & \dots & p_{2k} & 0 & 1 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots & \dots & \dots & \ddots & \vdots \\ p_{r1} & p_{r2} & \dots & p_{rk} & 0 & 0 & \dots & 1 \end{bmatrix}, \quad p_{ij}=0,1,2 \quad (i=1,2,\dots,r, \quad j=1,2,\dots,k)$$

According to linear coding theory[14], we first search a check matrix  $H$  of  $l-k$  row and  $l$  column,  $H$  is canonical form:  $H=[P \ I]$ , let  $r=l-k$ , where  $P$  is a  $r$  row  $k$  column matrix,  $I$  is a  $r$  rank identity matrix, so as to get any  $d-1$  column of  $H$ , whose  $d-1$  column vector is linearly independence. Second, check matrix  $H$  is turned to generator matrix  $G$  using  $G=[I \ -P^T]$ , where  $I$  is  $k$  rank identity matrix,  $-P^T$  is negative transpose of matrix  $P$ . Then,  $M=\{0,1,2\}^k$ ,  $W=M \times G$ , we get codewords matrix  $W$ , each row vector of matrix  $W$  is a codeword, the minimal Hamming distance is exactly  $d$ . We call these codewords as linear codes marked as  $[l, k, d]$ .

$$|W|=3^k \tag{2}$$

If we construct codewords which satisfy the minimal Hamming distance constraint in this way, amount of codewords generated is fixed( $3^k$ ), and easy to be operated. The key part of this method is searching for check matrix  $H$  with  $(d-1)$  linearly independence columns. To construct  $[l, k, d]$  linear codes, this paper use optimum searching method to get check matrix for linear codes that have  $[20,15,4]$ ,  $[14,8,5]$ ,  $[14,7,6]$  and  $[11,3,7]$ .

**2.2.3 The Length of Minimal Subsequence Constraint**

In all subsequences of sequences, there always exists a subsequence whose minimal length is  $s+1$  and which causes the subsequence appear only in all codewords. We call such subsequence as minimal subsequences. For example:  $\{ATCCAATTC\}$  and  $\{ACTACTATCC\}$ ,  $\{ATCC\}$  is maximal repeated subsequence and  $s=4$ .

Due to overlength of minimal subsequences may bring on baneful shift hybridization, the shorter the length of minimal subsequences, the better encoding performance for DNA computing is. In general the length of minimal subsequences is less than or equals half of codewords length, e.g  $s \leq l/2$ .

The minimal subsequences with length  $s+1$  have total  $3^{s+1}$  permutations for three-letter alphabets, and each sequences of codewords contain  $l-s$  minimal subsequences. So from the upper limit of amount of codewords sequences  $|W|$ , we get eq(3).

$$|W| \leq 3^{s+1} / (l - s) \quad (s < l) \tag{3}$$

The algorithmic experiment shows that through the random algorithm the amount of codewords that satisfy the length of minimal subsequences constraint may attain  $90\% \pm 5\%$  of eq(3) with  $W$  taking the maxium value[16]. This shows that it is a feasible way to evaluate amount of codewords which must satisfy constraint of minimal subsequences length. It also shows that random algorithm can efficiently find codewords that satisfy the constraint of minimal subsequences length.

**2.3 Algorithm of Construction and Search**

Through analysis of counting problem of codewords under single constraint we find that the length of minimal subsequences constraint and the minimal Hamming distance constraint are most stringent in DNA computation. They all come down to interrelation between any two codewords in encoding space, their computational complexity is high in algorithm realization and amount of desired codewords sometimes is very scarce. Other constraints is less stringent, they only restrict single codewords, their algorithms are easy to realize and their computational complexity is not high too.

To avoid searching codewords that satisfy constraints in fundamental space that will greatly decreases size of search space, we introduce a coding design algorithm called Construction and Search. This algorithm is: first constructing primary codewords that satisfy the minimal Hamming distance constraint; then sequencely filtrating primary codewords using other constraints, using less stringent constraint first and then more stringent constraints, and finally get consequential codewords. For example, given  $d$  as the minimal Hamming distance and  $s+1$  as the length of minimal subsequences and the fixed GC-content on three-letter alphabets as  $1/3$ , the steps of this algorithmis will be:

1. Seek for linearly independence any  $d-1$  columns of check matrix  $H$  in  $GF(3)$ .
2. Generate homologous linear codes with  $H$ , construct codewords that satisfy the minimal Hamming distance is  $d$  on three-letter alphabets, get primary codewords.
3. Filtrate primary codewords using feeble constraint that is  $GC\text{-content} \approx 1/3$ , get secondary codewords.
4. Finally, filtrate secondary codewords using random algorithm that solve the problem of minimal subsequences length  $s+1$ , get resulted codewords.

As to  $[l, k, d]$  linear, there exists the relation of  $l-k \geq d+1$  [14] (not getting equal sign when codewords designed for DNA computation), so search space of wordcodes is only  $3^{-d}$  of fundamental space, thereby decrease computational complexity for search by leaps and bounds.

### 3 Counting Problem of Codewords Under Combinatorial Constraints

To effectively solve problem of codewords quality and amount, our purpose is to reward high quality of codewords and not blindly intensify constraint so that amount of codewords decreases very much. So we need to research on counting problem of codewords for DNA computation, to get expressions between amount of codewords and parameters of combinatorial constraints for counting, thus to find optimum parameters of constraints when amount of codewords is fixed.

#### 3.1 Constrain Strength

This paper introduces a new concept--Constrain Strength in order to solve counting problem of codewords that satisfy combinatorial constraints. Given  $|W|$  as maximum amount of codewords that satisfy a constraint  $\tau$ , then the Constrain Strength of constraint  $\tau$  marked as  $A(\tau)$ . The definition of  $A(\tau)$  is

$$A(\tau) = (|Z| - |W|) / |W|, |Z| \text{ is size of fundamental space of codewords} \tag{4}$$

The more stringent the constraint, the smaller the  $|W|$ , and the bigger  $A(\tau)$ . When  $|W|=|Z|$ , constraint  $\tau$  is nothing, here  $A(\tau)=0$ ; when  $|W|=0$ , constraint  $\tau$  is so stringent that no codewords can satisfy it,  $A(\tau)=\infty$ .

The length of minimal subsequences  $s+1$  marked as constraint  $\tau_s$ , according to definition we substitute eq(3) into eq(4) and get  $A(\tau_s)$ . Using  $\tau_d$  as the minimal Hamming distance constraint, we get the Constrain Strength  $A(\tau_d)$  by substitute eq(2) into eq(4) for construct  $[l, k, d]$  linear codes. The  $\tau_{sd}$  is combinatorial constraints that satisfy constraint both  $\tau_s$  and  $\tau_d$ . How to get the Constrain Strength  $A(\tau_{sd})$ ? Through a great deal of computing experiment, we have found that

$$A(\tau_{sd}) = A(\tau_s) + A(\tau_d) \tag{5}$$

Over three-letter alphabets for DNA computation, if  $n_s$  is maximal amount of codewords that satisfy constraint  $\tau_s$ ,  $n_d$  is maximal amount of codewords that satisfy

constraint  $\tau_d$  and  $n_{sd}$  is maximal amount of codewords that satisfy combinatorial constraints  $\tau_{sd}$ , by eq(5) and eq(4) we get

$$n_{sd} = \lfloor n_s n_d / ((n_s + n_d) - n_s n_d / |Z|) \rfloor \tag{6}$$

So eq(5) is true only when eq(6) is true, the evaluated result  $n_{sd}$  from eq(6) can be validated by result of construction and search algorithm. After the random algorithm is run time after time independently, we select maximal amount of resultant codewords, we get the experimental result as in table 1. The formula of evaluated result  $n_{sd}$  may be substituted using the approximate formula eq(7) in verification, see evaluated value in table 1.

$$n_{sd} \approx \lfloor n_s n_d / (n_s + n_d) \rfloor \tag{7}$$

From eq(2) we get  $n_d = 3^k$  in eq(7). From eq(3) and search efficiency (90%±5%) of random algorithm we get  $n_s$  as

$$n_s = \lfloor (\lfloor 3^{s+1} / (l - s) \rfloor) \times (90\% \pm 5\%) \rfloor \tag{8}$$

**Table 1.** Here lists all sorts of combinatorial constraints  $\tau_{sd}$  with  $d=5\sim 6$ ,  $s=4\sim 7$ , to compare maximum value of  $n_{sd}$  for evaluate and experiment. Here, we get the minimal Hamming distance  $d$  using linear codes [10,5,5], [11,5,6], [11,6,5], [12,6,6], [13,6,6] and [14,7,6].

| $l, k, d$ | $s=4$     |            | $s=5$     |            | $s=6$     |            | $s=7$     |            |
|-----------|-----------|------------|-----------|------------|-----------|------------|-----------|------------|
|           | evaluated | experiment | evaluated | experiment | evaluated | experiment | evaluated | experiment |
| 10,5,5    | 31±2      | 31         | 84±3      | 87         | 162±3     | 163        | 216±2     | 220        |
| 11,5,6    | 26±2      | 26         | 74±3      | 74         | 150±4     | 150        | 208±2     | 210        |
| 11,6,5    | 28±2      | 27         | 94±5      | 97         | 255±10    | 270        | 487±9     | 481        |
| 12,6,6    | 26±2      | 24         | 82±4      | 79         | 225±9     | 219        | 450±10    | 456        |
| 13,6,6    | 23±2      | 23         | 72±4      | 75         | 202±8     | 203        | 418±10    | 414        |
| 14,7,6    | 20±1      | 21         | 69±4      | 70         | 220±11    | 222        | 608±25    | 609        |

If we compare the values for evaluated and experiment in tab2, we find they are in accord with each other in error range. This has not only validated correctness of eq(5), but also enriched connotation of Constrain Strength. With the Constrain Strength we can solve codewords counting problem under combinatorial constraints in DNA computation.

### 3.2 Evaluated Amount of Codewords Under Three-Combination Constraints

In DNA codewords designing for computing, besides taking into account the length of minimal subsequences and the minimal Hamming distance, we also have to consider the other important factor that is the fixed GC-content. As to three-letter alphabets, from eq(1) and figure 1 we find that GC-content distribution density of fundamental codes is maximal when the GC-content locate at 1/3.

Following is the algorithm evaluated for amount of codewords that includes the fixed GC-content constraint.

1. Through linear codes $[l, k, d]$  the amount of codewords is  $n_d=3^k$ .
2. Integral of eq(1) is  $\sum_i C_i^l \times 2^{l(i-1)} / 3^l$ , from which we get amount percentage of codewords that satisfy the fixed GC-content  $i/l$  ( $i$  is weight of a codewords for base  $C$ ), then amount of linear codes that satisfy the fixed GC-content,  $n_d = \left[ 3^{k-l} \times \sum_i (C_i^l \times 2^{l(i-1)}) \right]$  (presume the GC-content distribution is identical in linear and in fundamental codes).
3. According to the length of minimal subsequence constraint and search efficiency of random algorithm, we get  $n_s$  from eq(8).
4. Finally, from eq(6) or eq(7), we evaluate amount of codewords under three-combination constraints.

**Table 2.** The values of counting codewords for evaluated and experiment compare under three-combination constraints (The value of evaluation in the table is calculated according as before-mentioned evaluational approach for amount of codewords, the experimental value is result of algorithm of Construction and Search in section 2.3, the algorithm run time after time independently on various instances, we select maximal amount of resultant codewords.)

| $l, k, d$ | $w_C(W)$ | $s=4$     |            | $s=5$     |            | $s=6$     |            | $s=7$     |            |
|-----------|----------|-----------|------------|-----------|------------|-----------|------------|-----------|------------|
|           |          | evaluated | experiment | evaluated | experiment | evaluated | experiment | Evaluated | experiment |
| 10,5,5    | 3        | 22±1      | 22         | 42±1      | 41         | 55±1      | 55         | 61±1      | 61         |
|           | 3,4      | 27±1      | 26         | 61±2      | 60         | 95±1      | 91         | 111±1     | 111        |
| 11,5,6    | 4        | 19±1      | 18         | 37±1      | 36         | 49±1      | 48         | 54±1      | 56         |
|           | 3,4      | 23±2      | 22         | 55±2      | 51         | 88±2      | 85         | 106±1     | 106        |
| 11,6,5    | 4        | 25±2      | 22         | 66±2      | 64         | 120±3     | 115        | 154±1     | 156        |
|           | 3,4      | 27±2      | 25         | 82±4      | 75         | 184±5     | 173        | 280±3     | 273        |
| 12,6,6    | 4        | 23±2      | 21         | 60±2      | 55         | 113±3     | 108        | 150±1     | 149        |
|           | 4,5      | 24±2      | 22         | 71±3      | 66         | 159±4     | 144        | 246±3     | 228        |
| 13,6,6    | 3,4,5    | 25±2      | 23         | 77±4      | 70         | 192±7     | 178        | 334±5     | 310        |
|           | 4        | 20±1      | 18         | 54±2      | 47         | 104±2     | 94         | 142±1     | 135        |
| 14,7,6    | 4,5      | 22±2      | 19         | 64±3      | 55         | 148±5     | 129        | 240±4     | 226        |
|           | 5        | 20±1      | 18         | 62±3      | 54         | 160±6     | 139        | 300±6     | 267        |
| 14,7,6    | 4,5      | 20±1      | 18         | 66±4      | 55         | 194±9     | 157        | 443±13    | 384        |

Comparing the evaluated result and experiment result in table 2, we know that the calculated value of evaluational approach accord with the result of algorithmic experiment by and large. When  $k$  increases, and amount of linear increases at exponential speed, computational quantity of filtration in algorithm increase speedly, so that the times of the algorithm running independently decrease, such causing discrepance between evaluated result and experinent increase, but range of error still is 10% inside.

So that, we can evaluate the code amount using above evulational method. Given the amount of codewords, we can select select high quality (high reliability) code-words basic parameters (code length  $l$ , GC-content, length of minimal subsequence  $s+1$  and minimal Hamming distance  $d$ ) for practical computation model. For instance, to solve three-coloring for graph of 20 vertex in DNA computation, we need 60 codewords for all color vertexs, so we may select  $(l, d, s, w_C(W))=(12, 6, 5, (4,5))$  from evaluated values in table2. Also we may select  $(11, 5, 5, 4)$  or  $(10, 5, 5, (3,4))$ . Amount of codewords for small-scale DNA computation need is not bigger than 20, then we can select  $l=11, s=4, d=6$ .

## 4 Conclusion

This paper research on codewords for DNA computing based on linear encoding method over three-letter alphabets. In it we present a new conception of Constrain Strength and evaluational approach for coding amount of combinatorial constraints. Through result of Construction and Search algorithm, we validate evaluational approach, it is useful in selecting appropriate parameters for codewords designing, it has guiding significance for DNA computing coding. The above method can also be applied to four-letter alphabets coding counting problem which satisfies some of four-letter alphabets constraints because it has much more constraints.

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# RNA Secondary Structure Prediction with Simple Pseudoknots Based on Dynamic Programming

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**Abstract.** RNA molecules are sequences of nucleotides that serve as more than mere intermediaries between DNA and proteins, e.g. as catalytic molecules. The sequence of nucleotides of an RNA molecule constitutes its primary structure, and the pattern of pairing between nucleotides determines the secondary structure of an RNA. Computational prediction of RNA secondary structure is among the few structure prediction problems that can be solved satisfactorily in polynomial time. Most work has been done to predict structures that do not contain pseudoknots. Pseudoknots have generally been excluded from the prediction of RNA secondary structures due to its difficulty in modelling. In this paper, we present a computation the maximum number of base pairs of an RNA sequence with simple pseudoknots. Our approach is based on pseudoknot technique proposed by Akutsu. We show that a structure with the maximum possible number of base pairs could be deduced by a improved Nussinov's trace-back procedure. In our approach we also considered wobble base pairings (G-U). We introduce an implementation of RNA secondary structure prediction with simple pseudoknots based on dynamic programming algorithm. To evaluate our method we use the 15 sequences with simple pseudoknots of variable size from 19 to 25 nucleotides. We get our experimental data set from PseudoBase. Our program predicts simple pseudoknots with correct or almost correct structure for 53% sequences.

## 1 General Introduction

A ribonucleic acid (RNA) is one of the two types of nucleic acids found in living organisms (the other one is deoxyribonucleic acid—DNA). An RNA molecule represents a long chain of monomers called nucleotides. RNAs contain four different nucleotides, adenine (A), guanine (G), cytosine (C), and uracil (U). RNA differs from DNA by being single stranded and by having the nucleic acid Uracil (U) replace thymine.

The sequence of nucleotides of an RNA molecule constitutes its primary structure, and the pattern of pairing between nucleotides determines the secondary structure of

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RNA. In other words primary structure is the linear sequence of nucleotides and secondary structure refers to strong intramolecular contacts between pairs of non-adjacent nucleotides, each nucleotide being paired with either none or one other nucleotide.

The most stable pairs form between GC, AU, and GU and their mirrors, CG, UA, and UG. Their stability also makes them the most common pairs. These pairs are called canonical base pairs. One of property of secondary structure is that pairs tend to form in groups yielding higher order structure. Common RNA substructures are hairpin loops, internal loops and bulges, multi-branch loops, and dangling ends. Forming adjacent pairs tends to increase the stability. These stacked pairs are also called stems, or helices.

RNA serves several functions: coding, catalysis, structure. Messenger RNA (mRNA) carries to the ribosome the coding of a gene with the introns spliced out. The ribosome translates the mRNA codon by codon to a string of amino acids. Each amino acid is brought to the ribosome by a transfer RNA (tRNA) that corresponds to the codon currently being translated. The ribosome itself is a complex consisting of proteins and ribosomal RNA (rRNA). The function of the RNA within the cell is determined in large part by the three-dimensional structure of the RNA molecule, when it folds. In turn, the three-dimensional structure is partly determined by the secondary structure of the molecule.

Determining the secondary structure of an RNA molecule is an integral part of understanding the function of the RNA molecules. Methods for determining the structure of an RNA molecule in a biology lab are expensive, and so a computational means for reliably predicting the secondary structure directly from the base sequence would be very valuable.

Thus, the knowledge of secondary and tertiary structures of an RNA molecule is highly desirable when investigating its role in a cell. Since experimental determination of RNA structure is time-consuming and expensive, its computational prediction is of great interest, and some efficient solutions are known.

## 2 Related Work

Conventionally, most methods developed so far for predicting the secondary structure of RNAs might be roughly classified into two categories: energy minimization and phylogenetic comparisons.[1,2,3]

The energy minimization technique comprises combinatorial and dynamic programming approaches, and is based on computation of the lowest free energy structure(s) of a sequence. [3,4]

The combinatorial approach first generates all the possible helices of a sequence; and in a second step a branch and bound algorithm combines compatible helices until optimal or suboptimal structures are formed [5,6]. This technique, that exhaustively search the solution space, cannot deal with sequences much longer than 200 nucleotides.

Dynamic programming approach computes the lowest free energy structure by mean of an energy base-pairing optimization based on a recursive relation between the best structures of length  $k$  and the best structures of length  $k-1$  [7,8,9,10,11].

Dynamic programming allows to treat sequences containing up to 2000 nucleotides, however such methods neither consider pseudo-knots nor find sub-optimal solutions.

A more recent method partially solves the last problem [12]. The phylogenetic methods use covariation analysis to identify conserved paired bases among a set of homologous sequences. This is a satisfying procedure that gives excellent results, including pseudo-knots identification. [2,3,11,13]

However the procedure requires a prior alignment of sequences and multiple alignment is, in turn, a difficult problem. One must also quote miscellaneous methods based either on parallel algorithms, or formal grammar, graph theory and simulation of the RNA folding process.

Recent methods intend both to align RNA sequences and to predict their consensus secondary structure[14,15,16,17,18].

Finally few recent methods have been proposed in order to predict the secondary structure, possibly including pseudoknots, of a single RNA sequence:

Rivas and Eddy [1,4,19,20] described a dynamic programming algorithm for predicting optimal RNA secondary structure, including pseudoknots. The algorithm has a worst case complexity of  $O(N^6)$  in time and  $O(N^4)$  in storage. They presented an implementation of the algorithm that generates the optimal minimum energy structure for a single RNA sequence, using standard RNA folding thermodynamic parameters augmented by a few parameters describing the thermodynamic stability of pseudoknots.

Akutsu[1] and Uemura[22] also describe dynamic programming algorithms that can handle a more general class of structures than Dirks and Pierce [23], but uses a more simplistic energy model.

Dirks and Pierce [23] described dynamic programming algorithm for computing the minimum energy structure over a more restricted class of secondary structures. This algorithm uses  $O(n^5)$  time and  $O(n^4)$  space.

### 3 Preliminaries

#### 3.1 RNA Secondary Structure

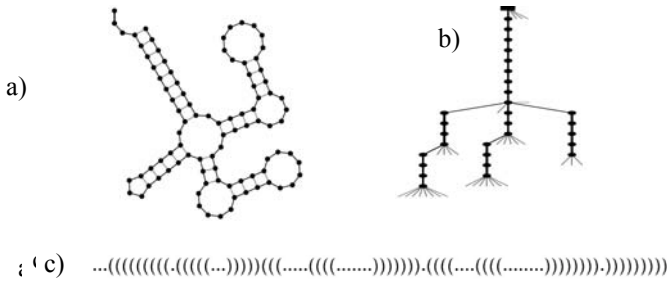
A secondary structure  $S$  is formally defined as the set of all base pairs  $(i, j)$  with  $i < j$  such that for any two base pairs  $(i, j)$  and  $(k, l)$  with  $i \leq k$  the two following conditions:

1.  $i = k$  if and only if  $j = l$ .
2. There are no knots or pseudo knots allowed. For any two base pairs  $(i, j)$  and  $(k, l)$  the condition  $i < k < l < j$  or  $k < i < j < l$  must be satisfied.

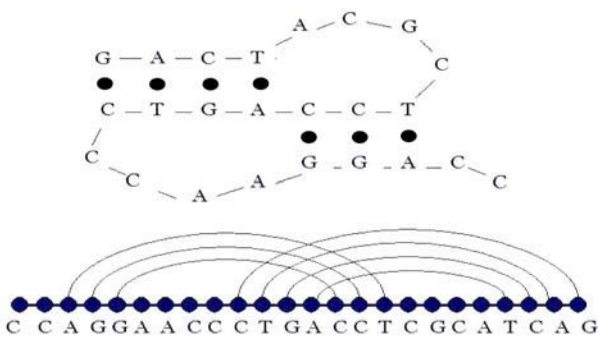
#### 3.2 RNA Secondary Structure with Pseudoknots

A folding of RNA secondary structure such as that shown in Figure 2 is a pseudoknotted structure.

To define a pseudoknot, let us consider a RNA sequence which consists of bases with index 0 to  $n$ . We also define a base-pair to be  $(i, j)$  if a base with index  $i$  form a pair with another base with index  $j$  in the same sequence. A pseudoknot is then defined as two base-pairs  $(i, j)$  and  $(i', j')$  such that  $0 < i < i' < j < j' < n$  where 0 and  $n$



**Fig. 1.** Different representations of one RNA secondary structure. Notation a) shows the secondary structure as a planar graph, b) is the corresponding tree, and c) gives the linear string encoding for the structure. There are several other representations are well known including mountain plot, circle and arc representation.



**Fig. 2.** Pseudoknotted RNA secondary structure

are the indices to the two ends of the RNA. In other words, if the base-pairs overlap each other, we have a pseudoknot as shown in Figure 2. In an arc diagram of a pseudoknotted secondary structure, at least one arc crosses another arc in the structure.

Pseudoknots can be classified into 3 main types:

- I-type pseudoknot (interior loop)
- B-type pseudoknot (bulge loop)
- H-type pseudoknot (hairpin loop)

H-type pseudoknots are the most abundant of all known pseudoknots, furthermore they are the only type of pseudoknot for which an energy model exists.

### 4 Proposed Algorithm

An RNA secondary structure prediction with simple pseudoknots which has the maximum number of base pairs can be computed by the dynamic programming algorithm in  $O(N^4)$  time and  $O(N^3)$  space.

Generally all dynamic programming algorithms have to pass three stages:

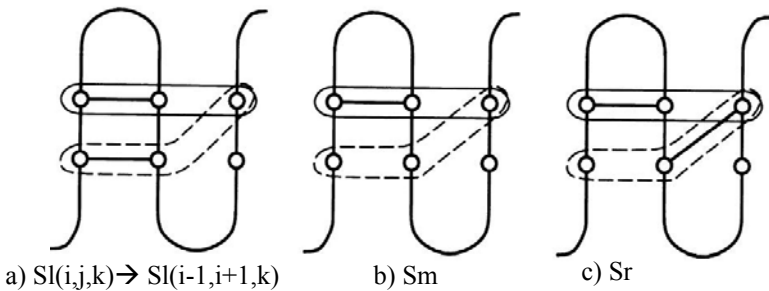
- Initialization of the matrices
- Matrix filling - scoring
- Traceback/Backtracking

Depending on the scoring function in step two several problems with different time and space complexity can be solved for a given RNA sequence.

Our approach is based on combining a dynamic programming formulation for the basic version of RNA secondary structure prediction with simple pseudoknots presented in [21] with earlier Nussinov's [8] RNA secondary structure prediction method.

We used Akutsu's algorithm to calculate Optimal score matrix and score matrix with Pseudoknotted case. In order to describe the pseudoknot algorithm we need to introduce three three-dimensional ( $N \times N \times N$ ) matrices, to be called  $Sl$ ,  $Sm$ , and  $Sr$  and one triangular  $N \times N$  matrix to be called  $PS$ .

For finding a simple pseudoknot substructure whose endpoints are  $I$ th and  $K$ th residues, the algorithm considers three types of triplets  $Sl(i, j, k)$ ,  $Sm(i, j, k)$ , and  $Sr(i, j, k)$  for each  $i, j$ , and  $k$  such that  $(I \leq i < j < k \leq K)$ .



**Fig. 3.** Illustration of the recurrence used in the dynamic programming procedure

These matrices are defined in the following way:  $Sl(i, j, k)$  is the score of the best folding between positions  $I$  and  $i$ , and  $j$  and  $k$ , provided that  $i$ th and  $j$ th residues make a base pair;  $Sr(i, j, k)$  is the score of the best folding between positions  $I$  and  $i$ , and  $j$  and  $k$ , provided that  $j$ th and  $k$ th residues make a base pair;  $Sm(i, j, k)$  is the score of the best folding between positions  $I$  and  $i$ , and  $j$  and  $k$ , provided that neither  $i$  pairs with  $j$ , no  $j$  pairs with  $k$ .  $Sp(i, j)$  is the score of the best pseudoknot fold with ending points  $i$  and  $j$ . Recurrence relations for computing these triplet can be found in (Akutsu 2000). For each pair  $(I,K)$  we compute the above three matrices and obtain the score of a pseudoknot  $Sp(I,K)$  by

$$Sp(I,K) = \max_{I < i < K} \begin{cases} SL(i, i + 1, K) \\ SM(i, i + 1, K) \\ SR(i, i + 1, K) \end{cases} \quad (1)$$

Finally, the optimal score for each pair  $(i, j)$  can be computed by the following recurrence:

$$S(i, j) = \begin{cases} PS(i, j) \\ \max \{ \mu(i, j) + S(i+1, j-1) \\ \max_{i \leq m < j} \{ S(i, m) + S(m+1, j) \} \} \end{cases} \quad (2)$$

One drawback of the original Akutsu's algorithm is, it considers only regular base pairs. RNA base pairs are the canonical Watson-Crick A-U and G-C pairs. Crick proposed, after examining how tRNAs might recognize the genetic code, that G-U is also a valid base pair in RNA secondary structure [24]. The scoring table used by the Akutsu's dynamic programming algorithm, however, only counts regular base pairs and equate A-U with G-C.

In our RNAStruct software we compensate above problem to get more good result when predicting RNA secondary structures. Our sub function basepair begins with checking regular base pairs and it returns true if *i*-th element paired with *j*-th element, also it checks given two elements is paired irregularly (G-U). Otherwise our function returns NULL value.

Our matrix for score of pseudoknot Sp and matrix for optimal score S are logical matrix defined by define preprocessor command and originally we are using P pointer with integer type to save space.

Akutsu only described the procedures for computing scores or free energies in [21], but didn't described how to trace back that the optimal scoring matrix S and, pseudoknot Sp matrix.

Trace back method of Nussinov's algorithm is valid for only pseudoknot free structures of RNA. We considered three types of triplets Sl(*i*, *j*, *k*), Sm(*i*, *j*, *k*), and Sr(*i*, *j*, *k*) when predict simple pseudoknotted RNA secondary structure. Our recursive function traceback computes traceback starting from position (*i*, *j*) and it prints matched pairs to output.txt file when it found.

Our program input is simple pseudoknotted RNA sequence without any description and comment.

And our program **RNAStruct** outputs Optimal scoring matrix S, Score of Pseudoknot Sp and matched pairs.

## 5 Experimental Review

### 5.1 Experimental Settings and Results

We predicted the structure of 15 pseudoknotted RNA sequences taken from PseudoBase. PseudoBase is a database containing structural, functional and sequence data related to RNA pseudoknots. It can be reached by its central page at <http://www.bio.LeidenUniv.nl/~Batenburg/PKB.html>. From here one can retrieve pseudoknot data as well as submit data for pseudoknots that are not yet in the database.

Average lengths of our experimental sequences taken from PseudoBase were around 20 nucleotides.

To evaluate our software we compared our result to that of the currently best known software for globally optimal RNA pseudoknot prediction developed by Elena Rivas [19]. That algorithm has a worst case complexity of  $O(N^6)$  in time and  $O(N^4)$  in storage.

**Table 1.** Some output of our RNAStruct program, PKB # is the Sequence ID on PseudoBase database, PBase is denotes the bracket view of structure on PseudoBase

|    |            |                          |
|----|------------|--------------------------|
| 1. | PKB #      | PKB86                    |
|    | Sequence   | UAGGGGCUUACCGAAAUAAGCC   |
|    | PBase      | :(((:[[[[[]]])]:::]])]:  |
|    | Prediction | ::((:[[[[[]]])]:::]])]:  |
| 2. | PKB #      | PKB96                    |
|    | Sequence   | CCGUGGCGAGUACGAUAACUCGUA |
|    | PBase      | :(((:[[[[[]]])]:::]])]:  |
|    | Prediction | ::((:[[[[[]]])]:::]])]:  |
| 3. | PKB #      | PKB63                    |
|    | Sequence   | CGUGGUGCAUACGAUAAUGCAU   |
|    | PBase      | ((:[[[[[]]])]:::]])]     |
|    | Prediction | ::(:[[[[]]]:::]])]       |
| 4. | PKB #      | PKB102                   |
|    | Sequence   | GCGUAUCUCUUAUGUCAACAGAGA |
|    | PBase      | :(((:[[[[]]])]:::]])]:   |
|    | Prediction | :(((:[[[[]]])]:::]])]:   |

Our approach is based on pseudoknot technique for maximizing the number of base pairs proposed by Akutsu[21]. The algorithm has worst case time and space complexities of  $O(N^4)$  and  $O(N^3)$ , respectively.

**RNAStruct** folds 14 pseudoknots out of 15 in the Pseudobase database. Our program predicts simple pseudoknots with correct or almost correct structure for 53% sequences. From 130 pairs which are included in our total 15 pseudoknotted sequences, we predicted total 62 base pairs.

## 6 Conclusion

We presented an implementation of RNA secondary structure prediction with simple pseudoknots based on dynamic programming algorithm. Our experimental results indicate that our approach works well.

But due to the space complexity of dynamic programming technique for maximizing the number of base pairs, our algorithm cannot deal with sequences more than 100 nucleotides.

In the future work we will consider graphical representation of RNA secondary structure prediction and we will check the possibility of new solution for predicting more long sequences (we will consider space and time complexity) of pseudoknotted RNA secondary structure.

## Acknowledgement

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# Template Frame for DNA Computing

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**Abstract.** The encoding problem is very crucial for the information processing based on DNA computing. The main difficulty lies in that it is hard to control the shift hybridization between DNA sequences. In this paper, a new data structure, named Template Frame, is proposed based on the template strategy. As the Template Frame provides an effective tool to map the various concatenations of code sequences with the template set, thus it can be used to tackle the shift distance problem.

## 1 Introduction

DNA computing is the first paradigm trying to exploits the parallelism inherent in biochemical reactions. As information is encoded with specific DNA sequences, its retrieval is mainly accomplished through specific hybridization between complementary sequences [1]. Unfortunately, hybridization between DNA sequences may take place even in imperfect matching due to the false positive and the false negative. Up to now, most efforts have been focused on designing non-interacting code set by some combinatorial constraints [2][3][4] [5][6][7][8]. Though this could help to prevent some undesired hybridizations, but they are not capable of taking into account the overlapping region between two concatenated code sequences. For example, assuming two code sequences  $s_1$  and  $s_2$  hold enough unlikeness, the concatenation of them,  $s_1s_2$ , may contain some subsequence  $s$  which still keeps a high similarity with one of the code sequences. In this case, the complementary of some sequence  $s_i$  ( $i=1,2$ ) may hybrid with  $s$  instead of its correspondent counterpart. As a matter of fact, this is the reason that makes the encoding problem hard to deal with in DNA based computing.

The template strategy proposed by Frutos et al. intends to reduce the encoding problem in alphabet  $\Sigma_{DNA}=\{A,G,C,T\}$  to two sub-problems in alphabet  $\Sigma_{01}=\{0,1\}$  [10]. Thus it is convenient for us to take further theoretical analysis on the encoding problem. In this paper, a new data structure, named Template Frame, is proposed based on the template strategy to tackle the shift hybridization in DNA computing. In section 2, we briefly review the template strategy, and then give the definition of the

template frame and some theoretical analysis. Followed by, in section 3, we present some calculation results based on several template sets and discuss the optimization of template frame. Finally, we conclude in section 4 with some discussions and some future studying directions.

## 2 The Template Frame

### 2.1 The Template Strategy

In template strategy, DNA sequence is produced as the following steps: First, positions for [AT] and [GC] are determined by a template string  $t_i = t_{i_1}t_{i_2} \dots t_{i_n} (t_{ij} \in \{0,1\})$ , where 1 indicates [AT] and 0 indicates [GC]. Second, either A or T is chosen for template positions  $t_{ij} = 1$ , and either G or C for positions  $t_{ij} = 0 (1 \leq j \leq n)$  by a map string  $m_i = m_{i_1}m_{i_2} \dots m_{i_n} (m_{ij} \in \{0,1\})$ . Thus the production rule can be formulated as: “A” is derived from 1x0, “T” from 1x1, “C” from 0x0, and “G” from 0x1. Fig.1 shows the production of a DNA sequence through its template strand and map strand.

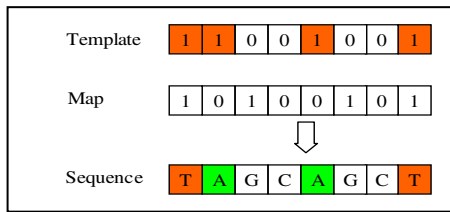


Fig. 1. A 8-mer sequence produced by a template strand and a map strand

As the likelihood of hybridization between DNA sequences decreases as the mismatches between them increases, it is usually required that the code set  $S$  should hold the following conditions:

1. In order to keep similar binding strength for all perfected matches, the GC content of the code sequences is fixed at around 50%;
2. The Hamming distance  $H(s_i, s_j) \geq d (s_i, s_j \in S)$ ;
3. The Hamming distance  $H(s_i^r, s_j^c) \geq d (s_i, s_j \in S)$ ;

where  $r$  denotes the reversal of a sequence,  $c$  denotes its Waston-Crick (in short WC) complement, and  $d$  is an integer equals to  $\lfloor n/2 \rfloor$  ( $\lfloor * \rfloor$  denotes the floor integer of a real number). The production of the code set  $S$  can be denoted as:

$$T \times M \rightarrow S \tag{1}$$

To get a further insight on the template strategy, the production of a code sequence  $s$ , its reversal  $s^r$  and its WC complementary  $s^c$  can be written as:

$$t \times m \rightarrow s \quad (5' \rightarrow 3') \tag{2}$$

$$t^r \times m^{rc} \rightarrow s^c \quad (3' \rightarrow 5') \tag{3}$$

$$t^r \times m^r \rightarrow s^r \quad (3' \rightarrow 5') \tag{4}$$

Because of the symmetry strings appeared in the template set  $T$  and the map set  $M$ , we decompose them as:

$$T = T_n \cup T_s \tag{5}$$

$$M = M_n \cup M_s \tag{6}$$

where  $T_n$  and  $T_s$  represent the non-palindrome subset and the palindrome subset respectively, and  $M_n$  and  $M_s$  are the corresponding map subset to them respectively.

**Lemma 2.1 ( the non-palindrome subset )**

For any two template strings  $t_i, t_j \in T_n$  and any two map strings  $m_p, m_q \in M_n$ , if  $H(t_i, t_j) \geq d$ ,  $H(t_i, t_j^r) \geq d$ , and  $H(m_p, m_q) \geq d$ , then all the DNA sequences  $s \in S_n$ , produced by  $T_n \times M_n \rightarrow S_n$ , will satisfy both condition 2 and 3 simultaneously.

**Lemma 2.2 ( the palindrome subset )**

For any two template strings  $t_i, t_j \in T_s$  and any two map strings  $m_p, m_q \in M_s$ , if  $H(t_i, t_j) \geq d$ ,  $H(m_p, m_q) \geq d$ , and  $H(m_p, m_q^c) \geq d$ , then all the DNA sequences  $s \in S_s$ , produced by  $T_s \times M_s \rightarrow S_s$ , will satisfy both condition 2 and 3 simultaneously.

**Theorem 2.1**

For any two template strings  $t_i \in T_n$  and  $t_j \in T_s$ , if  $H(t_i, t_j) \geq d$ , then the DNA sequences  $S = S_n \cup S_s$  will satisfy both condition 2 and 3 simultaneously.

Note: constraint  $H(t_i, t_j^r) \geq d$  in lemma 2.1 also holds for a template string itself and

$H(m_i, m_j^c) \geq d$  in lemma 2.2 also holds for a map string itself.

Then the basic idea of the template strategy can be formulated as: if the binary strings both in the template set  $T$  and the map set  $M$  hold some distance measure, then the DNA code sequences produced by them must hold some distance measures. Recently, we introduced the H–measure, proposed by Garzon [4], to the template strategy, and our result showed that it could be used to optimize the quality of sequences significantly. Detailed descriptions are recommended to refer [10][11].

**2.2 The Template Frame**

Under the template strategy, our previous work shows that the template set  $T$  plays a dominant role on the prosperities of the code set  $S$ . If we can find some data structure of the template set  $T$  to map it with the various concatenations of the code sequences, then the shift hybridization problem can be solved.

**Definition 2.2.1**

For a template set  $T=\{t_1,t_2,\dots,t_m\}$ , where  $t_i (1\leq i\leq m)$  is a binary string with length  $n$ . A template frame  $P$  of  $T$  is defined as a permutation of the  $m$  template strings

$$P=t_{i_1}t_{i_2}\dots t_{i_m}t_{i_1} \quad (1\leq i_1,i_2,\dots,i_m\leq m) \tag{7}$$

As the first template sequence appears twice in a template frame  $P$ , then its length becomes  $|P|=(m+1)n$  ( $|*|$  represent the length of a binary string). Obviously, there are  $m!$  template frames in total for template set  $T$ .

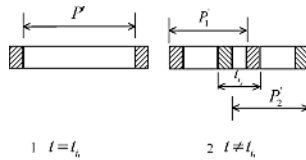
In order to count the mismatches of two strings in different length, Arita introduced a notation  $H_M(y,x) (|y|\geq|x|)$ , named the mass of string  $y$  to string  $x$ , which is defined as the minimal Hamming distance between  $|y|-|x|+1$  substrings of length  $|x|$  in string  $y$  and string  $x$  [8]. In the following, this definition of mass is also adopted.

**Definition 2.2.2**

To a template string  $t$ , the mass of template frame  $P$  is defined as:

$$\|P\|_t = \begin{cases} H_M(P',t) & t=t_{i_1} \\ \min[H_M(P'_1,t),H_M(P'_2,t)] & t\neq t_{i_1} \end{cases} \tag{8}$$

where  $P'$  is the substring of  $P$  without the terminal letters at either end;  $P'_1$  is the substring obtained by deleting the substring started at the last letter of  $t$ ;  $P'_2$  is the substring obtained by deleting the substring ended at the first letter of  $t$  ( see Figure 2 ).



**Fig. 2.** A demonstration of the subsequences  $P'$ ,  $P'_1$ ,  $P'_2$  in template frame  $P$

**Definition 2.2.3**

The mass of a template frame  $P$  for the template set  $T$  is defined as:

$$\|P\|_r = \min_{1\leq i\leq m} \|P\|_{r=t_i} \tag{9}$$

**Definition 2.2.4**

The average mass of a template frame  $P$  for the template set  $T$  is defined as:

$$Q = \sum_{i=1}^m \|P\|_{t_i} / m \tag{10}$$

Given a code set  $S$  and its template set  $T=\{t_1,t_2,\dots,t_m\}$ , strand  $W=W_1W_2\dots W_k (k\geq 1)$  is encoded under template frame  $P=t_{i_1}t_{i_2}\dots t_{i_m}t_{i_1} (1\leq i_1,i_2,\dots,i_m\leq m)$  if each of its subsequence

$W_i = s_{i_1} s_{i_2} \dots s_{i_m}$  ( $1 \leq i \leq k$ ) is composed of  $m$  code sequences whose template strings are  $t_{i_1}, t_{i_2}, \dots, t_{i_m}$  accordingly, and any code sequence  $s \in S$  is used at most once in .

**Theorem 2.2**

Under template strategy, if strand  $W$  is encoded under template frame  $P$ , then  $\|W\|_s \geq \|P\|_r$  holds. (proof is omitted)

**Proof**

For strand  $W$  encoded under template frame  $P$ , we can rewrite  $W$  and its corresponding template string  $(T)_w$  as follows:

$$W = s_{i_1} s_{i_2} \cdot s_{i_j} \cdot s_{i_m} s_{2_1} s_{2_2} \cdot s_{2_j} \cdot s_{2_m} \dots s_{k_1} s_{k_2} \cdot s_{k_j} \cdot s_{k_m} \tag{11}$$

$$(T)_w = \underbrace{t_{i_1} t_{i_2} \cdot t_{i_j} \cdot t_{i_m}}_1 \underbrace{t_{2_1} t_{2_2} \cdot t_{2_j} \cdot t_{2_m}}_2 \dots \underbrace{t_{k_1} t_{k_2} \cdot t_{k_j} \cdot t_{k_m}}_k \tag{12}$$

Under template strategy, it is easy to see that  $\|P\|_r \leq d$  always holds. Considering a code sequence  $s \in S$ , there are only two situations about its relation with strand  $W$  :

1. The code sequence  $s$  is not appeared in  $W$ , then  $\|W\|_s = H_M(W, s)$ . No loss of generality, we can assume its template string  $t = t_{i_j}$ . For clarity, we divide the subsequence in  $W$  into two groups: those share the same template string with  $t$  and the others. For the first case, the Hamming distance  $H(s_{i_j}, s) \geq d \geq \|P\|_r$  ( $1 \leq i \leq k$ ). For the second case, we have  $\|(T)_w\|_r = \|P\|_r \geq \|P\|_r$  by the equation (8), and then  $H(s', s) \geq \|P\|_r$  ( $s'$  is other subsequences in  $W$  where  $s' \neq s_{i_j}$ ). Then we have  $\|W\|_s = H_M(W, s) \geq \|P\|_r$ .
2. The code sequence  $s$  is appeared in a subsequence  $W_i$  ( $1 \leq i \leq k$ ). In this case, we have to calculate the mass of two substrands in  $W$  as in Figure 2.. By same method in used in 1, we can also reach  $\|W\|_s \geq \|P\|_r$ . Then theorem 2.2 is proved.

**3 Optimization of the Template Frame**

Theorem 2.2 shows that if the possible solution strands in DNA computing are encoded under a template frame  $P$  as that in  $W$ , then the Hamming distance between the code sequences and other subsequence in each solution strand can be held to be no less than  $\|P\|_r$  (except for the correspondent places for each code). Therefore it provides a useful data structure to improve the reliability of DNA computing. Now the problem is how to find the template frame with the largest mass  $\|P_{best}\|_r$  and average mass  $Q_{best}$ .

**Table 1.** The maximal mass  $\|P\|_r$  and  $mQ$  for different template sets with code length  $n = 8, 12$

| Label             | 8     |       |       |       |       | 12    |       |       |
|-------------------|-------|-------|-------|-------|-------|-------|-------|-------|
|                   | T1    | T2    | T3    | T4    | T5    | T1    | T2    | T3    |
| 0011              | 3(31) | 4(32) | 2(28) | 3(30) | 2(27) | 4(38) | 4(41) | 4(39) |
| 1100              | 3(31) | 4(32) | 2(28) | 3(30) | 2(27) | 4(43) | 4(43) | 4(36) |
| 0101              | 3(28) | 3(31) | 3(29) | 3(30) | 3(30) | 4(39) | 4(40) | 2(36) |
| 1010              | 3(28) | 3(31) | 3(29) | 3(30) | 3(30) | 4(36) | 3(35) | 2(36) |
| 0110              | 2(28) | 0(28) | 0(27) | 0(24) | 2(28) | 4(39) | 2(30) | 4(38) |
| 1001              | 2(26) | 0(28) | 0(27) | 0(24) | 2(28) | 4(42) | 4(38) | 4(40) |
| 00011             |       |       |       |       |       | 4(44) | 4(43) | 4(44) |
| 11000             |       |       |       |       |       | 5(46) | 4(45) | 3(37) |
| 01100             |       |       |       |       |       | 4(44) | 4(39) | 4(44) |
| 00110             |       |       |       |       |       | 4(44) | 4(42) | 5(44) |
| 10001             |       |       |       |       |       | 4(44) | 4(38) | 4(36) |
| none              | 1(12) | 1(11) | 1(10) | 0(9)  | 0(8)  | 2(19) | 2(22) | 2(21) |
| Average H-measure | 3.6   | 3.5   | 3.4   | 3.3   | 3.2   | 5     | 5.03  | 4.9   |

Table 1 shows the largest mass  $\|P\|_r$  and its corresponding  $mQ$  (in parentheses) for several template sets with code length 8 and 12. The results show:

1. The addition of suitable labels can greatly improve the quality of a template frame. The largest mass  $\|P\|_r$  and  $mQ$  are 1(12) and 2(22) respectively as the template strings are directly concatenated. In [10], the authors added a pair of labels at both ends of the code sequences to reduce the slide match. Here we introduce it to the template frame, the calculation results show that the property of a template frame can be improved significantly by using suitable labels, and the largest mass  $\|P\|_r$  and  $mQ$  are 4(32) and 5(46) respectively. In order to keep the uniform of GC content, we require the labels should also have a “01” content about 50%.
2. The average H-measure has a great influence on the property of a template frame. Generally speaking, if a template set has a larger average H-measure, it tends to have a larger mass  $\|P\|_r$  and parameter  $mQ$ .
3. The increase of the labels’ length can also improve the mass  $\|P\|_r$  and  $mQ$  of a template frame. The drawback of increasing the label length is that it also leads to the increase of the code length. So we should take a trade off between the quality of a template frame and the code length in practice. A parameter  $\sigma$  can be used to take an evaluation on this aspect:

$$\sigma = \frac{\|P_l\|_r / \|P\|_r}{n+l} = \frac{n\|P_l\|_r}{(n+l)\|P\|_r} \tag{13}$$

where  $P_l$  denotes the template frame with labels, and  $l$  denotes the length of it. For example in code length  $n=8,12$ , parameter  $\sigma$  can be calculated respectively as:  $\sigma_8 = \frac{n\|P_l\|_r}{(n+l)\|P_l\|_r} = \frac{8 \times 4}{(8+4) \times 1} = \frac{8}{3}$  and  $\sigma_{12} = \frac{n\|P_l\|_r}{(n+l)\|P_l\|_r} = \frac{12 \times 5}{(12+5) \times 2} = \frac{30}{17}$ . By its definition, it is easy to see that  $\sigma$  is actually a ratio of the relative mass for template frame  $P$ . Theoretically, the length of labels can be increased until the maximal  $\sigma$  is achieved.

Under template strategy, we can get lots of template sets satisfying the constraints in section 2.1 through a random search algorithm. So it is a hard problem for us to find a template set that has the largest mass  $\|P\|_r$  and largest average mass  $Q$ . However we find a template with relative good property by two steps:

1. Find the template sets with a larger average H-measure;
2. As the size of the template set  $T$  is relatively small, take an exhaustive search for the  $m!$  template frames for each template set with different labels.

## 4 Conclusions

One of the challenges in the encoding problem of DNA computing is the shift hybridization between DNA sequences. In order to tackle this problem, a new concept—Template Frame is proposed. As the template frame provides a useful data structure that set up a map between the combination of code sequences and its template set, then the shift hybridization in DNA computing can be effectively avoid by a suitable template frame. The template frame proposed by this paper can be easily adopted to models which has no special requirement on the arrangement of the code sequences, such as the DNA algorithms for the Graph Coloring Problem, the Minimal Set Covering Problem, the SAT problem, the construction of a DNA database proposed by Reif [12], and the design of DNA chips.

Although our result is exciting, there are still some open problem needed further research: First, theoretical analysis of the mass of the template frame and its optimization; Second, how to apply the template frame in those algorithms where the possible solution space are concatenated according to some constraints, for example the Directed Hamiltonian Path Problem in Adleman's paper[1].

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# A New DNA-Based Approach to Solve the Maximum Weight Clique Problem<sup>\*</sup>

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**Abstract.** Given an undirected graph with weights on the vertices, the maximum weight clique problem is to find a subset of mutually adjacent vertices, i.e. a clique, which have the largest total weight. We devised a new *DNA* encoding method to solve the maximum weight clique problem whose basic idea is that each vertex on weighted graph is encoded by two *DNA* strands of different length and each edge is encoded by one *DNA* strand with a length of 20. The longer *DNA* strand corresponding to vertex  $v_i$  consists of three parts and its center part is with a length of  $w_i$ ; the shorter *DNA* strand is the reverse complementation of the longer one's center part. We also gave the corresponding molecule algorithm and its biological implementation. The proposed *DNA* computing method can be expanded to solve other *NP*-hard problems, and it provides further evidence for the ability of *DNA* computing to solve numerical optimization problems.

## 1 Introduction

Based on the massive parallelism of *DNA* computing, many researchers tried to solve a host of difficult problems, especially *NP* problems. In 1994, Adleman[1] solved a 7-vertex instance of the *Hamiltonian path* problem by means of the molecular biology techniques, which was published in *Science*. The creative research opened up a new way to computation using *DNA* molecules.

A major goal of subsequent research in this area is to understand how to solve *NP*-complete problems. To address this goal, Lipton[2] abstracted a parallel model of molecular computation in 1995 on the basis of Adleman's experiment, and used it to solve the 3-*SAT* problem; Ouyang et al[3] solved the *maximal clique* problem(MCP) in 1997; Head et al[4] solved the *maximal independent set* problem using operations on *DNA* plasmids in 2000; Sakamoto et al[5] presented a molecular algorithm of Boolean calculation by *DNA* hairpin formation. These previous researches in *DNA*

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computing do not require the consideration of weight representation in *DNA* strands. However, there are many practical applications related to weights, such as the *shortest path* problem, the *traveling salesman* problem, the *minimum spanning tree* problem, and the *maximum weight clique* problem (MWCP).

To represent weight in the *DNA* computing model, Narayanan et al[6] presented a conceptual weight encoding method for the *shortest path* problem; Shin et al[7] proposed a weight representation method of varying the number of hydrogen bonds in fixed-length *DNA* strands for the *traveling salesman* problem; Yamamura et al[8] gave a concentration control method for the *shortest path* problem; Lee et al[9] proposed a melting temperature control method for the *traveling salesman* problem; Yin[10] introduced two weight encoding methods for the *minimum spanning tree* problem and the Chinese postman problem; Ma et al[11] introduced a *DNA* computing model for MWCP which is based on plasmids. The existing weight encoding methods are suitable for the specific instances, but they cannot be easily generalized. So we need to do further research on weight encoding method.

In this paper, we devised a new weight encoding method and a corresponding *DNA* algorithm for MWCP. It is organized as follows. In Section 2, we describe a new *DNA* encoding method for MWCP. In Section 3, we present a *DNA* algorithm based on the proposed encoding method and analyze its time complexity and space complexity. Section 4 gives the implementation of the *DNA* algorithm using biological operations. Section 5 compares the new *DNA* computing model with Ouyang's algorithm[3]. Finally, in Section 6, we draw some conclusions.

## 2 DNA Encoding Method for MWCP

In order to be convenient for describing the new *DNA* encoding method, we firstly give the representation method of orientation of *DNA* strand.

### 2.1 Orientation Representation of *DNA* Strand

When one *DNA* molecule combines with another to form a *DNA* strand, 5'-phosphate group of one nucleotide always combine with 3'-hydroxyl group of another nucleotide by phosphodiester bonds, shown in Fig.1. This is called as 5'-3' orientation or 3'-5' orientation[12]. In Fig. 1(a), the nucleotide with 5'-free end is located at the most left end and the nucleotide with 3'-free end is located at the most right end, which is marked as 5'-AGC-3' or 5'-AGC; In Fig. 1(b), the nucleotide with 3'-free end is located at the most left end and the nucleotide with 5'-free end is located at the most right end, which is marked as 3'-CGA-5' or 3'-CGA. In fact, 5'-AGC is the same as 3'-CGA, which can be seen by overturning Fig. 1(b). In order to be convenient for description, 5'-AGC is written as AGC, and 3'-CGA is written as -CGA in this paper. Note that -CGA=AGC.

*Definition 1.* For any a *DNA* strand  $s$ , let  $h$  represent a mapping function from each base to its Watson-Crick complementary base, or  $h(A)=T$ ,  $h(G)=C$ ,  $h(C)=G$ ,  $h(T)=A$ . The obtained *DNA* strand is called the *complementary strand* of  $s$ , and its reversal is called the *reverse complementation* of  $s$ .

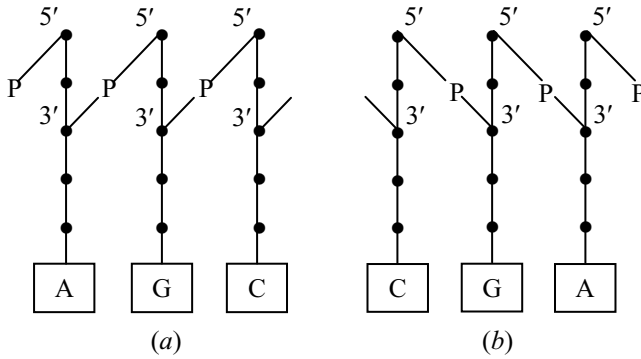


Fig. 1. Orientation of DNA strand

Let  $s=AGC$ . Its complementary strand is  $h(s)=TCG$ , and its reverse complementation is  $-h(s)=-TCG=GCT$ . Obviously, the DNA strand  $AGC$  can combine with  $GCT$  to form a double-stranded DNA (dsDNA) through hydrogen bonds. In general, the DNA strand  $s$  can combine with its reverse complementation  $-h(s)$  to form a dsDNA through hydrogen bonds.

### 2.2 DNA Encoding Method for MWCP

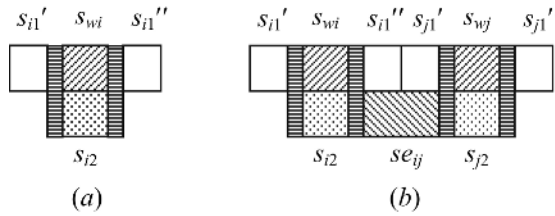
MWCP can be described as follows: For an undirected graph  $G=(V,E)$ ,  $v_i \in V$ ,  $e_{ij} \in E$ , where the weight on vertex  $v_i$  is  $w_i$ ,  $w_i \geq 0$ ,  $w_i \in \mathbb{Z}^+$ , it is to find a subset of mutually adjacent vertices which has the largest total weight. We suppose that  $G$  is a simple graph, or there aren't parallel edges on it. The DNA encoding method is as follows.

1) For any vertex  $v_i \in V$ , we use two DNA strands,  $s_{i1}$  and  $s_{i2}$ , to encode it. The longer DNA strand  $s_{i1}$  consists of three parts, which are respectively marked as  $s_{i1}'$ ,  $s_{wi}$  and  $s_{i1}''$ , where  $s_{wi}$  is with a length of  $w_i$ , and  $s_{i1}'$  or  $s_{i1}''$  is with a length of 10, that is, the longer DNA strand  $s_{i1}=s_{i1}'s_{wi}s_{i1}''$  is with a length of  $20+w_i$ . The shorter strand  $s_{i2}$  is the reverse complementation of  $s_{wi}$ , or  $s_{i2}=-h(s_{wi})$ . Obviously, the code  $s_{i2}$  can combine with the center part of  $s_{i1}$  to form a fragment of dsDNA. After each vertex is encoded, we embedded restriction sequences at both sides of  $s_{wi}$  and  $s_{i2}$ . The codes of vertex  $v_i$  are shown in Fig. 2(a).

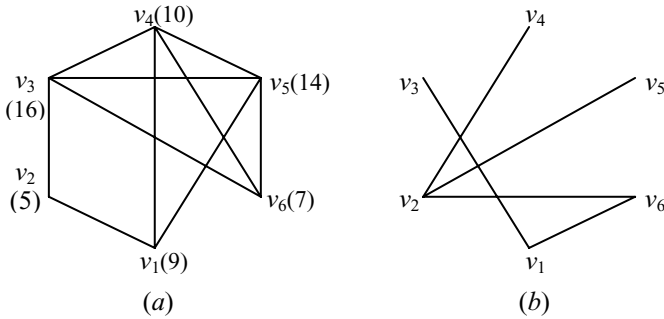
2) For any edge  $e_{ij} \in E$ , we encode it using the DNA strand  $se_{ij}$  which is the reverse complementation of the last part of  $s_{i1}$  and the first part of  $s_{j1}$ , or  $-h(s_{i1}''s_{j1}')$ . Obviously, the DNA strand  $se_{ij}$  is with a length of 20. Thus, the DNA strands corresponding to vertices  $v_i, v_j$  can combine with the DNA strand corresponding to edge  $e_{ij}$  to form a stable dsDNA, as shown in Fig. 2(b).

Take the graph shown in Fig. 3(a) as an example, where the number in each bracket represents the weight of the corresponding vertex. We illustrate the proposed DNA encoding method in the following.

<sup>1</sup> If  $w_i$  is a real number, all the weights multiplied by a certain integer (i.e. 10) and then they are rounded into integers.



**Fig. 2.** The DNA strands  $s_{i1}$  and  $s_{i2}$  to encode vertex  $v_i$  and the joint of DNA strands  $s_{i1}$ ,  $s_{i2}$ ,  $s_{j1}$ ,  $s_{j2}$  and  $se_{ij}$  to encode vertices  $v_i, v_j$  and edge  $e_{ij}$



**Fig. 3.** A weighted graph and its complementary graph

For the vertices  $v_1, v_2, \dots, v_6$  in Fig. 3(a), the following DNA strands  $s_{11}, s_{12}, s_{21}, s_{22}, \dots, s_{61}, s_{62}$  are respectively selected to encode them.

- $s_{11}=ATATCGCGGG-TTCAACGTG-CTCAACGTGC$
- $s_{12}=-h(TTCAACGTG)=CACGTTGAA$
- $s_{21}=CAGTTGACAT-GCAGG-ATCGAATCGA$
- $s_{22}=-h(GCAGG)=CCTGC$
- $s_{31}=TATAGTACTG-ATCGTAGTCAGTACTG-ATCGTAGTCA$
- $s_{32}=-h(ATCGTAGTCAGTACTG)=CAGTACTGACTCCGAT$
- $s_{41}=AACCTGGTAC-CAAGCTTGAC-CAAGCTTGAC$
- $s_{42}=-h(CAAGCTTGAC)=GTCAAGCTTG$
- $s_{51}=TGGTTTGGAC-TGGTCAAGTTGGAC-TGGTCAAGTT$
- $s_{52}=-h(TGGTCAAGTTGGAC)=GTCCAAGTTGACCA$
- $s_{61}=TTTAGCGCAT-GCAGGAT-CGAGGATCGA$
- $s_{62}=-h(GCAGGAT)=ATCCTGC$

For any edge  $e_{ij}$  in Fig. 3(a), we use one DNA strand  $se_{ij}=-h(s_i''s_j')$  to encode it. Consider the edges linked to vertex  $v_1$ . The corresponding codes are as follows:

- $se_{12}=ATGTCAACTGGCACGTTGAG$
- $se_{14}=GTACCAGGTTGCACGTTGAG$
- $se_{15}=GTCCAAACCAGCACGTTGAG$

When we select the above DNA strands to encode the vertices and the edges, we must avoid the following situations[13]: (1) one part of a DNA strand may combine with another part of it through intercrossing in a molecule; (2) one DNA strand may

combine with another *DNA* strand through intercrossing between molecules; (3) one *DNA* strand may combine with other two or more *DNA* strands through intercrossing between molecules.

With the help of the property of *reverse complementation* between the *DNA* strands, the codes corresponding to vertices can combine with the codes corresponding to edges to form many *dsDNAs*, some of which are given in Fig. 4.

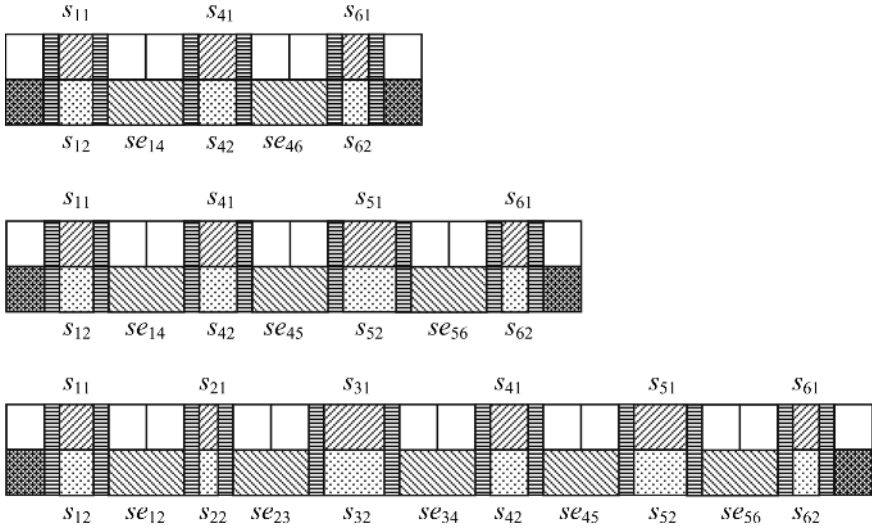


Fig. 4. Joint of the vertex codes and the edge codes

### 3 DNA Algorithm for MWCP

MWCP has been proved to be *NP*-complete. The determinate algorithms of solving it are with exponential time complexity. By means of massive parallel computation of *DNA* molecules and the principle of Watson-Crick complementary bases, the optimal solution of MWCP can be found in polynomial time. In order to be convenient for describing the *DNA* algorithm, we firstly give the definition of *complementary graph* in the following.

*Definition 2.* Given an undirected graph  $G$ , the graph  $G'$  containing all edges missing in  $G$  is called the *complementary graph* of  $G$ . For example, Fig. 3(b) is the *complementary graph* of Fig. 3(a). In this paper, the number of edges in the *complementary graph* is marked as  $nc$ .

Obviously, any two vertices connected in the *complementary graph* are disconnected in the original graph, so they cannot be members of the same clique. Thus, we can give the new *DNA* algorithm of solving MWCP as follows:

(1) For any vertex  $v_i \in V$ , two *DNA* strands,  $s_{i1}$  and  $s_{i2}$ , are used to encode it. The *DNA* strand  $s_{i1} = s_{i1}' s_{wi} s_{i1}''$  is with a length of  $20 + w_i$ , where the length of  $s_{wi}$  is equal to  $w_i$  and the length of  $s_{i1}'$  and  $s_{i1}''$  is 10 respectively. The strand  $s_{i2} = -h(s_{wi})$ ;

- (2) For any edge  $e_{ij} \in E$ , the DNA strand  $se_{ij} = -h(s_{i1}''s_{j1}')$  is used to encode it. Obviously,  $se_{ij}$  is with a length of 20;
- (3) By means of *merge* operation, sufficient DNA strands  $s_{i1}$ ,  $s_{i2}$  and  $se_{ij}$  ( $1 \leq i, j \leq n$ ) are mixed together in a single ligation reaction;
- (4) Let  $sumw = \sum_{i=1}^n w_i$ . Based on the principle of Watson-Crick complementary bases, the various dsDNAs are generated randomly, and the dsDNAs starting with  $v_1$  and ending at  $v_n$  are amplified by polymerase chain reaction (PCR) with the primers  $-h(v_1)$  and  $-h(v_n)$ . Only those amplified dsDNAs whose length is equal to or less than  $sumw$  are saved. The set of the saved dsDNAs is called the complete data pool;
- (5) Digesting the dsDNAs in the complete data pool with restriction enzymes. The enzymes break DNA at specific restriction sites, which were embedded within the sequences for  $v_i$  ( $1 \leq i \leq n$ );
- (6) For  $k:=1$  to  $nc$  do {For any edge  $e_{ij}$  in the complementary graph, let  $sumw = sumw - \min\{w_i, w_j\}$ . Separate away all the dsDNA whose length is above to the updated  $sumw$ ;
- (7) Separate the longest dsDNAs in the remaining data pool by means of gel electrophoresis;
- (8) Sequencing the longest dsDNAs to determinate its nucleotides sequence. The sequence corresponds to the optimal solution.

In the following, the time complexity of the DNA algorithm is analyzed according to the data structure used in the algorithm<sup>[14,15]</sup>. The steps 1 and 2 are preliminaries for DNA computing. The steps 3 and 4 are irrelevant to the scale of problem, so their time complexity is  $O(1)$ . In steps 5 and 6, the digestion operation need to do  $nc$  times which is at most  $n(n-1)/2$ , so its time complexity is  $O(n^2)$ . In steps 7 and 8, separating and sequencing the paths are irrelevant to the scale of problem, so their time complexity is  $O(1)$ . Therefore, the total time complexity of our DNA algorithm is  $O(n^3)$ , where  $n$  is the number of vertices in graph  $G$ .

The space complexity of the DNA algorithm is analyzed as follows. In step 1, the number of the vertex codes is  $2n$ . In step 2, the number of the edge codes is  $m$ ,  $m = O(n^2)$ . Let  $d_i$  denote the degree of vertex  $v_i$  in graph  $G$ , and  $d_{max}$  denotes the maximum of all the vertex degrees. In step 3 and 4, the number of the dsDNAs in the complete data pool is  $O(C_{d_1}^1 C_{d_2}^1 C_{d_3}^1 \dots C_{d_{n-1}}^1) = O(d_{max}^n)$ . In steps 5 and 6, the digestion operation doesn't increase the number of storage unit, so its space complexity is still  $O(d_{max}^n)$ . In steps 7 and 8, the separating and sequencing operations doesn't increase the number of storage unit either, so its space complexity is also  $O(d_{max}^n)$ . Therefore, the total space complexity of our DNA algorithm is  $O(d_{max}^n)$ .

#### 4 Biological Implementation of DNA Algorithm

By means of the basic molecular biological operations, the steps 1~4 and 6~8 in the DNA algorithm can be easily carried on. In the following, we only give the implementation of step 5. In step 5, the dsDNAs are digested by restriction enzymes. The restriction enzymes break the dsDNAs at specific restriction sites, which were embedded within the sequences for  $v_i$  ( $1 \leq i \leq n$ ).

To cut a connection in the *complementary graph*, for example, the 1-3 connection, we first divided the dsDNAs into two test tubes,  $t_0$  and  $t_1$ . In  $t_0$  we cut the DNA fragments located at the center part of the codes corresponding to  $v_1$  with specific restriction enzymes; in  $t_1$  we cut the DNA fragments located at the center part of the codes corresponding to  $v_3$  with other specific restriction enzymes. And then we combined  $t_0$  and  $t_1$  into test tube  $t$ , which didn't contain the codes corresponding to  $v_1$  and  $v_3$  at the same time. Let  $sumw = sumw - \min\{w_1, w_3\}$ .

By  $nc$  sequential restriction operations with different enzymes, all the DNA fragments connected by the edges in the *complementary graph* are digested. Each time of digesting the DNA fragments connected by edges  $e_{ij}$  in the *complementary graph*, let  $sumw = sumw - \min\{w_i, w_j\}$ . Thus, through  $n-1$  times digestion operations, the total weight value of the remaining dsDNAs is less than or equal to the updated  $sumw$ .

## 5 Comparison with Ouyang's DNA Algorithm

At present, there exists some previous works<sup>[1-9,11,16-20]</sup> to compute NP problems with DNA molecules. Our DNA computing method for MWCP is an improvement on Ouyang's algorithm[3] of solving MCP. The main improvements are as follows. (1) On the basis of Ouyang's DNA computing model, we added weight representation in DNA strands. Thus, it can be expanded to solve NP-hard problems. (2) In Ouyang's algorithm of solving MCP, the number of elements in the complete data pool is  $O(n^n)$ , or its space complexity is  $O(n^n)$ . And in our DNA algorithm for MWCP, the number of elements in the complete data pool is  $O(d_{max}^n)$ , or its space complexity is  $O(d_{max}^n)$ . Obviously, the number of storage unit used in our DNA algorithm is less than that in Ouyang's algorithm because the degree of any vertex is always less than the number of vertices in graph. So our DNA algorithm is with less space complexity than Ouyang's algorithm. (3) In Ouyang's algorithm, all the combinations of vertices are in the complete data pool, whereas in our algorithm, those vertices disconnected by edge in graph  $G$  aren't in the complete data pool. So the number of DNA molecules being cut in each digestion operation is reduced in our algorithm.

## 6 Conclusion

We presented a new weight encoding method and the corresponding molecular algorithm for MWCP. The results show that a series of biological experiment operations successfully find the optimal solution of the MWCP instance shown in Fig.3(a), which consists of 10 edges and 6 vertices with six different costs. One of the most important features of our weight encoding method is that it uses two DNA strands of different length to encode one vertex, or it can handle quantitative expression of numerical values using DNA strands of different length. The ability of representing and manipulating numerical data opens up the possibility of solving a wide range of numerical optimization problems. Our work provides further evidence for the ability of DNA computing to solve numerical optimization problems.

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# A New DNA Encoding Method for Traveling Salesman Problem\*

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**Abstract.** We have devised a new *DNA* encoding method to represent weight and apply it to solve the traveling salesman problem, an instance of optimization problems on weighted graphs. For any weighted graph  $G=(V,E)$ ,  $v_i \in V$ ,  $1 \leq i \leq n$ , where exists weight  $w_{ij}$  on edge  $v_i v_j$ , we use two *DNA* strands with different lengths to encode each of the edges. The longer *DNA* strand consists of three parts: one for the departure vertex, another for the weight, and the last for the arrival vertex. The shorter *DNA* strand is the *reverse complementation* of the center part of the longer one. The proposed weight encoding method is an improvement on the previous weight encoding methods, and it can more easily find the optimal solutions than the former ones. This work extends the capability of *DNA* computing to solving numerical optimization problems, which is contrasted with other *DNA* computing methods focusing on decision problems.

## 1 Introduction

*DNA* computing is a computational paradigm that uses synthetic or natural *DNA* molecules as information storage media, in which the techniques of molecular biology, such as polymerase chain reaction(*PCR*), gel electrophoresis, and enzymatic reactions, are used as computational operators for copying, sorting, and splitting/concatenating the information respectively.

Based on the massive parallelism of *DNA* computing, many researchers tried to solve a host of difficult problems. In 1994, Adleman [1] solved a 7-vertex instance of the *Hamiltonian path* problem by means of the molecular biology techniques. The creative research opened up a new way to computation using *DNA* molecules. A major goal of subsequent research in this area is to understand how to solve *NP*-complete problems. To address this goal, Lipton [2] abstracted a parallel model on the basis of Adleman's experiment, and applied it to solve the 3-*SAT* problem; Ouyang *et al* [3] solved the *maximal clique* problem; Head *et al* [4] solved the *maximal independent set* problem based on *DNA* plasmids; Sakamoto *et al* [5] presented a *DNA* algorithm of Boolean calculation by *DNA* hairpin formation. These previous

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researches do not require the consideration of the representation of weight in *DNA* strands. However, many practical applications involve weighed graphs. The representation of weight in *DNA* strands is an important issue toward expanding the capability of *DNA* computing to solve numerical optimization problems. There exists previous work to represent weight with *DNA*. Narayanan *et al* [6] presented a conceptual encoding method that represents costs with the lengths of *DNA* strands. Shin *et al* [7] proposed a method to represent real numbers by varying the number of hydrogen bonds. Yamamura *et al* [8] gave a concentration control method which encodes weight by the concentrations of *DNA* strands. Lee *et al* [9] introduced a melting temperature control method which represents costs by melting temperatures of fixed-length *DNA* strands. Yin [10] presented a kind of weight encoding method which can be easily generalized.

In this paper, we introduce a new weight encoding method in which two *DNA* strands with different lengths are designed to encode one edge to improve the previous work. The *traveling salesman* problem (*TSP*) is used as a test problem for the proposed weight encoding method. This paper is organized as follows. In Section 2, we describe a new *DNA* encoding method to represent weight. Section 3 describes a *DNA* algorithm of solving *TSP* based on the proposed encoding method. Section 4 gives the implementation of the *DNA* algorithm using biological operations. Section 5 compares the new *DNA* encoding method with the previous encoding methods. Finally, in Section 6, we draw some conclusions.

## 2 DNA Encoding Method for TSP

Representation of weight for weighted-graph problems is one of the most important but challenging problems. This paper presents a new weight encoding method that can more easily find the optimal solution than the former ones. In order to be convenient for description, we firstly give the orientation representation of *DNA* strand.

### 2.1 Representation of DNA Orientation

When one *DNA* molecule combines with another to form a *DNA* strand, 5'-phosphate group of one nucleotide always combine with 3'-hydroxyl group of another nucleotide by phosphodiester bonds. This is called as 5'-3' orientation or 3'-5' orientation. The nucleotide with 5' free-end being located at the most left end and 3' free-end being located at the most right end is marked as 5'-XX...X-3', and the nucleotide with 3' free-end being located at the most left end and 5' free-end being located at the most right end is marked as 3'-XX...X-5', where *X* denotes a letter in the set {A,G,C,T}. In this paper, 5'-AGTC-3' is briefly written as *AGTC*, and 3'-CTGA-5' is written as -*CTGA*. Note that -*CTGA*=*AGTC*.

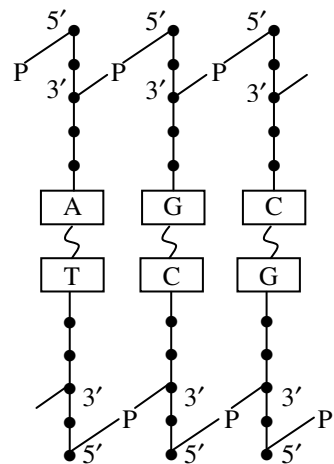


Fig. 1. A double-stranded *DNA*

*Definition 1.* For any DNA strand  $s$ , let  $h$  represent a mapping function from each base to its Watson-Crick complementary base, or  $h(A)=T, h(G)=C, h(C)=G, h(T)=A$ . The obtained DNA strand is called as *complementary strand* of  $s$ , and its reversal is called as *reverse complementation* of  $s$ . The mapping function  $h$  is called as *complementary mapping*.

Take the double-stranded DNA (dsDNA) shown in Fig. 1 as an example. Let  $s=AGC$ . Its *complementary strand* is  $h(s)=TCG$ , and its *reverse complementation* is  $-h(s)=-TCG=GCT$ . Obviously, the DNA strands  $AGC$  and  $GCT$  can combine with each other to form a dsDNA through hydrogen bonds. In general, DNA strand  $s$  and its *reverse complementation*  $-h(s)$  can combine with each other to form a dsDNA through hydrogen bonds.

## 2.2 DNA Encoding Method for TSP

TSP is to find a minimum cost path for a given set of cities and roads. The path must begin at a specified city and end there after passing through all the given cities. TSP can be abstracted as follows: for a connected, weighted, undirected graph  $G=(V,E), v_i \in V, 1 \leq i \leq n$ , where the weight on edge  $v_i v_j$  is  $w_{ij}, w_{ij} \geq 0, w_{ij} \in Z^1$ , it is to find a circuit with minimum weight which begins at a specified vertex and ends there after through all the given vertexes. We suppose that  $G=(V,E)$  is a simple graph just as well, or there aren't parallel edges on it. The DNA encoding method for TSP is as follows.

1) For any vertex  $v_i(1 \leq i \leq n)$ , DNA stand  $s_i$  of length 20 is used to encode it.

2) For any edge  $v_i v_j(1 \leq i, j \leq n)$ , we encode it using two different length DNA strands. The longer strand  $s_{ij1}$  consists of three parts, which are respectively marked as  $s_{ij1}', s_{ij1}'', s_{ij1}'''$ , where  $s_{ij1}'$  is the *reverse complementation* of the second half of  $s_i, s_{ij1}''$  is the *reverse complementation* of  $s_{wij}$  whose length is equal to  $w_{ij}$ , and  $s_{ij1}'''$  is the *reverse complementation* of the first half of  $s_j$ . The shorter strand  $s_{ij2}$  is the *reverse complementation* of  $s_{ij1}'$ . Specifically,  $s_i$  and  $s_j$  are respectively divided into two substrands with equal length, or  $s_i = s_i' s_i'', s_j = s_j' s_j''$ . The longer DNA strand  $s_{ij1} = -h(s_i'' s_{wij} s_j')$ , whose length is  $20 + w_{ij}$ , and the shorter DNA strand  $s_{ij2} = -h(s_{ij1}') = s_{wij}$ .

Note that, for any undirected edge  $v_i v_j$ , when walking from  $v_i$  to  $v_j$ , the longer code  $s_{ij1}$  is the *reverse complementation* of  $s_i'' s_{wij} s_j'$ , or  $s_{ij1} = -h(s_i'' s_{wij} s_j')$ , and the shorter code  $s_{ij2} = -h(s_{ij1}') = s_{wij}$ ; when walking from  $v_j$  to  $v_i$ , the longer code  $s_{ji1}$  is the *reverse complementation* of  $(-s_j)'' (-s_{wij}) (-s_i)'$ , or  $s_{ji1} = -h((-s_j)'' (-s_{wij}) (-s_i)') = h(s_i'' s_{wij} s_j') = -s_{ij1}$ , and the shorter code  $s_{ji2} = -h(s_{ji1}') = -s_{wij} = -s_{ij2}$ . That is, only need  $s_{ij1} = -h(s_i'' s_{wij} s_j')$  and  $s_{ij2} = s_{wij}$  to encode edge  $v_i v_j$ .

Take the weighted graph  $G$  shown in Fig. 2 as an example. We specifically analyze the pro-posed DNA encoding method. For the vertices  $v_1, v_2, \dots, v_7$ , the following DNA strands  $s_1, s_2, \dots, s_7$  are respectively selected to encode them.

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<sup>1</sup> If  $w_{ij}$  is a real number, all the weights multiplied by a certain integer (i.e. 10) and then they are rounded into integers.

$s_1=ATATCGCGGGTTCAACGTGC,$   
 $s_2=CAGTTGACATGCAGGATCGA,$   
 $s_3=TATAGTACTGATCGTAGTCA,$   
 $s_4=AACCTGGTACCAAGCTTGAC,$   
 $s_5=TGGTTTGGACTGGTCAAGTT,$   
 $s_6=TTTAGCGCATGCAGGATCGA,$   
 $s_7=GTTACGTGAGTCTGACTGAC.$

For any edge  $v_i v_j$ , we use two different length DNA strands  $s_{ij1}=-h(s_i''s_{wij}s_j')$  and  $s_{ij2}=s_{wij}$  to encode it. For example, the codes of edge  $v_1 v_2$  are as follows:

$s_{121}=-h(s_1''s_{w12}s_2')=-h(TTCAACGTGCAGTGCATGCTGATCGATGCAGTTGACAT)$   
 $=-AAGTTGCACGTCACGTACGACTAGCTACGTCAACTGTA$

$s_{122}=s_{w12}=AGTGCATGCTGATCGATG$

The DNA strands  $s_1, s_2, s_{121}$  and  $s_{122}$  can combine with each other, as shown in Fig.3.

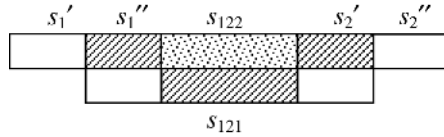


Fig. 3. Joint of DNA strands  $s_1, s_2, s_{121}$  and  $s_{122}$

Based on Fig.3, the next is to extend forward right to  $s_3$  or  $s_6$  and to extend forward left to  $s_7$  or  $s_6$ . The right extension is shown in Fig.4, and its left extension can be similarly drawn.

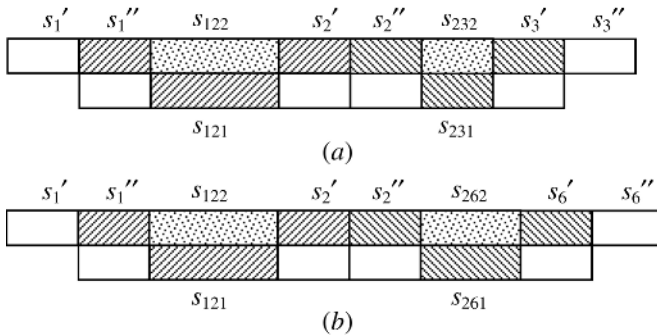


Fig. 4. The right extension of Fig.3

On the basis of Fig. 4(a), the next is to extend forward right to  $s_4, s_5$  or  $s_6$ , and to extend forward left to  $s_7$  or  $s_6$ , and so on. Thus, with the help of the property of reverse complementation between the vertex codes and edge codes, the dsDNAs may extend continually to form various random paths including the optimal solution.

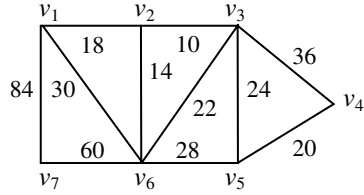


Fig. 2. A weighted graph

### 3 DNA Algorithm for TSP

*TSP* has been proved to be *NP*-hard. The determinate algorithms of solving it so far have only complete enumeration, which is with exponential time complexity. By means of massive parallel computation of *DNA* molecules and the principle of Watson-Crick complementary bases, the optimal solution of *TSP* can be found in polynomial time. We suppose that  $v_1$  is the original vertex just as well. This is because that, for any a shortest circuit  $C$  going through all the given vertexes, the length of the route which begins at  $v_1$  and ends there along  $C$  is equal to that of the route which begins at  $v_i$  ( $i \neq 1$ ) and ends there along  $C$ .

Note that our *DNA* algorithm searches for the shortest *path* instead of the shortest *circuit*. This is because that the length of a shortest path which begins at  $v_1$  and end there after going through all the given vertexes is equal to that of a shortest circuit which begins at  $v_1$  and end there after going through all the given vertexes. Moreover, *PCR* in the biological techniques is generally carried out on a linear template, and there isn't circular template so far.

In order to generate more molecules which correspond to the optimal solution, we add the primer  $-h(s_1')$  to one end of the *PCR* template and add the primer  $-h(s_1'')$  to another end. For the *DNA* strand  $s_1$  given in section 2, the primers are as follows:

$-h(s_1') = -h(ATATCGCGGG) = -TATAGCGCCC$

$-h(s_1'') = -h(TTCAACGTGC) = -AAGTTGCACG$

The *DNA* algorithm of *TSP* is given as follows:

(1) By means of *merge*<sup>2</sup> operation, sufficient *DNA* strands  $s_i$ ,  $s_{ij1}$  and  $s_{ij2}$ ,  $1 \leq i, j \leq n$ , are mixed together in a single ligation reaction, and the primers  $-h(s_1')$  and  $-h(s_1'')$  are respectively added to the two ends of the *PCR* template;

(2) Based on the principle of Watson-Crick complementary bases, randomly generate various *DNA* molecules corresponding to the random paths;

(3) Separate away all the paths without the departure vertex  $v_1$ , or separate away all the *DNA* molecules without 5'-end being  $s_1$ ;

(4) Separate away all the paths without the arrival vertex  $v_1$ , or separate away all the *DNA* molecules without 3'-end being  $s_1$ ;

(5) For each vertex  $v_i$  ( $2 \leq i \leq n$ ), separate away all the paths without  $v_i$ ;

(6) Separate the shortest path by means of gel electrophoresis;

(7) Sequencing the shortest path to determinate its nucleotides sequence. The sequence corresponds to the optimal solution.

In the *DNA* algorithm of *TSP*, the steps of inputting *DNA* strands, generating various random paths, and separating away all the paths without  $v_1$  are irrelevant to the scale of problem, so the time complexity is  $O(1)$ ; for each vertex  $v_i$  ( $2 \leq i \leq n$ ), separating away all the paths without  $s_i$  is relevant to the number of vertexes in  $G$ , so its time complexity is  $O(n)$ ; separating the shortest path through agarose gel electrophoresis and sequencing the shortest paths are irrelevant to the scale of problem, so the time complexity is  $O(1)$ . Therefore, the total time complexity of *DNA* algorithm is  $O(n)$ , where  $n$  is the number of vertexes in  $G$ .

<sup>2</sup> The function and implementation of *merge* is given in section 4.

## 4 Biological Implementation of DNA Algorithm

By means of the molecular biology techniques, the steps 1, 2 and 6 can be easily carried on. In the following, we only give the implementation of steps 3~5 and 7.

### 4.1 Separation of Random Paths

The various random paths generated in our *DNA* algorithm are put in a tube  $N$ , and then heat the tube to make the dsDNAs become *DNA* strands. Through *separate* operation, all the paths without the departure vertex  $v_1$  are separated away, or remain the *DNA* molecules with 5'-free end being  $s_1$ ; and then separate away all the paths without the arrival vertex  $v_1$  from the *DNA* molecules with 5'-free end being  $s_1$ , or remain the *DNA* molecules with 5'-free end and 3'-free end being  $s_1$ . Finally, through a  $n-1$  times circle of *separate* operations, separate away all the paths without  $s_i(2 \leq i \leq n)$ . The *DNA* program is as follows:

- Step 1.  $N \leftarrow B(N, s_1)$ ;
- Step 2.  $N \leftarrow E(N, s_1)$ ;
- Step 3. FOR  $i:=2$  TO  $n$  DO  $N \leftarrow +(N, s_i)$ ;

### 4.2 Sequencing the Shortest Paths

The *DNA* molecules with  $s_1$  being at the two ends and including  $s_i(2 \leq i \leq n)$  are separated through agarose gel electrophoresis, and the furthest *DNA* molecules correspond to the shortest paths. By means of *PCR* amplification and purification, it is carried out several times to increase its purity. Sequencing the shortest paths to determinate its nucleotide sequence. The sequence corresponds to the shortest circuit.

## 5 Comparison with Other DNA Encoding Methods

For the classical *NP*-hard problems, there exists previous work to represent the numerical values with *DNA*. Narayanan *et al*[6] presented a conceptual encoding method which represents costs with the lengths of *DNA* strands. This method requires very long *DNA* strands to solve an instance containing a wide range of costs, and this makes experimental implementation impossible. Shin *et al*[7] proposed a method to represent weight by varying the number of hydrogen bonds. Although the number of hydrogen bonds is an important factor in deciding the thermal stability of *DNA* strands, it is not a sufficient factor. Yamamura *et al*[8] proposed a concentration control method which encodes the weights using the concentrations of *DNA* strands. Though they showed the possibility of concentration control method, they failed in finding the final solution. Lee *et al*[9] proposed a melting temperature control method which represents costs by melting temperatures of fixed-length *DNA* strands. All of the above methods are suitable for some specific instances, but they cannot easily be generalized. Yin[10] introduced a kind of weight encoding methods which can easily be generalized whose feature is that the edge code is divided into three parts, and the center part is used to represent weight. This makes the generated paths in a single

ligation reaction are alternant DNA strands or double strand, as shown in Fig.5. Since the stable structure of DNA molecules is dsDNA, the part of DNA strand easily combined with other molecules through hydrogen bonds based on the principle of Watson-Crick complementary bases. Therefore, the methods affected the generation of the optimal solution when the difference between the biggest weight and the smallest weight is large or when the lengths of DNA strands are large.

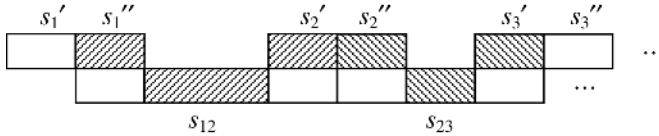


Fig. 5. Alternant DNA strand or double strand

Our weight encoding method is an improvement on the previous encoding methods, and it can more easily generate the optimal solutions than the former ones. In our encoding method, each vertex  $v_i$  ( $1 \leq i \leq n$ ) is encoded using DNA strand  $s_i$  of length 20, and each edge is encoded using two different length DNA strands: the longer strand  $s_{ij1}$  consists of three parts, which are respectively marked as  $s_{ij1}'$ ,  $s_{ij1}''$ ,  $s_{ij1}'''$ , where  $s_{ij1}'$  is the reverse complementation of the second half of  $s_i$ ,  $s_{ij1}''$  is the reverse complementation of  $s_{wij}$  whose length is equal to  $w_{ij}$ , and  $s_{ij1}'''$  is the reverse complementation of the first half of  $s_j$ ; the shorter strand  $s_{ij2}$  is the reverse complementation of  $s_{ij1}''$ . Thus, the generated random paths in a single ligation reaction are dsDNAs, as shown in Fig.4. The generated dsDNAs are more stable than alternant DNA strand or double strand, so our encoding method can generate the optimal solution even when the difference between the biggest weight and the smallest weight is large or when the lengths of DNA strands are large. Moreover, the proposed weight encoding method is suitable for the larger scale graph at least in theory, and it can be generalized and implemented automatically. Our weight encoding method also has characteristics of easy encoding and low error rate.

## 6 Conclusion

We presented a new weight encoding method and an associated molecular algorithm for TSP. The results show that a series of biological experiment operations successfully find the optimal solution of the TSP instance shown in Fig. 2, which consists of 7 vertexes and 11 edges of eleven differing cost values. One of the most important features of our weight encoding method is that it uses two different length DNA strands to encode one edge, or it can handle quantitative expression of numerical values using DNA strands with different lengths. The ability of representing and manipulating numerical data in DNA computing opens up the possibility of solving a wide range of numerical optimization problems. In items of efficiency, it makes optimization problems be dealt with in the same efficiency as decision problems.

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# Computational Design Approach to Hydrodynamic Focusing in a Flow Cytometer

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**Abstract.** A two-fluid theoretical model was developed to simulate the hydrodynamic focusing process formed by the coflowing sample and sheath fluids in a flow cytometer. The analysis consists of two groups of time-dependent three-dimensional conservation equations of mass and momentum. To validate the computer code, the predicted focused width in the two-dimensional test configuration was compared with Lee et al.'s measured data. The present study also examines the pressure distribution of the three-dimensional hydrodynamic focusing flowfield. For the  $u_{SI}/u_S$  ratio ranging from 10 to 80, the focused width was determined to explore the applicability of the proposed flow cytometer.

## 1 Introduction

The application of flow cytometers for cell counting and sorting is one of the most widely used analytical techniques in the biological, biomedical, and forensic sciences [1, 2]. A flow cytometer is designed to transport cells individually into a certain location intersected by the illuminating beams. In practice, the sample cells are pushed through a coaxial liquid stream encircled by the sheath stream. The sheath stream is essentially a tube of cell-free fluid surrounding the core sample stream containing the cells aligned in a single file. The associated phenomenon is described as hydrodynamic focusing [3, 4]. The sheath flow can be regulated to position the cells into the proper observation area in the center of the core stream under a stable laminar flow environment.

Considerable efforts have been made to study the manipulations of fluid flows in cytometers for counting and sorting particles or cells [5-8]. To study the hydrodynamic focusing behavior, Lee et al. [9, 10] designed and fabricated a novel flow cytometer to measure the cellular characteristics with the magnified visualized images of coflowing dye-containing sample and sheath water flows. Chung et al. [11] also conducted a lumped analysis with the Poiseuille-flow assumption to calculate the shape of the focused flow in a microchip flow cytometer.

To assist the design process of flow cytometers, a computational fluid dynamics (CFD) computer code is useful to probe the complicated focusing flows. The purpose of this paper is to study the hydrodynamic focusing behavior in a cytometer. The predictions were compared with the measured results of the focused width from Lee et al. in Ref. 10 to validate the theoretical model for the two-dimensional test

configuration. Numerical experiments were then extended to the three-dimensional focusing flow by varying the ratios of the sheath to the sample fluid velocity for determining the focused width

## 2 Theoretical Approach

In the analysis, the sample and the sheath fluids are considered to be incompressible, laminar, isothermal flows. A three-dimensional two-fluid model is developed using two groups of transient conservation equations of mass and momentum, with considering the interfacial momentum exchange between two fluids. The mean flow properties are evaluated through the volume fraction [12-14]. The governing equations are given as below.

$$\frac{\partial(\alpha_k)}{\partial t} + \nabla \cdot (\alpha_k \vec{u}_k) = 0. \quad (1)$$

$$\frac{\partial(\alpha_k \rho_k \vec{u}_k)}{\partial t} + \nabla \cdot (\alpha_k \rho_k \vec{u}_k \vec{u}_k) = -\alpha_k \nabla P + \nabla \cdot \alpha_k \tau_k + \alpha_k \rho_k \vec{g} + \vec{M}_k. \quad (2)$$

In this study, the subscript  $k$  is the phase indicator, which can be  $S$  or  $Sh$  to denote the sample and sheath fluids, while the variables  $\rho$ ,  $\alpha$ ,  $\vec{u}$ ,  $P$ ,  $\tau$ ,  $\vec{g}$ , and  $\vec{M}_k$  stand for density, volume fraction, velocity vector, pressure, stress tensor, gravitational acceleration, and interfacial momentum exchange rate. For instance, the variable  $\alpha_S$  defines the volume fraction of each computational cell taken by the sample fluid. And the sum of the volumetric fractions for the sample and the sheath fluids is equal to unity ( $\alpha_S + \alpha_{Sh} = 1$ ). In Eq. (2), the  $\vec{M}_k$  term represents the interfacial momentum transfer due to the effects of drag and virtual mass ( $\vec{M}_k = \vec{M}_{D,k} + \vec{M}_{V,k}$ ). In the momentum equation of the sample fluid, the terms  $\vec{M}_{D,S}$  and  $\vec{M}_{V,S}$  can be described as below.

$$\vec{M}_{D,S} = \frac{3}{4} \frac{C_D}{D} \alpha_{Sh} \rho_S \left[ \vec{u}_S - \vec{u}_{Sh} \left( \vec{u}_S - \vec{u}_{Sh} \right) \right], \quad (3)$$

$$\vec{M}_{V,S} = -\alpha_{Sh} \rho_S C_{vm} \left[ \left( \frac{\partial \vec{u}_S}{\partial t} + \vec{u}_S \cdot \nabla \vec{u}_S \right) - \left( \frac{\partial \vec{u}_{Sh}}{\partial t} + \vec{u}_{Sh} \cdot \nabla \vec{u}_{Sh} \right) \right]. \quad (4)$$

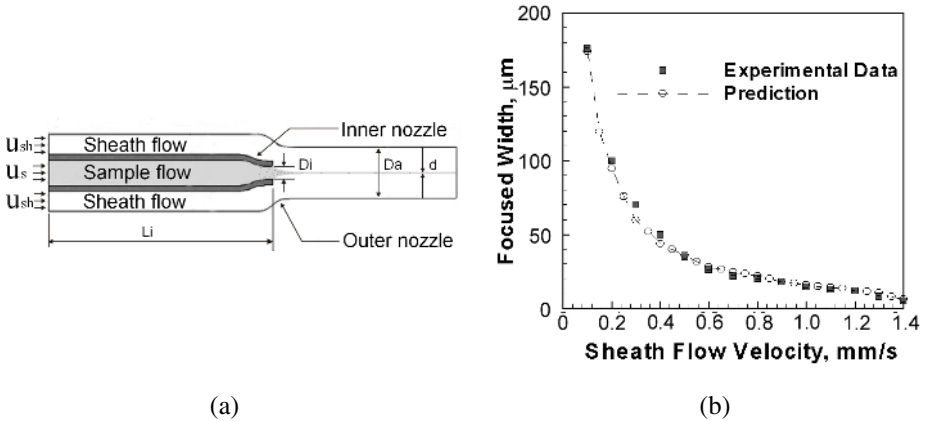
Where  $D$  and  $C_D$  are the interfacial characteristic length and the drag coefficient [15, 16]. The symbol  $C_{vm}$  is the virtual mass coefficient with a typical value of 0.5 [17]. In addition, the  $\vec{M}_{Sh}$  term on the sheath-fluid part is given as  $\vec{M}_{Sh} = -\vec{M}_S$ .

In the setting of the boundary equations, the velocity and volumetric fraction of the incoming sample flow are specified to be uniform profiles with a given pressure at the inlet. The zero normal gradient of pressure and the no-slip condition are imposed along the wall. At the exit, the flowfield becomes fully developed and all primitive variables are extrapolated from the interior values. The theoretical model is solved

using a numerical procedure unifying two sets of conservation equations for the sample and the sheath fluids with the consideration of inter-fluid interactions. An iterative semi-implicit method for pressure-linked equations consistent (SIMPLEC) algorithm is employed for treating the velocity-pressure coupling [18- 20]. The velocities for the sample and the sheath fluids as well as the distributions of pressure and void fractions are solved after completing the calculation procedure.

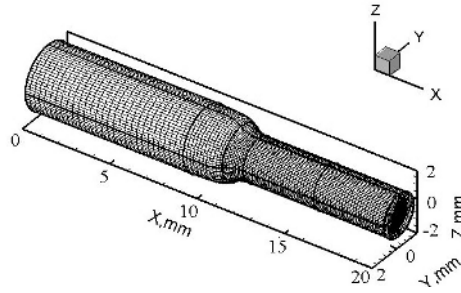
### 3 Results and Discussion

The current theoretical model was validated by comparing the predictions with Lee et al.'s experimental observations for a cytometer [10]. The flow cytometer was fabricated on plastic substrates with the sample fluid focused in a quasi-two-dimensional manner. Figure 1 shows the schematic diagram of a flow cytometer and the comparison of the predicted focused width with measured data at different  $u_{sh}/u_s$  ratios. For computation and visualization purposes, the iso-contour of  $\alpha_s = 0.5$  was employed to identify the boundary of the sample stream, which in turn determines the focused width. When the  $u_{sh}/u_s$  ratio increases, the calculated focused width tends to be reduced and agrees well with experimental results. The discrepancy of the prediction with the measurement of the focused width is 2.6 % at  $u_{sh}/u_s = 35$ .



**Fig. 1.** (a) Schematic diagram of a flow cytometer; (b) Comparison of the predicted focused width with Lee et al.'s measured data at different  $u_{sh}/u_s$  ratios ( $u_s = 0.02 \text{ mm/s}$ ,  $u_{sh} = 0.1-1.4 \text{ mm/s}$ )

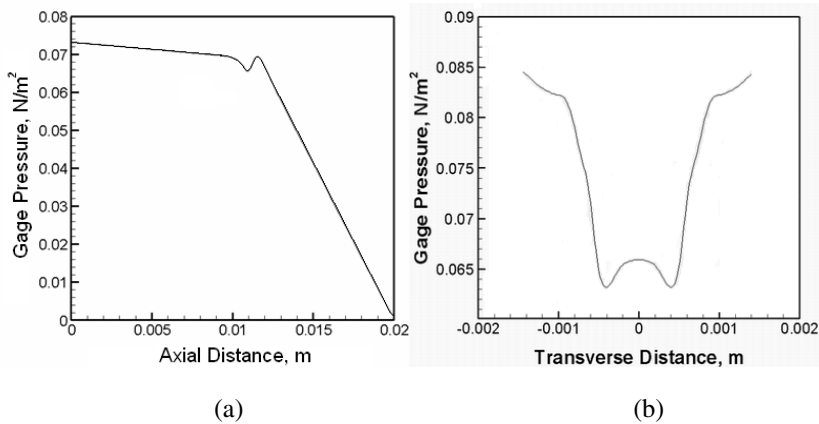
For three-dimensional calculations, the numerical grid setup of the flow cytometer is displayed in Fig. 2. The dimensions of the proposed cytometer in an axisymmetric configuration are 20 mm in length and 3.6 mm/2.4 mm in diameter for the inflow/outflow section. The inner nozzle length is 11 mm, while the wall thickness and exit diameter are 0.21 mm and 0.6 mm, respectively. The geometries and design profiles of the inner and outer nozzles can be found in Ref. 10. To capture the sharp variations of the flow properties associated with the flow focusing progress, finer grids have been arranged in the convergent regions of the nozzles and near wall boundaries. The



**Fig. 2.** Numerical grid setup of the proposed flow cytometer

smallest spacing of the grids is around  $1.8\mu\text{m}$ . Using water with dye as the testing liquid, the density and viscosity of the dye-containing sample fluid and the sheath water are  $998\text{ kg/m}^3$  and  $0.001\text{ N}\cdot\text{s/m}^2$  for the baseline case.

Figure 3 presents (a) the centerline profile and (b) the transverse profile (at the axial location of 11.2 mm) of gage pressure ( $P - P_{atm}$ ) in the hydrodynamic focusing flow field for the case of  $u_{sh}/u_s = 50$ . The inlet velocities of the sample and the sheath flows are  $0.02\text{ mm/s}$  and  $1.0\text{ mm/s}$ , with the annular sheath flow surrounding the core sample fluid issued from the inner nozzle. In general, the pressure decreases with the axial distance from  $0.074\text{ N/m}^2$  at the inlet to  $0.068\text{ N/m}^2$  at the outlet of the flow cytometer. When two streams merge near the exit area of the inner nozzle, the high-velocity sheath water tends to flow inwards and to develop a pressure bulge for compressing and stretching the sample fluid. Hence, the diameter of the sample stream is significantly narrowed when the flow exhibits the phenomenon of hydrodynamic focusing.



**Fig. 3.** (a) Centerline pressure profile and (b) transverse pressure profile at the axial location of 11.2 mm of the proposed flow cytometer ( $u_s = 0.02\text{ mm/s}$ ,  $u_{sh} = 1.0\text{ mm/s}$ )

A lower pressure can also pull the cells to stay in the core region and continue to move individually along the focused stream.

In effect, the human red/white cells have a typical size of  $7\ \mu\text{m}/10\ \mu\text{m}$  [21]. Accordingly, the required width of the focused sample stream should be around  $15\ \mu\text{m}$  to sort and count sample cells. Figure 4 shows the predicted focused width at different  $u_{Sh}/u_S$  ratios. In operating the proposed flow cytometer, the focused width decreases as the  $u_{Sh}/u_S$  ratio is increased. The computed focused width can lower to  $15\ \mu\text{m}$  at  $u_{Sh}/u_S = 80$ . In this study, the  $u_{Sh}/u_S$  ratio should be regulated to 80 in order to obtain a  $15\text{-}\mu\text{m}$  width for holding cells in single file.

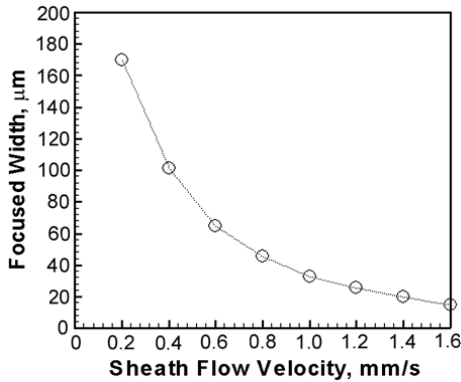


Fig. 4. Focused width at different  $u_{Sh}/u_S$  ratios ( $u_S = 0.02\ \text{mm/s}$ ,  $u_{Sh} = 0.2\text{-}1.6\ \text{mm/s}$ )

## 4 Conclusions

Numerical calculations were performed using a two-fluid theoretical model to simulate the hydrodynamic focusing flow process in a flow cytometer. For the computer code validation in the two-dimensional configuration, the calculated focused width agrees well with the Lee et al.'s measured data for the  $u_{Sh}/u_S$  ratio ranging from 5 to 70. The predictions indicate a pressure gap occurred at the merging layer of the sample and sheath streams associated with the hydrodynamic focusing, which can squeeze the sample fluid to form a focused sample stream. The focused width is substantially reduced when varying the  $u_{Sh}/u_S$  ratio from 10 to 80. The focused width can be narrowed to  $15\ \mu\text{m}$  at  $u_{Sh}/u_S = 80$ , indicating that the proposed flow cytometer can achieve a proper focused width to sort and count cells.

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# A Biometric Encryption Approach Incorporating Fingerprint Indexing in Key Generation<sup>\*</sup>

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**Abstract.** This paper presents a new biometric encryption protocol in which encryption key is incorporated with fingerprint indexing. Based on the extended chaotic Baker map, the pixel permutation and gray level value substitution are performed to shuffle pixel positions in the original fingerprint images. The encryption key of the pixel permutation is generated by the combination of the random pixel distribution of a fingerprint imprint as well as features used for the fingerprint indexing. In addition to the advantage enjoyed by biometric keys over traditional password/PINs, the proposed biometric encryption approach is very efficient in identity identification within a large database due to the pre-filtering feature of the fingerprint indexing incorporated in the keys. This approach is applicable to the centralized matching scenario where fingerprints need to be encrypted before transmitted. Simulation results have validated the proposed schemes.

## 1 Introduction

Fingerprint images have long been used for person recognition due to their uniqueness and immutability. Large volumes of fingerprints are collected and used in a wide range of applications, including forensics, access control, and driver license registration [1]. In a centralized system, when used in personal identification, biometric images should be encrypted before transmitted to the central server. Fingerprint representations are of two types: local and global. The uniqueness of a fingerprint can be determined by the global pattern of ridges and valleys as well as the local anomalies [a ridge bifurcation or a ridge ending, called minutiae points] [2].

There are two general ways in which fingerprint based biometric systems are used: verification and identification. In verification, the user inputs a fingerprint image and claims an identity (ID), the system then verifies whether the input image is consistent with the input ID. In an identification system, the user only inputs a fingerprint image, and the system identifies potential corresponding fingerprints in the database [3]. Identification has found most popular applications in the forensic field. Identification is more complex than verification as it includes an additional task of searching the target. This will be a time consuming huge work as the normal biometric database is

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of prohibitive large. Fingerprint classification helps to reduce the workload. The Henry system of fingerprint classification that classifies fingerprints into five classes: Right Loop (R), Left Loop (L), Whorl (W), Arch (A), and Tented Arch (T), is based on the global patterns of ridges, and is commonly used by most of the developers and users [4]. However, the problem with this classification technique is that the number of principal class is small and the fingerprints are unevenly distributed (31.7%, 33.8%, 27.9%, 3.7%, and 2.9% for class R, L, W, A, and T). The classification approach does not narrow down enough search space in the database for efficient identification of a fingerprint. Continuous classification schemes slightly increases the performance, but is still not acceptable for commercial use in large database [9]. To reduce the search time and computational complexity, it is desirable to classify these fingerprints in an accurate and consistent manner such that the input fingerprint needs to be matched only with a subset of the fingerprints in the database [5]. These approaches are called indexing techniques in the fingerprint recognition area, which is achieved by extracting features from the fingerprints and first matching the fingerprints that have the smallest feature distance to the query fingerprint [9]. Some indexing algorithms have been proposed recently [2, 3, 6-11], which are mainly based on three possible indexing features: the registered directional field estimate [10, 11], FingerCode [2] and minutiae triplets [3, 6-9]. Further effort is the combination of above three methods [8, 9]. The global features of a fingerprint are typically used for indexing, but they do not offer very good individual discrimination [2]. Automatic fingerprint identification (AFI) systems, that match a query print against a large database of prints, rely on the pattern of ridges in the query image to narrow their search in the database (fingerprint indexing), and then use the minutiae points to determine an exact fingerprint matching.

AFI systems normally need to send the fingerprint to the back-end server for processing which requires encryption at the sender. A conventional approach is to encode the fingerprint at the pixel level and treat it as a normal text using symmetric encryption scheme. At the receiver side, decryption is done and then global features are retrieved to go through the stages of indexing and matching. There are several issues with such schemes. First, distribution and maintenance of a shared secret key is a well known hard problem. Secondly it is expensive to encrypt images using conventional cryptography. Researchers are set out to find a better way of combining biometrics and cryptography. A biometric system may be viewed as a pattern recognition system. The hardest problem with biometrics is the unreliability of biometric features used to encode cryptographic keys in the template, while cryptography demands correctness in keys. There have been a number of attempts to bridge the gap between the fuzziness of biometrics and the exactitude of cryptography [16].

To avoid the contradiction of unreliability of biometric template and the exactitude of cryptography key, this paper proposes a new protocol for scenarios where fingerprint images are encrypted at the sender. In this protocol, the parameters of fingerprint indexing with features of minutiae triplet [3] and the random pixel distribution are suggested to be used as the encryption key; and extended chaotic Baker map is employed to permute the pixels position. The advantage of the proposed scheme is that the encryption key is extracted from the query fingerprint image and is generated randomly at each fingerprint impression. Furthermore, the generation of encryption is the byproduct of fingerprint image processing which will save workloads in large



fingerprint database. In addition, the encryption key is separated from the fingerprint template which located at central server.

The rest of the paper is organized as follows: Section 2 introduces the extended chaotic Baker map. Incorporation of cipher key with fingerprint indexing is presented in Section 3. Simulations and evaluations are presented in Section 4. Conclusions are given in Section 5.

## 2 Improved Baker Map for Fingerprint Image Encryption

In order to protect the user’s biometric templates in centralized matching circumstance, the fingerprint samples/templates must be encrypted before transmitted. Generally, there are two major approaches that are used to protect digital image/video from attacker. One is information hiding such as digital watermarking of image/video. The other is encryption, which includes conventional encryption and others such as chaotic encryption. There are two classes of key-based cryptographic algorithms, which are symmetric (private-key) and asymmetric (public-key) cryptographic algorithms. Symmetric cryptographic algorithms use the same key for both encryption and decryption, such that the decryption key can easily be derived from the encryption key. Asymmetric cryptographic algorithms use different keys for encryption and decryption. The decryption key cannot be derived from the encryption key. The problem with public-key system is its lower speed compared to that of private-key system. Private-key cryptographic systems, which are designed for text-based encryption, can be used to encrypt image. But the image data must be converted to bit-stream first in order up to match the standard encryption system. With the development of nonlinear dynamics and chaos theory, some common features between chaos and cryptography such as sensitivity to variables and parameters, were revealed, and a number of digital chaotic cryptographic schemes have been proposed [12-15]. But most of chaotic ciphers are vulnerable to attacks for their small key space. To encrypt a fingerprint image, this section introduces the extended chaotic Baker map which is efficiency and has a large key space. A few rounds of iterations will make the original images being permuted thoroughly.

Assume a square image consists of  $N \times N$  pixels with  $L$  levels of gray, the two-dimensional Baker map  $B$  is described as:

$$\begin{cases} B(x, y) = (2x, 0.5y) & 0 \leq x < 0.5 \\ B(x, y) = (2x - 1, 0.5y + 0.5) & 0.5 \leq x \leq 1 \end{cases} \quad (1)$$

The discretized Baker map is denoted as  $B_{(n_1, \dots, n_k)}$ , where the sequence of  $k$  integers,  $n_1, \dots, n_k$  is chosen such that each integer  $n_i$  divides  $N$ , and  $n_1 + \dots + n_k = N$ . Denoting  $N_i = n_1 + \dots + n_{i-1}$ , the pixel  $(r, s)$ , with  $N_i \leq r < N_i + n_i$ , and  $0 \leq s < N$  is mapped to

$$B_{(n_1, \dots, n_k)}(r, s) = \left( \frac{N}{n_i}(r - N_i) + s \bmod \frac{N}{n_i}, \frac{n_i}{N}(s - s \bmod \frac{N}{n_i}) + N_i \right). \quad (2)$$

Eq.(2) is used to permute pixels in a square image. In addition to the pixel permutation, a gray level value substitution which can create a random-looking image with a uniform histogram appearing in only one round of iteration should be used. The gray

level value substitution is performed as: Consider an  $N \times N$  square image with 256 gray levels. Let  $g_{ij}$  denote the gray level of the pixel  $(i, j)$ . A map  $h: N^N_0 \times N^N_0 \times N^L_0 \rightarrow N^L_0$  needs to be found such that the pixel  $(i, j)$  with gray level  $g_{ij}$  is mapped to  $B(i, j)$  with a gray level  $h(i, j, g_{ij})$ . The three-dimensional map  $B_3: N^N_0 \times N^N_0 \times N^L_0 \rightarrow N^N_0 \times N^N_0 \times N^L_0$  should be invertible to make deciphering possible. This means that  $B_3(i, j, g) \neq B_3(i, j, g')$  for each  $(i, j) \in N^N_0 \times N^N_0$  and  $g, g' \in N^L_0$ . For example this gray level value permutation can be done with:  $h(i, j, g_{ij}) = g_{ij} + \hat{h}(i, j) \bmod L$ , where  $\hat{h}$  is any (possible not one-to-one) function of  $i$  and  $j$ , and it produces an acceptable map  $h$ . In this case,  $h$  can be interpreted as a simple shift cipher with the shift size  $\hat{h}(i, j)$  dependent on the position of the pixel  $(i, j)$ . The shift size  $\hat{h}(i, j)$  could be computed quickly using some bit operations on  $i$  and  $j$ , or it could be stored in a look up table. The details are referenced to [14].

In [14], the author only presented formula when integer  $n_i$  divides  $N$ , where a small key space is generated which is weak in security. The improvement proposed in this section is a pixel permutation. With this improvement, a pixel permutation formula that integer  $n_i$  does not divide  $N$  is presented.

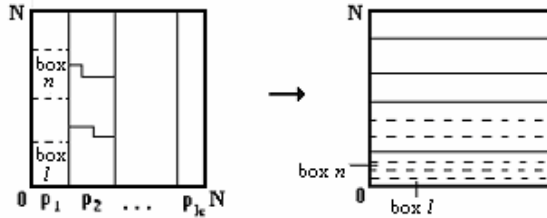


Fig. 1. Permutation of pixels in a square image

In Fig.1, a sequence of  $k$  integer,  $p_1, \dots, p_k$ , are employed as the encryption key for the permutation of pixels in an  $N \times N$  square image, where  $p_1 + \dots + p_k = N$ . The image is divided into  $k$  vertical rectangles, and there are  $p_i$  ( $i = 1, \dots, k$ ) pixels in one row. The pixels in the original images are represented as  $P(r, s)$ ,  $r, s = 1, 2, \dots, N$  are the vertical and pixel horizontal coordinate. After permutation, the pixels are represented as  $Q(\cdot; \cdot)$

If  $p_i$  divides  $N$ , the pixels permutation is similar to formula (2). If  $p_i$  does not divide  $N$ , inside each column, the pixels are divided into  $p_i$  boxes, each box containing exactly  $N$  pixels. In this case, the permutation formulae are as follows:

$$Q(N - N_i - j + 1, j) = P(N - (s - 1) - m_2(j), N_i + r) \tag{3}$$

$$r = 1, 2, \dots, n_i; s = 1 - l_{dd}; \dots; d - l_{uu}; j = 1, 2, \dots, n_i; i = 1, 2, \dots, k$$

with

$$d = \text{fix} \left( \frac{N - l_d(j) + p_i - 1}{p_i} \right)$$

$$l_{dd} = \text{fix}\left(\frac{p_i - j - l_d(j)}{p_i - j - l_d(j) + 0.1}\right)$$

$$l_{uu} = \text{fix}\left(\frac{p_i - j - l_u(j)}{p_i - j - l_u(j) + 0.1}\right)$$

and

$$l_u(j) = d - p_i + l_d(j) - N, \quad l_d(j+1) = l_u(j), \quad l_d(1) = 0$$

$$m_2(j+1) = m_2(j) + d, \quad m_2(1) = 0$$

where  $\text{fix}(X)$  is a function which rounds the elements of  $X$  to the nearest integers towards zero.

The decryption key is the same with that of encryption key. Only with valid fingerprint, can the fingerprint image be recovered correctly at central server. Then it is possible to get a successful fingerprint matching.

The proposed fingerprint image encryption scheme is more applicable and effective. The encryption key can be an arbitrary combination of integers. It can be designed purposely, for example, extracted from the features of fingerprint images, from random pixels distribution in the fingerprint impressions, or from pseudo random number generator, et al. The only requirement for key is the sum of all digits equals to the pixels number in a row/column (for square image). This chaotic encryption approach has a large key space, and the fingerprint images can be fully recovered.

### 3 Key Generation by Incorporating Fingerprint Indexing

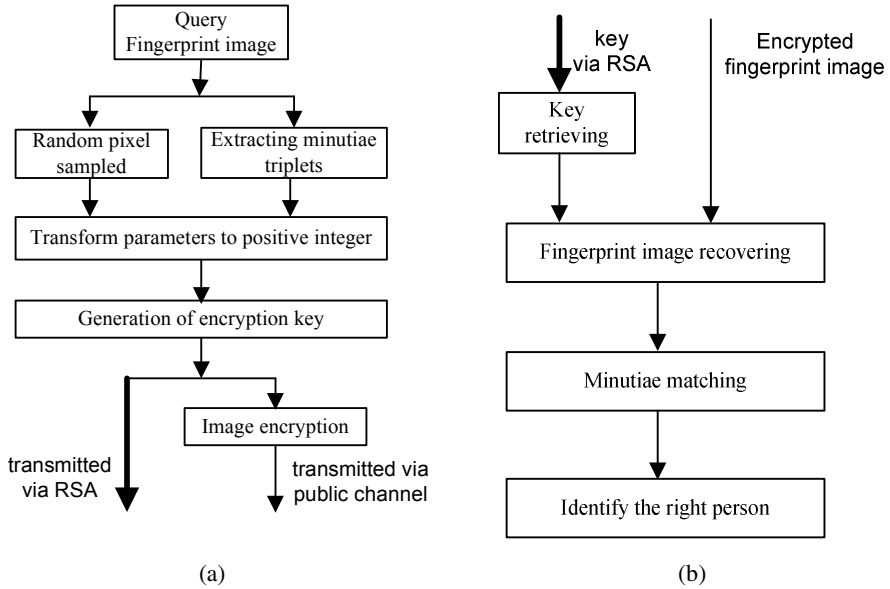
In this section, we propose a protocol in a fingerprint identification system, in which the encryption key is integrated with fingerprint indexing.

When transmitted over insecure channel, fingerprint images should not be disclosed to any unauthorized persons. They need to be encrypted before transmitted. In addition, a completely loss-free image should be recovered for further matching. To save the computational complexity and meet the above two requirements, we proposed a protocol to transmit the images over public channel:

- Private-key cryptography system, such as extended Baker map, is used in transmitting the encrypted images, while the public key cryptosystem is employed to encrypt the private key.
- The encryption keys are directly derived from the query fingerprint images.

The extended Baker map is used to encrypt the query fingerprint images in this protocol. The pixels permutation, together with gray level values substitution result in a fully recoverable encrypted image with high security and low computation complexity.

The block diagram of incorporating encryption key with fingerprint indexing is as shown in Fig.2.



**Fig. 2.** Block diagram of incorporating private key with fingerprint indexing; (a) At a terminal. (b) At central server.

As shown in Fig.2(a), the encryption key is directly derived from query fingerprint imprint. After a qualified image is captured, some random pixels are picked up; their coordinates and gray values are processed as part of the private key. Then the image is being pre-processed. The fingerprint indexing method proposed in [3] is suggested to be used here. The features of the query fingerprint  $H(\alpha_{mins}, \alpha_{meds}, \varphi, \eta, \lambda, \chi, \xi)$  (details are referenced to [3]) are extracted and computed, which are transformed into positive integer and used as part of key. After that, improved Baker map is used to encrypt the fingerprint images. The encrypted image is transmitted to the central server via private key cryptosystems, while the key is transmitted to the central server via public key cryptosystems such as RSA. It can be seen from Fig.2(b), after encryption key being retrieved, the minutiae matching is used at last to identify the query fingerprint image. While part of the encryption key is used as fingerprint indexing directly in order to narrow the candidates to be matched.

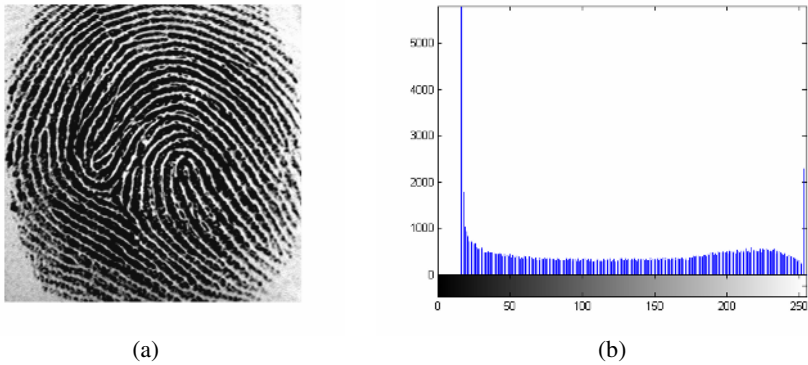
## 4 Simulation and Security Analysis

In this section, the proposed fingerprint image encryption which key being derived from features of fingerprint indexing is tested. Simulation results are presented.

Fig.3 shows a  $380 \times 380$  gray level fingerprint image and its histogram. Using the proposed extended chaotic Baker map and encryption key being incorporated with fingerprint index scheme, the encryption key is composed of minutiae triplets and random pixels distribution. For the random pixel distribution, for example, coordinates and gray values of ten points in the query fingerprint imprint can be picked up.

For the features of minutiae triplets, twenty minutiae triplets are found, the feature values are computed. These parameters can be divided into five groups, which are the iteration times of extended Baker map. Some transformation and mod operations are conducted to guarantee each digit is a positive integer. And the last digit in each group is the supplementary digit to make the sum of key equals to 380 (pixel number in a row of the square image).

For example, 180 parameters are obtained from the processed minutiae triplets and random pixels distribution in a query fingerprint image. These parameters are further divided into five groups. After processing, the first group contains 25 positive integers: [16,17,6,28,27,25,5,35,15,8,9,5,3,12,6,11,4,33,10,7,16,20,50,4,8], which are used as the encryption key to perform the first round extended Baker map. The encrypted fingerprint image and histogram are shown in Fig.4(a), (b). There are 32, 40, 27, 56 positive integers in the other four groups, which are used as encryption keys in the four iterations followed. After five times extended Baker map with different key each time, the encrypted image and histogram are shown in Fig.4 (c) and (d), respectively.

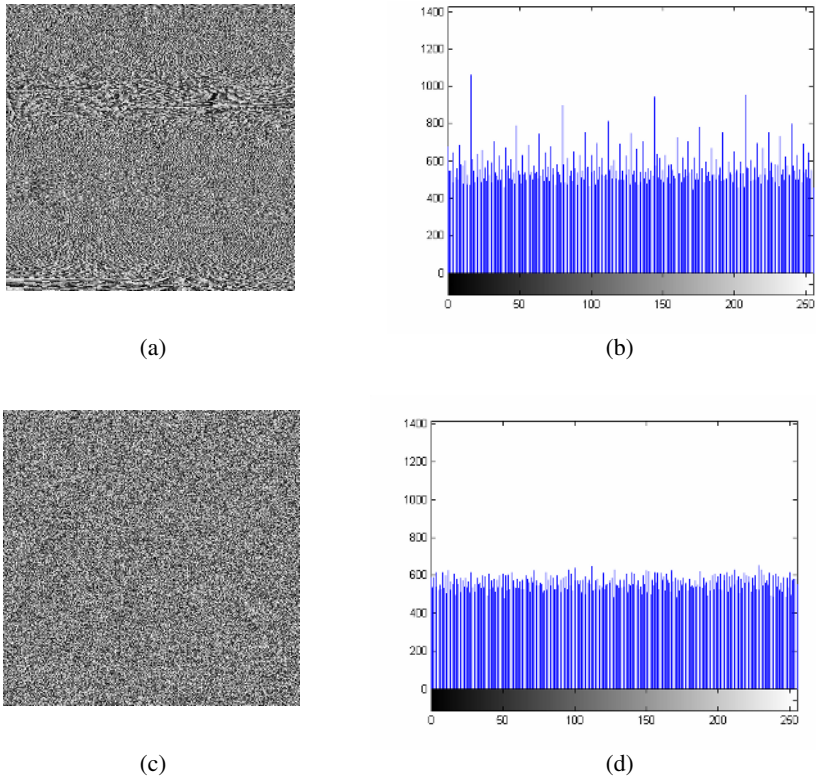


**Fig. 3.** Gray level fingerprint image and histogram. (a) Fingerprint image; (b) Histogram.

From Fig.4, one can see that after one round of iteration, the pixels have been permuted significantly, and the histogram has been uniformed. After five rounds of iteration with different encryption key each time, the original image has been scrambled perfectly. One can also see that the histogram in Fig.4(d) has much better statistic character than that in Fig.3(b). So the image can be well hidden.

The decryption is the inverse of the encryption. Only with the right key can the fingerprint image being fully recovered.

In this example, without taking diffusion into consideration, there are 180 elements in the key, and the value of each element can be processed between 0 to 99. Preliminary analysis indicates that the keyspace for five rounds of iteration can be as large as  $100^{180} = 10^{360}$ . For this fingerprint image, five rounds of pixel permutation should yield a secure cipher which would mean that an exhaustive search of key space is infeasible. The randomness of parameters in individual fingerprint query image can make contributions to the key entropy.



**Fig. 4.** The encrypted images. (a) After one round of iteration; (b) Histogram of Fig.4(a); (c) After five rounds of iterations; (d) Histogram of Fig.4(c).

*Remark:*

The advantages of the proposed protocol are:

- 1) The protocol proposed in this paper aiming at generating cryptography key directly from the query fingerprint images. While the objective of Biometric Encryption algorithm in literatures is to provide a mechanism for the linking and subsequent retrieval of a digital key using a biometric such as a fingerprint. This digital key can then be used as a cryptographic key [17].
- 2) With the proposed encryption key being incorporated with fingerprint indexing scheme, part of the fingerprint matching load in the fingerprint matching stage is performed in the processing of private key generation. This can reduce the computation load of fingerprint matching greatly.
- 3) The length of the encryption key can be as long as one desired with key being generated from the coordinates and gray values of random picked pixels and from features of minutiae triplets. This could result in a large key space which is vital to the strength of cryptography.

- 4) At central server, the encrypted fingerprint images are fully recovered, which guarantee the successive fingerprint matching for identify the owner of the query fingerprint image.

## 5 Conclusions

A biometric encryption protocol which incorporates encryption key with fingerprint indexing has been proposed. The extended chaotic Baker map is employed to encrypt the fingerprint image. The encryption key is directly generated from the query fingerprint image: from features of minutiae triplets and from some random pixels distribution. At the central server, after the key being retrieved and the fingerprint image is fully recovered, then fingerprint image pre-processing are employed as the fingerprint indexing, which will reduce computation load in fingerprint minutiae matching stage significantly. The successful fingerprint minutiae matching at last identify the identity. As the key has included a random pixel distribution at each imprint and it has a large space, this biometric encryption scheme is strong in security.

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# A General Solution for the Optimal Superimposition of Protein Structures

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**Abstract.** The theorem presented in this paper is a general solution for the optimal superimposition between two protein structures, which is actually the problem of the weighted optimal rigid superimposition between two vector sets with the same size. The theorem gives not only the rotational and translational parameters, but also the minimal value of the mean squared deviation of the optimal superimposition.

## 1 Introduction

Protein structure alignment is to establish structural equivalences between three-dimensional (3D) structures of two protein folds based on their amino acid positions, which is an indispensable bioinformatics tool for studying protein function and evolution [1, 2], due to the rapid accumulation of protein 3D structures in the Protein Data Bank [3]. Most alignment methods rely on a structure superimposition procedure, which finds the transformation (i.e. rotation and translation) to optimally match the aligned residue pairs of two proteins, in terms of their RMSD (Root Mean Squared Deviation) [4].

The problem of the optimal superimposition between two protein structures is actually the weighted optimal rigid superimposition between two vector sets, which are the 3D coordinates of atoms in the protein molecules. The solution of superimposition has attracted attentions of a number of researchers, notably Mclachlan [5, 7], Kabsch [8, 9], Diamond [10, 11], Ferro & Hermans [12], Lesk [13], Kaindl & Steipe [14] and Steipe [15]. All of the above methods achieve the optimal superimposition by obtaining the optimal rotation matrix under the precondition that the centroids of two vector sets are coincident.

Without the coincidence of both centroids as the precondition, the presented theorem is a general solution for the optimal superimposition, which gives not only the transformational parameters but also the minimal value of the mean squared deviation. This work is inspired by Umeyama's work [16], which is applied in the field of computer vision.

## 2 Representation of the Superimposition Problem

The structure of a protein molecular that consists of  $n$  atoms can be described by  $n$  3D coordinate vectors such as  $(x_1, y_1, z_1)$ ,  $(x_2, y_2, z_2)$ , ...,  $(x_n, y_n, z_n)$ . Therefore, the

problem of protein structure optimal superimposition can be stated in mathematics as follows.

Given two sets  $X_0$  and  $Y_0$  of  $n$  3D column vectors  $x_k$  and  $y_k$  ( $k = 1, 2, \dots, n$ ), find a  $3 \times 3$  orthogonal rotation matrix  $R$  with determinant  $+1$  and a  $3 \times 1$  translation vector  $t$  which convert the coordinates  $x_{ik}$  ( $i = 1, 2, 3$ ) to

$$x'_{ik} = \sum_j R_{ij} x_{jk} + t_i, \tag{1}$$

and minimize the function

$$e^2(R, t) = \frac{1}{n} \sum_{ik} w_k (y_{ik} - x'_{ik})^2, \tag{2}$$

here  $w_k$  is a weighting factor assigned to the  $k$ th atom. The Eq.(2) can be converted to

$$\begin{aligned} e^2(R, t) &= \frac{1}{n} \sum_k \left\| \sqrt{w_k} y_k - \sqrt{w_k} (R x_k + t) \right\|^2 \\ &= \frac{1}{n} \sum_k \left\| \tilde{y}_k - (R \tilde{x}_k + \sqrt{w_k} t) \right\|^2 \\ &= \frac{1}{n} \left\| Y - (R X + t w^T) \right\|^2, \end{aligned} \tag{3}$$

where  $\tilde{x}_k = \sqrt{w_k} x_k$ ,  $\tilde{y}_k = \sqrt{w_k} y_k$ ,  $X$  and  $Y$  are two sets consisting of  $n$  column vectors of  $\tilde{x}_k$  and  $\tilde{y}_k$  respectively,  $w = (\sqrt{w_1}, \sqrt{w_2}, \dots, \sqrt{w_n})^T$ . Thus, the problem of the optimal superimposition between two protein structures is converted to obtain the rotational and translational parameters  $R$  and  $t$  of the transformation between two vector sets  $X$  and  $Y$ .

### 3 Theorem of a General Solution for Optimal Superimposition

Umeyama proposed a very useful theorem for finding the similarity transformational parameters (rotation, translation, and scaling) between two point sets that give the least mean squared error [16]. In this section, we derive a valuable theorem, which gives a general solution for the considered problem of optimal superimposition by introducing weighting factors to the vector sets and canceling the scaling component of the transformation considered in Umeyama's theorem. Not only the rotational and translational parameters, but also the minimal value of the mean squared deviation of the optimal superimposition is obtained from the datum of the superimposed vector sets in the presented theorem. Before showing the theorem, we introduce a lemma presented and proved in Umeyama's correspondence [16], in which the rotational parameters of least-squares residual are given. The proof of the Lemma is shown in Appendix.

**Lemma**

Let  $A$  and  $B$  be  $m \times n$  matrices, and  $R$  an  $m \times m$  rotation matrix, and  $UDV^T$  a singular value decomposition of  $AB^T$  ( $UU^T = VV^T = I$ ,  $D = \text{diag}(d_i)$ ,  $d_1 \geq d_2 \geq \dots \geq d_m \geq 0$ ).

Then the minimum value of  $\|A - RB\|^2$  with respect to  $R$  can be written as

$$\min_R \|A - RB\|^2 = \|A\|^2 + \|B\|^2 - 2\text{tr}(DS), \tag{4}$$

where

$$S = \begin{cases} I, & \text{if } \det(AB^T) \geq 0; \\ \text{diag}(1, 1, \dots, 1, -1), & \text{if } \det(AB^T) < 0. \end{cases} \tag{5}$$

When  $\text{rank}(AB^T) \geq m-1$ , the optimum rotation matrix  $R$  which achieves the above minimum value is uniquely determined as

$$R = USV^T, \tag{6}$$

where  $S$  in Eq.(6) must be chosen as

$$S = \begin{cases} I, & \text{if } \det(U)\det(V) = 1; \\ \text{diag}(1, 1, \dots, 1, -1), & \text{if } \det(U)\det(V) = -1, \end{cases} \tag{7}$$

when  $\det(AB^T) = 0$  ( $\text{rank}(AB^T) = m-1$ ).

We can derive the following theorem using this lemma.

**Theorem**

Let  $X = \{x_1, x_2, \dots, x_n\}$  and  $Y = \{y_1, y_2, \dots, y_n\}$  be corresponding point sets in  $m$ -dimensional space. The mean squared deviation of the optimal rigid superimposition between these two point sets with respect to the transformational parameters [ $R$  (rotation) and  $t$  (translation)] is expressed by

$$e^2(R, t) = \frac{1}{n} \sum_{i=1}^n \|Y - (RX + tw^T)\|^2. \tag{8}$$

The minimum value  $\mathcal{E}^2$  of the mean squared deviation  $e^2(R, t)$  is given as the following:

$$\mathcal{E}^2 = \frac{1}{n} \left\{ \|YK\|^2 + \|XK\|^2 - 2\text{tr}(DS) \right\}, \tag{9}$$

where

$$K = I - \frac{1}{w_0} ww^T, \tag{10}$$

here,  $I$  is the identity matrix,  $w_0 = \sum_k w_k$ ,  $D$  is derived by letting a singular value decomposition of  $YKK^T X^T$  be  $UDV^T$ , the expression of  $D$  is  $D = \text{diag}(d_i)$ ,  $d_1 \geq d_2 \geq \dots \geq d_m \geq 0$ , and

$$S = \begin{cases} I, & \text{if } \det(YKK^T X^T) \geq 0; \\ \text{diag}(1,1,\dots,1,-1), & \text{if } \det(YKK^T X^T) < 0. \end{cases} \quad (11)$$

When  $\text{rank}(YKK^T X^T) \geq m-1$ , the optimum transformational parameters are determined uniquely as the listed below:

$$R = USV^T, \quad (12)$$

$$t = \frac{1}{w_0}(Yw - RXw), \quad (13)$$

where  $S$  in Eq.(12) must be chosen as

$$S = \begin{cases} I, & \text{if } \det(U)\det(V) = 1; \\ \text{diag}(1,1,\dots,1,-1), & \text{if } \det(U)\det(V) = -1, \end{cases} \quad (14)$$

when  $\text{rank}(YKK^T X^T) = m-1$ .

**Proof of the Theorem**

To prove the theorem, we introduce an  $n \times n$  symmetry matrix

$K = I - \frac{1}{w_0}ww^T$  ( $K = K^T$ ). Here,  $w_0 = \sum_k w_k$ . Using the following equations,

$$X = XK + \frac{1}{w_0}Xww^T, \quad (15)$$

$$Y = YK + \frac{1}{w_0}Yww^T, \quad (16)$$

the mean squared deviation  $e^2(R,t)$  is further reformulated as

$$\begin{aligned} e^2(R,t) &= \frac{1}{n} \left\| YK + \frac{1}{w_0}Yww^T - RXK - \frac{1}{w_0}RXww^T - tw^T \right\|^2 \\ &= \frac{1}{n} \left\| YK - RXK + \left( \frac{1}{w_0}Yw - \frac{1}{w_0}RXw - t \right) w^T \right\|^2 \\ &= \frac{1}{n} \left\| YK - RXK - t'w^T \right\|^2 \\ &= \frac{1}{n} \{ \|YK - RXK\|^2 + \|t'w^T\|^2 - 2\text{tr}(K^T(Y^T - X^T R^T)t'w^T) \}, \end{aligned} \quad (17)$$

where

$$t' = -\frac{1}{w_0} Yw + \frac{1}{w_0} RXw + t. \tag{18}$$

Since the following equations

$$\begin{aligned} \text{tr}(K^T(Y^T - X^T R^T)t'w^T) &= \text{tr}(w^T(I - \frac{1}{w_0}ww^T)(Y^T - X^T R^T)t') \\ &= \text{tr}((w^T - \frac{1}{w_0}w^Tww^T)(Y^T - X^T R^T)t') \\ &= \text{tr}((w^T - w^T)(Y^T - X^T R^T)t') \\ &= 0, \end{aligned} \tag{19}$$

and

$$\|t'w^T\|^2 = w_0\|t'\|^2, \tag{20}$$

are derived, we have

$$e^2(R, t) = \frac{1}{n}\|YK - RXK\|^2 + \frac{w_0}{n}\|t'\|^2. \tag{21}$$

From Eq.(21),  $t'$  must be equal to 0 in order to minimize  $e^2(R, t)$ , that is,

$$t = \frac{1}{w_0}Yw - \frac{1}{w_0}RXw = \frac{1}{w_0}(Yw - RXw). \tag{22}$$

Next, let  $UDV^T$  be a singular value decomposition of  $YKK^T X^T$ . Then, the minimum value  $e^2$  of  $\frac{1}{n}\|YK - RXK\|^2$  with respect to  $R$  is given from the above lemma as follows:

$$\mathcal{E}^2 = \frac{1}{n}\{\|YK\|^2 + \|XK\|^2 - 2\text{tr}(DS)\}, \tag{23}$$

where

$$S = \begin{cases} I, & \text{if } \det(YKK^T X^T) \geq 0; \\ \text{diag}(1,1, \dots, 1, -1), & \text{if } \det(YKK^T X^T) < 0. \end{cases} \tag{24}$$

Also from the lemma, if  $\text{rank}(YKK^T X^T) \geq m - 1$ ,

$$R = USV^T, \tag{25}$$

where  $S$  must be chosen as

$$S = \begin{cases} I, & \text{if } \det(U)\det(V) = 1; \\ \text{diag}(1,1, \dots, 1, -1), & \text{if } \det(U)\det(V) = -1, \end{cases} \tag{26}$$

when  $\text{rank}(YKK^T X^T) = m - 1$ .

The theorem is proved.

**Q.E.D.**

The presented theorem is an extension of Umeyama's theorem [16]. It is proved by replacing  $c$  and  $h$  in Umeyama's formulae with 1 and  $w$ , respectively. Accordingly,  $n$  is replaced with  $w_0$  in the computation of  $K$ . Here  $c$  is the scaling parameter of transformation and  $h = (1, 1, \dots, 1)^T$ .

## 4 Examples

In order to elucidate the validity of the proposed theorem, some numerical results of RMSD are shown in Table 1. Since the superimposition method requires the same number of pairs of vector sets,  $N$  residues are selected to be superimposed from the beginning of the  $N$ -terminal of the protein. Generally, according to the atoms of protein molecules used in the superimposition process, researchers adopt two kinds of superimposition. One is when only the alpha-carbon atom; the other is where four atoms, nitrogen, alpha-carbon, carbon and oxygen, of the peptide backbone are superimposed for per residue. The weighting factors assigned to these four kinds of atoms in this paper are 0.6, 1, 0.8 and 0.9, which may not have any biological significance but demonstrates the RMSD results. When only alpha-carbon atom of each residue is used, the number of atom pairs in the superimposition sequence is  $N$ . When four atoms (nitrogen, alpha-carbon, carbon and oxygen) of each residue are used, the number of atom pairs is  $4 \times N$ . In this experiment, three pairs of protein molecules are superimposed. The values of RMSD listed in table 1 are then calculated with pairs of the transformed vector sets. It is indicated that the same RMSD values are derived as applying Kabsch's method [8]-[9].

**Table 1.** Some results of RMSD between two sets of atom pairs

| Atoms used                                      | PDB pair IDs   | RMSD (Å) |        |         |
|-------------------------------------------------|----------------|----------|--------|---------|
|                                                 |                | $N=10$   | $N=50$ | $N=100$ |
| alpha-carbon only                               | 1LYZ .vs. 2LZM | 1.26     | 1.69   | 1.48    |
|                                                 | 1HFC .vs. 1MNC | 1.03     | 0.52   | 0.37    |
|                                                 | 1ULB .vs. 2CTC | 1.34     | 1.45   | 1.25    |
| nitrogen,<br>alpha-carbon,<br>carbon and oxygen | 1LYZ .vs. 2LZM | 0.58     | 0.83   | 0.73    |
|                                                 | 1HFC .vs. 1MNC | 0.49     | 0.25   | 0.18    |
|                                                 | 1ULB .vs. 2CTC | 0.64     | 0.72   | 0.62    |

Formally, given  $N$  atom positions from protein structures  $x$  and  $y$  respectively with the weighting factors  $w(i)$ , the RMSD is defined as:

$$\text{RMSD}(N; x, y) = \left[ \frac{\sum_{i=1}^N w_i \|x_i - y_i\|^2}{N \sum_{i=1}^N w_i} \right]^{\frac{1}{2}}. \quad (27)$$

## 5 Conclusion

A general solution for the optimal superimposition between two protein structures, which is actually the weighted optimal rigid superimposition between two 3D vector sets, is presented in this paper. Not only the rotational and translational parameters, but also the minimal value of the mean squared deviation of the optimal superimposition is obtained from the datum of the superimposed vector sets in the presented theorem.

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### Appendix: Proof of the Lemma

Define an objective function  $F$  as

$$F = \|A - RB\|^2 + \text{tr}(L(R^T R - I)) + g\{\det(R) - 1\}, \tag{28}$$

where  $g$  is a Lagrange multiplier and  $L$  is a symmetric matrix of Lagrange multipliers. The second and third term of  $F$  represent the conditions for  $R$  to be an orthogonal and proper rotation matrix respectively. Partial differentiations of  $F$  with respect to  $R$ ,  $L$  and  $g$  lead to the following system of equations:

$$\frac{\partial F}{\partial R} = -2AB^T + 2RBB^T + 2RL + gR = 0, \tag{29}$$

$$\frac{\partial F}{\partial L} = R^T R - I = 0, \tag{30}$$

$$\frac{\partial F}{\partial g} = \det(R) - 1 = 0, \tag{31}$$

where we used

$$\frac{\partial}{\partial L} \det(R) = \text{adj}(R^T) = \det(R^T)(RT)^{-1} = R, \tag{32}$$

since  $R$  is rotation matrix ( $\text{adj}(R^T)$  is an adjoint matrix of  $R^T$ ).

From Eq.(29),

$$RL' = AB^T, \text{ where } L' = BB^T + L + \frac{1}{2}gI. \tag{33}$$

By transposing the both sides of Eq.(33), we obtain the following equation (note that  $L'$  is symmetric),

$$L'R^T = BA^T. \tag{34}$$

If we multiply each side of Eq.(33) with each side of Eq.(34), respectively, Eq.(35) is obtained since  $R^T R = I$ ,

$$L'^2 = BA^T AB^T = VD^2V^T. \tag{35}$$

Obviously  $L'$  and  $L'^2$  are commutative ( $L'L'^2 = L'^2L'$ ), hence both can be reduced to diagonal forms by the same orthogonal matrix.



Thus we can write

$$L' = VDSV^T, \tag{36}$$

where  $S = \text{diag}(s_i)$ ,  $s_i = 1$ , or  $-1$ .

Now, from Eq.(36),

$$\det(L') = \det(VDSV^T) = \det(V) \det(D) \det(S) \det(V^T) = \det(D) \det(S). \tag{37}$$

On the other hand, from Eq.(33)

$$\det(L') = \det(R^T AB^T) = \det(R^T) \det(AB^T) = \det(AB^T). \tag{38}$$

Thus,

$$\det(D) \det(S) = \det(AB^T). \tag{39}$$

Since singular values are nonnegative,  $\det(D) = d_1 d_2 \cdots d_m \geq 0$ . Hence  $\det(S)$  must be equal to 1 when  $\det(AB^T) > 0$ , and  $-1$  when  $\det(AB^T) < 0$ .

Next, extremum values of  $\|A - RB\|^2$  is derived as follows: from Eq.(33),

$$\begin{aligned} \|A - RB\|^2 &= \|A\|^2 + \|B\|^2 - 2\text{tr}(AB^T R^T) \\ &= \|A\|^2 + \|B\|^2 - 2\text{tr}(R^T AB^T) \\ &= \|A\|^2 + \|B\|^2 - 2\text{tr}(L'). \end{aligned} \tag{40}$$

Substituting Eq.(36) into Eq.(40), we have

$$\begin{aligned} \|A - RB\|^2 &= \|A\|^2 + \|B\|^2 - 2\text{tr}(VDSV^T) \\ &= \|A\|^2 + \|B\|^2 - 2\text{tr}(DS) \\ &= \|A\|^2 + \|B\|^2 - 2(d_1 s_1 + d_2 s_2 + \cdots + d_m s_m). \end{aligned} \tag{41}$$

Thus, the minimum value of  $\|A - RB\|^2$  is obviously achieved when  $s_1 = s_2 = \cdots = s_m = 1$ , if  $\det(AB^T) \geq 0$ , and  $s_1 = s_2 = \cdots = s_{m-1} = 1, s_m = -1$ , if  $\det(AB^T) < 0$ . This concludes the first half of the lemma.

Next, we determine a rotation matrix  $R$  achieving the above minimum value. When  $\text{rank}(AB^T) = m$ ,  $L'$  is nonsingular, thus it has its inverse  $L'^{-1} = (VDSV^T)^{-1} = VS^{-1}D^{-1}V^T = VD^{-1}SV^T$  (note that  $S^{-1} = S, SD^{-1} = D^{-1}S$ ). Therefore, from Eq.(33) we have

$$R = AB^T L'^{-1} = UDV^T VD^{-1}SV^T = USV^T. \tag{42}$$

Finally, when  $\text{rank}(AB^T) = m-1$ , from Eq.(33) and Eq.(36)

$$RVDSV^T = UDV^T. \tag{43}$$

Multiplying  $V$  by both sides of Eq.(43) from the right and using  $DS = D$  (since  $d_m = 0$  and  $s_1 = s_2 = \dots s_{m-1} = 1$ ),

$$RVD = UD \tag{44}$$

is obtained. If we define an orthogonal matrix  $Q$  as follows,

$$Q = U^T RV, \tag{45}$$

we have

$$QD = D. \tag{46}$$

Let the column vectors of  $Q$  be  $q_1, q_2, \dots, q_m$  ( $Q = [q_1, q_2, \dots, q_m]$ ). The following equations are obtained by comparing both sides of Eq.(46),

$$d_i q_i = d_i e_i, \quad 1 \leq i \leq m-1. \tag{47}$$

Hence,

$$q_i = e_i, \quad 1 \leq i \leq m-1, \tag{48}$$

where  $e_i$  is a unit vector which has 1 as an  $i$ th element,

$$e_i = (0, 0, \dots, \overset{i}{1}, \dots, 0)^T. \tag{49}$$

The last column vector  $q_m$  of  $Q$  is orthogonal to all other vectors  $q_i$  ( $1 \leq i \leq m-1$ ) since  $Q$  is an orthogonal matrix. Thus we have

$$q_m = e_m \quad \text{or} \quad q_m = -e_m. \tag{50}$$

On the other hand,

$$\det(Q) = \det(U^T) \det(R) \det(V) = \det(U) \det(V). \tag{51}$$

Thus,  $\det(Q) = 1$ , if  $\det(V) = 1$  and  $\det(Q) = -1$ , if  $\det(U) \det(V) = -1$ . Therefore we have

$$R = UQV^T = USV^T, \tag{52}$$

where

$$S = \begin{cases} I, & \text{if } \det(U) \det(V) = 1; \\ \text{diag}(1, 1, \dots, 1, -1), & \text{if } \det(U) \det(V) = -1. \end{cases} \tag{53}$$

**Q.E.D.**

# A Personalized Biological Data Management System Based on BSML

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**Abstract.** A mass of biological sequence and structural information have been produced in biological laboratories since the techniques to get the sequences of genomes or proteins have been improved in HGP (Human Genome Project). Unfortunately, there are scarcely software packages available to deal with the biological data in most of biological laboratories and they are just stored in file formats. An integrated management system of biological data is required to manage the sequence and annotation data taken from other open databases to improve the analysis of sequence data in biological laboratories. We therefore suggest a personalized system to edit, store and retrieve biological information, and convert the formats of sequence data, as well as to integrate and manage data.

## 1 Introduction

Biologists connect the public biological databases and retrieve sequences which are similar to sequences they have, then the results of retrieval are used in homology research, functional analysis, and prediction. Unfortunately, there are scarcely software packages available to deal with the sequence data in most biological laboratories and they are just stored in file formats.

The integration and management technique of heterogeneous sequence data from public sequence databases is widely used to manage diverse information and prediction. Thus a database management technique that is suitable for biological data is required. In particular, an integrated data model which handles the modification of program and data is needed for analysis on the various programs.

In this work, our system supports editing and converting among heterogeneous public biological database flat files as well as sequences users produce in laboratories. BSML (Bioinformatic Sequence Markup Language) based on XML is used for representing the complex and hierarchical biological data. Biologists easily analyze their accumulated biological data using our system and apply the results of biological data analysis to medical science and pharmacy at the level of biological laboratories.

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## 2 Related Work

There are some program packages that handle biological data. We will briefly introduce main function, its features, and formats which these analysis tools support.

### 2.1 BSML

BSML [1] (<http://www.bsml.org/>) is one of open standards of XML data in bioinformatics research. BSML represents good bio-physical features as well as visualization of biological sequence data comparing with other languages such as abstract annotations. It also supports converting formats among biological flat files base on flat-form independence. In this point, BSML is more complete and specifiable than other XML formats in bioinformatics. BSML which our system supports is used in the area of representing gene research results and biological molecules, and exchanging them, hence many laboratories and company choose BSML as a new standard.

### 2.2 Genomic Workspace

Recent tools which convert formats among standards are implemented by JAVA or Perl module. One of these worthy converting softwares is the Genomic Workspace [2]. It converts Genbank [3] flat file into BSML format and includes Genomic Viewer for a good graphic visualization of biological information. The Genomic Workspace doesn't have an own local database so that biological information which users modified is not stored into database.

### 2.3 Staden Package

Staden Package [4] is developed for managing and analyzing the sequence from sequencing machine by Medical Research Council Laboratory in U.K. It is constituted of several tools. *Trev* represents raw experimental file from sequencing machine. *Trace\_diff* describes the mutation information of reference and trace data. *GAP4* edits contigs and assembly of sequences. *Pregap4* is used for pre-processing the assembly data. Spin analyzes the result sequence such as retrieving similar sequences and some other operations.

Staden Package analyzes and simply manages sequences in sequence experimental files but doesn't store sequences into database and retrieve. It can't process a mass of sequences.

### 2.4 Sequence Data Formats

Each flat file from public biological database has different format. Genbank, Swiss-Prot [5], PIR-Codata [6], and PDB [7] flat files are generally used. Also, each sequence analyzing software uses different format. One of them, FASTA [8] established by Pearson is the most common format.

The problems of biological formats we mentioned above are following. The formats can be modified when they are released. To understand the range of field and its value is difficult and data types in the same field in each format can be different. The conversion among different formats needs different parsers to extract the user-interesting field.

```
> SQ2002060300001
GGTACCTTCTGAGGCGGAAAGAACCAG
CCGGATCCCTCGAGGGATCCAGACATG
CTTACCGGATACTG
```

**Fig. 1.** An example of FASTA format

Thus applying XML is essential to visualize and exchange the sequence data and bio-molecules because XML has high level format conversion technology and re-usability. There are a lot of markup languages to represent the genome data such as BSML, BioML (Biopolymer Markup Language) [9]. The public biological databases [3], [5], [6], [7] are also trying to produce the XML based formats to represent biological information.

### 3 System Architecture

Fig. 2 shows the system architecture we suggest. We briefly explain each component of our system which consists of File Transformation, Biological Information Editor, Query/Retrieval Processor, and Biological Data Storage Manager. In particular, Biological Information Editor constitutes of Mypage Editor, Annotation Editor, and Sequence Editor.

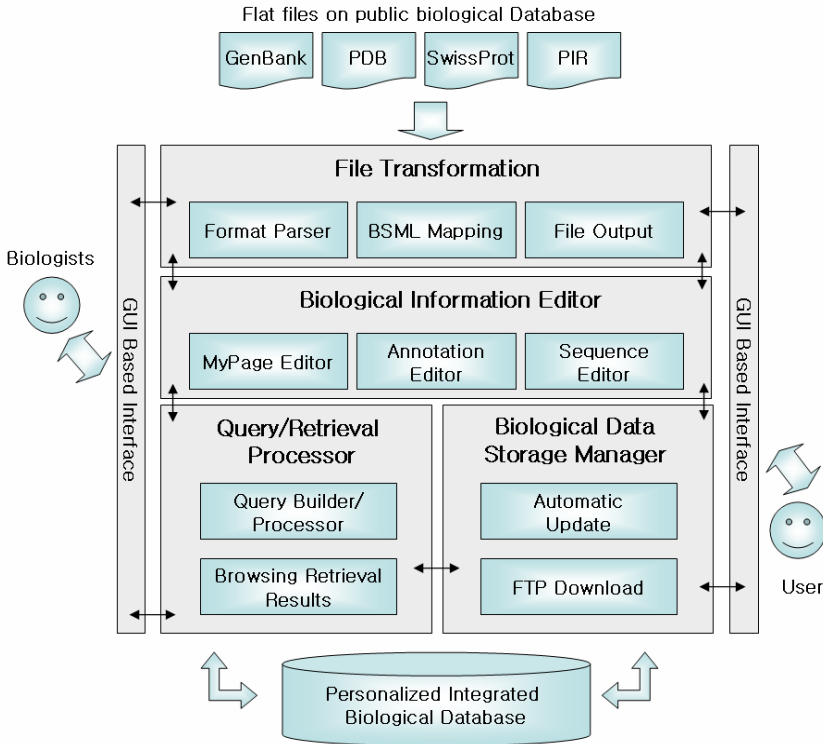
#### 3.1 File Transformation

File Transformation Module extracts meaningful data fields from each flat file in order to integrate heterogeneous formats from various public biological databases. The Flat File Parser which is suitable for each flat file is developed to extract the interesting fields from divergent biological flat files. The integrated BSML model is created with extracted data. We developed each Flat File Parser such as Genbank, Swiss-Prot, PIR-Codata, PDB, FASTA, BSML, and so on. The mapping information between the parsed fields and BSML elements (attributes) is considered in order to load on the system.

#### 3.2 Biological Information Editor

Biological Information Editor edits annotation and sequence data. Our Editor consists of MyPage Editor, Annotation Editor, and Sequence Editor.

MyPage Editor supports to make user defined formats that consist of interesting fields extracted from various flat files such as Genbank, Swiss-Prot, PDB, PIR-Codata, BSML, FASTA, and data on the local database. Once MyPage format is created by user, and then modification, insertion, and deletion of the field in the format are also performed by MyPage Editor. The user defined format through MyPage Editor is stored as an XML format on the disk or local database.



**Fig. 2.** System Architecture

While MyPage Editor creates user-defined formats and performs insertion, modification, and deletion of the interesting field extracted from each format, Annotation Editor performs the same operations for annotation data in each format. Therefore original source (flat file) is maintained their own frame. The modified original source stored as BSML format on the disk or local database if the user wants. Annotation Editor mainly handles annotation data of interesting sequence such as types, taxonomic information, citations, reference data, authors, and specific sites of sequences and so on.

Sequence Editor supports the useful operations to handle sequence, so it produces a new sequence from original sequence. We will briefly introduce several operations in

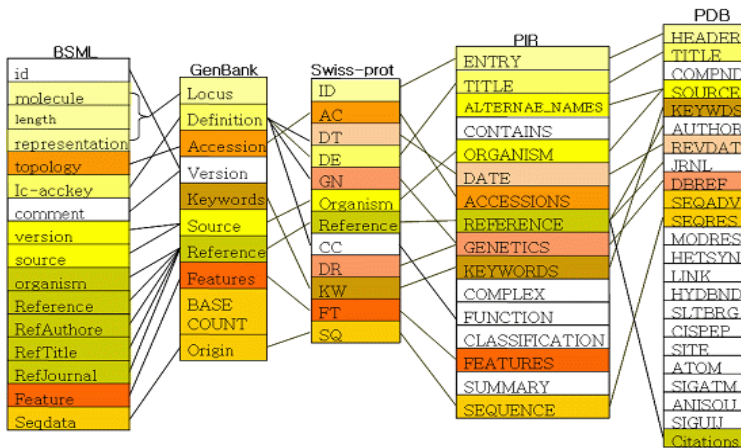


Fig. 3. Mapping Information among biological Formats

Fig. 4. *Base Composition* operation calculates the composition of DNA (Deoxyribo-Nucleic Acid) and shows us the percentage and the numbers of each Nucleotide (Adenine, Guanine, Cytosine, and Thymine). *Set-Subsequence* operation makes a new sequence from original sequence with starting and ending index which the user defines. *Complementary* operation produces complementary sequence of the original sequence. *Transcription* operation transforms the original sequence which is proven as gene, into mRNA (Messenger Ribo-Nucleic Acid) sequence. *Translation* operation transforms mRNA sequence into Protein sequence.

### 3.3 Query/Retrieval Processor

Through GUI (Graphic User Interface) environments, biologists input keywords to retrieve and Query/Retrieval Processor retrieves the local database and returns the suitable results which are compatible with the user-selected options such as AND and OR. Query results are displayed on the MyPage Editor when retrieving user-defined XML format through MyPage Editor. Also the results are showed on Annotation Editor when retrieving annotation data.

Query results on the MyPage and Annotation Editor are also modified by adequate Editors whenever user wants.

### 3.4 Biological Data Storage Manager

Sequence and its annotation data are separately stored because of the fast accession to biological data and retrieval. When biologists want to make other format from the database, for example FASTA format, the necessary data from the database are retrieved in order to make a new format.

|                                                                                                                                                                             |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>The original Sequence:</p> <pre>012345678901234567890123456789012345678901234567 atggtctacgtggttatatgcatactggaagcctacgacgtcatctaa       10      20      30      40</pre> |
| <p>(a) Base composition</p> <p style="text-align: center;">A: 13 bp T: 15 bp G: 10 bp C: 10 bp</p>                                                                          |
| <p>(b) Set-Subsequence</p> <pre>012345678901234567890123456789012345678901234567 tctacgtggttatatgcatactggaagcctacgacgtcatc 5      15      25      35      45</pre>          |
| <p>(c) Complementary</p> <pre>012345678901234567890123456789012345678901234567 ttagatgacgtcgtaggcttccagtatgcataataaccacgtagaacat       10      20      30      40</pre>     |
| <p>(d) Transcription</p> <pre>012345678901234567890123456789012345678901234567 auguucuacgugguuauaugcauacuggaagccuacgacgucaucuaa       10      20      30      40</pre>      |
| <p>(e) Translation</p> <pre>012345678901234567890123456789012345678901234567 Mfyvvicileaydvi       10      20</pre>                                                         |

**Fig. 4.** Sequence Operations

Our database maintains up-to-date biological information through automatic FTP (File Transfer Protocol) download and update. Users can monitor new release information of public biological database on the web using our system. Users store the absolute FTP path in our FTP lists. When biological databases release a new version, what users have to do is just choosing appropriate FTP path in FTP lists.

A new flat file from FTP downloading is compared with existing entry in the database to be updated. In this procedure, the system asks whether the database is updated as a new flat file or not.

## 4 Implementation

Implementation environments are as the following. MySQL 4.0.17 is used to store genomic sequence and annotation data. JAVA SWING by Sun-Mirco System is used to implement the major interface and JAXP (JAVA API for XML Processing) v1.2 for parsing XML documents. Our system is distributed on the web (<http://dblab.chungbuk.ac.kr/~SeqMan>) and an archive contains install-files such as MySQL 4.0.17 and our implementations. We have two examples to show our implementation.



**Example 1.** User wants to make Complementary, Transcription, Translation, and Set-Subsequence operations of original sequence (locus name 'DRONCX') in Genbank. The upper window in Fig. 5 shows the original sequence and the lower table shows the derived sequences from operations.

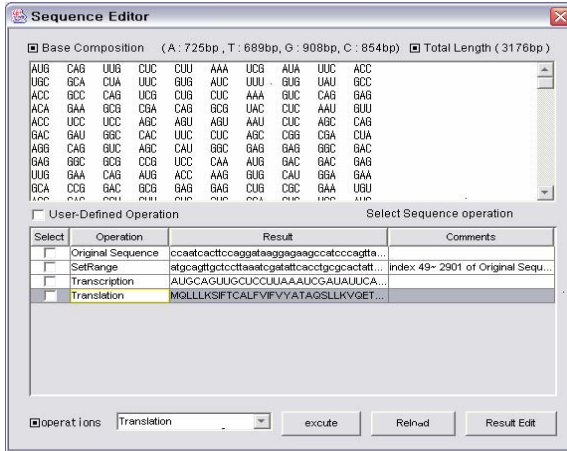


Fig. 5. Sequence Editor

**Example 2.** User wants to create a user defined format that consists of interesting fields from various file formats on MyPage Editor. Fig. 6 illustrates how a user defined format is created from Swiss-Prot (id 100K\_RAT), Genbank (locus name DRONCX), and PIR-Codata (entry CCHU).

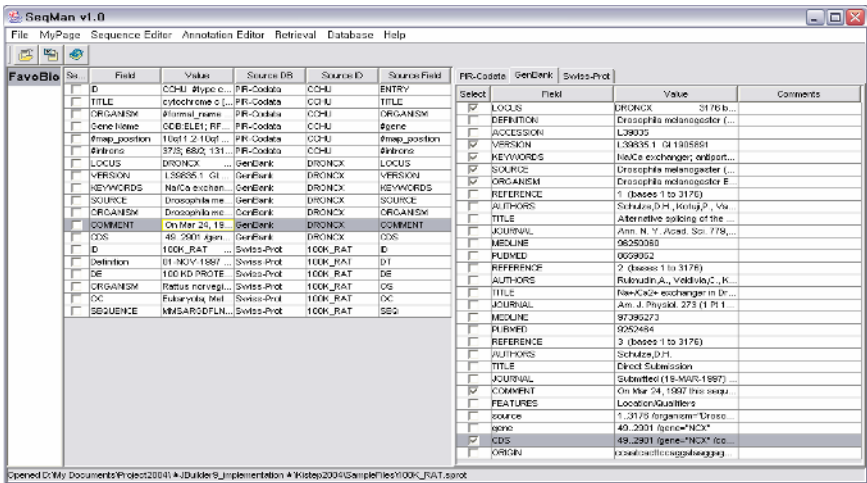


Fig. 6. MyPage Editor

## 5 Evaluation

In this paper, we implement new issues that we mentioned in introduction with deep consideration. The evaluation of the proposed system is performed according to comparing with Staden Package, Genbank, Genomic Workspace, and so on. Table 1 shows the result of comparison.

**Table 1.** Comparison with existing Sequence Management Systems

| Item                  | Staden Package | Genbank              | Genomic Workspace    | Proposed System              |
|-----------------------|----------------|----------------------|----------------------|------------------------------|
| Sequence Manipulation | Support        | None                 | None                 | Support                      |
| File Format           | EMBL format    | Genbank /ASN.1 /BSML | BSML                 | XML Format based on BSML DTD |
| Storing Sequence      | File           | DBMS                 | BSML Documents/ Text | DBMS                         |
| Sequence Versions     | None           | Support              | None                 | Support                      |
| File Transformation   | None           | None                 | Support              | Support                      |

Storing the historical data of released sequence (version) is useful to analyze the change of protein sequence. We expect that new useful protein and drug can be discovered based on analysis of version sequences.

Creating and designing new proteins from experiment and analyzing them using Sequence Editor are possible. The purpose of a PCR (Polymerase Chain Reaction) is to make huge copies of a gene. This is necessary to have enough starting template for sequencing. In this work, a complementary sequence of DNA strand is needed and a known Primer is required to synthesize. Therefore sequence operations we suggest are useful enough to design Primer.

Sequence information in our system is represented as XML format and converted into other formats to support efficient sequence analysis and easy format exchanging. That is, because of XML representation based on BSML DTD (Document Type Definition), sequence information is easily converted into other formats which are used in various analysis programs. FASTA is the most common format that the most analyzing software uses. One of advantages of our system is converting sequence from database or various sources into FASTA format.

## 6 Conclusion

According to improving techniques to get the biological information, a mass of biological data have been produced. Characteristics of these biological data including genome sequences are heterogeneous and various. Although the need of management systems which should reflect biological characteristic has been raised, the most current biological databases provide restricted function and act as repositories for biological data.

Therefore, this paper describes the management system of genome sequences and annotation data in order to manipulate the formats in bioinformatics. It includes format transforming, editing, storing and retrieving among collected nucleotide sequences from public databases, and handles sequence produced by experiments. It uses BSML format which is based on XML as a common format in order to extract data fields and exchange heterogeneous sequence formats. To manage sequences and their changes, that is, version management system for originated DNA is also useful to analyze and synthesize a new protein. This system automatically updates information in local database using FTP. This research is widely used for a long term study of biology, medical science, pharmacy and helps to accumulate the own sequence information at the level of biological laboratories.

Now, we are trying to extend our system in order to improve the analyzing ability. For instance, inserting sequence similarity module (such as Blast [10] and Psi-Blast [11]) and one-touch retrieval module which queries to public biological databases with one interface. After we implement sequence similarity checking modules, users don't need to connect sequence analyzing site on the web. In this process, we prevent our valuable information in the laboratory from revealing to exterior. One-touch querying interface using web agent and synonym semantic search make users retrieve results from more than one public database at same time, with one interface.

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# An Automatic Nematode Identification Method Based on Locomotion Patterns

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**Abstract.** Nematodes are primitive creatures that are endangering and devouring many of the essential resources beneficial to human beings. For effective inspection and quarantine, we have devised an image based system for quantitatively characterizing and identifying nematodes, and achieved average successful identification rate of 71.2% for the Uncoordinated (Unc) mutant types and 91.2% for other types. To enhance system performance, here we introduce the worm-body Trunk Coordinate System for defining and characterizing the locomotion patterns of representative mutants. At least 60,000 frames for each species, totally 480,000 frames, representing wild type and 7 other mutant types, were analyzed. The average correct classification rate, measured by Classification and Regression Tree (CART) algorithm, was 79.3% for Unc types. The scheme devised and the features extracted are good supplements for the previous automated nematode identification system.

## 1 Introduction

Nematodes are the most numerous multicellular animals on the earth, and there are nearly 20,000 described species classified in the phylum *Nemata*. Many of them are parasites of insects, plants and animals. Among them, some species are threatening the development of farming and forestry all over the world. Lesion nematode, *Pratylenchus Goodeyi*, for example, claims as high as 47% U.S. commercial pineapple reduction centered in Hawaii in 2002, according to the NCFAP report [6]. So detection and identification of nematodes are the prerequisite for controlling and checking them from spread. However the subtle differences between some species make it difficult to distinguish them simply by naked-eye observation. Therefore there exists the challenge of precisely defining and the quantitatively measuring nematode behavior patterns.

One way to address these problems is using compute-driven systems for recording and analyzing nematode behaviors. Some scholars have been doing relevant jobs with different methods and different features. Geng et al. [3] solved behavior phenotype classification of some *C. elegans*. Their work focused on the movement of centroid, the location of head and tail, and the position relationship between head to tail, head

to centroid, and tail to centroid. Silva et al. [7] proposed an intelligent nematode detection system. But the system only detected whether worms exist or not. We built an automatic identification system based on the head and tail locomotion patterns in the worm-body Trunk Coordinate System.

Based on our previous works [1] [9], we built an advanced system that can automatically identify different nematodes using Trunk Polar Coordinate System. The system can get approximately 80% for Unc types, and 90% or higher success rates for other types after we added some new locomotion features to head and tail upon the existing features. And the processing procedure in this system can be divided into several stages, seen in Fig. 1.

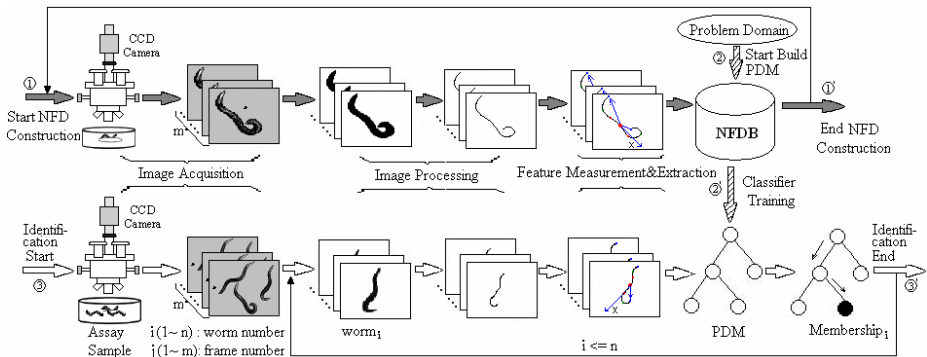


Fig. 1. The system architecture and processing stages

The system starts with constructing a general Nematode Feature Database (NFDB). By feeding Image Acquisition Block (IAB) each time with a new type-known assay sample, after Image Processing Block (IPB) and Feature Extraction Block (FEB), NFDB can record as much species information as possible so as to let it cover most of the problem domains. In the second phase, the system builds the Problem Domain Model (PDM) by querying NFDB. The querying terms come from the domain requirements, and the queried result is the domain-scope nematode features. These features, as training data, are used to build the classifier model for that domain nematode identification. In the third phase, the classifier decides the assay nematode memberships by feeding the assay sample features to the PDM.

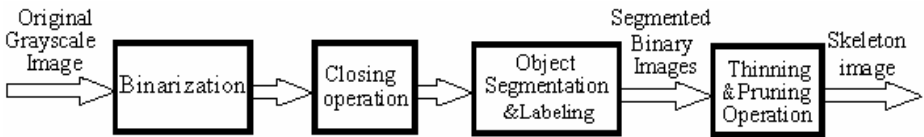
The paper is organized according to the processing stages. The image acquisition and processing, feature extraction, and feature selection are discussed in section 2, section 3, and section 4 respectively. Section 5 gives the *C. elegans* worm experiment results. Section 6 concludes this article.

## 2 Image Acquisition and Processing

The original images are acquired from a stereomicroscope mounted with a device video camera [1], an automatic track system motorized microscope that could record an individual animal's behaviors at high magnification. In our system, the *C. elegans*

locomotion was tracked with a stereomicroscope mounted with a high performance CCD video camera. For each species, in order to get one time-continuous footage, around 600 frames of that species were snapped with the frequency of 2Hz for time span of about 5 minutes, and this process was implemented 100 times for that species. So, at least 60,000 frames for each species, totally 480,000 frames, representing 8 types of sample worms, were analyzed. These captured image frames were trimmed by the smallest axis-aligned rectangles that contain the worm body, and then saved as eight-bit grayscale data with time-index.

To facilitate feature extraction, the grayscale data were subjected to image processing to reduce irrelevant information or noise and to enhance the image properties. Besides, considering the features to be extracted from skeleton images, thinning and pruning are necessary operations. The image processing includes several procedures shown in Fig. 2.

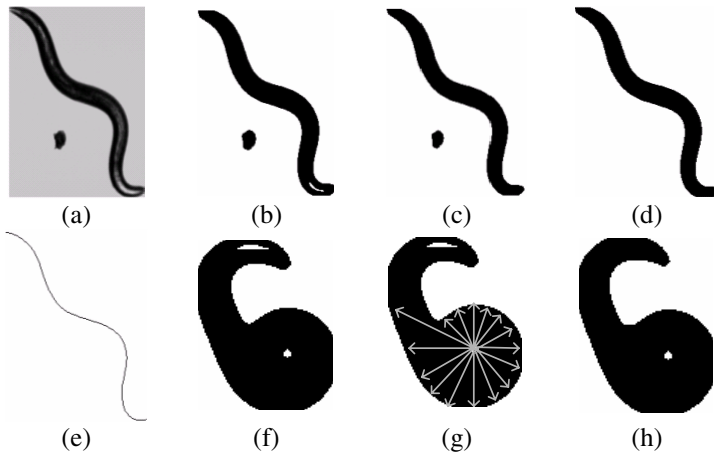


**Fig. 2.** Image processing procedure

The first step is to convert gray level image into binary image with a local threshold using a  $5 \times 5$  scanning window (Fig. 3b). But we need decide the threshold value to discern the worm body and background by using statistic data such as histogram. Based on the histogram of the gray images, two peak values representing worm body and background can be found respectively according the distribution of the worm body gray value and the background gray value, and the relationship between them can be found. While considering the influence of factors as light and point of view, a moving window was scanned over the trimmed image, and the grayscale images can be converted smoothly into binary images according to the computation of the mean and standard deviation of the pixel inside the moving window.

The second step is to clean the spots inside the worm body with a morphological closing operator [4]. Because of the influence of light and view, some spots can be seen inside the worm body. Such morphological operations as dilation and erosion can be used to clean these spots (Fig. 3c). Yet these operations can also remove the looped holes at the same time. To remove the spots inside the worm body and to remain the holes simultaneously, we measure thickness of these two regions with 16 vectors (Fig. 3g). The number of pixels, or thickness, from the centroid to the background in each vector direction is counted for every spot region. If the total thickness is less than a threshold, in our experiment it is 25, the region is considered as noise. Otherwise, we preserve the region as a hole.

The third step is to remove isolated small objects with the sequential algorithm for component labeling [5]. The connected components were labeled by scanning the image in x and y directions sequentially, and the different components were segmented into different areas. The areas containing isolated objects such as eggs are removed by setting off pixel (Fig. 3d).



**Fig. 3.** (a) Original gray level image, (b)(f) Binary image after thresholding operation, (c) Binary image following closing operation, (d) Final clean binary image after removal of isolated object, (e) Skeleton obtained through thinning and pruning, (g) Hole detection using 16 measuring vectors, (h) The result of hole detection and noise removal

In addition, the morphological skeleton was obtained by applying a skeleton algorithm [8]. Finally, by iterating dilation operation along the binary image, a clean skeleton can be obtained. And by tracing the skeleton, we got the pixel sequence on the skeleton, which will be used to sample points.

### 3 Feature Extraction

Based on the segmented binary image and skeleton image, we can extract the features to describe the body shape and locomotion pattern of the Nematode. In order to avoid the extreme values introduced by noise, top 10% minimum value and top maximum values are discarded. At the same time, we use max, min and average to analyze some features. The measured features in our system include the minimum, maximum, and average values of the following: distance moved in 0.5, 5, 10, 15, 20, 25, and 30s; and 5 min, number of reversals in 40, 80, and 120s; and 5 min, worm area, worm length, width at center and head/tail, ratio of thickness to length, fatness, eccentricity and lengths of major/minor axes of best-fit ellipse, height and width of minimum enclosing rectangle (MER), ratio of MER width and height, ratio of worm area to MER area, angle change rate. These features can be seen as [9]. Here we just discuss the new feature details.

We kept the features to describe the worm shape and movement in our previous system [9]. The features to describe the body shapes and locomotion patterns can be extracted based on the segmented binary images and skeleton images. The measured features in our system include the centroid moving distance, number of reversals, worm area, worm length, worm width, fatness, eccentricity and lengths of major/minor axes of best-fit ellipse, height and width of minimum enclosing rectangle (MER), angle change rate etc.



But as we mentioned in our previous work [9], using these features cannot classify the Unc classes well. In order to improve the performance of the identification results, we added the locomotion trend information of the nematodes into the feature space using the moving distance and absolute angle change of the sample points. In the following part, we will explain the details about these new features.

### 3.1 Head and Tail Recognition for Each Frame

Our work is based on two clues that come from human observers: 1) the movement of the worm starts from the head; 2) the head moves more frequently than the tail. Based on the domain knowledge, first, we can recognize the head and tail, and then select some sample points from the skeleton and contour to describe the locomotion current. We just used the movement degree to discern the head and tail in our experiments.

Based on the image processing described above, we can get binary image, skeleton image and contour image. We can get two end points and the skeleton pixel sequence. These two end points will be divided into two groups (group1 and group2) according to the position similarity between two consecutive frames. Let  $Endptm(t)=(endptmx(t), endptmy(t))$  denotes the  $m$ th endpoint in frame  $t$ , and  $Endptn(t+1)=(endptnx(t+1), endptny(t+1))$  as the  $n$ th endpoint in frame  $t+1$ . The distance between endpoint  $n$  in frame  $t+1$  and the endpoint  $m$  in frame  $t$  is  $d(m,n)$ . We initialize the *group1* as  $(endpt1x, endpt1y)$  and *group2* as  $(endpt2x, endpt2y)$ .

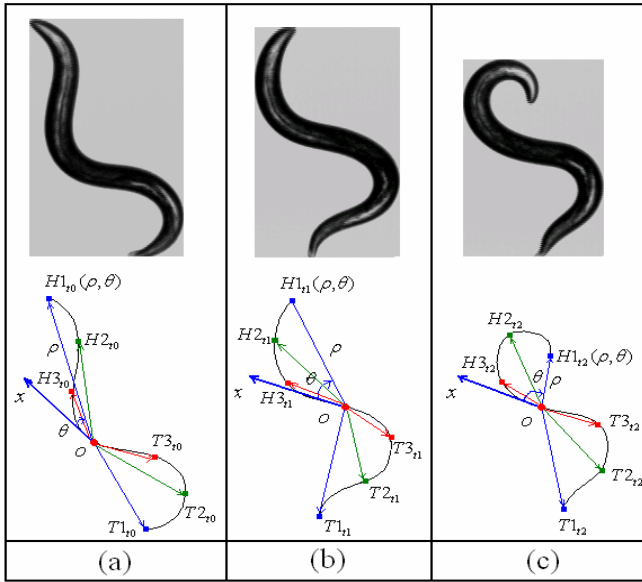
For each following frame, if the head and tail are not being accidentally flipped, the  $k$ th endpoint in frame  $(t+1)$   $Endptk(t+1)$  will be assigned as group  $g$  like the equations (1) provided that another point  $\overline{Endptv(t+1)}$  which was assumed into the other group  $\bar{g}$ , and the distance between  $\overline{Endptv(t+1)}$  and the endpoint that belongs to group  $\bar{g}$  in frame  $t$  is not the maximum at the same time. Here  $g(v)$  is the group to which the  $v$ th endpoint in frame  $t$  belongs. This group rule actually is implemented according to the coordinate of the end points in adjacent two frames.

$$\begin{aligned}
 (k, g) &= \arg \overline{(k, g(v))} \{d(Endptk(t+1), Endptv(t)) = \min \{d(m, n)\}\} \\
 \text{where } d(\overline{Endptk(t+1)}, \overline{Endptv(t)}) &\neq \max \{d(m, n)\} \\
 m &= \{Endpt1(t), Endpt2(t)\}, n = \{Endpt1(t+1), Endpt2(t+1)\}
 \end{aligned}
 \tag{1}$$

For these groups, we can mark them head group (*Headg*) with bigger offset or tail group (*Tailg*) with smaller offset.

### 3.2 Feature Extraction from Head and Tail Segments

We described the worm movement using sample point positions from head and tail segments in the Trunk Polar Coordinate System (Fig 4). From the figure, we can see the head and tail move trend can be reflected well under this new coordinate system. The head and tail segments are 1/3 skeleton-length. 10 points are sampled from two segments respectively. The center position on the skeleton is set as original point and the best-fit line from a 9-pixel long segment on the skeleton list near this position is set as the major axis, and the positive direction  $(p_x, p_y)$  is assigned as the same side



**Fig. 4.** Feature extracting based on Trunk Polar Coordinate System among three consecutive frames; the overstriking blue narrow line is the polar axis; the other narrow lines are the sample point vectors

with the head side as equation 2. The distance and angle of the sample point  $(\rho_i, \theta_i)$  in this new system are the measurements by using equation 3 and 4.

$$(p_x, p_y) = \arg(l_{xk}, l_{yk}) \left\{ \cos^{-1} \frac{(x_i - x_c) \cdot l_{xk} + (y_i - y_c) \cdot l_{yk}}{\sqrt{(x_i - x_c)^2 + (y_i - y_c)^2} + \sqrt{l_{xk}^2 + l_{yk}^2}} > 0 \right\}, \quad (2)$$

where  $k \in \{1, 2\}$ ,  $(l_{x1}, l_{y1})$  is the vector that x increases on the fitting line,

$(l_{x2}, l_{y2})$  is the opposite vector of  $(l_{x1}, l_{y1})$

$$\rho_i = \sqrt{(x_i - x_c)^2 + (y_i - y_c)^2}, \quad (3)$$

where  $(x_c, y_c)$  is the center position on the skeleton

$$\theta_i = \cos^{-1} \frac{(x_i - x_c) \cdot p_x + (y_i - y_c) \cdot p_y}{\sqrt{(x_i - x_c)^2 + (y_i - y_c)^2} + \sqrt{p_x^2 + p_y^2}}, \quad (4)$$

where  $(p_x, p_y)$  is the direction vector of the positive polar axis.

The difference of these two measurements  $(\Delta\rho_i, \Delta\theta_i)$  is used to describe the moving trend.  $\Delta\rho_i$  is the distance offset of the  $i$ th sample point to the original point in this new coordinator system from the  $t$ th frame to the  $(t+1)$ th frame. And the

minimum, average and maximum statistic of these measurements are used in our system as new features to improve the identification performance.

## 4 Feature Selection

After adding the new features, we used the classification and regression tree (CART) algorithm [2] to evaluate the importance of the feature variables and 10-fold cross validation to determine the performance and the right size of the optimal tree. The CART approach involves recording a set of examples of each worm type according to the problem domain modeling. In our system, we set Unc type as the problem domain. And CART is used to evaluate the feature importance to classify or to identify Unc types. From the measured featured obtained in section 3, a training vector is generated, each vector element recording the values for each feature measurement. Using this learning sample, CART produced a binary classification tree in which each binary split of the data involves a splitting question of the form ‘Is  $x_m \leq c$ ’, where  $x_m$  is the measurements, and  $c$  is a threshold. The root node of the tree contains all the training cases; the worm types are equally mixed together in this node.

In our experiment, the original measurement vector is consisted of 94 features used in our previous system [9] and 12 new features as discussed in section 3. According to the report from CART, we built an optimal classification tree using only 14 parameters which are listed in Table 1. Here the point worthy mentioning is that the average distance offset of head, the average offset distance of tail, and the maximum head angle offset are added as important new features. And the cross validation classification probability for each type is given in Table 2. The success rates are listed along the diagonal and the misclassification error rates are listed in the off-diagonal entries. Compared with the results in [9], we can see the distinctly improved performance of *unc-36* and *unc-38*.

**Table 1.** Important features identified by CART

| Category   | Description                                  |
|------------|----------------------------------------------|
| LNMFRMAX   | Max ratio of worm length to MER fill         |
| MVHLFAVG   | Average distance moved in 0.5 seconds        |
| ANCHRMAX   | Max angle change rate                        |
| TOTRV      | Total number of reversals in 5 minutes       |
| CNTRLRMIN  | Min ratio of center thickness to length      |
| RV80MAX    | Max number of reversals in 40 sec/ 80 frames |
| LPSUM      | Total number of frames the worm is looped    |
| AREAMAX    | Max area of the worm                         |
| CNTMVAVG   | Average thickness at the center position     |
| MVHLFMAX   | Max distance moved in 0.5 seconds            |
| LNMFRMAX   | Average ratio of worm length to MER fill     |
| HDISOFFAVG | Average offset distance of head              |
| HANGOFFMAX | Max head angle offset                        |
| TDISOFFAVG | Average offset distance of tail              |

## 5 Experiment Results

We programmed in Visual C++ to process the image to get the filtered binary image and skeleton image. Based on these two images, some shape features such as length, fatness, best-fit ellipse height and width, worm area and so on and some locomotion features like reversals, angle change rate, the number of holes are computed. And the two endpoints in every frame are divided into two groups, and the sample point positions at the Trunk Polar Coordinate System are computed using the Visual C++ program. The offsets of the head position and tail position are obtained by using MATLAB codes based on the coordinate data in Visual C++. And we also built the optimized classification tree using CART, which is used to evaluate the feature importance and to select features.

**Table 2.** Classification results from 10-fold cross validation

| Actual | Predicted |       |       |        |        |        |       |        |
|--------|-----------|-------|-------|--------|--------|--------|-------|--------|
|        | Wild      | Goa-1 | Nic-1 | Unc-36 | Unc-38 | Egl-19 | Unc-2 | Unc-29 |
| Wild   | 0.951     | 0.000 | 0.000 | 0.000  | 0.000  | 0.000  | 0.020 | 0.030  |
| Goa-1  | 0.010     | 0.933 | 0.000 | 0.020  | 0.010  | 0.000  | 0.000 | 0.020  |
| Nic-1  | 0.000     | 0.000 | 0.890 | 0.000  | 0.060  | 0.000  | 0.000 | 0.000  |
| Unc-36 | 0.000     | 0.000 | 0.000 | 0.800  | 0.050  | 0.020  | 0.120 | 0.050  |
| Unc-38 | 0.000     | 0.000 | 0.000 | 0.040  | 0.847  | 0.000  | 0.050 | 0.170  |
| Egl-19 | 0.000     | 0.000 | 0.000 | 0.020  | 0.000  | 0.933  | 0.000 | 0.020  |
| Unc-2  | 0.033     | 0.067 | 0.017 | 0.150  | 0.100  | 0.000  | 0.767 | 0.000  |
| Unc-29 | 0.000     | 0.000 | 0.000 | 0.120  | 0.080  | 0.010  | 0.110 | 0.767  |

**Table 3.** The comparison of the proposed method with the previous method in [9]

| Methods  | Predicted (Success Ratio) |       |       |        |        |        |       |        |
|----------|---------------------------|-------|-------|--------|--------|--------|-------|--------|
|          | Wild                      | Goa-1 | Nic-1 | Unc-36 | Unc-38 | Egl-19 | Unc-2 | Unc-29 |
| Previous | 0.950                     | 0.930 | 0.880 | 0.760  | 0.730  | 0.930  | 0.717 | 0.760  |
| Proposed | 0.951                     | 0.933 | 0.891 | 0.800  | 0.847  | 0.933  | 0.767 | 0.767  |

In our experiment, the learning samples are from 800 data files. And we identified these 8 different uncoordinated mutants with distinct locomotion patterns: wild-type, *unc-36*, *unc-38*, *egl-19*, *nic-1*, *unc-29* and *unc-2*. Each strain has 100 5-min recordings, with images captured every 0.5s. Every stain has 100 data file, and every data file has about 600 frames. From the experiment results of CART analysis in Table 3, we can see better identification performance for Unc type worms compared with the result using method in [9]. However, the successful classification ratios of *unc-2* and *unc-29* are still less than 80%. We analyzed the data generated by this proposed system; lots of frames are regarded as invalid, which leads to the incomplete feature sets. And after observing the recording of *unc-2* and *unc-29*, we found that their locomotion patterns tend to coil which is not supported by our feature extraction block. The holes and loops in the worm body make it hard to describe the worm body using a sequence of data point. Because at the cross points, we have not found out a suitable method to get a correct sequence of data points.

## 6 Conclusion

This image based automatic identification of nematode system can avoid subjectivity from observation, and be much more reliable at detecting representative abnormalities and behavior patterns that are subtle during a short time span or manifested in long time span. And also we can find that better identification results can be made by combining both shape and locomotion features. Especially for the Unc types, which have special locomotion pattern, the identification results can be improved greatly by using the locomotion pattern with the offset of the head and tail position.

Yet the identification performances of some worm types are still not excellent. After analyzing the data generated by this proposed system, we found some of frames are marked as invalid by the proposed system due to the worms postures are not suitable for the further processing and feature extraction, which eventually leads to the incompleteness of the feature sets. We are still trying to find better ways to match the loops or the holes locomotion pattern for the Unc type.

## Acknowledgements

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# An Efficient Attribute Ordering Optimization in Bayesian Networks for Prognostic Modeling of the Metabolic Syndrome

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**Abstract.** The metabolic syndrome has become a significant problem in Asian countries recently due to the change in dietary habit and life style. Bayesian networks provide a robust formalism for probabilistic modeling, so they have been used as a method for prognostic model in medical domain. Since K2 algorithm is influenced by an input order of the attributes, optimization of BN attribute ordering is studied. This paper proposes an evolutionary optimization of attribute ordering in BN to solve this problem using a genetic algorithm with medical knowledge. Experiments have been conducted with the dataset obtained in Yonchon County of Korea, and the proposed model provides better performance than the comparable models.

## 1 Introduction

The metabolic syndrome is composed of a cluster of metabolic disorders including abdominal obesity, insulin resistance, dyslipidemia and hypertension, and the correlation between metabolic syndrome and coronary heart disease was reported in previous studies [1]. It affects around 25% of adults over the age of 20 and up to 45% over age 50 in the United States [2]. In Asian countries, it has become a significant problem lately due to the change in dietary habit and life style. In situations like this, many groups have been studying the metabolic syndrome from all over the world [1-2].

The Bayesian network has emerged in recent years as a powerful technique for handling uncertainty in complex domains [3]. It is a model of a joint probability distribution over a set of random variables. The Bayesian network is represented as a directed acyclic graph where nodes correspond to variables and arcs correspond to probabilistic dependencies between connected nodes [3]. Bayesian networks have been used for prediction or classification problem in the medical domain and shown high performance. In particular, they have been applied successfully to the modeling of diagnosis and prognosis for diverse diseases [4-6]. There have been many black box tools that classify or predict several diseases, and neural networks are the representative example. Bayesian networks have strengths that they can use the domain knowledge easily and analyze the results compared to them [5]. Even though

sometimes they are not better than neural networks in terms of accuracies, Bayesian networks are appropriate methods in the medical domain that require analyzing the results with medical knowledge.

This paper deals with a problem that predicts the metabolic syndrome with the dataset obtained in Yonchon County of Korea. This paper makes a prognostic model using Bayesian network, and has used the K2 algorithm by Cooper and Herskovits in order to learn its structure [7]. Since the result of the K2 algorithm is influenced by an input ordering of the attributes, an optimization of this ordering has been also studied [7]. This paper proposes an efficient optimization method using a genetic algorithm with medical domain knowledge in order to solve this problem. Contrary to the conventional methods, after clustering similar attributes into each group, an ordering of the groups and an ordering of the attributes in each group have been performed in turns. By applying the medical domain knowledge, an efficient and reliable evolution process can be conducted. Subsequently, the experiments using the proposed prognostic model have been done after the structure and parameter learning processes in order to show its usefulness.

## 2 The Problem: The Metabolic Syndrome

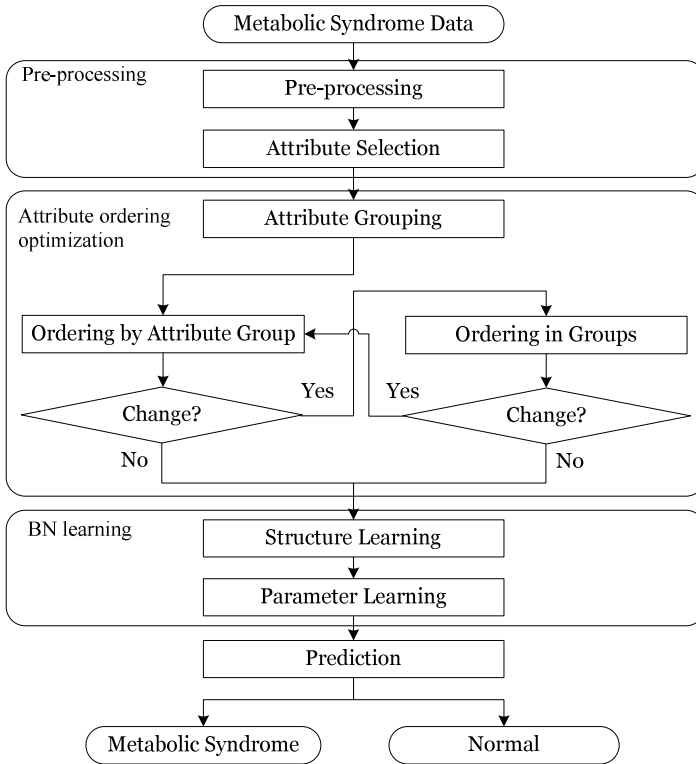
The definition of the metabolic syndrome was provided by the National Cholesterol and Education Program, Adult Treatment Panel III (ATP III). It requires the presence of three or more of the following components [1, 2]:

- 1) Abdominal obesity  
(waist circumference  $>102$  cm in men and  $>88$  cm in women),
- 2) Hypertriglyceridemia ( $\geq 150$  mg/dL),
- 3) Low high density lipoprotein (HDL) cholesterol  
 $<40$  mg/dL in men and  $<50$  mg/dL in women),
- 4) High blood pressure (systolic  $\geq 130$  mmHg or diastolic  $\geq 80$  mmHg) and
- 5) High fasting glucose ( $>110$  mg/dL).

Since this original standard is not appropriate for Asian, we have used modified the definition for Asian of the abdominal obesity (waist circumference  $>90$  cm in men and  $>80$  cm in women) in this paper [8].

## 3 Prognostic Modeling of the Metabolic Syndrome

Fig. 1 illustrates the flowchart that makes the proposed prognostic model. This process can be divided into four main parts: pre-processing, attribute ordering, BN learning, and prediction processes. For the pre-processing part, medical domain knowledge has been applied, so the prediction model would be more reliable. For the attribute ordering part, a genetic algorithm has been also used in order to optimize the ordering of the model efficiently. The structure and parameter learning processes have been conducted after the attribute ordering, and the whole process is finished with prediction of input samples.



**Fig. 1.** The overall flowchart of the proposed method

### 3.1 Data Pre-processing and Attribute Selection

The pre-processing part subdivides into the pre-processing and an attribute selection. Here, we have decided the discrete states of the attributes since most attributes have continuous values and BN requires discrete states. The medical literatures [1, 2, 8] and experts have given a help for this process.

Table 1 demonstrates the attributes and their possible states. Explaining a few important attributes here, fasting glucose is divided into normal ( $<110$ ), impaired glucose metabolism ( $110\sim 125$ ) and diabetes ( $>125$ ). Triglyceride is increased if its value is larger than 150, or normal. In case of HDL cholesterol, it is decreased (abnormal) when it is smaller than standard value, 40 in men and 50 in women. The standards for state discrimination used here are significant since they have been used by medical experts [8].

We have chosen the informative attributes for the prognostic model after the pre-processing. As described in section 2, basic attributes required for defining metabolic syndrome are eight. However, there are more attributes that influence the metabolic syndrome such as age, 2-hour postprandial glucose, hypertension and body mass



index [9]. Among these four attributes, the information of hypertension is redundant with the information of basic attributes. Therefore, we have proposed the Bayesian network model using 11 attributes, which include eight basic attributes and additional three informative attributes of age, 2-hour postprandial glucose and body mass index for the prognostic model of the metabolic syndrome. It is well-known that age is closely related to the metabolic syndrome and 2-hour postprandial glucose influence fasting glucose of an important attribute [9, 10]. Body mass index is selected because it is related to obesity, which is related to the metabolic syndrome.

**Table 1.** Attributes and the possible states

| Attribute                        | Possible states                               |
|----------------------------------|-----------------------------------------------|
| Age                              | young, middle aged, old                       |
| Sex                              | male, female                                  |
| Fasting glucose                  | normal, impaired glucose metabolism, diabetes |
| 2-hour postprandial glucose      | normal, impaired glucose metabolism, diabetes |
| Waist circumference              | normal, abdominal obesity                     |
| Triglyceride                     | normal, increased                             |
| HDL cholesterol                  | decreased, normal                             |
| Body mass index                  | low weight, normal, over weight, obesity      |
| Ratio of waist-hip circumference | normal, abdominal obesity                     |
| Systolic blood pressure          | normal, hypertension                          |
| Diastolic blood pressure         | normal, hypertension                          |

### 3.2 Evolutionary Optimization of Attribute Ordering

For the structure learning process of the Bayesian network, we have used the K2 algorithm, which is subject to an ordering of attributes when they are input. Therefore, an attribute ordering optimization has been studied to make Bayesian network more accurate. Larranaga *et al.* regarded this ordering problem as an ordering of cities in the TSP (Traveling Salesman Problem), and applied several genetic algorithms that had been used for the TSP [7]. We have also used the genetic algorithm to optimize attribute ordering and applied medical domain knowledge to make a model more efficiently.

#### 1) Optimizing Attribute Group Ordering

As illustrated in attribute ordering part of Fig. 1, grouping of similar attributes is performed first. It is so complicated that we cannot simplify the causal relationship among attributes, but it is known that the attributes related to obesity are expressed first and ones related to metabolic disorder follow generally [10]. We have grouped twelve attributes, 11 attributes and a label, based on this information, so three attributes (waist circumference, body mass index, and ratio of waist-hip circumference) related to obesity and four attributes (fasting glucose, 2-hour postprandial glucose, triglyceride, and HDL cholesterol) related to metabolic disorder are grouped, respectively. The remaining five attributes are treated as five groups with a single attribute, respectively.

Subsequently, an ordering of these seven attribute groups is optimized. Ordering of attribute groups is optimized first, and then ordering of attributes in each group is optimized. These two processes are repeated until there is no change of ordering after each optimization step.

2) Application of the Genetic Algorithm

Details of chromosome representation, selection, and genetic operations are as follows.



Fig. 2. Chromosome representation

As shown in Fig. 2, supposing each chromosome consists of  $m$  attribute groups, each group has group ID, the number of attributes in each group, and attributes themselves in each group, general genetic operations can be conducted. Attribute ordering of initial chromosome is decided randomly, and the fitness of each individual is evaluated in terms of the predictive accuracy because this paper focuses on the prognostic modeling.

After evaluating the fitness of individuals, individuals for the next generation are selected using rank-based selection method. In (1),  $I_{(g,j)}$  means the  $j$ th individual in the  $g$ th generation, and  $\text{Rank}(f(I_{(g,j)}))$  means the rank of each individual based on the fitness.  $n$  represents the number of individuals, and  $p_{(g,j)}$ , the probability that each individual  $I_{(g,j)}$  is selected, can be provided as shown in (1).

$$p_{(g,j)} = \frac{n - \text{Rank}(f(I_{(g,j)})) + 1}{n(n+1)/2} \tag{1}$$

Crossover and mutation operations follow the selection process. Larranaga *et al.* compared several crossover operators on the TSP, and cycle crossover (CX) operator was the best [9]. This operator provides high performance even though the number of individuals is small. It attempts to create an offspring from the parents where every position is occupied by a corresponding element from one of the parents [7]. Fig. 3 illustrates an example of CX operation. There are two cycles in each individual, and they are crossed over each other.

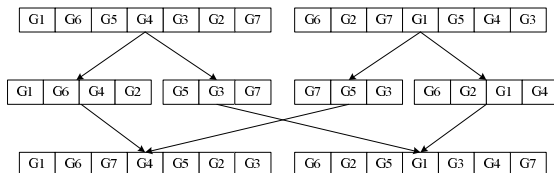


Fig. 3. An example of CX operation

Displacement mutation (DM) operator has been used for mutation operation. This operator provided the best performance when it was used with CX operator in Larranaga’s work [7]. First, it selects a random substring and removes it, and it inserts this substring into random position. Fig. 4 shows an example of DM operation.

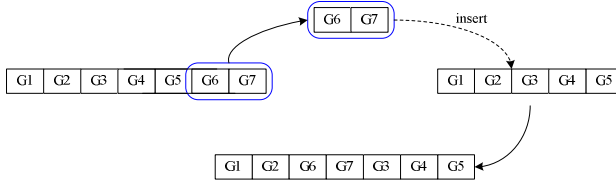


Fig. 4. An example of DM operation

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The K2 Algorithm

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**Input :**  
 A set of  $n$  nodes,  
 An ordering on the nodes,  
 An upper bound  $u$  on the number of parents a node can have,  
 A dataset  $D$  including  $m$  cases.

**Output :**  
 A printout of each node and its parents.

---

```

for ($i=1$; $i<n$; $i++$) {
 $\Pi_i = 0$;
 $P_{old} = g(i, \Pi_i)$;
 OK2Proceed = TRUE;
 while (OK2Proceed && $|\Pi_i| < u$) {
 Let Z be the node in $\text{Pred}(X_i) - \Pi_i$ that maximizes
 $g(i, \Pi_i \cup \{Z\})$;
 $P_{new} = g(i, \Pi_i \cup \{Z\})$;
 if ($P_{new} > P_{old}$) {
 $P_{old} = P_{new}$;
 $\Pi_i = \Pi_i \cup \{Z\}$;
 }
 OK2Proceed = FALSE;
 }
 print("node: ", X_i , "parents: ", Π_i);
}

```

---

Fig. 5. The K2 algorithm

### 3) Structure and Parameter Learning

With the evolved ordering decided before, we train the Bayesian network using the K2 algorithm [13]. The K2 algorithm narrows down the search space by fixing an

order of the attributes. The probabilities of nodes have been calculated from the frequency counts of the learning data. Fig. 5 provides the pseudo-code of the K2 algorithm.

Given dataset  $D$ , the K2 algorithm searches the set of parent nodes that maximizes  $P(B_s, D)$  for every node. K2 starts by assuming that nodes do not have parents. For every step, it incrementally adds specific parent whose addition increases the probability of the result structure most. These processes continue until the addition of a single parent cannot increase the probability. K2 is a greedy heuristic, and it does not guarantee the structure with the highest probability. The details are provided in [13].

Once the structure of Bayesian network is decided, parameter values of each node are calculated from the frequency of learning data, and then the prognostic model of the metabolic syndrome is completed.

## 4 Experimental Results

### 4.1 Experimental Data

The dataset used in this paper was examined for epidemiological research of the local community. The surveys were conducted twice in 1993 and 1995 in Yonchon County of Korea. 2,293 subjects were participated in the first survey, and 1,193 of them were participated in the second survey [12]. We have used the data of 1,135 subjects who did not include missing values and the 18 attributes that could influence the prediction of the metabolic syndrome. After that we have decided whether each sample would belong to the metabolic syndrome or not. 18 attributes and the distribution by states are shown in Table 2.

### 4.2 Parameters and Settings

In order to compare the result of Bayesian network model with the other models, neural network (NN) and  $k$ -nearest neighbors (kNN) prediction models have been used. 11 input nodes, 20 hidden nodes, and 2 output nodes are used for NN, and  $k$  of kNN is fixed as 3 having shown the best performance in a preliminary experiment.

For the genetic algorithm, population size is set as 20, and the process has evolved by the generation of 100. The population size is small because the total search space is not so large. The number of possible combinations is  $7!$ , but the time cost is expensive using an exhaustive method since the learning and inference processes are required for every individual of every generation. The selection rate of 0.8 and mutation rate of 0.02 are used. Crossover rate is set as 1.0, but it is less than that because the result of the CX operation sometimes is not changed.

For experiments before evolution, 10-fold cross validation is repeated 30 times, and the average is used for the result. For evolution process, we have divided the data into three parts with the ratio of 3:1:1. The first part is used for the learning, the second one is used for the validation, and the last one is used for the test.

**Table 2.** The attributes of the dataset and the distribution by states

| <b>Attributes</b>                | <b>n</b> | <b>Percentage</b> |
|----------------------------------|----------|-------------------|
| Age                              |          |                   |
| Young                            | 111      | 9.78              |
| Middle aged                      | 512      | 45.11             |
| Old                              | 512      | 45.11             |
| Sex                              |          |                   |
| Female                           | 646      | 56.92             |
| Male                             | 489      | 43.08             |
| Fasting glucose                  |          |                   |
| Normal                           | 942      | 82.99             |
| Impaired glucose metabolism      | 166      | 14.63             |
| Diabetes                         | 27       | 2.38              |
| 2-hour postprandial glucose      |          |                   |
| Normal                           | 985      | 86.78             |
| Impaired glucose metabolism      | 150      | 13.22             |
| Diabetes                         | 0        | 0.00              |
| Waist circumference              |          |                   |
| Normal                           | 456      | 40.18             |
| Abdominal obesity                | 679      | 59.82             |
| Triglyceride                     |          |                   |
| Normal                           | 731      | 64.41             |
| Increased                        | 404      | 35.59             |
| HDL cholesterol                  |          |                   |
| Decreased                        | 873      | 76.92             |
| Normal                           | 262      | 23.08             |
| Body mass index                  |          |                   |
| Low weight                       | 36       | 3.17              |
| Normal                           | 405      | 35.68             |
| Over weight                      | 267      | 23.52             |
| Obesity                          | 427      | 37.62             |
| Ratio of waist-hip circumference |          |                   |
| Normal                           | 771      | 67.93             |
| Abdominal obesity                | 364      | 32.07             |
| Systolic blood pressure          |          |                   |
| Normal                           | 838      | 73.83             |
| Hypertension                     | 297      | 26.17             |
| Diastolic blood pressure         |          |                   |
| Normal                           | 773      | 68.11             |
| Hypertension                     | 362      | 31.89             |

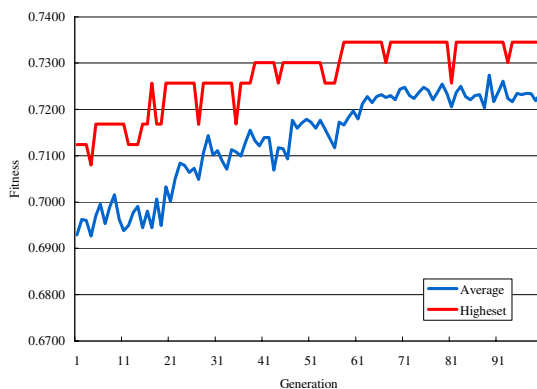
### 4.3 Experimental Results

First, we have conducted comparison experiments among Bayesian network models that have different numbers of attributes. The first model is BN with eight basic

attributes, the second one is the proposed model with 11 selected attributes, and the last one is the BN model with all attributes. Table 3 indicates that the result of 11 attributes is the best.

**Table 3.** The comparison of accuracies by the number of attributes

| Attribute size | 8                      | 11                                     | 18                     |
|----------------|------------------------|----------------------------------------|------------------------|
| Accuracy (%)   | 70.74 ( $\pm 0.0017$ ) | <b>72.15 (<math>\pm 0.0082</math>)</b> | 70.82 ( $\pm 0.0079$ ) |



**Fig. 6.** The fitness transition graph during an evolution process

**Table 4.** The comparison of accuracies before and after optimization

| Ordering         | Accuracy (%)                      |
|------------------|-----------------------------------|
| <b>Optimized</b> | <b>72.12 (<math>\pm 0</math>)</b> |
| Random           | 70.09 ( $\pm 0.0513$ )            |

**Table 5.** The comparison of accuracies by the number of attributes

| Prediction model | Accuracy (%)                      |
|------------------|-----------------------------------|
| <b>BN</b>        | <b>72.12 (<math>\pm 0</math>)</b> |
| NN               | 63.19 ( $\pm 0.0152$ )            |
| 3NN              | 62.56 ( $\pm 0$ )                 |

We have applied the proposed method to total 1,135 data, and Fig. 6 illustrates the evolution process. It evolves well since average and the highest fitness values get a little higher accordingly as the generation grows. The highest fitness converges after the 60th generation, and the average fitness converges after a few generations.

After that, we have compared the model of optimized ordering with the model of random ordering. Table 4 provides the comparison result in terms of accuracy. Here, the difference between two models is statistically significant ( $p < 0.001$ ).

Finally, we have compared the BN model after attribute optimization with two other models of neural networks and  $k$  nearest neighbors that have been frequently used in pattern recognition field in order to solve the prediction problem. Table 5 shows the comparison result with accuracy, and the differences of the proposed model and other

models (BN vs. NN, BN vs. 3NN) are statistically significant ( $p < 0.001$ ). Generally, NN has strength in accuracy though it cannot be interpreted easily. However, BN model has provided better performance, and we can guess that the pre-processing and attribute selection processes using medical domain knowledge were effective.

## 5 Conclusions

This paper proposed a Bayesian network model with evolutionary algorithm in order to predict the metabolic syndrome. In processes of building the prognostic model, we applied the medical domain knowledge in order to make the model more reliable. We also adopted the genetic algorithm to optimize attribute ordering, and completed the model efficiently using the medical domain knowledge in the optimization process.

We verified that the proposed method provided better performance compared with the model before ordering optimization as well as other models such as neural networks and  $k$ -nearest neighbor.

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# Analysis and Simulation of Synchronization for Large Scale Networks

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**Abstract.** Networks of coupled large scale oscillators have been studied in biology for a number of years. It has been recognized that transient in the nearest neighbor connected networks may take far too long to die out. In the model of mammalian rhythm, it is considered that a few long distance interconnections exist. Typically, these long distance interconnections are considered to occur in a random way. In this study, we discuss the synchronization problem for coupled oscillator networks which can model the mammalian rhythm. Then, the distribution model for the random long distance connections is proposed and is demonstrated by simulation. Furthermore, simulation also shows that synchronization still holds even a large part of the network is destroyed.

## 1 Introduction

Recently, trying to understand the behavior of symmetrically coupled oscillators in biological networks has been a well studied subject [1][9][10]. Traditionally, it is assumed that such networks only have nearest neighbor interconnections. Under suitable assumptions on the connectivity pattern and strength, it is shown that such networks begin to display synchronized oscillatory behavior. However, it has been recognized that this type of coupling has the drawback that transient time is too long. It has been suggested by Watts and Strogatz [8] that a few long distance interconnections may have a dramatic effect on speeding up transient response. The so-called “small world networks” have intermediate connectivity properties but exhibit a high degree of clustering as in the regular networks and a small average distance between vertices as in the random network. They also found that the small world networks of coupled phase oscillators can synchronize almost as readily as the globally coupled networks, despite the fact that they have much fewer edges [9].

One problem is how to quantify the effects of long distance connections on the transient response times of a small world network [4][7]. Many simulation results have shown that a couple of generic long distance connections have the same effect in reducing transients compared to a dozen or so nearest neighbor connections. Until now, no model has been reported that can support this comparison. It is considered

that transient dynamics of a typical oscillator network can be related to a dominant eigenvalue of the coupled matrix. Thus, the distribution of the random long distance interconnection must be firstly clarified. In this paper, firstly, we try to analyze the relation between the interconnection and the dominant eigenvalue of the coupled matrix of the coupled oscillator networks which can model the mammalian rhythm. Then, we try to give a distribution model of the long distance connections between the corresponding neurons. Finally, the proposed model is demonstrated by simulation.

## 2 Preliminaries

Circadian rhythms are observed in the physiology of mammals and other higher organisms. In mammals, they are generated in a pacemaker located in the suprachiasmatic nucleus (SCN) of the hypothalamus [2][3]. SCN consists of 16000 neurons arranged in a symmetric bilateral structure, and it is generally believed that each isolated SCN neuron behaves as an oscillator by itself. Kronauer [3] proposed a model to describe the oscillations in a single SCN cell in 1990. A van der Pol oscillator is used to model stable oscillations in SCN neurons, with an additive term to model response due to light,

$$\left(\frac{12}{\pi}\right)\dot{x} = y + \varepsilon\left(x - \frac{4}{3}x^3\right) + B, \tag{1}$$

$$\left(\frac{12}{\pi}\right)\dot{y} = -\left(\frac{24}{\tau}\right)^2 x + By, \tag{2}$$

where  $\varepsilon$  is a constant which determines the size of the periodic orbit of the van der Pol oscillator (usually chosen as 0.13) [5][6],  $\tau$  is a constant which represents the period of the oscillator (roughly equals to 24),  $B$  is defined by  $B = (1 - px)CL^{\frac{1}{3}}$ ,  $L$  is the light intensity in lux, and  $p$  and  $C$  are constants ( $p = \frac{1}{3}$ ,  $C = 0.018$ ).

We consider a network consisting of  $N$  nonlinear oscillators arranged in the form of a ring. Each of the oscillators represents an SCN neuron, and internal dynamics is represented by a van der Pol oscillator, where the term  $B$  in (1)-(2) will not be considered.

$$\left(\frac{12}{\pi}\right)\dot{x}_i = y_i + \varepsilon\left(x_i - \frac{4}{3}x_i^3\right) + \sum_{j=1}^N a_{ij}x_j, \tag{3}$$

$$\left(\frac{12}{\pi}\right)\dot{y}_i = -\left(\frac{24}{\tau}\right)^2 x_i + \sum_{j=1}^N a_{ij}y_j, \tag{4}$$

$x_i$  and  $y_i$  are the state of the  $i$ -th neuron. The matrix  $A = (a_{ij}) \in R^{N \times N}$  is called the coupling matrix which represents the coupling configuration of the network. For

$i \neq j$ ,  $a_{ij} = a_{ji} \geq 0$  is the strength of the connectivity between the  $i$ -th neuron and the  $j$ -th neuron. If  $a_{ij} = a_{ji} = 0$ , then there is no connection between the  $i$ -th neuron and

the  $j$ -th neuron. For  $i = j$ ,  $a_{ii} = -\sum_{\substack{j=1 \\ j \neq i}}^N a_{ij} = -\sum_{\substack{j=1 \\ j \neq i}}^N a_{ji}$ .  $x_i$  and  $y_i$  satisfy  $x_{i+N} = x_i$ ,

$$y_{i+N} = y_i.$$

Suppose the network is connected in the sense that there are no isolated neurons. Then the coupling matrix  $A$  is irreducible. Thus, it can be shown that zero is an eigenvalue of  $A$  with multiplicity 1 and all the other eigenvalues are negative.

### 3 Synchronization Stability Analysis

The dynamical network (3)-(4) is said to achieve synchronization if

$$\begin{bmatrix} x_1 \\ y_1 \end{bmatrix} = \dots = \begin{bmatrix} x_N \\ y_N \end{bmatrix} = S(t) \tag{5}$$

as  $t \rightarrow \infty$ , where  $S(t)$  is the limit cycle generated by

$$\left(\frac{12}{\pi}\right)\dot{x} = y + \varepsilon\left(x - \frac{4}{3}x^3\right), \tag{6}$$

$$\left(\frac{12}{\pi}\right)\dot{y} = -\left(\frac{24}{\tau}\right)^2 x. \tag{7}$$

Clearly, the stability of the synchronized states of the network (3)-(4) is determined by the limit cycle  $S(t)$  and the coupling matrix  $A$ .

**Lemma 1:** Let  $0 = \lambda_1 > \lambda_2 \geq \dots \geq \lambda_N$  be the eigenvalues of the coupling matrix  $A$ . If the following  $N - 1$  of 2-dimensional linear time-varying systems are exponentially stable

$$\left(\frac{12}{\pi}\right)\dot{w}_1 = \left(\varepsilon - 4\varepsilon x^2 \Big|_{x \in S(t)} + \lambda_k\right)w_1 + w_2, \tag{8}$$

$$\left(\frac{12}{\pi}\right)\dot{w}_2 = -\left(\frac{24}{\tau}\right)^2 w_1, \tag{9}$$

for  $k = 2, \dots, N$ , then the synchronized states (5) are exponentially stable.

**Proof:** Let  $\begin{pmatrix} x_i \\ y_i \end{pmatrix} = S(t) + \begin{pmatrix} \rho_{1i} \\ \rho_{2i} \end{pmatrix}$ . Now linearize (3)-(4) about  $S(t)$  yields

$$\left(\frac{\pi}{12}\right)\dot{\Theta} = \Theta \left[ \begin{pmatrix} \varepsilon - 4\varepsilon x^2 \Big|_{x \in S(t)} \\ -\left(\frac{24}{\tau}\right)^2 \end{pmatrix} \right] + A\Theta, \tag{10}$$

where  $\Theta = \begin{pmatrix} \rho_{11} & \rho_{21} & \cdots & \rho_{N1} \\ \rho_{11} & \rho_{22} & \cdots & \rho_{N2} \end{pmatrix}^T$ . Since  $A$  is a real symmetric matrix, there exists an unitary matrix  $\Phi = [\phi_1 \ \phi_2 \ \cdots \ \phi_N]$  such that

$$A\phi_k = \lambda_k \phi_k, \quad k = 1, 2, \dots, N. \tag{11}$$

By expanding the two columns of  $\Theta$  on the basis of  $\Phi$ , we have

$$\Theta = \Phi v. \tag{12}$$

where the matrix  $v \in R^{N \times 2}$  obeys the following equations

$$\left(\frac{\pi}{12}\right)\dot{v} = v \left[ \begin{pmatrix} \varepsilon - 4\varepsilon x^2 \Big|_{x \in S(t)} \\ -\left(\frac{24}{\tau}\right)^2 \end{pmatrix} \right] + \Lambda v \tag{13}$$

with  $\Lambda = \text{diag}(\lambda_1, \lambda_2, \dots, \lambda_N)$ . Let  $v_k = (v_{k1}, v_{k2})$  be the  $k$ -th row of  $v \in R^{N \times 2}$ . It yields

$$\dot{v}_k^T = \begin{pmatrix} \left( \varepsilon - 4\varepsilon x^2 \Big|_{x \in S(t)} + \lambda_k \right) v_{k1} + v_{k2} \\ -\left(\frac{24}{\tau}\right)^2 v_{k1} \end{pmatrix}. \tag{14}$$

Note that  $\lambda_1 = 0$  corresponds to the synchronization of the system states. If the following  $N-1$  pieces of 2-dimensional linear time varying systems described in (8)-(9) are exponentially stable, then  $\Theta$  will exponentially tend to the origin, which implies that the synchronized states (5) are exponentially stable. The lemma is proved.

Based on Lemma 1, we have the next result.

**Lemma 2:** If  $\lambda_2 \leq -\varepsilon$ , then the synchronized states (5) are exponentially stable.

**Proof:** The result is obvious by observing equation (8)-(9).

By Lemma 1 and Lemma 2, it can be concluded that transient time of the oscillator network is governed by the dominant eigenvalue  $\lambda_2$  of the coupled matrix  $A$ .

## 4 Synchronization in Scale-Free Networks

### 4.1 Synchronization Influenced by Connections

In this section, the influence of the connections on synchronization will be studied. In the following, we are interested in discussing the synchronization of a scale free network.

To begin with, we introduce the following lemma [11].

**Lemma 3:** Let  $C \in R^{n \times n}$  and  $D \in R^{n \times n}$  be symmetric matrices. If  $D$  is a negative semi-definite matrix, then

$$\lambda_2(C + D) \leq \lambda_2(C), \tag{15}$$

where the inequality holds when  $D$  is negative definite.

First, let us study the nearest neighbor coupling configuration. In this case, the corresponding coupling matrix is described by

$$A_{nc} = \begin{bmatrix} a_{11} & a_{12} & & & a_{1N} \\ a_{12} & a_{22} & a_{23} & & \\ & \ddots & \ddots & \ddots & \\ & & a_{N-1, N-2} & a_{N-1, N-1} & a_{N-1, N} \\ a_{1N} & & & a_{N-1, N} & a_{NN} \end{bmatrix}. \tag{16}$$

Let  $\min_{i \neq j} a_{ij} = q$ . Since the eigenvalues of the matrix

$$A_{\min} = \begin{bmatrix} -2q & q & & & q \\ q & -2q & q & & \\ & \ddots & \ddots & \ddots & \\ & & q & -2q & q \\ q & & & q & -2q \end{bmatrix} \tag{17}$$

are  $-4q \sin^2(\frac{k\pi}{N})$ ,  $k = 0, 1, \dots, N-1$ , by Lemma 3, it is obvious that the dominant eigenvalue  $\lambda_2$  of the matrix  $A_{nc}$  described in (16) is smaller than or equal to  $-4q \sin^2(\frac{\pi}{N})$ . Thus, according to Lemma 2, the nearest neighbor coupled network will synchronize if

$$4q \sin(\frac{k\pi}{N}) \geq \varepsilon \tag{18}$$

Therefore, when the network is very large and the coupling strengths are not strong (which means that many  $a_{ij}$  ( $i \neq j$ ) are smaller than 1), the nearest neighbor coupled network may not synchronize. Furthermore, if the coupling strengths are very weak, then the nearest neighbor coupled network may not synchronize even when the network is not very large.

Secondly, let us study the global coupled network. In this case, the corresponding coupling matrix is described by

$$A_{nc} = \begin{bmatrix} a_{11} & a_{12} & a_{13} & \cdots & a_{1N} \\ a_{12} & a_{22} & a_{23} & \cdots & a_{2N} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ a_{1, N-1} & a_{2, N-1} & a_{3, N-1} & a_{N-1, N-1} & a_{N-1, N} \\ a_{1N} & a_{2N} & a_{3N} & a_{N-1, N} & a_{NN} \end{bmatrix}. \tag{19}$$

Let  $\min_{i \neq j} a_{ij} = q$ . By Lemma 3, it can be easily seen that the dominant eigenvalue  $\lambda_2$  of the matrix  $A_{nc}$  described in (19) is smaller than or equal to  $-Nq$  (with  $N-1$  multiplicity). According to Lemma 2, the global coupled network will synchronize if  $qN \geq \varepsilon$ .

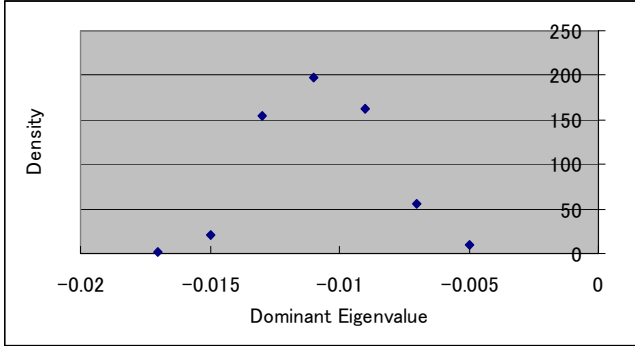
If many coupling strengths  $a_{ij}$  ( $i \neq j$ ) are very small, then the global coupled network may not synchronize.

Thirdly, let us consider the coupled network where each neuron is adjacent to its  $n$  neighboring neurons on each side. The corresponding coupling matrix is described by

$$A_{nc} = \begin{bmatrix} a_{11} & \cdots & a_{1n} & 0 & a_{1, N-n+1} & \cdots & a_{1N} \\ \vdots & \ddots & & \ddots & \ddots & \ddots & \vdots \\ a_{1n} & & & & \ddots & \ddots & a_{n, N-n+1} \\ 0 & \ddots & & \ddots & & \ddots & 0 \\ a_{1, N-n+1} & \ddots & \ddots & & & & a_{N-n+1, N} \\ \vdots & \ddots & \ddots & \ddots & & \ddots & \vdots \\ a_{1N} & \cdots & a_{n, N-n+1} & 0 & a_{N-n+1, N} & \cdots & a_{NN} \end{bmatrix}. \tag{20}$$



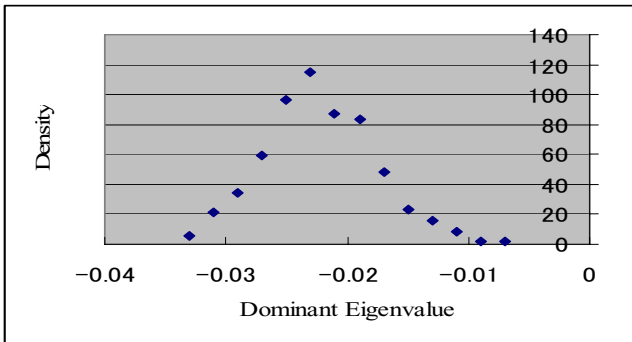
means the neurons numbered from  $i + \left\lceil \frac{N}{4} \right\rceil$  to  $i + \left\lceil \frac{3N}{4} \right\rceil$ . Furthermore, suppose there are  $m$  long distance connections in the network, and the distribution of each long distance connection obeys the uniform distribution. For simplicity, suppose these long connection strengths are same, say  $\alpha$  which meets  $\alpha \geq 1$ .



**Fig. 1.** Simulation results for  $N=2000, m=250$

Now, let us give the simulation of the proposed distribution model. For simplicity, the connection strength is set to 1. Suppose the neurons are arranged in a ring, i.e.  $n=1$ . The simulations are done 600 times. The densities of the dominant value are shown in Figures 1-3. Figure 1 shows the simulation results for the distribution model when  $N=2000, m=250$ . Figure 2 shows the simulation results when  $N=2000, m=400$ . Figure 3 shows the simulation results when  $N=2000, m=600$ .

It can be seen that, when  $m$  is increased, the dominant value moves to left. This is also consistent to the analysis in the above section.



**Fig. 2.** Simulation results for  $N=2000, m=400$



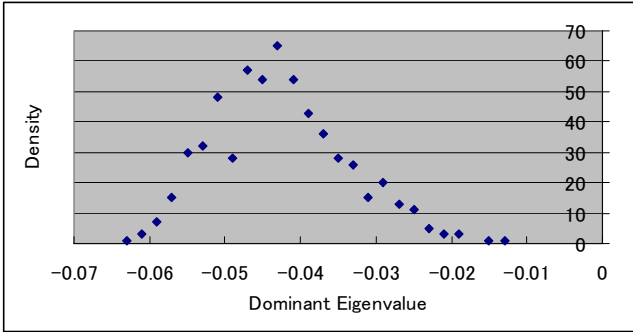


Fig. 3. Simulation results for  $N=2000, m=600$

### 4.3 Synchronization Simulations

In this section, the synchronization time will be investigated by computer simulation based on the proposed long distance connection model for  $N=2000$ . In the presented simulation results, “synchronization” means that the norm of state difference between one oscillator and another oscillator becomes smaller than  $5 \times 10^{-4}$  after an instant  $t_s$ . The instant  $t_s$  is called “synchronization time”. Table 1 shows the mean synchronization times for different values of  $m$ , where 600 times of the simulations are done for each  $m$ . It can be seen that the synchronization becomes faster if the number of long distance connections are larger. This is also consistent to the analysis in the above sections.

Table 1. The mean synchronization time for different  $m$

|                          |                 |                 |        |                 |
|--------------------------|-----------------|-----------------|--------|-----------------|
| Value of $m$             | $2 \times 10^3$ | $4 \times 10^3$ | $10^4$ | $3 \times 10^4$ |
| Synchronization Time (s) | 24.57           | 8.65            | 2.54   | 0.50            |

Now, based on the above setting, let us discuss the case when a part of the network is destroyed. It is supposed that the destroyed oscillators are neighbored ones. For the network with 2000 oscillators and 30000 long distance connections, Table 2 shows the mean synchronization times for different numbers of destroyed oscillators, where 600 times of the simulations are done for each  $m$ . It is clear that synchronization still exists even a large part of the network is destroyed (However, the synchronization time becomes longer when more oscillators are destroyed). By observing the existence of synchronization in a destroyed network, the validity of the proposed model for mammalian rhythm can also be supported by the phenomenon that the instinct of the animals still works even the brain is seriously injured.

Table 2. The mean synchronization time via the number of destroyed oscillators

|                                 |      |      |      |      |      |      |
|---------------------------------|------|------|------|------|------|------|
| Number of destroyed oscillators | 0    | 100  | 200  | 300  | 400  | 500  |
| Synchronization Time (s)        | 0.50 | 0.55 | 0.63 | 0.73 | 0.87 | 1.00 |

## 5 Conclusion

This paper discusses the synchronization problem for the coupled large scale oscillator networks which can model the mammalian rhythm. Long distance connections with “strong” coupling strength are necessary to synchronize a large scale network. Furthermore, the transient time of the network also depends on these long distance connections. The long distance interconnections are considered to occur in a random way. The distribution model for the random long distance connections in a network is proposed. Simulations results are carried out to illustrate the synchronization theory and to show the validity of the proposed distribution model.

## Acknowledgments

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# Detection of Basal Cell Carcinoma by Automatic Classification of Confocal Raman Spectra

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**Abstract.** Raman spectroscopy has strong potential for providing non-invasive dermatological diagnosis of skin cancer. In this study, we investigated various classification methods with confocal Raman spectra for the detection of basal cell carcinoma (BCC), which is one of the most common skin cancer. The methods include maximum a posteriori (MAP) probability, probabilistic neural networks (PNN),  $k$ -nearest neighbor (KNN), multilayer perceptron networks (MLP), and support vector machine (SVM). The classification framework consists of preprocessing of Raman spectra, feature extraction, and classification. In the preprocessing step, a simple half Hanning method is adopted to obtain robust features. Classification results involving 216 spectra gave about 97% true classification rate in case of MLP and SVM, which is an evident proof of the effectiveness of confocal Raman spectra for BCC detection. In addition to it, spectral regions, which are important for classification, are examined by sensitivity analysis.

**Keywords:** Raman spectroscopy, pattern recognition, sensitivity analysis, basal cell carcinoma detection.

## 1 Introduction

Skin cancer is one of the most common cancers in the world. Recently, the incidence of skin cancer has dramatically increased due to the excessive exposure of skin to UV radiation caused by ozone layer depletion, environmental contamination, and so on. If detected early, skin cancer has a cure rate of 100%. Unfortunately, early detection is difficult because diagnosis is still based on morphological inspection by a pathologist. There are two common skin cancers: BCC and squamous cell carcinoma (SCC). Both BCC and SCC are nonmelanoma skin cancers, and BCC is the most common skin neoplasm[1].

The accurate detection of BCC has attracted much attention from clinical dermatologists since it is difficult to distinguish BCC tissue from surrounding noncancerous tissue. The routine diagnostic technique used for the detection of BCC is pathological examination of biopsy samples. This involves removal of tissue from suspected areas, which is then sliced and stained to enable the

pathologist to identify morphological abnormalities. The method relies upon a subjective judgment, which is dependent on the level of experience of the individual pathologist and can lead to the excessive biopsy of tissues. Thus, a fast and accurate diagnostic technique for the initial screening and selection of lesions for further biopsy is needed [2].

Raman spectroscopy has the potential to resolve this problem. It can be applied to provide an accurate medical diagnosis to distinguish BCC tissue from surrounding normal (NOR) tissue. Recently, some of the researchers carried out BCC detection using Raman spectroscopy. By far, the most widely used method is Fourier transform (FT) Raman spectroscopy [3] [4]. In the previous studies, a long wavelength excitation laser was used to minimize autofluorescence from skin tissue. However, the longer wavelength laser gives poor Raman scattering intensities compared to the shorter one. As a result, FT Raman spectra in poor signal-to-noise ratio suffer from so called background noise [2]. The background noise introduces both variance into the spectra and correlation between frequency components which makes robust feature extraction difficult. Thus FT Raman spectra require complicated statistical treatments to eliminate background noise as [3].

More recently, direct observation method based on the confocal Raman technique was presented for the dermatological diagnosis of BCC using the shorter wavelength argon ion laser [2]. According to the study, confocal Raman spectra provides promising results for detection of precancerous and noncancerous lesions without special treatment. Hence, with the confocal Raman spectra, we could expect that an automatic classifier having robust detection results would be designed. In this paper, we investigate various classification methods and compare the classification results. The methods include MAP, PNN, KNN, MLP, and SVM. Experimental results will be given to confirm that the confocal Raman spectra provide a promising results for automatic detection of BCC.

## 2 Confocal Raman Measurements and Preprocessing of Data

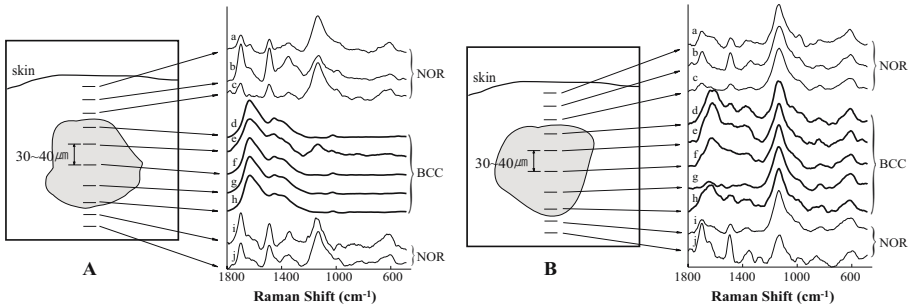
The preparation of data includes confocal Raman measurement and preprocessing. Raman spectra were obtained using a commercial Renishaw 2000 Raman microscope system. After the measurements, normalization and windowing were carried out for the spectra. Dimension reduction was followed using principal component analysis (PCA) for feature extraction. We will describe the procedures in turn.

### 2.1 Sample Preparation and Raman Measurements

The tissue samples were prepared with the conventional treatment, which is exactly the same as [2]. BCC tissues were sampled from 10 patients with a routine biopsy. Cross sections of  $20\mu m$  were cut with a microtome at  $-20^{\circ}C$  and stored in liquid nitrogen. Two thin sections of every patients were used

for experiments. One section was used for classification and the other section was stained with H&E and used as a reference after locating the boundaries between BCC and NOR by an expert pathologist with a routine cancer diagnosis.

A Renishaw 2000 confocal Raman microscope system was set up in such a way that the light from the region in focus be accepted, while the light from the adjacent regions is rejected. In this way, the spectral interference or contamination from the surrounding regions could be minimized compared to nonconfocal Raman spectra. An argon ion laser operating at  $\lambda = 514.5nm$  was used as an excitation source with about  $20mW$  power.



**Fig. 1.** Confocal Raman profiles of skin tissue with an interval of  $30\text{-}40\ \mu m$

The confocal Raman spectra for the skin samples are shown in Figure 1, where no strong background noise is not observed as expected. In the Figure, most of the spectra show a clear distinction between BCC and NOR tissues while it is not so evident for the case of Fig. 1 B(g) and Fig. 1 B(i). Figure 1 B(g) is considered to be an outlier because it is very different from the surrounding spectra. On the other hand, Fig. 1 B(i) looks similar to a BCC spectrum and can not be considered as an outlier. It is probably caused by the fact that the spectrum was obtained from the vicinity of the boundary between BCC and NOR. There might be a false marking.

A skin biopsy was performed in the perpendicular direction from the skin surface, and it is the same for the spectral measurements. That is the direction from the epidermis to the dermis in Fig. 1. Raman spectra of BCC tissues were measured at different spots with an interval of  $30\text{-}40\ \mu m$ . In this way, 216 Raman spectra were collected from 10 patients.

## 2.2 Preprocessing of Data and Dimension Reduction

It is known that the near infrared FT Raman spectra suffer from background noise that originates from skin fluorescence [3]. On the other hand, the confocal Raman spectra do not show any strong background noise as you see in the Fig. 1. That is the reason why we should use confocal Raman spectroscopy. We normalized the spectra so that they fall in the interval  $[-1,1]$ , which is often

called *minmax* method. Needless to say, there are many normalization methods. For example, one can normalize a given data set so that the inputs have means of zero and standard deviations of 1 or have the same area. According to our preliminary experiments, however, the *minmax* method gave the best results.

Next to the data normalization, a clipping window was applied so that unnecessary data should be discarded. We adopted the same clipping window in [5] so as to discard unnecessary data and lower the false positive ratio. For dimension reduction, well known principal component analysis (PCA) was applied. Since PCA identifies orthogonal bases on which projections are uncorrelated, it is the most preferred method for data reduction. Principal components can be obtained via eigenvalue decomposition of the following scatter matrix  $\mathbf{S}$ .

$$\mathbf{S} = \sum_k (\mathbf{d}_k - \boldsymbol{\mu})(\mathbf{d}_k - \boldsymbol{\mu})^T \tag{1}$$

where  $\mathbf{d}_k$  is a  $k$ -th input pattern and  $\boldsymbol{\mu}$  is the mean of  $\mathbf{d}_k$ . If we let  $\mathbf{D}$  be a diagonal matrix of eigenvalues in descending order and  $\mathbf{E}$  be an orthogonal matrix whose columns are the corresponding eigenvectors, we can obtain principal components  $\mathbf{x}_k$  as follows.

$$\mathbf{S} = \mathbf{E}\mathbf{D}\mathbf{E}^T \tag{2}$$

$$\mathbf{x}_k = \mathbf{E}^T \mathbf{d}_k \tag{3}$$

Data reduction is accomplished by discarding the unimportant elements of  $\mathbf{d}_k$ . The number of retained principal components was determined experimentally according to classification methods.

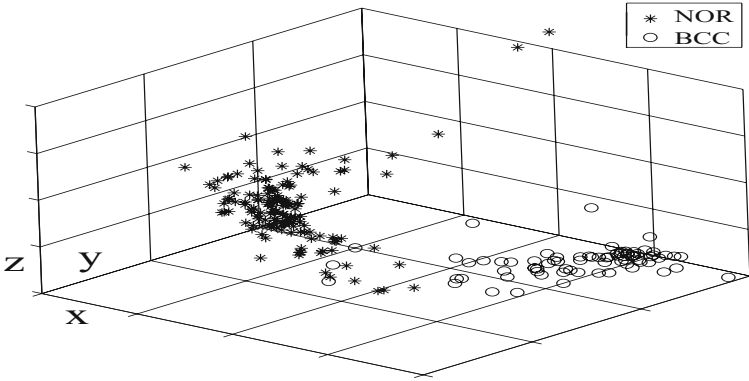
### 3 Classification Methods and Experimental Results

To see how well the feature vectors of two different classes, BCC and NOR, are separated, we plotted them in the Fig. 2, where  $x, y, z$  correspond to the first, the second, and the third component of the transformed feature vector. The figure clearly shows that the input feature vectors are reasonably well separated as expected. Thus we could expect that a classifier operate well, which will be confirmed at the latter of this section.

#### 3.1 Classification Methods

Five types of classifiers including MAP, PNN, KNN, MLP, and SVM were examined. In the MAP classification, we select the class,  $w_i$ , that maximizes the posterior probability  $P(w_i|\mathbf{x})$ . Given the same prior probability, it is equivalent to the selection of the class that maximizes the class conditional probability density. Let  $w_1, w_2$  be BCC class and NOR class respectively. MAP classification rule is expressed as follows.

$$\text{Decide } w_1 \text{ if } P(\mathbf{x}|w_1) \geq P(\mathbf{x}|w_2) \tag{4}$$



**Fig. 2.** Distribution of the first three components of PCA transformed spectra

Since input vectors are well separated and could be thought to be distributed around the class mean, we can model the class conditional probability with the multivariate Gaussian probability density function. The parameters, mean vector  $\boldsymbol{\mu}$  and covariance matrix  $\boldsymbol{\Sigma}$ , were estimated in the maximum likelihood sense. Let  $n_i$  be the number of data in  $w_i$ . Then the decision rule is expressed with a discriminant function,  $g_i(\mathbf{x})$ , as follows.

Decide  $w_1$  if  $P(\mathbf{x}|w_1) \geq P(\mathbf{x}|w_2)$ :

$$g_i(\mathbf{x}) = -(1/2)\mathbf{x}^T \boldsymbol{\Sigma}_i^{-1} \mathbf{x} + \boldsymbol{\Sigma}_i^{-1} \boldsymbol{\mu}_i + r_i \tag{5}$$

$$r_i = -(1/2)\boldsymbol{\mu}_i^T \boldsymbol{\Sigma}_i^{-1} \boldsymbol{\mu}_i - (1/2) \ln |\boldsymbol{\Sigma}_i^{-1}| \tag{6}$$

$$\boldsymbol{\mu}_i = (1/n_i) \sum_{k=1}^{n_i} \mathbf{x}_k \tag{7}$$

$$\boldsymbol{\Sigma}_i = (1/n_i) \sum_{k=1}^{n_i} (\mathbf{x}_k - \boldsymbol{\mu})(\mathbf{x}_k - \boldsymbol{\mu})^T \tag{8}$$

In the PNN classification, each feature vectors in the training set is scaled to have unit length. An input vector is also to be normalized before classification [6]. The activation function,  $\varphi_i(\mathbf{x})$ , is evaluated for every data in the training set. Let  $\mathbf{p}_i$  be the normalized feature vector in the training set. The discriminant function of PNN is given by

$$\varphi_i(\mathbf{x}) = \exp((\mathbf{p}_i^T \mathbf{x} - 1)/\sigma^2) \tag{9}$$

$$g_i(\mathbf{x}) = (1/n_i) \sum_{\mathbf{p}_i \in w_i} \varphi_i(\mathbf{x}), \tag{10}$$

where parameter  $\sigma$  was determined to be 0.01 experimentally.

We used the following Mahalanobis distance for the KNN classification.

$$d(\mathbf{x}, \mathbf{y}) = (\mathbf{x} - \mathbf{y})^T \boldsymbol{\Sigma}(\mathbf{x} - \mathbf{y}) \tag{11}$$

where  $\Sigma$  is a sample covariance matrix computed from all the data in the training set. The discriminant function of the KNN classifier,  $g_i(\mathbf{x})$ , is the number of training data belonging to  $i$  class among the  $k$  nearest neighbors of  $\mathbf{x}$ . The number of nearest neighbors  $k$  was set to be 5. The KNN algorithm requires a large number computation in proportion to the number of training data. Fortunately, there are many fast algorithms. In the experiments, we used the algorithm in [7].

MLP is the most powerful and flexible classifier since they can adapt to arbitrarily complex posterior probability functions [8]. Such extreme flexibility calls for careful control of overfit and detection of outliers. But for the well separated data, overly careful adjustment of the parameters of the networks is not necessary. That is the benefit of confocal Raman spectra. The network operation is characterized by the equation,  $\mathbf{o}_k = f(\text{net}_k)$ . The input to the unit,  $\text{net}_k$ , and the bipolar sigmoidal function,  $f()$ , is given by the following equations.

$$\text{net}_k = \sum_i w_{ik} \mathbf{o}_i + \text{bias}_k \tag{12}$$

$$f(\text{net}_k) = \frac{2}{1 + \exp(-2\text{net}_k)} - 1 \tag{13}$$

In the experiment, the number of hidden unit was set to be 9. Since there are only two classes, we used one output unit. MLP models were trained to output -1 for the NOR class and +1 for the BCC class using back propagation algorithm. At the classification, output value is hard limited to give a classification result. The performance of MLP undergoes a change according to the initial condition. Thus the experiments were carried out 20 times and the results were averaged.

SVM is also a powerful methodology for solving problems in nonlinear classification. In the simplest pattern recognition tasks, SVM uses a linear separating hyperplane to create a classifier with a maximal margin. In cases when given classes cannot be linearly separated in the original input space, SVM first nonlinearly transforms original features into a higher dimensional feature space. This transformation can be achieved by using various nonlinear mappings: polynomial, sigmoid, and radial basis function (RBF). After the nonlinear transformation, linear optimal separating hyperplane can easily be found. The resulting hyperplane will be optimal in the sense of being a maximal margin classifier with respect to training data [9]. In the experiments, we used the following Gaussian RBF kernel.

$$K(\mathbf{x}_i, \mathbf{x}_j) = e^{-\frac{\|\mathbf{x}_i - \mathbf{x}_j\|^2}{\sigma^2}} \tag{14}$$

where  $\sigma^2$  is set to 20. Least squares SVM were used as an optimization method, where the regularization parameter is set to 1 [10].

### 3.2 Experimental Results

Overall 216 data were divided into two groups. One is a training set and the other is a test set. Actually, the data from 9 patients were used as a training set and the



data from the remaining patient were used as a test set. Once the classification completes, the data from one patient are eliminated from the training set and used as new test data. The previous test data are now inserted into the training set. In this way, the data from every patients were used as a test set. That is the process of 'leaving one out'. The average number of BCC and NOR spectra in the test set is 8 and 14 and that in the training set is 68 and 126 respectively.

The classification results without the data windows are summarized in the Table 1. The number of principal components was 5 for all the methods. In the table, we can see that the the sensitivity of every methods is over 91.5%. Among them, MAP, MLP, and SVM show the sensitivity over 93% and outperform the other methods. Since there aren't enough BCC data, nonparametric methods such as PNN and KNN might be inferior to the others for BCC detection. But the situation is somewhat different in the case of NOR data. The specificity of PNN and KNN is now nearly equal to the others.

**Table 1.** Classification results with original spectra. Stars indicate the decision of an expert pathologist.

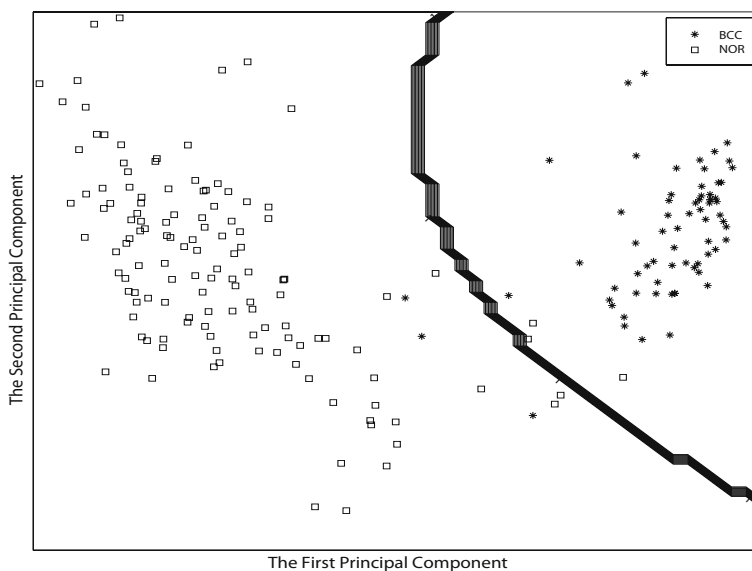
|      | MAP  |      | PNN  |      | KNN  |      | MLP  |      | SVM  |      |
|------|------|------|------|------|------|------|------|------|------|------|
|      | BCC  | NOR  | BCC  | NOR  | BCC  | NOR  | BCC  | NOR  | BCC  | NOR  |
| BCC* | 93.0 | 7.0  | 91.6 | 8.4  | 91.8 | 8.2  | 93.2 | 6.8  | 93.4 | 6.6  |
| NOR* | 4.2  | 95.8 | 3.6  | 96.4 | 6.9  | 97.1 | 5.6  | 96.4 | 4.3  | 95.7 |

To show the effectiveness of the clipping window, another experiments were carried out with a half Hanning window. The results are shown in the Table 2. With the clipping window, the sensitivity of every methods is improved over 94%. But the averaged specificity remains nearly the same when comparing the results with the previous ones. Considering that the overall performance of each methods gets better, this indicates that the clipping window contributes to lowering the false positive ratio more than the false negative ratio. In case of MLP and SVM, overall true classification rate is over 96.7%.

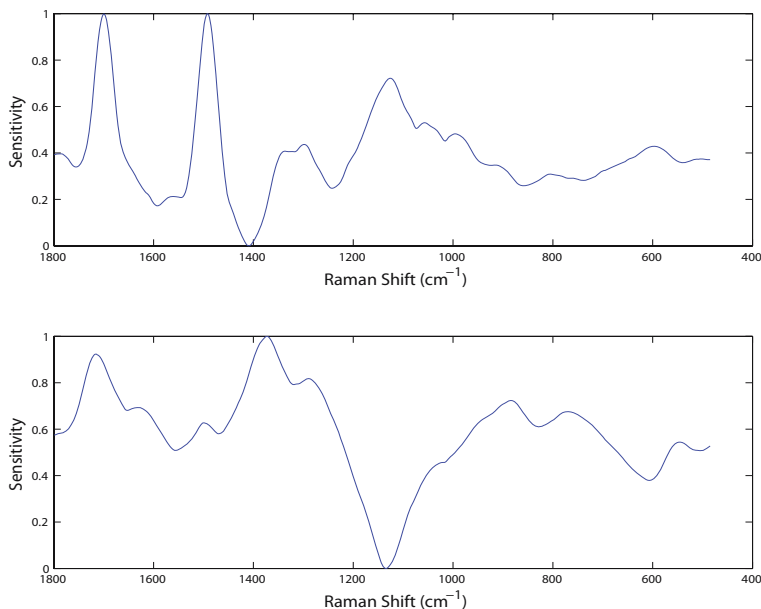
**Table 2.** Classification results processed with the half Hanning window. Stars indicate the decision of an expert pathologist.

|      | MAP  |      | PNN  |      | KNN  |      | MLP  |      | SVM  |      |
|------|------|------|------|------|------|------|------|------|------|------|
|      | BCC  | NOR  | BCC  | NOR  | BCC  | NOR  | BCC  | NOR  | BCC  | NOR  |
| BCC* | 94.6 | 5.4  | 94.6 | 5.4  | 95.9 | 4.1  | 97.3 | 2.7  | 96.1 | 3.9  |
| NOR* | 2.3  | 97.7 | 5.9  | 94.1 | 2.9  | 97.1 | 3.5  | 96.5 | 2.9  | 97.1 |

To see an example of decision boundary, we plotted them in the Fig. 3 in case of SVM, where  $x, y$  axis corresponds to the first and the second principal component. The figure clearly shows that some misclassified data lie in the vicinity of the decision boundary.



**Fig. 3.** The decision region of SVM with two principal components



**Fig. 4.** Examples of sensitivity map for BCC (upper) and NOR (lower)

The sensitivity analysis, which is analogous to the factor analysis in statistics, can be used to examine the impact of each input variable. Generally it provides a gross indicator of key factors via measuring the effect of altering an

input variable on the output value by integrating over all input patterns. We performed a sensitivity analysis of MAP for simplicity. Let the absolute value average sensitivity  $\mathbf{s}_i$  given for class  $\omega_i$ . Given the same prior probability, it can be derived as follows.

$$\mathbf{s}_i = \frac{1}{n_i} \sum_{k=1}^{N_i} \left| \frac{\partial p(\mathbf{x}^k | \omega_i)}{\partial \mathbf{d}^k} \right| \quad (15)$$

$$\frac{\partial p(\mathbf{x}^k | \omega_i)}{\partial \mathbf{d}^k} = p(\mathbf{x}^k | \omega_i) \tilde{\mathbf{E}} \Sigma_i^{-1} (\boldsymbol{\mu}_i - \mathbf{x}^k)^T \quad (16)$$

$$p(\mathbf{x}^k | \omega_i) = \frac{1}{(2\pi)^{d/2} |\Sigma|^{1/2}} \exp\left[-\frac{1}{2} (\mathbf{x}^k - \boldsymbol{\mu}_i)^T \Sigma_i^{-1} (\mathbf{x}^k - \boldsymbol{\mu}_i)\right] \quad (17)$$

where  $\mathbf{d}^k$  is the  $k$ -th data before PCA,  $n_i$  is the number of pattern in class  $\omega_i$ , and  $\tilde{\mathbf{E}}$  is a reduced PCA transformation matrix with 5 column vectors. Then we normalize the sensitivity factor for each class to have unit vector length. Figure 4 shows examples of sensitivity map for BCC and NOR. Large sensitivity peaks are observed at 1658, 1457, 1340, 1317  $cm^{-1}$  which correspond to amide I, lipid and protein, amide III vibrational mode. The results are consistent with those in [2] and confirm that the adopted clipping is appropriate.

## 4 Conclusion

In this paper, we investigated various classification methods with confocal Raman spectra to detect BCC. At the preprocessing stage, data was processed with a clipping window to lower the false positive classification rates. The experimental results with and without the clipping window revealed that the application of the clipping window could lower the false positive ratio. The MLP and SVM classification performance involving 216 Raman spectra was over 96.7%. The results indicate that the confocal Raman spectra provides discriminating spectra for the classification of BCC and NOR tissue. In addition to it, we showed that there is a consistency between automatic classification and direct observation by human with sensitivity analysis.

## Acknowledgement

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# Clustering Gene Expression Data for Periodic Genes Based on INMF

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**Abstract.** In this paper, we have explored the use of improved non – negative matrix factorization (INMF) to analyze gene expression data. Firstly, the mathematical principle of INMF algorithm is analyzed; Secondly, we proposed an INMF - based method for clustering periodic genes, which can provide valuable information for gene network research. Using simulated data, our approach is able to extract periodic genes subsets even when the signal-to-noise ratio is low. Subsequently, our approach is tested by real gene expression datasets from Yeast and is compared with the related other approaches. Our results showed that our scheme is feasible and effective.

## 1 Introduction

One particular aim when analyzing microarray data is to find statistical evidence of periodicity, and then to identify this subset of genes that is responsible during the cell cycle. A comprehensive catalog of cell cycle regulation genes can serve as a starting point for functional discovery [1-4]. Usually only a small fraction of the genes under investigation exhibits some evidence of periodically varying expression during the cycle so that the overall signal in the data is dominated by non – periodic components.

There are a number of methods discussed in the literature for obtaining this subset of genes with periodic variation. These methods include: 1) cluster analysis, which has been demonstrated to be of significant value for exploration of gene expression profiles [5-8]. However, such cluster analyses provide little insight into the relationships between groups of co-regulated genes or the behavior of biological networks as a whole. 2) parametric methods, such as Principal Component Analysis (PCA) and the singular value composition (SVD) [9-13], independent component analysis (ICA) [14-15] and separation correlation metric (SCM), alternatively known as the Fisher's discrimination criterion (FDC) [16]; and 3) nonparametric methods, such as support vector machines[17], neural networks, expectation maximization<sup>[18]</sup>, statistical analysis[19 - 20], etc. It is well known that the accuracy and reliability of the results are often dependent on the measurement approaches applied, and no single measurement so far is guaranteed to generate a satisfactory result [21].

The recent controversial argument with regard to the suitability of both available methods and current microarray data showed that it is difficult to identify correctly

the subset of genes with clear periodic signature. For instance, Shedden and Cooper [22] questioned the presence of generic cell – cycle specific signal in the datasets concerning yeast cells that were previously analyzed by Spellman *et al.* Their results were inconsistent with those obtained by Spellman *et al.*[2]. In another foundational work, Wichert *et al.* presented a statistical method based the average periodogram and Fisher’s  $g$  – statistic for identifying genes relevant for the cell cycle, which has some potential drawbacks. First, the  $g$  – statistic assumes as null – model a purely Gaussian process, while this assumption has not been verified so far. Second, it is sensitive to the size of the sample number and the size of the subset of cyclic genes in the data[20].

The above analysis shows that a further development of methodology for identifying periodic genes is necessary. In this paper, we propose a method based on improved non – negative matrix factorization (INMF) to extract the subset of the genes periodically expressed in gene expression data. Pascual-Montano, A. D.*et al.* have applied NMF to gene expression data to identify highly correlated genes and experiments that behave in a similar manners in only a sub portion of the data, and also applied this methodology to freeform texts in MEDLINE abstracts for a semantic analysis of scientific articles[23]. In their work, NMF algorithm is classical one, while we improved the classical NMF algorithm in this work. Otherwise, the focusing problems are different in two works. Previously, we have also used NMF to extract the characteristic patterns from gene expression profiles [24]. In our previous work, NMF algorithm was still traditional one. This work, which improves the classical NMF algorithm and further applies INMF to extract the periodic genes subsets, extends our previous work.

## 2 INMF Algorithms

Firstly, we analyzed the traditional NMF algorithm. A positive  $n \times m$  matrix  $\mathbf{V}$  is factorized into two low-rank factors  $\mathbf{W}$  and  $\mathbf{H}$  of sizes  $n \times r$  and  $r \times m$  respectively, where  $r$  is the desired rank of the factorization.

$$\mathbf{V}^{(n \times m)} = \mathbf{W}^{(n \times r)} \mathbf{H}^{(r \times m)} \quad (1)$$

In general,  $(n+m)r < nm$ . At each step of the algorithm there will exist an error between the product  $\mathbf{WH}$  and the target matrix  $\mathbf{V}$ . This error  $\mathbf{E}$  is defined as

$$\mathbf{E} = \mathbf{WH} - \mathbf{V} \quad (2)$$

The natural way to quantify the magnitude of  $\mathbf{E}$  is in terms of the 2-norm  $N_{(2)}$ , which is the sum of the squares of the element of  $\mathbf{E}$ . It can also be expressed (and computed) more conveniently in terms of the *trace* function  $tr(\mathbf{X})$ , which is defined as the *sum of the elements* on the lead diagonal of  $\mathbf{X}$ . In these terms,  $N_{(2)}$  is:

$$N_{(2)}(\mathbf{X}) = tr(\mathbf{X}^T \mathbf{X}) = tr(\mathbf{X} \mathbf{X}^T)$$

(To minimize computation in the case of non-square  $\mathbf{X}$ , we choose the order of multiplication to minimize the dimension of the product.) Thus, the error norm  $s$  of  $\mathbf{E}$  is:

$$s = tr(\mathbf{E}^T \mathbf{E}) = tr((\mathbf{WH} - \mathbf{V})^T (\mathbf{WH} - \mathbf{V})) \quad (3)$$

We can infer that the change  $\delta s$  in  $s$  at each step is:

$$\delta s = -2\mu \{tr(\mathbf{Y}) + tr(\mathbf{Z})\} \quad (4)$$

where  $\mathbf{Y} = \mathbf{H}\mathbf{E}^T\mathbf{E}\mathbf{H}^T$  and  $\mathbf{Z} = \mathbf{W}^T\mathbf{E}\mathbf{E}^T\mathbf{W}$ . In this form, it is clear that the matrices  $\mathbf{Y}$  and  $\mathbf{Z}$  are of the form  $\mathbf{U}^T\mathbf{U}$  that is always at least a semi-positive definite matrix, and hence its trace must be *positive*. Therefore,  $\delta s$  is always *negative* and the error is always *reduced* at each step. Although we obviously cannot achieve it, our ambition would be to minimize the error in one step, that is, we would like  $\delta s = -s$ . Using this to solve for the critical value of  $\mu$ , we have:

$$\mu = s / \{2 [N_{(2)}(\mathbf{H}\mathbf{E}^T) + N_{(2)}(\mathbf{W}^T\mathbf{E})]\} \quad (5)$$

The classical NMF algorithm is as follows:

- Input  $\mathbf{V}$
- Set  $\mu \leftarrow \mu_0$  (say 0.001, or anything small)
- Set  $\mathbf{W} \leftarrow$  random positive  $n \times r$  matrix
- Set  $\mathbf{H} \leftarrow$  random positive  $r \times m$  matrix
- Loop until  $s < \textit{tolerance}$ 
  - $\mathbf{W}_{\text{temp}} \leftarrow \mathbf{W} - \mu(\mathbf{W}\mathbf{H} - \mathbf{V})\mathbf{H}^T$
  - $\mathbf{H} \leftarrow \mathbf{H} - \mu\mathbf{W}^T(\mathbf{W}\mathbf{H} - \mathbf{V})$
  - $\mathbf{W} \leftarrow \mathbf{W}_{\text{temp}}$
  - $\mathbf{E} \leftarrow \mathbf{W}\mathbf{H} - \mathbf{V}$
  - $\mu \leftarrow s / \{4 [N_{(2)}(\mathbf{H}\mathbf{E}^T) + N_{(2)}(\mathbf{W}^T\mathbf{E})]\}$
- Return  $\mathbf{W}$  and  $\mathbf{H}$

Von Neumann first described this algorithm in 1950 in terms of finding the projection onto the intersection (or direct sum) of two closed sub-spaces of a Hilbert space [25]. He showed that projecting a point into each sub-space in turn would ultimately yield the projection onto the intersection. His classic paper includes proof that such an algorithm (if properly formed) will always converge.

Note that we have divided  $s$  by 4 times the trace and not 2 times the trace, as we derived. This is because the value of  $\mu$  derived is the critical value – it is the *absolutely maximum* value  $\mu$  can take for stability. However, remember that our analysis omitted to take account of the second order terms and occasionally these can become sufficiently significant that the  $\mu$  generated goes past the point of criticality and the algorithm goes into positive feedback and blows up. Therefore, for safety we “throttle back” on  $\mu$  by halving its calculated value. Actually, this is very over-cautious. In practice, scaling  $\mu$  to around 0.9 of its calculated value is usually fine.

This algorithm will work very well for many matrices with strongly positive elements. Note, however, that there is nothing *inherent* in the algorithm to stop it generating negative elements in the factors. In cases where  $\mathbf{V}$  has a low-rank

approximation with *sparse* factors, the above algorithm can occasionally generate negative elements in those places where zeros should appear in the factors. To cure this, we make improvement for the classical algorithm.

For the improved NMF (INMF) algorithm, we define  $\mathbf{W} = \mathbf{A} \bullet \mathbf{A}$  and  $\mathbf{H} = \mathbf{B} \bullet \mathbf{B}$  where  $[\bullet]$  denotes the element-wise (Hadamard) product of matrices. If we now recast the algorithm in terms of updates to  $\mathbf{A}$  and  $\mathbf{B}$ , when we compute  $\mathbf{W}$  and  $\mathbf{H}$ , their elements cannot be negative as each is a square of an element in  $\mathbf{A}$  and  $\mathbf{B}$  respectively. Once an element is zero, it stays zero. Thus

$$\mathbf{W} = \mathbf{A} \bullet \mathbf{A} \quad \text{and} \quad \mathbf{H} = \mathbf{B} \bullet \mathbf{B}$$

$$\delta \mathbf{W} = 2\mathbf{A} \bullet \delta \mathbf{A} \quad \text{and} \quad \delta \mathbf{H} = 2\mathbf{B} \bullet \delta \mathbf{B}$$

So

$$\delta \mathbf{A} = \delta \mathbf{W} \bullet / 2\mathbf{A} = -\mu \mathbf{E} \mathbf{H}^T \bullet / 2\mathbf{A}$$

$$\delta \mathbf{B} = -\delta \mathbf{H} \bullet / 2\mathbf{B} = -\mu \mathbf{W}^T \mathbf{E} \bullet / 2\mathbf{B}$$

where  $\delta \mathbf{W} = -\mu \mathbf{E} \mathbf{H}^T$ ,  $\delta \mathbf{H} = -\mu \mathbf{W}^T \mathbf{E}$  and  $[\bullet/]$  indicates element-wise (Hadamard) division of matrices. Thus, we have the improved NMF algorithm:

- Input  $\mathbf{V}$
- Set  $\mu \leftarrow \mu 0$  (say 0.001, or anything small)
- Set  $\mathbf{A} \leftarrow$  random positive  $n \times r$  matrix
- Set  $\mathbf{B} \leftarrow$  random positive  $r \times m$  matrix
- Loop until  $s < \text{tolerance}$ 
  - $\mathbf{W} \leftarrow \mathbf{A} \bullet \mathbf{A}$
  - $\mathbf{H} \leftarrow \mathbf{B} \bullet \mathbf{B}$
  - $\mathbf{E} \leftarrow \mathbf{W} \mathbf{H} - \mathbf{V}$
  - $\mu \leftarrow s / \{4 [\mathbf{N}_{(2)}(\mathbf{H} \mathbf{E}^T) + \mathbf{N}_{(2)}(\mathbf{W}^T \mathbf{E})]\}$
  - $\mathbf{A} \leftarrow \mathbf{A} - \mu (\mathbf{E} \mathbf{H}^T \bullet / 2\mathbf{A})$
  - $\mathbf{B} \leftarrow \mathbf{B} - \mu (\mathbf{W}^T \mathbf{E} \bullet / 2\mathbf{B})$
- Return  $\mathbf{W}$  and  $\mathbf{H}$

Our simulation results show that this algorithm is *stable* and converges *very fast*. The improvement for NMF algorithm is a little, but very efficient.

Compared with other matrix factorization methods, such as Principal Component Analysis (PCA), Singular Value Decomposition (SVD) and Independent Component Analysis (ICA), Improved Non – negative Matrix Factorization (INMF) has three characteristics:

- (1) There is no the distribution requirements for the latent variables in the dataset;
- (2) The localized information hidden in the dataset can be extracted by INMF;
- (3) The original dataset can be directly processed, that is, need not be normalized.



### 3 INMF – Based Cluster Method for Periodic Genes

The method can be divided into two steps. In the first step, various characteristic expression patterns hidden in gene expression data are extracted by INMF algorithm. Usually, it is easy to select periodic expression patterns from the characteristic pattern sets. According to our previous analysis<sup>[24]</sup>, the method for extracting characteristic patterns can be stated as follows. Suppose that  $\mathbf{V}$  is gene expression dataset,  $v_{ij}$  in  $\mathbf{V}$  is the expression level of the  $i^{\text{th}}$  gene in the  $j^{\text{th}}$  sample. The elements of the  $i^{\text{th}}$  row of  $\mathbf{V}$  form an  $n$ -dimensional vector  $g_i$ , which we refer to as the *transcription response* of the  $i^{\text{th}}$  gene. In practical terms, this factorization finds a small set of “basis vectors”  $\mathbf{W}$  and a set of “hidden” describing factors  $\mathbf{H}$ . Since the columns of  $\mathbf{H}$  are in one – to – one correspondence with the columns of  $\mathbf{V}$ , the results can be interpreted as each column of  $\mathbf{V}$  being described as weighted of a few basis vectors, the weights being the corresponding column of  $\mathbf{H}$ . Our analysis shows that the vector in the  $l^{\text{th}}$  row of the matrix  $\mathbf{H}$ ,  $e_l$  lists the expression of the  $l^{\text{th}}$  eigengene across the different samples. So, we infer that  $e_l$  represent a characteristic expression pattern across all samples, while this pattern is biological interpretable. From  $\mathbf{H}$ , we select out whole periodic patterns and establish a new transformation matrices  $\mathbf{H}'$  with dimension  $k \times m$ , where  $k$  is the number of periodic expression patterns. In step two, the periodic expression genes in  $\mathbf{V}$  are identified. For this purpose, the Pearson correlation method is used to identify interesting genes that have similar periodic expression patterns to those eigengenes in  $\mathbf{H}'$ , that is, we calculated the correlation coefficients  $R$  between the  $l^{\text{th}}$  eigengene in  $\mathbf{H}'$  ( $l = 1, 2, \dots, k$ ) and all genes  $g_i$  ( $i = 1, 2, \dots, n$ ) in  $\mathbf{V}$ . If the correlation coefficient  $R$  between the  $i^{\text{th}}$  gene and the  $l^{\text{th}}$  eigengene exceeds a specified *threshold of similarity*  $\theta_R$  (empirically or analytically), the  $i^{\text{th}}$  gene is deemed to have a similar expression pattern to that of the  $l^{\text{th}}$  eigengene and so they are in a cluster. The larger  $\theta_R$  is, the higher the accuracy of the identification is.

## 4 Experiment Results

In order to verify the feasibility and the effectiveness of our methodology, we designed simulated datasets and select Yeast gene expression datasets, which have been used as benchmark dataset in previous studies, to do test experiments.

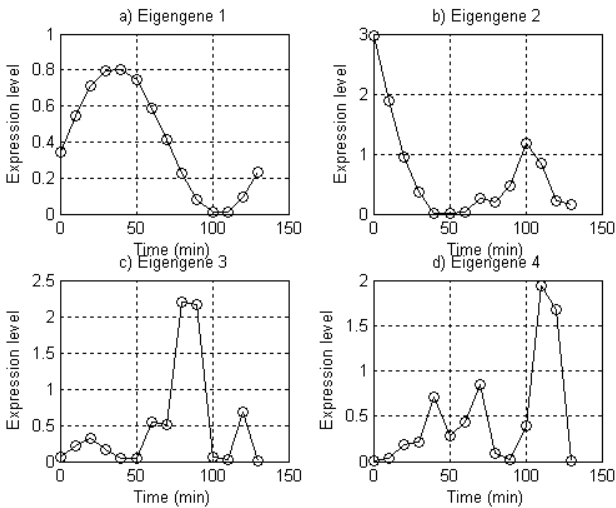
### 4.1 Simulated Data Analysis

Firstly, genes in the simulated dataset have one of three kinds of transcriptional response, inspired by experimentally observed patterns in the Cho *et al.* cell cycle data [1]:

- noise (1600 genes)
- noisy sine pattern (200 genes)
- noisy exponential pattern (200 genes).

Noise for all three groups of genes was modeled by sampling from a uniform distribution within the interval  $(0, 1)$ . The sine pattern has the functional form  $a\sin(2\pi t/140)$  and the exponential pattern the form  $be^{-t/100}$  where  $a$  is sampled uniformly over the interval  $(1.5 - 3)$ ,  $b$  is sampled uniformly over  $(4 - 8)$ ,  $t$  is the time (in minutes) associated with each sample, and time points are sampled every ten minutes beginning at  $t = 0$ .

Four characteristic patterns (or eigengenes) of the transcriptional response are extracted by INMF when taking  $r = 4$ . The results are showed in Fig. 1. Obviously, only eigengene 1 in Fig. 1(a) has periodic structure, the eigengene 2 shows a clear exponential pattern, while eigengene 3 and 4 denote two noisy patterns because they do not exhibit any regulatory. These patterns are same with the known patterns.

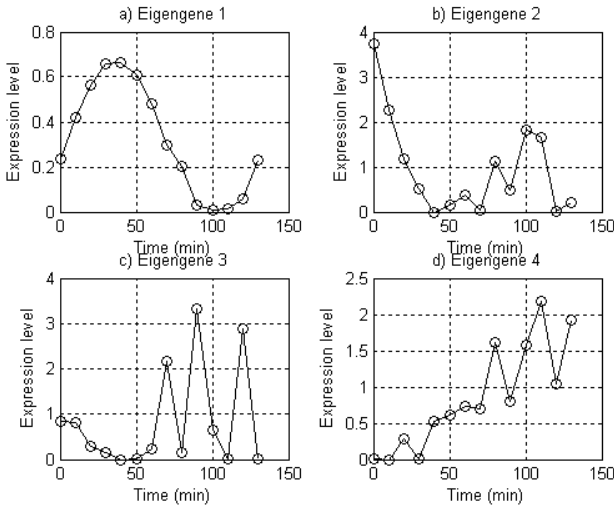


**Fig. 1.** The expression patterns extracted by INMF from the synthetic data set

To illustrate the ability of our method to extract *weak* expression patterns, we increased the noise intensity into about 67% of the maximum sine amplitude and about 50% of the maximum exponent initial value. Fig. 2 shows the characteristic patterns extracted by our method. We know from Fig. 2, even under these difficult signal-to-noise ratio conditions, eigengene 1 still reveals the sine pattern very clearly, eigengene 2 still displays an exponential pattern and eigengene 3 and 4 again lack any obvious structure. So, our method has good ability to resist the noise.

Further, we studied the sensitivity of our method with respect to the number of cyclic genes in the dataset by decreasing 200 sine genes into 125, 100, 75, 60, 50, 40, 20 genes respectively. The results showed that the above changes have no effect on the pattern extraction ability of INMF method and the desired sine expression patterns can still be extracted (data not show).

In order to obtain the periodic gene clusters, we identify respectively those genes with periodic structure in the simulated data using the extracted sine pattern. The



**Fig. 2.** The Extracted weak patterns by INMF under these difficult signal-to-noise ratio conditions

**Table 1.** The clustering results of periodic genes by three different methods ( $\theta_r = 0.992$ )

| Case                               | Signal – to – noise ratio 1 |           |     | Signal – to – noise ratio 2 |           |     |
|------------------------------------|-----------------------------|-----------|-----|-----------------------------|-----------|-----|
|                                    | INMF                        | K – means | SOM | INMF                        | K – means | SOM |
| Number of clustered periodic genes | 200                         | 136       | 200 | 199                         | 40        | 194 |

experimental results under above two different signal - to - noise radio cases are showed in table 1 and are compared with those of K – means and Self – Organizing Maps (SOM) cluster methods when noisy sine genes are 200 in the dataset.

From a large number of experiments, we found that 200 sine genes can be precisely identified by our method when the specified threshold  $\theta_R$  of similarity was taken as 0.992 in the case of signal - to - noise radio 1. We checked these sine genes and found that they are exactly 200 known sine genes. In the case, SOM method can also cluster 200 sine genes. But K – means method only clustered 136 sine genes and 64 sine genes were missed. In the case of signal – to - noise radio 2, the noise intensity was increased. 199 sine genes are clustered by our method when  $\theta_R = 0.922$  and they are among 200 known sine genes. Only one gene was missed. When we decrease  $\theta_R$  into 0.919, 205 genes were identified. We checked the results and found that 5 false genes from noise were detected. Thus, the reasonable  $\theta_R$  value is 0.922 in this case. SOM clustered 194 sine genes, while K – means clustered only 40 sine genes.

The above analysis showed that our method is effective for clustering periodic genes when the appropriate  $\theta_R$  is taken.

## 4.2 Biological Data Analysis

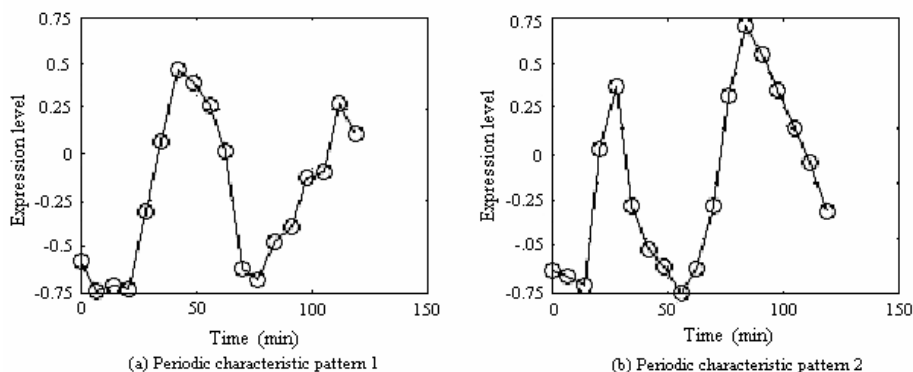
Spellman *et al.* [2] used DNA microarrays and samples from yeast cultures synchronized by three independent methods:  $\alpha$  factor arrest, elutriation, and arrest of a *cdc15* temperature-sensitive mutant, and identified the approximately 800 genes that meet an objective minimum criterion for cell cycle regulation using periodicity and correlation algorithms. The related information on three biological datasets from Spellman *et al.* is showed in table 2. In addition, some other authors also selected these biological datasets to test their methods<sup>[9, 11-12, 20]</sup>. Hence, alpha dataset (DS), elutriation DS and *cdc15* DS (the results not show) are used to validate our methodology in this work.

**Table 2.** Summary of the biological datasets

| Dataset         | Method of arrest                  | start | end   | sample                                                        | sample number |
|-----------------|-----------------------------------|-------|-------|---------------------------------------------------------------|---------------|
| alpha DS        | Alpha mating factor               | 0 m   | 119 m | every 7 m                                                     | 18            |
| elutriation DS  | elutriation                       | 0 m   | 390 m | every 30 m                                                    | 14            |
| <i>cdc15</i> DS | Temp. sensitive <i>cdc</i> mutant | 0 m   | 290 m | ev. 20 m for 1 hr. ev. 10 m for 3 hr. ev. 20 min for final hr | 24            |

### 4.2.1 Alpha DS

For alpha dataset, genes with missing values and constant expression levels for all sample points were removed from the study. Two characteristic patterns, which show a periodic behaviour, are extracted by our method when taking  $r = 5$ . The results are showed in Fig. 3. Two cell – cycle behaviour is mainly of the form  $A \sin(\omega t + \phi)$  with the same  $\omega$  but differing  $\phi$  value and possibly due to desynchronization, where  $\omega = 1 / T$ ,  $T \cong 67$  minutes. Two periodic characteristic patterns can be explained to represent cell cycle expression oscillations.



**Fig. 3.** The extracted periodic patterns from alpha dataset

Further, we take threshold criterion  $\theta_R = 0.922$  according to the previous analysis for the simulated data and clustered the periodic genes in alpha DS. The results and the comparisons with those results of Spellman, *et al* [2], Alter, *et al*[12] and Wichert[20], *et al* are showed in table 3.

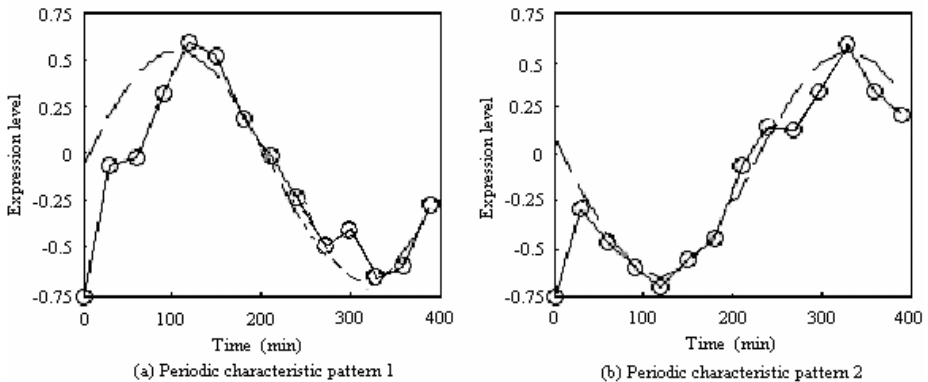
**Table 3.** The cluster results and the comparisons for alpha DS

| Method  | Our method | Spellman’s method | Alter’s method | Wichert’s method |
|---------|------------|-------------------|----------------|------------------|
| Results | 636/4579   | 638/4579          | 544/4579       | 468/4415         |

For alpha DS, Spellman *et al.* identified 638 cell cycle-regulated genes from 4579 genes and Alter *et al.* identified 544 genes from 4579 genes. 468 periodic expression genes were identified by the method of Wichert, *et al.* Using our method when taking  $\theta_R = 0.922$ , the number of identified genes (636) with periodic structure is almost same as that of Spellman *et al.* Two genes were missed by our method.

**4.2.2 Elutriation DS**

For elutriation dataset, genes with missing values and constant expression levels for all sample points were removed from the study. Firstly, two periodic characteristic patterns called pattern 1 and pattern 2 were extracted when taking  $r = 5$ . The results are showed in Fig. 4. The time variation of periodic characteristic pattern 1 fits a normalized sine function of period  $T$  (about 390 min),  $A \sin (2\pi/T)$ . The time variation of periodic characteristic pattern 2 fits a cosine function of period  $T$  (about 390 min) with the amplitude  $B$  of a normalized cosine with this period,  $B\cos (2\pi/T)$ . We infer that the periodic characteristic pattern 1 and 2 are consistent with gene expression oscillations during a cell cycle.



**Fig. 4.** The extracted periodic patterns from elutriation dataset

Secondly, we clustered the periodic genes in elutriation DS. The results and the comparisons with those results of Spellman, *et al.*, Alter, *et al* and Wichert, *et al* are showed in table 4.

**Table 4.** The cluster results and the comparisons for elutriation DS

| Method  | Our method | Spellman's method | Alter's method | Wichert's method |
|---------|------------|-------------------|----------------|------------------|
| Results | 785/5981   | 784/5981          | 641/5981       | 193/5695         |

For the elutriation dataset, Spellman *et al.* identified 784 cell cycle-regulated genes from 5981 genes and Alter *et al.* identified 641 periodic genes from 5981 genes. Only 193 periodically expressed genes were identified by the method of Wichert, *et al.* They explained that the elutriation data provided only little statistically significant information with regard to cell cycle regulation. The number of periodic genes clustered by our method is 785 when taking  $\theta_R = 0.922$ , which is closed to that of Spellman *et al.* When we compared these periodic genes with the results of Spellman *et al.*, we found that only one periodic gene is not belong to Spellman's periodic genes cluster and is possibly from noise. Our results seem to support again Spellman *et al* and better than the results of Alter, *et al.* and Wichert, *et al.*

## 5 Conclusions

In this paper, we have analyzed the weak of the traditional non – negative matrix factorization algorithm and proposed an improved non – negative matrix factorization algorithm for gene expression data analysis. Based on INMF algorithm, we presented an approach to cluster gene expression data for periodic gene subsets. Our approach includes two steps. Firstly, the periodic characteristic expression patterns are extracted by improved non – negative matrix factorization algorithm. Secondly, Pearson correction was suggested to identify individual periodic genes for the periodic gene clusters. Compared with other related approaches, our approach can be applied to gene expression data with any size and distribution and has strong ability to extract the characteristic expression patterns hidden in gene expression data, even under the condition of high noise levels. Our approach performed well in clustering genes periodically expressed for the simulated dataset and Yeast gene expression datasets, which deliver valuable information for gene network research and gene function discovery.

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# Feature Selection for Microarray Data Analysis Using Mutual Information and Rough Set Theory

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**Abstract.** Cancer classification is one major application of microarray data analysis. Due to the ultra high dimension of gene expression data, efficient feature selection methods are in great needs for selecting a small number of informative genes. In this paper, we propose a novel feature selection method MIRS based on mutual information and rough set. First, we select some top-ranked features which have higher mutual information with the target class to predict. Then rough set theory is applied to remove the redundancy among these selected genes. Binary particle swarm optimization (BPSO) is first proposed for attribute reduction in rough set. Finally, the effectiveness of the proposed method is evaluated by the classification accuracy of SVM classifier. Experiment results show that MIRS is superior to some other classical feature selection methods and can get higher prediction accuracy with small number of features. Generally, the results are highly promising.

## 1 Introduction

The development of microarray technology has made it easy to monitor the expression pattern of thousands of genes simultaneously and a huge amount of gene expression data has been produced during microarray experiments. These data has widely been applied to accurate prediction and diagnosis of cancer. Especially cancer classification [1] is an important issue because it can identify many genes relevant to cancer. The results reported in the literature have confirmed the effectiveness of mining cancer information from gene expression data. But microarray data often consists of small number of samples and large number of genes. The ultra high dimension of gene expression data makes it necessary to develop effective feature selection methods in order to reduce the computation cost and improve the classification accuracy.

There are two general approaches to feature selection: filters [2] and wrappers [3]. In a filter method, features are selected based on the intrinsic characteristics which determine their relevance with the target classes. In wrapper type methods, the usefulness of a feature is directly judged by the estimated accuracy of a learning method and typically requires huge computational effort. Thus, it is difficult for wrappers to deal with large feature sets such as gene expression data. We mainly focus on the selection of a few tens features among several thousands by developing an efficient filter methods for cancer classification. When a small number of informative genes are selected, their biological relationship with the target disease can easily be identified.

Mutual information [4] has recently been proposed for feature selection. One common practice to use this method is to simply select the top-ranked genes with higher mutual information. But a deficiency of this simple ranking approach is that the features can be correlated among themselves. If gene  $g_i$  is ranked high for classification task, other genes highly correlated with gene  $g_i$  are also likely to be selected. This raises the issue of redundancy in feature set. Rough sets theory provides a feasible way to deal with redundancy [5]. An important concept is reduct in rough sets theory. Reduct is those minimal attribute sets of information system, which keep the same classification capability with original attribute set. The aim of reduction is to find out a minimum set of relevant attributes (features) that describe the dataset as well as all the original attributes do. Thus finding reduct can select the most relevant genes with the target class to predict and remove the redundancy among the selected features.

In this paper, we propose a novel feature selection method MIRS based on mutual information and rough set theory. First, mutual information is used to select some top-ranked genes which have higher mutual information from each data set. Then rough set theory is applied to remove the redundancy among these selected genes. Binary particle swarm optimization (BPSO) is first suggested as an attribute reduction algorithm for rough sets. Finally, the effectiveness of MIRS is evaluated by the classification accuracy of SVM classifiers. The entire system is shown in Figure 1. Experiment results show that the proposed method is superior to some other classical feature selection methods and can always get higher classification accuracy with fewer features.

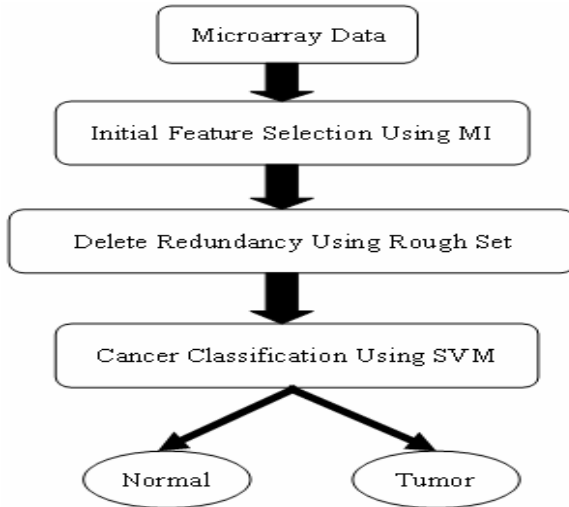


Fig. 1. Cancer classification system

## 2 Mutual Information for Feature Selection

In accordance with Shannon’s information theory [6], the uncertainty of a random variable  $Y$  can be measured by the entropy  $H(Y)$ . For two variables  $X$  and  $Y$ , the

conditional entropy  $H(Y|X)$  measures the remaining uncertainty of  $Y$  when  $X$  is known. The mutual information (MI)  $I(X;Y)$  measures the certainty about  $Y$  that is resolved by  $X$ . Apparently, the relation of  $H(Y)$ ,  $H(Y|X)$  and  $I(X;Y)$  is as follows:

$$I(X;Y) = H(Y) - H(Y|X) \tag{1}$$

The objective of training a classification model is to minimize the uncertainty about predictions on class labels  $Y$  for the known observations  $X$ . Thus, it is equivalent to increase the MI  $I(X;Y)$  as much as possible for training a classifier. The goal of feature selection process for classification is naturally to achieve the smallest subset of possible features which have higher values of  $I(X;Y)$ . With the entropy defined by Shannon, the prior entropy of  $Y$  is expressed as follows:

$$H(Y) = -\sum_{y \in Y} P(y) \log P(y) \tag{2}$$

Where  $P(y)$  represents the probability of  $Y$ . The conditional entropy  $H(Y|X)$  is computed according to the following formula:

$$H(Y|X) = -\int P(x) \left( \sum_{y \in Y} P(y|x) \log P(y|x) \right) dx \tag{3}$$

The mutual information MI between  $X$  and  $Y$  is presented formally as follows:

$$I(X;Y) = \sum_{y \in Y} \int P(y|x) \log \frac{P(y,x)}{P(y)P(x)} dx \tag{4}$$

The probability density function is required in order to estimate the mutual information. One of the most popular methods is to use a histogram. In a two dimensional space, histogram can be constructed feasibly. But there would be many problems in higher dimensional data space. The increase of data dimension may decrease the estimation accuracy. In addition, the required memory will increase exponentially.

In this paper, the estimation of probability density is based on the distribution of mutual information [7] in a Bayesian framework by a second-order Dirichlet prior distribution. Beta approximation of the distribution is adopted in this paper. The top-ranked 700 genes and 500 genes with higher mutual information for the leukemia data set and the colon data set discussed in section 5 are selected respectively.

If too many genes are selected, there must be much noise retained in the data. On the other hand, if we select very few genes, some information contained in the data set for classification may be lost. The number of genes we select for the two data sets is determined with respect to the observation from classification experiments. Subsequently the redundancy among these selected genes will be removed in section 4.

### 3 Background on Rough Set Theory

Rough set theory is first introduced by Pawlak [8] in the 1980s as a mathematical tool to deal with uncertainty. In this section, we will introduce the principal concepts of rough sets theory related to our attribute reduction approach.

**Information System:** In rough sets theory, an information system  $S$  is denoted as  $S = \{U, A, V, f\}$ , where  $U$  is a finite set of instances  $U = \{x_1, x_2, \dots, x_n\}$ .  $A$  is a finite set of attributes (features) and consists of condition attribute set  $C$  and decision attribute set  $D$ .  $f: U \times A \rightarrow V$  is a function that  $f(x_i, q) \in V_p$  for every  $q \in A, x_i \in U$ .

**Indiscernibility Relation:** Let  $P \subseteq A, x_i, x_j \in U$ , a binary relation  $IND$  called indiscernibility relation is defined as follows:

$$IND(P) = \{(x_i, x_j) \mid (x_i, x_j) \in U \times U, a \in P, f(x_i, a) = f(x_j, a)\} \quad (5)$$

Let  $U / IND(P)$  denote the family of all equivalence classes of the relation  $IND(P)$ . For simplicity notation  $U / IND(P)$  will be written as  $U / P$ .

**Lower Approximation:** Let  $R \subseteq C$  and  $X \subseteq U$ , the R-lower approximation set of  $X$  is the set of all elements of  $U$  which can be certainly classified as elements of  $X$  according to knowledge  $R$ . It can be presented formally as follows:

$$\underline{R}X = \bigcup \{Y \in U / R : Y \subseteq X\} \quad (6)$$

**Positive Region:** The positive region of decision attribute set  $D$  with respect to  $R$  is the set of all objects from universe  $U$  that can be classified with certainty to classes of  $U / D$  employing attributes from  $R$ . It can be defined as follows:

$$POS_R(D) = \bigcup_{X \in U / D} \underline{R}X \quad (7)$$

**Dispensable and Indispensable Features:** Let  $c \in C$ . A feature  $c$  is dispensable if  $POS_{(C-\{c\})}(D) = POS_C(D)$ ; Otherwise feature  $c$  is indispensable.

**Reduct:** A set of features  $R \subseteq C$  is called a reduct of  $C$  if all  $c \in R$  are indispensable and  $POS_R(D) = POS_C(D)$ . In other words, a reduct is the minimal feature subset preserving the above condition.

### 4 Support Vector Machine

The Support Vector Machine (SVM) [9] is a statistic learning method first proposed by Vapnik in 1995 and its structure is shown in Figure 2. It is based on the theories of VC dimension and structure risk minimization. For two-class classification problem, when two types of examples are nonlinear separable, SVM uses a nonlinear mapping

known as kernel function to map the training data into a higher dimensional feature space, and then constructs an optimal separating hyperplane in the higher dimensional space corresponding to a nonlinear classifier in the input space. The kernel function can be linear, polynomial, sigmoid, or Gaussians (RBF). With the kernel functions and the high dimensional space, the hyperplane computation requires a quadratic programming, which is computationally intensive.

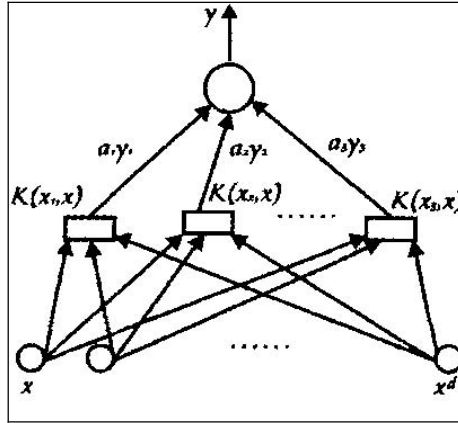


Fig. 2. Structure of support vector machine

## 5 BPSO for Attribute Reduction in Rough Set

Particle swarm optimization (PSO) is an evolutionary computation technique first introduced for use in real number space by Kennedy and Eberhart in 1995. It has been shown to be a powerful optimization method in many practical applications. In 1997, a binary version of particle swarm optimization (BPSO) is proposed and its performance has been tested on five benchmark functions [10]. But it has not been widely used and still need much further research.

Rough set can be used to find out all possible feature subsets. However, examining exhaustively all subsets of features for selecting the optimal one has been proved to be NP-hard [11]. Heuristic algorithms provide a new way to solve this NP-hard optimization problem. In this section, we suggest binary particle swarm optimization as an attribute reduction algorithm in rough set and apply it to find minimal reduct by removing the redundancy among the genes selected by mutual information.

### 5.1 Data Preprocessing

The values of gene expression level are continuous. But rough set can only handle discrete attribute value. Hence in order to use the attribute reduction algorithm, all the express level values of selected genes must be discretized firstly. The Entropy/MDL discretization algorithm of Rosetta [12] is used in our experiments. During the entire

procedure of attribute discretization and attribute reduction, we combine the training samples with the testing samples together for each data set.

### 5.2 Population Initialization

Let  $n$  be the number of selected features (genes) by mutual information from the original data set. The velocity of  $i_{th}$  particle is initialized as a  $n$ -dimensional vector with the following form:  $V_i = (v_{i1}, v_{i2}, \dots, v_{in})$ . Then the initial position of the  $i_{th}$  particle  $X_i = (x_{i1}, x_{i2}, \dots, x_{in})$  can be computed according to Eq. (11). Where  $v_{ij} \in [-6, 6]$ ,  $x_{ij} \in \{0, 1\}$ ,  $j \in \{1, 2, \dots, n\}$ .  $x_{ij}$  is equal to 1 or 0 which indicates the corresponding feature is selected or not. We put all the selected features of the  $i_{th}$  particle into the attribute set  $P_i$ .

### 5.3 Fitness Evaluation

The goal of reduction is to use fewer features to achieve the same or better performance compared with that obtained using the complete feature set. Hence, individual evaluation contains the following two objectives: (1) Minimization of the feature numbers; (2) Maximization of the classification capability. We have to make some tradeoffs between the two objectives. In this paper, classification capability is always have higher priority. If two individuals have the same classification capability, the individual with fewer features will have higher fitness. A simple weighting method is adopted to define the fitness of particles as follows:

$$f(i) = w_1 \cdot fc(i) + w_2 \cdot (1 - fn(i)) \tag{8}$$

$$fc(i) = card(POS_{P_i}(D)) / card(U) \tag{9}$$

Where  $w_1$  and  $w_2$  are weight coefficients,  $fc(i)$  is the classification capability we can get by using the feature set  $P_i$ ,  $fn(i)$  is the number of features contained in  $P_i$ ,  $card(U)$  represents the cardinality of the set  $U$ .

### 5.4 Update Velocity and Position

Each particle represents a candidate solution with four state variables:  $v_i, x_i, P_i, P_g$ . These variables present the current velocity, current position, previous best position and current global best position of the  $i_{th}$  particle respectively. The velocity and position vector are updated according to the following equations:

$$V_{ij} = w \cdot V_{ij} + c_1 \cdot r \text{ and } () \cdot (P_{ij} - X_{ij}) + c_2 \cdot r \text{ and } () \cdot (P_{gj} - X_{ij}) \tag{10}$$

$$X_{ij} = \begin{cases} 0, & \text{if } \rho \geq sig(V_{ij}) \\ 1, & \text{if } \rho < sig(V_{ij}) \end{cases} \tag{11}$$

Where  $c_1$  and  $c_2$  are known as acceleration coefficients,  $X_{ij}$  represents the  $j_{th}$  element of the  $n$ -dimensional vector  $X_i$ .  $Rand()$  produces a random number between 0 and 1.  $\rho$  is a random number selected from the uniform distribution in  $[0, 1]$ . The function  $sig(V_{ij})$  is a sigmoid limiting transformation.

## 6 Gene Expression Data Sets

There are several microarray data sets published from cancer gene expression studies. Two data sets of them are used to test the effectiveness of our proposed method. Because the benchmark data sets have been studied in many papers, we can compare the results of our method with others conveniently.

Leukemia data set [13] consists of 72 samples: 25 samples of acute myeloid leukemia (AML) and 47 samples of acute lymphoblastic leukemia (ALL). Each sample contains the expression levels of 7129 genes measured using high density oligonucleotide microarrays. In our experiments, 38 samples are used as training data and the remaining 34 samples are used as test data.

Colon data set consists of 62 samples of colon epithelial cells taken from cancer patients [14]. Each sample contains 2000 gene expression levels. 20 out of 62 samples are normal samples and the remaining are cancer samples. In our different experiments, 31 or 44 samples are used as training data and the remaining 31 or 18 samples are used as test data.

## 7 Experiment Results

In all the experiments, BPSO is run with a population size of 30 and it is terminated when the maximum generation of 600 is arrived. The five parameters in the Eq. (8) and Eq. (10) are set to as follows:  $w = 1, c_1 = c_2 = 2, w_1 = 100, w_2 = 0.06$ . All the algorithms are implemented in matlab 6.5. The features selected by BPSO are used for testing the classification accuracy by support vector machine. The classification accuracy is measured by the number of correct predictions made by the classifier over the test set.

In table 1, experiment results are displayed by using different feature selection methods (No indicates no feature selection). The classification accuracy is obtained by using linear SVM. For the colon data set, 44 samples are used as training data and 18 samples as testing data in this experiment. We can observe that our proposed feature selection method MIRS can always obtain higher classification accuracy with fewer features compared with using MI only. The effectiveness of MIRS is also verified by the remarkable improvement of classification accuracy compared with not using feature selection.

**Table 1.** The comparison results on feature number and classification accuracy

| Dataset  | Original No. | FS method | Selected No. | Accuracy |
|----------|--------------|-----------|--------------|----------|
| Leukemia | 7129         | No        | 7129         | 58.8%    |
|          | 7129         | MI        | 700          | 94.1%    |
|          | 7129         | MIRS      | 48           | 97.1%    |
| Colon    | 2000         | No        | 2000         | 50.0%    |
|          | 2000         | MI        | 500          | 66.7%    |
|          | 2000         | MIRS      | 32           | 94.4%    |

We have also compared the performance of MIRS with some other classical feature selection techniques on the two real gene expression data sets. The comparison results are shown in table 2. The results of other techniques are extracted from a survey reported by Sung [15]. These feature selection techniques being compared include principal components (PC) and correlational coefficient (CC).

In this experiment, we use 31 samples as training data and the other 31 samples as testing data for the colon data set so that we can compare with the results of Sung directly. We try the following two kinds of support vector machines: (1) Linear SVM (no kernel); (2) Radial basis function SVM (RBF kernel). It is obvious that our proposed method is consistently better than the above methods in all the two data sets.

**Table 2.** Comparison of classification accuracy between MIRS and other methods

| Data set | Feature selection | Linear SVM | Rbf SVM |
|----------|-------------------|------------|---------|
| Leukemia | MIRS              | 97.1%      | 97.1%   |
|          | PC                | 79.4%      | 79.4%   |
|          | CC                | 85.3%      | 85.3%   |
| Colon    | MIRS              | 80.7%      | 83.9%   |
|          | PC                | 64.5%      | 64.5%   |
|          | CC                | 64.5%      | 64.5%   |

## 8 Conclusions

Mutual information has recently been proposed for feature selection. But it often contains redundancy in the feature set selected by this method. Attribute reduction in rough set theory provides a feasible way to deal with redundancy and does not reduce the contained information. In this paper, we propose a novel feature selection method MIRS based on mutual information and rough set. First, we select some top-ranked features which have higher mutual information with the target class to predict from two public available real gene expression data sets. Then rough set theory is applied to remove the redundancy among these selected genes. Binary particle swarm optimization (BPSO) is first proposed for attribute reduction in rough set. Finally, the effectiveness of the proposed method is evaluated by the classification accuracy of SVM classifier. Experiment results show that MIRS can always get higher prediction accuracy with small number of features compared with using MI only and is superior to some other classical feature selection methods. Generally, the results are highly promising.



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# Feature Subset Selection for Protein Subcellular Localization Prediction

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**Abstract.** Most of the existing methods for protein subcellular localization prediction are based on a large number of features that are considered to be potentially useful for determining protein subcellular localizations. However, predictors with large numbers of input variables usually suffer from the curse of dimensionality as well as the risk of overfitting. Using only those features that are relevant for protein subcellular localization might improve the prediction performance and might also provide us with some biologically useful knowledge. In this paper, we present a feature ranking based feature subset selection approach for subcellular localization prediction of proteins in the context of support vector machines (SVMs). Experimental results show that this method improves the prediction performance with selected subsets of features. It is anticipated that the proposed method will be a powerful tool for large-scale annotation of biological data.

## 1 Introduction

The availability of massive amounts of genomic data from large-scale sequencing projects has given impetus in recent years to a large effort in developing statistical and machine learning methods to infer biological models from data. Predicting protein subcellular localization is a hot topic in bioinformatics community, which attempts to classify proteins by their amino acid sequence into sets of cellular compartments using a reliable computational method. The subcellular localization resource is helpful to understand protein function because each cell compartment has maintained a characteristic physicochemical environment [1].

Current computational methods for protein subcellular localization prediction are mostly based on multiple information resources that could be extracted from amino acids and amino acid properties, such as sorting signal sequence [2,3], amino acid composition or dipeptide composition [4-10], n-peptide composition [11], amino acid property [12,13], quasi-sequence-order [14], pseudo-amino acid composition [15], functional domain composition [16], Zp curve [17], gene ontology (GO) [18], homology [19,20], and cellular automata image [21]. Though protein N-terminal sorting signal contains all the information used to localize a cellular protein, the assignments of gene 5'-regions or protein N-terminal sequences are often unreliable in genome sequencing projects. Thus, the existing methods on this basis might be

problematic in cases that these leader sequences are missing or only partially included. Moreover, prediction methods based on amino acid composition alone may lose some other kinds of information relevant to the prediction of protein subcellular localizations. It has been shown that incorporating such information resource may improve the prediction performance to some extent [22-28].

Since it remains unknown how many and which features are relevant to protein subcellular localization, the dimension of feature set used in some methods is usually very high. However, predictors with large numbers of variables may suffer from the curse of dimensionality as well as the risk of overfitting. On the other hand, apart from using machine learning methods merely for prediction, biologists are also interested in the discovery of domain-specific knowledge behind the complex process. A well-known method to get more insight into original data is the application of feature selection approaches [29-31]. By eliminating irrelevant or redundant features, a subset of relevant features can be discovered. One potential advantage of feature selection is that it would decrease the cost of computation as well as the risk of overfitting. Another is that it might improve the prediction performance and might also provide us with some biologically useful knowledge.

In this paper, we present a feature selection approach for the prediction of protein subcellular localizations. A classifier based on support vector machines (SVMs) was used to estimate the prediction performance of subsets of features by 5-fold cross-validation. The proposed method was applied to a freely available protein dataset to demonstrate its efficiency and the experimental results show that our approach selects features that improve the prediction performance against the use of all features.

## 2 Materials and Methods

### 2.1 Protein Dataset

Dataset used in this paper was constructed by Park and Kanehisa [10]. All proteins in the dataset were extracted from SWISS-PROT release 39.0 and only those eukaryotic proteins with unique and experimentally determined subcellular localization were included. After a sequence similarity check operation, no sequence has more than 80% similarity to any other sequences in the dataset. The dataset contains 7579 proteins for 12 subcellular locations. The number of proteins in each location is shown in Table 1.

### 2.2 Protein Representation

An important issue in the prediction of protein subcellular localization is to represent the protein with certain encoding scheme, i.e. to quantify the protein as the input of a machine learning algorithm. However, most of the existing methods for the prediction of protein subcellular localization are based on a large number of input features with comparably few samples, such as the SVM-based method by Park and Kanehisa [10]. They characterize each protein in the training dataset by a 400D (dimensional) feature vector, whereas the size of samples in several compartments is very small, such as the cytoskeleton (40), golgi apparatus (47) and vacuolar (54). Therefore, feature selection is necessary to alleviate the curse of dimensionality.

**Table 1.** The number of proteins in each location of the dataset used in this paper

| Subcellular location  | Number of proteins |
|-----------------------|--------------------|
| Chloroplast           | 671                |
| Cytoplasmic           | 1241               |
| Cytoskeleton          | 40                 |
| Endoplasmic reticulum | 114                |
| Extracellular         | 861                |
| Golgi apparatus       | 47                 |
| Lysosomal             | 93                 |
| Mitochondrial         | 727                |
| Nuclear               | 1932               |
| Peroxisomal           | 125                |
| Plasma membrane       | 1674               |
| Vacuolar              | 54                 |
| Total                 | 7579               |

### 2.2.1 Feature Extraction

There are 20 natural amino acids that may occur in a protein sequence and are denoted as  $\{A, C, D, E, F, G, H, I, K, L, M, N, P, Q, R, S, T, W, V, Y\}$ . In this paper, we represent proteins with features of amino acid composition and amino acid pair composition extracted directly from their primary sequence. Amino acid composition comprises the percentages of the 20 amino acids in a protein sequence. Although this is a simple representation of proteins, its correlation with protein function, secondary structure and subcellular localization are well-known. Amino acid pair composition can be considered as a 2-gram method as stated by Wu *et al.* [32]. The 2-gram encoding scheme extracts various patterns of 2 consecutive amino acid residues from a protein sequence in a sliding window fashion and counts the number of occurrences of the extracted residue pairs. So there are 400 possible amino acid pairs in total. The occurrence frequency of each amino acid pair is then calculated and used as the element of a 400D feature vector for characterizing the protein. Amino acid pair composition has been used for predicting protein secondary structure and classifying protein function in the past [33,34]. It is proved to be a better representation of proteins than amino acid composition because it encapsulates some information about the order of residues.

We also employ the 9-letter exchange group  $\{e_1, e_2, e_3, e_4, e_5, e_6, e_7, e_8, e_9\}$  to represent a protein, which is a re-substitution of the 20-letter amino acids by a 9-letter amino acids according to their physicochemical properties, where  $e_1 \in \{C\}$ ,  $e_2 \in \{M\}$ ,  $e_3 \in \{N, Q\}$ ,  $e_4 \in \{D, E\}$ ,  $e_5 \in \{S, T\}$ ,  $e_6 \in \{P, A, G\}$ ,  $e_7 \in \{I, V, L\}$ ,  $e_8 \in \{F, Y, W\}$  and  $e_9 \in \{H, K, R\}$ , see Table 2 [33]. Thus, we get 90 additional features with the similar encoding scheme for the 20 amino acids. Finally, we extract an original set of 510 features in total. Due to the problem of curse of dimensionality, we attempt to use feature selection to reduce the dimension of feature space.

**Table 2.** The 9-letter exchange group for the 20 amino acids based on their physicalchemical properties

| Group | Residues | Description                                 |
|-------|----------|---------------------------------------------|
| 1     | C        | Cysteine, remains strongly during evolution |
| 2     | M        | Hydrophobic                                 |
| 3     | N, Q     | Amides, polar                               |
| 4     | D, E     | Acids, positive, polar                      |
| 5     | S, T     | Alcohols                                    |
| 6     | P, A, G  | Aliphatic, small                            |
| 7     | I, V, L  | Aliphatic                                   |
| 8     | F, Y, W  | Aromatic                                    |
| 9     | H, K, R  | Bases, charged                              |

**2.2.2 Feature Selection**

In this paper, we introduce the feature subset selection approach by Wang, *et al.* [34], and apply it to the problem of protein subcellular localization prediction. We define a distance function to measure the relevance score of each feature and use it afterwards to rank and select features. Let  $S_i$  and  $S_j$  be two classes of proteins. Let  $X$  be a feature and  $x$  be its value. Let  $D_{i,j}(X)$  denote the distance function between  $S_i$  and  $S_j$ , which measures the discriminatory power of feature  $X$  to separate the two classes, defined as

$$D_{i,j}(X) = \frac{(m_i - m_j)^2}{d_i^2 + d_j^2}. \tag{1}$$

where  $m_i$  and  $d_i$  ( $m_j$  and  $d_j$ ) are the mean value and standard deviation of feature  $X$  in class  $S_i$  ( $S_j$ ), respectively. The mean value  $m$  and the standard deviation  $d$  of feature  $X$  in class  $S$  are defined by

$$m = \frac{1}{N} \sum_{i=1}^N x_i. \tag{2}$$

$$d = \sqrt{\frac{1}{N-1} \sum_{i=1}^N (x_i - m)^2}. \tag{3}$$

where  $x_i$  is the value of feature  $X$  with respect to protein sequence  $S_i \in S$ , and  $N$  is the total number of protein sequences in  $S$ . We define average distance function  $D(X)$  by

$$D(X) = \frac{\sum_{i,j(i < j)}^k D_{i,j}(X)}{k}. \tag{4}$$

where  $k$  is the number of classes, here  $k = 12$ . The distance measure prefers feature  $X$  to feature  $Y$  if  $D(X) > D(Y)$ . Intuitively, this means it is easier to distinguish

between two classes by using feature  $X$  than using feature  $Y$ . The values of  $D(X)$  are ranked and features with the smallest values are removed first from the original set. Let  $X_1, X_2, \dots, X_{N_g}$  be the top  $N_g$  features with the largest  $D(X)$  values, they are used in the present work to characterize proteins. Instead of returning an optimal subset of features, this feature selection approach ranks the features from most relevant to least relevant and removes the least relevant features.

### 2.3 Support Vector Machine

Support vector machine (SVM) [35] is a popular machine learning technique based on structural risk minimization for pattern classification. The basic idea of SVM can be described briefly as follows.

Given a series of training vectors  $\mathbf{x}_i \in \mathbf{R}^d$  ( $i = 1, 2, \dots, n$ ) in two classes with corresponding labels  $y_i \in \{+1, -1\}$  ( $i = 1, 2, \dots, n$ ), here +1 and -1 are used to stand for the two classes, respectively. The goal is to construct a binary classifier or derive a decision function from the available training samples which has a small probability of misclassifying a future sample. SVM performs a mapping of the training vectors  $\mathbf{x}_i$  ( $i = 1, 2, \dots, n$ ) from the training space  $\mathbf{R}^d$  into a higher dimensional space  $\mathbf{H}$  by a kernel function  $K(\mathbf{x}_i, \mathbf{x}_j)$  and finds an optimal separating hyperplane (OSH), which maximizes the margin between the hyperplane and the nearest data points of each class in the space  $\mathbf{H}$ . Training a SVM is equivalent to resolving the following convex quadratic optimization problem:

$$\text{Min : } \frac{1}{2} \sum_{i=1}^n \sum_{j=1}^n \alpha_i \alpha_j y_i y_j K(\mathbf{x}_i, \mathbf{x}_j) - \sum_{i=1}^n \alpha_i \tag{5}$$

$$\text{subject to } \sum_{i=1}^n y_i \alpha_i = 0, \tag{6}$$

$$\text{and } 0 \leq \alpha_i \leq C, \quad i = 1, 2, \dots, n. \tag{7}$$

where  $n$  is the number of training samples,  $C$  is the regularization parameter used to decide the trade-off between training error and the margin, and  $\alpha_i$  ( $i = 1, 2, \dots, n$ ) are the coefficients. The decision function is

$$\text{sgn}(\sum_{i=1}^n y_i \alpha_i K(\mathbf{x}_i, \mathbf{x}) + b). \tag{8}$$

Two popular kernel functions are defined by

$$K(\mathbf{x}_i, \mathbf{x}_j) = (\mathbf{x}_i \cdot \mathbf{x}_j + 1)^d. \tag{9}$$

$$K(\mathbf{x}_i, \mathbf{x}_j) = \exp(-\gamma \|\mathbf{x}_i - \mathbf{x}_j\|^2). \tag{10}$$

Equation (9) is the polynomial kernel function with degree  $d$ . Equation (10) is the Radial Basic Function (RBF), where  $\gamma = 1/\sigma$  and  $\sigma$  is called the width of the kernel.

For a given dataset, only the kernel function and the regularization parameter  $C$  are selected to specify one SVM.

Protein subcellular localization prediction is a multiclass classification problem. Here the number of classes is 12. One simple strategy to handle the multiclass classification problem is to convert the multi-classification into a series of binary classifications. For the 12-class classification problem, we constructed 12 SVM classifiers. The  $i$ th SVM is trained with the positive samples in  $i$ th class and negative samples in the other classes. We refer to SVMs trained in this way as 1- $v$ - $r$  (one-versus-rest) SVMs, which classify an unknown sample into the class that corresponds to the SVM with the highest output value. This strategy has been sufficiently justified in some literatures [36,37].

We used the LibSVM library by Chang [38] to develop the classifier of SVMs, which can be downloaded freely from <http://www.csie.ntu.edu.tw/~cjlin/libsvm/> for scientific use.

## 2.4 Performance Measurement

The prediction performance was evaluated by 5-fold cross-validation test. In this test, the training data set of proteins was separated into five balanced sets. Each of these sets contained approximately the same number of proteins. In each round of cross-validation, we used four sets to train the SVMs while one set was set aside for evaluating the method. This procedure was repeated five times, once for each set. The total accuracy (TA), location accuracy (LA), and Matthew's correlation coefficient (MCC) were used to summarize the prediction performance of the present method. They are defined by [9,10]

$$TA = \frac{\sum_{i=1}^k p(i)}{N}. \quad (11)$$

$$LA(i) = \frac{\sum_{i=1}^k \frac{p(i)}{N_i}}{k}. \quad (12)$$

$$MCC(i) = \frac{p(i)n(i) - u(i)o(i)}{\sqrt{(p(i) + u(i))(p(i) + o(i))(n(i) + u(i))(n(i) + o(i))}}. \quad (13)$$

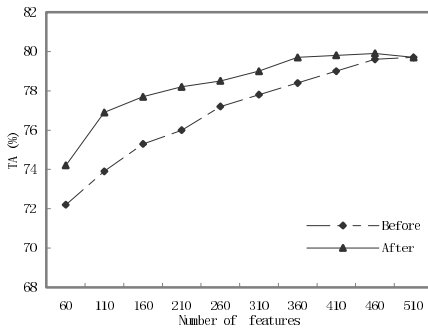
where  $N$  is the total number of proteins in the dataset,  $k$  is the number of subcellular locations,  $N_i$  is the number of proteins in location  $i$ ,  $p(i)$  is the number of correctly predicted proteins in location  $i$ ,  $n(i)$  is the number of correctly predicted proteins not in location  $i$ ,  $u(i)$  is the number of under-predicted proteins and  $o(i)$  is the number of over-predicted proteins. To assess the prediction reliability, a Reliability Index (RI) is usually assigned according to the difference between the highest and the second-highest output value of the SVMs in multiclass classification [9], which is a useful

indication of the level of confidence in the prediction of a protein. The assignment of RI is not performed in this study.

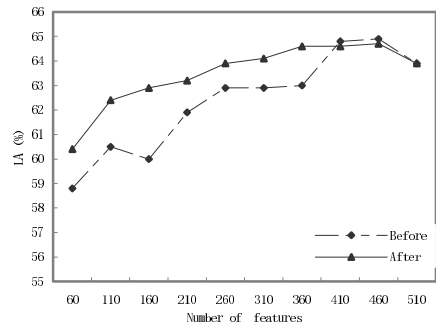
### 3 Results and Discussion

#### 3.1 Results

The prediction performance based on different subsets of features was evaluated by SVMs. In this paper, RBF kernel with parameters  $C = 100$  and  $\gamma = 60$  was used to train the SVMs. The RBF kernel has been investigated in other domains and achieved good performance. Feature selection was done according to a backward elimination procedure. In this work, backward elimination started with the complete set of 510 ranked features. For the limitation of computational power, we removed 50 features each time from the current set of features. Features with the least relevance score were removed first. The total accuracy (TA) and location accuracy (LA) were calculated by 5-fold cross-validation performed on the dataset. The dependency relationship of TA and LA with the number of features before and after feature selection is shown in Figure 1 and Figure 2, respectively. Figure 1 demonstrates that our approach select features with the highest scores that achieve better performance when compared with the use of the same number of features before feature selection. Figure 2 indicates LA changes smoothly after feature selection, whereas it changes sharply before feature selection.



**Fig. 1.** The dependency relationship of TA with the number of features before and after feature subset selection



**Fig. 2.** The dependency relationship of LA with the number of features before and after feature subset selection

The prediction accuracy for each subcellular location based on the 510 features and a subset of 460 features are shown in Table 3. The TA and LA were calculated to measure the prediction performance of the present method. The prediction accuracy and MCC for each location were also calculated to measure the performance of each classifier. From Table 3 we know that the TA and LA based on the selected 460 features were 79.9% and 64.7%, respectively, higher than 79.7% and 63.9% based on



all 510 features. The results indicate that our method improves the prediction performance by selecting relevant features.

**Table 3.** Prediction performance for the 12 subcellular locations based on all 510 feature and the selected 460 features

| Location              | 510 features |      | 460 features |      |
|-----------------------|--------------|------|--------------|------|
|                       | Accuracy (%) | MCC  | Accuracy (%) | MCC  |
| Chloroplast           | 76.8         | 0.75 | 77.9         | 0.75 |
| Cytoplasmic           | 73.8         | 0.66 | 73.5         | 0.66 |
| Cytoskeleton          | 70.0         | 0.81 | 70.0         | 0.81 |
| Endoplasmic reticulum | 57.9         | 0.70 | 58.8         | 0.68 |
| Extracellular         | 82.5         | 0.80 | 82.0         | 0.81 |
| Golgi apparatus       | 31.9         | 0.50 | 34.0         | 0.46 |
| Lysosomal             | 67.7         | 0.73 | 68.8         | 0.72 |
| Mitochondrial         | 55.4         | 0.58 | 56.4         | 0.58 |
| Nuclear               | 89.5         | 0.75 | 89.5         | 0.76 |
| Peroxisomal           | 31.2         | 0.44 | 34.4         | 0.44 |
| Plasma membrane       | 91.5         | 0.91 | 91.9         | 0.91 |
| Vacuolar              | 38.9         | 0.54 | 38.9         | 0.56 |
| TA                    | 79.7         | —    | 79.9         | —    |
| LA                    | 63.9         | —    | 64.7         | —    |

### 3.2 Comparison with Previous Methods

In order to examine the performance of our method, we made comparison with the method by Park and Kanehisa [10]. They also used SVMs to evaluate the prediction performance of their method on the same dataset. The comparison results are shown in Table 4. Although the size of the dataset was small (7579 versus 7589 entries), our method improved the LA dramatically, from 57.9% to 64.7%, and improved the TA

**Table 4.** Performance comparison of our method with Park and Kanehisa [10] by 5-fold cross-validation test

| Location              | Park and Kanehisa | Our work     |
|-----------------------|-------------------|--------------|
|                       | Accuracy (%)      | Accuracy (%) |
| Chloroplast           | 72.3              | 77.9         |
| Cytoplasmic           | 72.2              | 73.5         |
| Cytoskeleton          | 58.5              | 70.0         |
| Endoplasmic reticulum | 46.5              | 58.8         |
| Extracellular         | 78.0              | 82.0         |
| Golgi apparatus       | 14.6              | 34.0         |
| Lysosomal             | 61.8              | 68.8         |
| Mitochondrial         | 57.4              | 56.4         |
| Nuclear               | 89.6              | 89.5         |
| Peroxisomal           | 25.2              | 34.4         |
| Plasma membrane       | 92.2              | 91.9         |

|          |      |      |
|----------|------|------|
| Vacuolar | 25.0 | 38.9 |
| TA       | 78.2 | 79.9 |
| LA       | 57.9 | 64.7 |

to some extent, from 78.2% to 79.9%. The results in Table 4 indicate that our method outperforms their method particularly for some small groups, such as cytoskeleton (58.5% versus 70.0%), endoplasmic reticulum (46.5% versus 58.8%), golgi apparatus (14.6% versus 34.0%), peroxisomal (25.2% versus 34.4%) and vacuolar (25.0% versus 38.9%). In contrast, their method excels our method for some large groups, the examples are nuclear (89.6% versus 89.5%) and plasma membrane (92.2% versus 91.9%).

## 4 Conclusion

In this paper, a feature ranking based feature subset selection approach is proposed for the prediction of protein subcellular localization in the context of SVMs. High prediction performance has been achieved in a 5-fold cross-validation test performed on a freely available protein dataset. This demonstrates the effectiveness of the present method. One potential benefit of feature selection is that it might improve the prediction performance of a predictor. Another is that it might also provide us with some biologically useful knowledge. It is especially important when the prediction models are not transparent to biologists, such as the SVMs. It is anticipated that the proposed method will be a powerful tool for large-scale annotation of biological data in post-genome era.

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# Fuzzy $k$ -Nearest Neighbor Method for Protein Secondary Structure Prediction and Its Parallel Implementation

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**Abstract.** Fuzzy  $k$ -nearest neighbor method is a generalization of nearest neighbor method, the simplest algorithm for pattern classification. One of the important areas for application of the pattern classification is the protein secondary structure prediction, an important topic in the field of bioinformatics. In this work, we develop a parallel algorithm for protein secondary structure prediction, based on the fuzzy  $k$ -nearest neighbor method, that uses evolutionary profile obtained from PSI-BLAST (Position Specific Iterative Basic Local Sequence Alignment Tool) as the feature vectors.

## 1 Introduction

Although the prediction of the three-dimensional structure of a protein from its amino acid sequence is one of the most important problems in bioinformatics [1,2,3,4], *ab initio* prediction of the tertiary structures based solely on sequence information has not been successful so far. For this reason, lots of research efforts have been made for the determination of the protein secondary structure [5,6,7,8,9,10,11,12,13,14,15,16], which can serve as an intermediate step toward determining its tertiary structure.

The most common definition of the secondary structure is based on Dictionary of Secondary Structure of Proteins (DSSP) [17] where the secondary structure is classified as eight states. By grouping these eight states into three classes Coil (C), Helix (H), and Extended (E), one obtains three state classification, which is more widely used. Therefore, the protein secondary structure prediction is a typical pattern classification problem, where one of the three possible states is assigned to each residue of the query protein.

The first step for solving such a problem is the feature extraction, where the important features of the data are extracted and expressed as a set of numbers, called feature vectors. The performance of the pattern classifier depends crucially on the judicious choice of the feature vectors. It has been shown that constructing feature vectors from the evolutionary profile obtained from PSI-BLAST (Position Specific Iterative Basic Local Alignment Search Tool) [18], a bioinformatics tool for the search of homologous protein sequences, gives better prediction results than other choices [6,16] (see Sect. 2.1).

Once an appropriate feature vector has been chosen, a classification algorithm is used to partition the feature space into disjoint regions with decision boundaries. The decision boundaries are determined using feature vectors of a reference sample with known classes, which are also called the reference dataset or training set. The class of a query data is then assigned depending on the region it belongs to. Various pattern classification algorithms such as artificial neural network or support vector machine have been used for the protein secondary structure prediction.

The  $k$ -nearest neighbor method is the simplest algorithm for the pattern classification. Moreover, it can be easily adapted for parallel computation. Although the  $k$ -nearest neighbor method has been used for the secondary structure prediction [11,12,14,15], the fuzzy variant of the algorithm [19] has never been used for the secondary structure prediction, although it has been used for the solvent accessibility prediction [20].

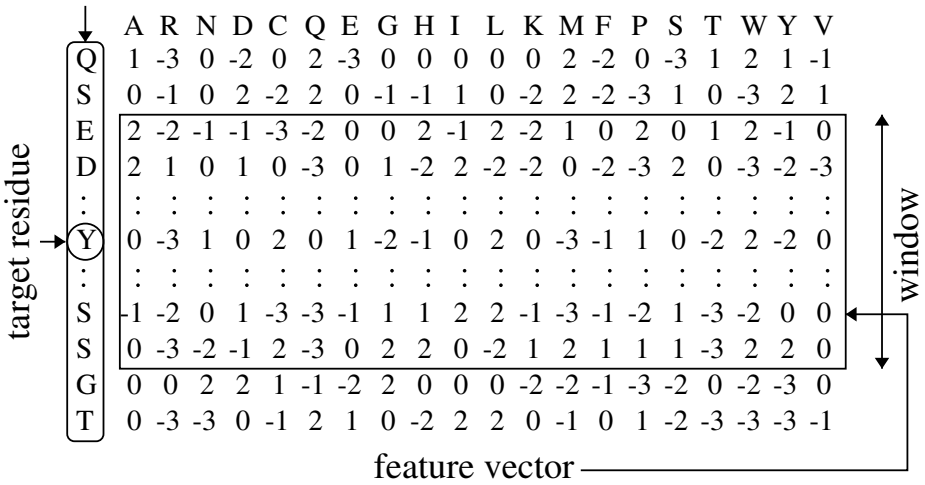
In this work, we develop a parallel algorithm for the protein secondary structure prediction, based on the fuzzy  $k$ -nearest neighbor method [19], where PSI-BLAST profiles are used as the feature vectors. As a test of our algorithm, we perform a benchmark test on EVA common set 1 consisting of 60 proteins [22].

## 2 Methods

### 2.1 The Feature Vectors

In order to construct the feature vector for a protein residue, we first perform database search with PSI-BLAST [18]. PSI-BLAST then calculates the rate of substitution of each residue of the query protein to another amino acids. By multiplying appropriate normalization factors, taking logarithms, and rounding off to integer values, these numbers are converted to what is called the position specific scoring matrix, also called profile, a matrix of the size (protein length)  $\times$  20. This PSI-BLAST profile contains evolutionary information that cannot be obtained from the raw sequence only. For a protein residue whose secondary structure is to be predicted, one takes a window of size  $N_w$  centered around this residue, and uses the matrix of size  $N_w \times 20$  as the feature vector to be input into the pattern classification algorithm (see Fig. 1). We use  $N_w = 15$  in this work. The resulting feature vector is a  $15 \times 20 = 300$  dimensional matrix. This feature vector is the same as the one used in previous works [6,16] based on other pattern classification methods.

protein sequence



**Fig. 1.** The relation between PSI-BLAST profile and the feature vector of a residue. The feature vector corresponding to a target residue is constructed from the PSI-BLAST profile by considering a window of finite size (15 residues in this work) centered on the residue.

2.2 The Distance Measure

There are various ways of defining the distance between two feature vectors A and B, but in this work we use three methods, Euclidean, Cosine, and Correlation distances, defined as

$$D_{AB}(Euc) = \sum_{i=1}^{N_w} w_i \sum_j (P_{ij}(A) - P_{ij}(B))^2, \tag{1}$$

$$D_{AB}(Cos) = 1 - \sum_{i=1}^{N_w} w_i \frac{\sum_j P_{ij}(A) \cdot P_{ij}(B)}{\sqrt{\sum_p P_{ip}(A)^2 \sum_q P_{iq}(B)^2}}, \tag{2}$$

$$D_{AB}(Corr) = 1 - \sum_{i=1}^{N_w} w_i \frac{\sum_j (P_{ij}(A) - \bar{P}_i(A)) \cdot (P_{ij}(B) - \bar{P}_i(B))}{\sqrt{\sum_p (P_{ip}(A) - \bar{P}_i(A))^2 \sum_q (P_{iq}(B) - \bar{P}_i(B))^2}}, \tag{3}$$

respectively, where  $P_{ij}(A) (i = 1, 2, \dots, 15; j = 1, 2, \dots, 20)$  is a component of the feature vector A,  $w_i$  a weight parameter, and

$$\bar{P}_i(A) \equiv \frac{1}{20} \sum_{j=1}^{20} P_{ij}(A).$$

Since we expect the profile elements for residues nearer to the target residue to be more important in determining the local environment of the target residue, we use weights  $w_i = (8 - |8 - i|)^2$ .

### 2.3 The Reference Dataset

In order to construct the reference dataset consists of representative protein chains without bias, we utilize the ASTRAL SCOP database, where the protein chains are hierarchically classified into structural families, and representative proteins are selected for each of them. In particular, we used ASTRAL SCOP (version 1.63) chain-select-95 subset and chain-select-90 subset [21]. We then clustered these sequences with BLASTCLUST (NCBI BLAST 2.2.5, <http://www.ncbi.nlm.nih.gov/BLAST/>) and selected the representative chain for each cluster, in order to remove additional homologies. The resulting reference dataset consists of 4362 non-redundant proteins (905684 feature vectors) that have less than 25% sequence identity with each other.

### 2.4 Fuzzy $k$ -Nearest Neighbor Method

In the simplest version of the fuzzy  $k$ -nearest neighbor (FKNN) method [19], the fuzzy class membership  $u_s(\mathbf{x})$  to the class  $s$  is assigned to the query data  $\mathbf{x}$  according to the following equation:

$$u_s(\mathbf{x}) = \frac{\sum_{sec(j)=s} D_j^{-2/(m-1)}}{\sum_{j=1}^k D_j^{-2/(m-1)}} \quad (4)$$

where the summation of  $j$  in the numerator is restricted to those belonging to the class  $s$ ,  $m$  is a fuzzy strength parameter, which determines how heavily the distance is weighted when calculating each neighbor's contribution to the membership value,  $k$  is the number of nearest neighbors, and  $c$  is the number of classes, and  $D_j$  is the distance between the feature vector of the query data  $\mathbf{x}$  and the feature vector of its  $j$ -th nearest reference data  $\mathbf{x}(j)$ .

The advantage of the fuzzy  $k$ -nearest neighbor algorithm over the standard  $k$ -nearest neighbor method is quite clear. The fuzzy class membership  $u_s(x)$  can be considered as the estimate of the probability that the query data belongs to class  $i$ , and provides us with more information than a definite prediction of the class for the query data. Moreover, the reference samples which are closer to the query data are given more weights, and an optimal value of  $m$  can be chosen along with that for  $k$ , in contrast to the standard  $k$ -nearest neighbor method with fixed value of  $2/(m-1) = 0$ . In fact, the optimal value of  $k$  and  $m$  are found from the leave-one-out cross-validation procedure (see below), and the resulting value for  $2/(m-1)$  is indeed nonzero.

The optimal values of  $k$  and  $m$  were determined by leave-one-out cross validation test, where the prediction was performed for one of the chains in the reference dataset, using the remaining 4361 chains as the reference dataset, procedure being repeated for each of the 4362 chains. The optimal values of  $k$  and



$m$  are determined as the ones yielding the maximum average value of  $Q_3$  score, which is define as:

$$Q_3 \equiv 100\% \times \frac{N_{corr}}{N} \quad (5)$$

with  $N$  and  $N_{corr}$  being the total number of residues of the query protein, and the total number of correctly predicted residues, respectively.

The optimal value of  $m$  turns out to be 1.29, and that of  $k$  is 85 when using Euclidean and Correlation distances, and 70 when using Cosine.

## 2.5 The Parallel Implementation

The FKNN method can be easily adapted for parallel computation. In the parallel implementation, the computational load is shared between computational nodes, resulting in drastic increase in computational speed. The advantage of the parallel program in terms of computational time can also be seen from Fig. 2 (see Results and Discussions). To elaborate on the parallel algorithm, each of the nodes is assigned a distinct subset of the feature vectors in the reference dataset, and each member of this set is compared with query vector, and  $k_{nn}$  of them with the smallest distance from the query vector are chosen. The numbers of the feature vectors assigned to the nodes are all equal up to roundoff error, so that the loads are balanced. The 0-th node, which we call the master, performs the job of collecting  $k_{nn}$  candidates of nearest neighbors from each of the nodes. It then sorts these  $N_{nodes} \times k_{nn}$  indices with respect to the distance  $D$  to select the final  $k_{nn}$  nearest neighbors. The master then produces the final output. The pseudo-code for the parallel algorithm is given in algorithm 1., along with the sub-algorithms 2., 3., and 4..

---

**Algorithm 1.** parallel FKNN algorithm for the protein secondary structure prediction

---

- 1:  $k_{nn}$  = Number of nearest neighbors (constant)
  - 2:  $N_{nodes}$  = Total number of computing nodes
  - 3:  $Rank$  = The number of this node, a number between 0 and  $N_{nodes} - 1$
  - 4: Construct the feature vector for each residue of the query protein {algorithm2.}
  - 5: Construct the feature vector for each residue in the database {algorithm3.}
  - 6:  $st = Rank * N_f / N_{nodes} + 1$
  - 7:  $ed = (Rank + 1) * N_f / N_{nodes}$  { $st$  and  $ed$  is the starting and ending number of feature vectors the current node will look into. This is to divide computational load between nodes.}
  - 8: **for**  $j_q = 1$  to  $L_q$  **do**
  - 9:   Calculate the probabilities  $prob(j_q, s)$  of the residue  $q$  being in each of the conformational state  $s$  (=C,H,E) {algorithm4.}
  - 10:   The predicted secondary structure  $S(j_q) = (s \text{ that maximizes } prob(j_q, s))$
  - 11:   print out  $j_q$ ,  $S(j_q)$ , and  $prob(j_q, s)$  ( $s = C,H,E$ )
  - 12: **end for**
-

**Algorithm 2.** Constructing feature vectors for each residue of the query protein

---

```

Read in query profile
 $L_q =$ Length of the query sequence
for $j_q = 1$ to L_q do
 Construct matrix $\mathbf{P}_q(j_q)$ of size 15×20 , centered around the residue j_q , from the
 query profile
end for

```

---

**Algorithm 3.** Constructing feature vectors for each residue in the database

---

```

 $N_f = 0$ { N_f will be the total number of feature vectors in the reference dataset,
equal to the total number of residues in the dataset}
 $N_p =$ Number of protein chains in the reference dataset
Read in profiles in the reference dataset (database profiles)
for $i = 1$ to N_p do
 $L(i) =$ Length of the i -th protein chain
 for $j = 1$ to $L(i)$ do
 $N_f \leftarrow N_f + 1$
 Construct matrix $\mathbf{P}_{DB}(N_f)$ of size 15×20 , centered around the residue j of the
 i -th protein, from the database profile
 end for
end for

```

---

### 3 Results and Discussions

The benchmark test was performed on EVA common set 1 consisting of 60 proteins [22] and RS126 set consisting of 126 non-homologous protein [5], with the optimal values of  $m$  and  $k$  determined by the leave-one-out cross-validation on the reference dataset derived from ASTRAL SCOP (see Methods). The performance on EVA common set 1 was compared with three neural network based prediction methods, PSIPRED (v2.3) [6], PROFking (v1.0) [7], and SABLE (v2.0) [8], and the performance on RS126 set was compared with two methods based on support Vector Machine (SVM), SVM freq [9] and SVMpsi [10].

In addition to  $Q_3$  score (see section 2.4), two additional performance scores, SOV score [23] and three state correlation coefficient (Corr(3)) [24], are used for the assessment of performance. The average values and the standard errors of these scores for the performance on EVA common set 1, of the fuzzy  $k$ -nearest method with various distance measures, and the other three methods, are displayed in Table 1. The results of the test on RS126 set are shown on Table 2.

We see that in both of these test, the performance is best when the Correlation distance measure is used. We see that in the first test, average performance scores are lower than those of PSIPRED and SABLE, but higher than PROFking. However, considering the magnitudes of the standard error, these differences are not drastic, and we may say that the performances are more or less comparable to other methods. Also, the actual performances of the prediction algorithms depend on their versions and the set of proteins used for the test, and it should

---

**Algorithm 4.** Calculating the fuzzy membership of a query residue to each of the secondary structural class

---

```

for $s = C, H, E$ do
 membership(j_q, s) = 0
end for
for $m_{DB} = st$ to ed do
 $D(j_q, m_{DB}) =$ Distance between $\mathbf{P}_q(j_q)$ and $\mathbf{P}_{DB}(m_{DB})$
end for
Sort indices of the feature vectors the current node is examining, with respect to
 $D(j_q, m_{DB})$, in descending order.
if $Rank == 0$ then {This node is the master, so collect the results and re-sorts
them, and print the final output}
 indx() \Leftarrow save indices of k_{nn} nearest neighbors among the feature vectors exam-
ined by the master
 dscore() \Leftarrow save distances of k_{nn} nearest neighbors among the feature vectors
examined by the master
 for $i = 1$ to $N_{nodes} - 1$ do
 Receive indices and distances of k_{nn} nearest neighbors among the feature vectors
 examined by the i -th node
 indx() \Leftarrow add indices of k_{nn} nearest neighbors among the feature vectors ex-
 amined by the i -th node
 dscore() \Leftarrow add distances of k_{nn} nearest neighbors among the feature vectors
 examined by the i -th node
 end for
else
 Send indices and distances of k_{nn} nearest neighbors among the feature vectors
 examined by the i -th node to the master
end if
if $Rank == 0$ then
 Sort indices with respect to dscore() {The collection consists of $N_{nodes} \times k_{nn}$
 results, so master must sort them again to select k_{nn} nearest neighbors}
 for $j_{DB} = 1, k_{nn}$ do {Calculate the fuzzy membership from k_{nn} nearest neigh-
 bors}
 $s(j_{DB}) =$ secondary structural class corresponding to the j_{DB} -th feature vector

 membership($j_q, s(j_{DB})$) \Leftarrow membership($j_q, s(j_{DB})$) + fuzzy membership calcu-
 lated from $D(j_q, j_{DB})$
 end for
 for $s = C, H, E$ do
 prob(j_q, s) = membership(j_q, s) / $\sum_{s' \in \{C, H, E\}}$ membership(j_q, s')
 end for
end if

```

---

be emphasized that the result is not to be considered as an extensive test of these methods.

Since the programs based on SVM are not available for public use, we quote the values from the literature [9,10]. The values of performance measures not

**Table 1.** Average scores of secondary structure prediction on EVA common set 1, using fuzzy  $k$ -nearest neighbor (FKNN) method with Euclidean (Euclid), Cosine (Cos), and Correlation (Corr) distance measures. The average scores are given also for three other methods for comparison. The numbers in the parentheses are the standard errors.

|              | Q3         | SOV        | Corr(3)       |
|--------------|------------|------------|---------------|
| FKNN(Euclid) | 70.9 (1.8) | 64.5 (2.3) | 0.495 (0.024) |
| FKNN(Cos)    | 70.9 (1.8) | 64.5 (2.3) | 0.499 (0.034) |
| FKNN(Corr)   | 71.8 (1.9) | 67.9 (2.4) | 0.527 (0.026) |
| PSIPRED      | 75.1 (1.8) | 75.3 (2.4) | 0.557 (0.024) |
| PROFking     | 67.2 (2.3) | 64.3 (2.8) | 0.463 (0.029) |
| SABLE        | 75.6 (1.5) | 73.1 (2.5) | 0.532 (0.029) |

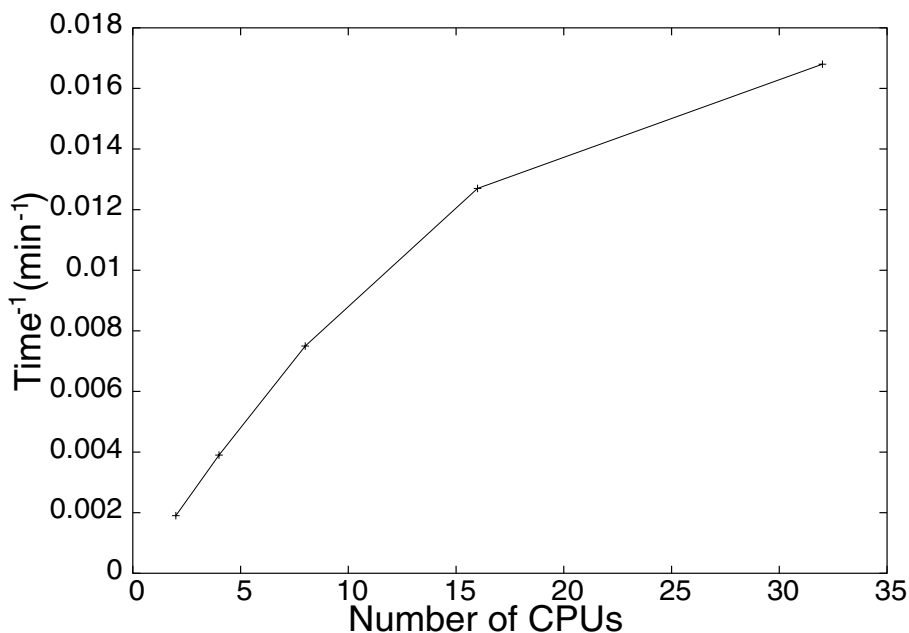
**Table 2.** Average scores of secondary structure prediction on RS126 set, using fuzzy  $k$ -nearest neighbor (FKNN) method with Euclidean (Euclid), Cosine (Cos), and Correlation (Corr) distance measures. The average scores are given also for two other methods based on SVM, for comparison.

|              | Q3   | SOV  | Corr(3) |
|--------------|------|------|---------|
| FKNN(Euclid) | 88.6 | 83.1 | 0.791   |
| FKNN(Cos)    | 88.6 | 83.1 | 0.744   |
| FKNN(Corr)   | 89.0 | 84.0 | 0.796   |
| SVMfreq      | 75.1 | -    | -       |
| SVMpsi       | 76.1 | 72.0 | -       |

reported in the references are omitted. We see that the fuzzy  $k$ -nearest neighbor method also shows good performance when compared with SVM-based methods.

The parallel code was implemented in mpi C, and run on 32 Intel Xeon processors. For 60 proteins in the EVA set, for the Euclidean, cosine, and correlation distance measures, respectively, the calculation took 47, 58, and 60 minutes of wall clock time, defined as the time elapsed between the start and end of the program.

The advantage of the parallel algorithm we introduced in this work is that the communication between computational nodes are kept to a minimal level. In fact, the most of the computations are performed by each of the nodes independently, and the communication occurs only at the end of such computations, and only between the king and slaves, when the master collects the results from the slaves and sorts them again to predict the secondary structure. In order to examine the parallel efficiency, we repeated the computation for EVA common set 1 using the correlation distance measure for different number of CPUs in order to obtain the response curve in Fig. 2. In the figure, the inverse of the time is plotted against the number of CPUs involved in the computation, in order to show the dependence of the computational speed on the number of CPUs. The result shows that, although the dependence is not exactly linear, the scalability is reasonably good, demonstrating the advantage of parallel computation over serial version.



**Fig. 2.** The inverse of wall time in  $\text{min}^{-1}$  (*vertical axis*) plotted against the number of CPUs used for the computation (*horizontal axis*). The curve shows excellent scalability of the parallel FKNN algorithm, due to minimal amount of communication between CPUs.

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# Gene Selection Based on Mutual Information for the Classification of Multi-class Cancer

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**Abstract.** With the development of microarray technology, microarray data are widely used in the diagnoses of cancer subtypes. However, people are still facing the complicated problem of accurate diagnosis of cancer subtypes. Building classifiers based on the selected key genes from microarray data is a promising approach for the development of microarray technology; yet the selection of non-redundant but relevant genes is complicated. The selected genes should be small enough to allow diagnosis even in regular laboratories and ideally identify genes involved in cancer-specific regulatory pathways. Instead of the traditional gene selection methods used for the classification of two categories of cancers, in the present paper, a novel gene selection algorithm based on mutual information is proposed for the classification of multi-class cancer using microarray data, and the selected key genes are fed into the classifier to classify the cancer subtypes. In our algorithm, mutual information is employed to select key genes related with class distinction. The application on the breast cancer data suggests that the present algorithm can identify the key genes to the BRCA1 mutations/BRCA2 mutations/the sporadic mutations class distinction since the result of our proposed algorithm is promising, because our method can perform the classification of the three types of breast cancer effectively and efficiently. And two more microarray datasets, leukemia and ovarian cancer data, are also employed to validate the performance of our method. The performances of these applications demonstrate the high quality of our method. Based on the present work, our method can be widely used to discriminate different cancer subtypes, which will contribute to the development of technology for the recovery of the cancer.

## 1 Introduction

Microarray technology, a recent development in experimental molecular biology, provides biomedical researchers the ability to measure expression levels of thousands of genes simultaneously. Such gene expression profiles are used to understand the

molecular variations among disease related cellular processes, and also to help the increasing development of diagnostic tools and classification platforms in the cancer research.

With the development of the microarray technology, the necessary processing and analysis methods grow increasingly critical. It becomes gradually urgent and challenging to explore the appropriate approaches because of the large scale of microarray data comprised of the large number of genes compared to the small number of samples in a specific experiment. For the data obtained in a typical experiment, only some of genes are useful to differentiate samples among different classes, but many other genes are irrelevant to the classification. Those irrelevant genes not only introduce some unnecessary noise to gene expression data analysis, but also increase the dimensionality of the gene expression matrix, which results in the increase of the computational complexity in various consequent researches such as classification and clustering. As a consequence, it is significant to eliminate those irrelevant genes and identify the informative genes, which is a feature selection problem crucial in gene expression data analysis [1, 2].

In the present paper, we propose a novel gene selection method based on the mutual information for the multi-class cancer classification using microarray data. Our method firstly calculates the mutual information (MI) between the discretized gene expression profiles and the cancer class label vector for all the samples. Then, the genes are ranked according to the calculated MI. These selected genes with high ranks are fed into the nearest neighbor method.

The rest of the present paper is organized as follows. In section 2, we first introduce the method to discretize the gene expression data, and then we in detail formulate the principle of GSMI. Section 3 describes the test statistics. And Section 4 describes the experiment. In Section 5, GSMI is applied to analyze the breast cancer dataset. Section 6 contains the conclusions.

## 2 Methods

Among the many thousands of genes simultaneously measured in a specific microarray experiment, it is impossible that all of their expressions are related to a particular partition of the samples. In the analysis of a biological system, the following ‘rules of thumb’ regarding gene functions are often assumed. 1) A gene can be in either the ‘on’ or ‘off’ state; 2) not all genes simultaneously respond to a single physiological event; 3) gene functions are highly redundant [3]. According to these assumptions, we consider the genes as random variables with two values, in which 1 denotes the ‘on’ state and 0 denotes the ‘off’ state. As a consequence, the gene expression data can be discretized into two states 0 and 1, respectively. The discretization of the gene expression data will be formulated later in Section 3.

Assume that a microarray dataset can be represented as a  $G \times S$  matrix  $A$  with generic element  $a_{gs}$  representing the expression level of the gene,  $g$  in sample,  $s$ . All the samples are divided into  $n$  categories, and with the class label denoted by  $C$  with its element  $a_{gs}$  standing for the class of  $i$ th sample. From the biological point of view, those genes, having higher mutual agreement with class label of the cancer microarray



data, contribute more significantly on the classification of the cancer subtypes. Consequently, these genes should be selected as the key genes and used to the sequent classification and clustering. According to the information theory, mutual information can be used to measure the mutual agreement between two object models. We then employ the mutual information to rank every gene according to mutual information between the gene and the class label of the cancer microarray data.

Based on the information-theoretic principle of mutual information, the mutual information of two random variables  $X$  and  $h_i = w_i / \sum w_i$  with a joint probability mass function  $p(x, y)$  and marginal probability mass functions  $p(x)$  and  $p(y)$  is defined as [4]:

$$I(X;Y) = \sum_{x_i, y_j} p(x_i, y_j) \log \frac{p(x_i, y_j)}{p(x_i)p(y_j)} . \tag{1}$$

Let us suppose that the domain of  $G_i, i \in \{1, \dots, G\}$ , is discretized into two intervals. After discretization, the domains of all the genes can be represented by  $dom(G_i) = \{v_{ik}, k = 1, 2\}$  where  $v_{i1=0}$  and  $v_{i2=0}$ . Denoted by  $\sigma$  the SELECT operation from relational algebra and  $|S|$  denote the cardinality of set  $S$  [8]. The probability of a gene in microarray data having  $G_i = v_{ik}, i \in \{1, \dots, G\}, k \in \{1, 2\}$  is then given by:

$$P(G_i = v_{ik}) = \frac{|\sigma_{G_i=v_{ik}}(A)|}{|\sigma_{G_i \neq \Phi}(A)|} . \tag{2}$$

And the joint probability of the gene in the gene expression data has  $G_i = v_{ik}$  and the class label  $C = c_i, i \in \{1, \dots, n\}$  is calculated by:

$$P(G_i = v_{ik} \wedge C = c_i) = \frac{|\sigma_{G_i=v_{ik} \wedge C=c_i}(A)|}{|\sigma_{G_i \neq NULL}(A)|} . \tag{3}$$

**Definition 1.** The interdependence measure  $I$  between the gene and the class label,  $G_i$  and  $C, i \in \{1, \dots, G\}$ , is defined as:

$$I(G_i : C) = \sum_{k=1}^2 \sum_{l=1}^n P(G_i = v_{ik} \wedge C = c_i) \log \frac{P(G_i = v_{ik} \wedge C = c_i)}{P(G_i = v_{ik})P(C = c_i)} . \tag{4}$$

$I(G_i : C)$  measures the average reduction in uncertainty about  $G_i$  that results from learning the value of  $C$  [9]. If  $I(G_i : C) > I(G_j : C), i, j \in \{1, \dots, G\}, i \neq j$ , the dependence of  $G_i$  and the class label  $C$  is greater than the dependence of  $G_j$  and  $C$ . Before ranking the genes according to the mutual information, the redundancy in the microarray should be decreased because of the fundamental principle of microarray technology. Due to the principle of micorarray technology, the gene expression matrix contains high redundancy since some genes are measured more than once.

**Definition 2.** The mutual information matrix of the microarray, named as  $M$  with its element  $m_{ij}$ , is given by:

$$m_{ij} = \sum_{k=1}^2 \sum_{l=1}^2 P(G_i = v_{ik} \wedge G_j = v_{jl}) \log \frac{P(G_i = v_{ik} \wedge G_j = v_{jl})}{P(G_i = v_{ik})P(G_j = v_{jl})}. \quad (5)$$

For simplicity, the mutual information matrix  $M$  is normalized to  $M^*$  with its element  $m_{ij}^*$  given as follows,

$$m_{ij}^* = \frac{m_{ij}}{H(G_i, G_j)} \quad (6)$$

where the joint entropy of the gene  $G_i$  and  $G_j$  is denoted by  $H(G_i, G_j)$ , which is given by:

$$H(G_i, G_j) = - \sum_{k=1}^2 \sum_{l=1}^2 P(G_i = v_{ik} \wedge G_j = v_{jl}) \log P(G_i = v_{ik} \wedge G_j = v_{jl}). \quad (7)$$

The redundancy in the microarray data is reduced by the following method. In the matrix  $M^*$ , the elements on the diagonal are all with the same value 1. These rows without containing the value less than 0.95 are labeled in the normalized mutual information matrix except these elements in the diagonal of the matrix. We then select these genes corresponding to these rows. Due to the error in the process of computing the mutual information, the cutoff value is set to 0.95 so that the redundancy can be reduced as much as possible. Otherwise, if the cutoff value is set to 1, the redundancy cannot be reduced to the expected extent.

After selecting the genes with little redundancy, if any, the selected genes (SGS) are ranked according to the interdependence measure  $I$  between the gene expression profiles and the class label. Then the SGS are used to train the RBF neural network to classify the cancer subtypes in the designed experiment formulated in the next section.

### 3 Test Statistics

A general statistical model for gene expression values will be firstly introduced followed by several test statistics in this section.

Assume that there are more than two kinds of distinct tumor tissue classes for the problem under consideration and there are  $p$  genes (variables) and  $n$  tumor mRNA samples (observations). After introducing the novel gene selection method, we now turn to some test statistics used for testing the equality of the class means for a fixed gene. The following five parametric test statistics will be considered [10].

#### 3.1 ANOVA F Test Statistics

The definition of this test is given by:

$$F = \frac{(n-k) \sum_i n_i (\bar{Y}_i - \bar{Y}_{..})^2}{(k-1) \sum_i (n_i - 1) s_i^2} \tag{8}$$

where  $\bar{Y}_{.j} = \sum_{i=1}^{n_j} Y_{ij} / n_j$ ,  $\bar{Y}_{..} = \sum_{i=1}^k n_i \bar{Y}_i / n$ , and  $s_i^2 = \sum_{j=1}^{n_i} (Y_{ij} - \bar{Y}_i)^2 / (n_i - 1)$ .

#### 3.2 Brown-Forsythe Test Statistic

Brown-Forsythe Test Statistic [11] is given by:

$$B = \frac{\sum_i n_i (\bar{Y}_i - \bar{Y}_{..})^2}{\sum_i (1 - n_i / n) s_i^2} \tag{9}$$

#### 3.3 Welch Test Statistics

Welch test statistics [12] is defined as

$$W = \frac{\sum_i w_i (\bar{Y}_i - \sum_i h_i \bar{Y}_i)^2}{(k-1) + 2(k-2)(k+1)^{-1} \sum_i (n_i - 1)^{-1} (1 - h_i)^2} \tag{10}$$

with  $w_i = n_i / s_i^2$  and  $h_i = w_i / \sum w_i$ .

## 4 Introduction to the Experiment

To evaluate the performance of GSMI, we applied it to the well-known gene expression data sets: the breast cancer data [5], in which RNA from samples of primary breast tumors from 7 carriers of the BRCA1 mutation, 8 carries of the BRCA2 mutation, and 7 patients with sporadic cases of breast cancer have been hybridized to a cDNA microarray containing 6512 complementary DNA clones of 5361 genes [6]; Leukemia 72 with 6817 genes, 38 ALL-Bcell, 9 ALL-Tcell, and 25 AML, and Ovarian with 7129 genes, 27 epithelial ovarian cancer cases, 5 normal tissues, and 4 malignant epithelial ovarian cell lines [13].

Before calculated the mutual information, the microarray expression level should firstly be preprocessed according to an alternative idea of the Optimal Class-Dependence Discretization Algorithm (OCDD) [11]. OCDD is a new method to convert variables into discrete variables for inductive machine learning, which can thus be employed for pattern classification problems. The discretization process is formulated as an optimization problem, then the normalized mutual information that measures the interdependence between the class labels and the variable to discretized as the objective function, and then iterative dynamic programming is applied to find its optimum [14]. For each continuous gene expression profile in microarray expression matrix  $A$ , its domain is typically discretized into two intervals for gene selection, which are denoted by 0 and 1, respectively. We then use the normalized mutual information measure that reflects interdependence between the class label and the attribute to be discretized as the objective function to find a global optimal solution separating the domain of the gene expression data.

We employ the nearest neighbor method to classify the cancer cases with different cancer subtypes. The leave-one-out cross-validation (LOOCV) is used to evaluate the accuracy of classification.

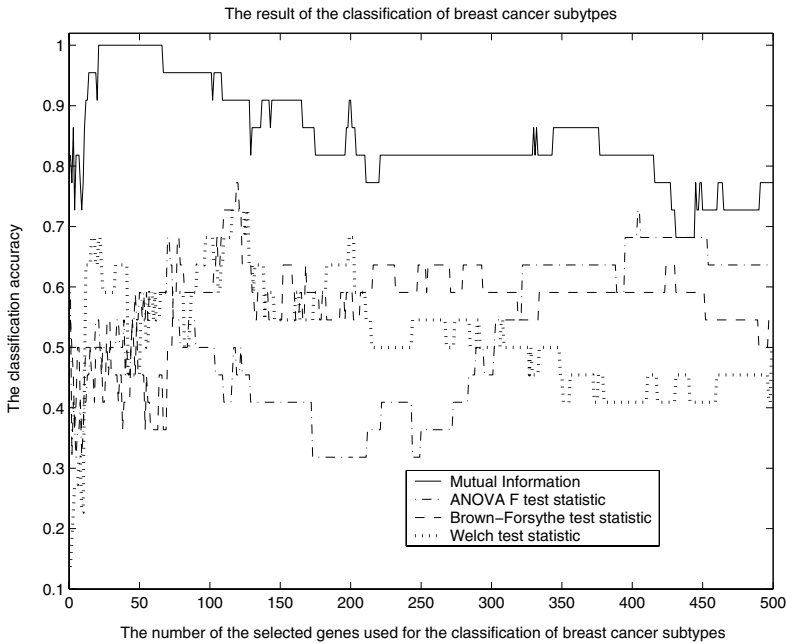
## 5 Experiment Results and Discussion

By using our method, genes are ranked by the mutual information between the genes and the class label. Then, the nearest neighbor classifier is employed as the benchmark to classify the three cancer microarray expression datasets.

In the classification performance evaluation process, we employed LOOCV, which is a widely used method for evaluating the performance of the classification of gene expression data [7].

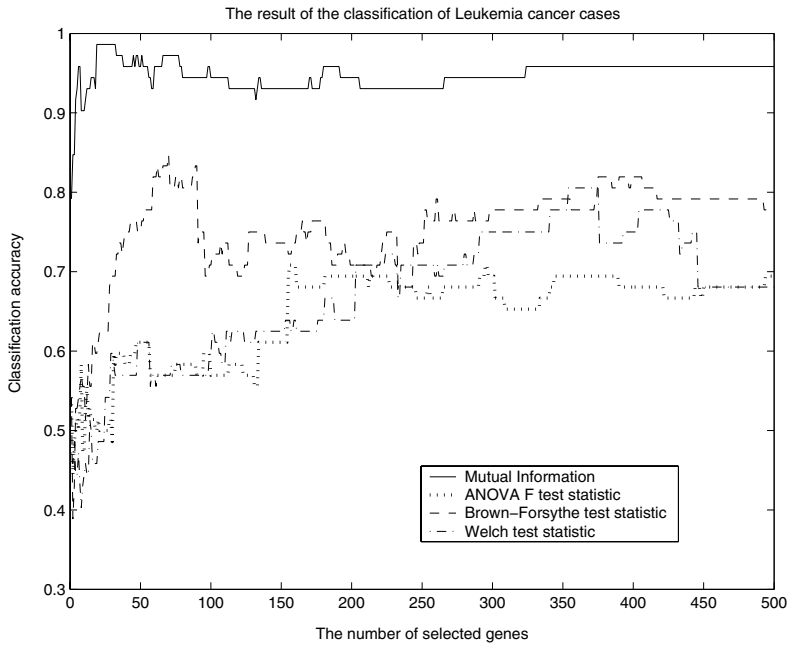
The results of our method on the three datasets are given in Figure 1, Figure 2 and Figure 3, respectively. From figure 1, the classification error rate minimized to 0% when 18 genes are selected according to our method, but the genes selected by all the test statistics used for classification are not as effective as ours since the classification accuracies maximize to 73% at 404 genes for the ANOVA test statistic, 78% at 119 genes for Brown-Forsythe test statistic, 73% at 116 genes for Welch test statistic. From figure 2, the classification error rate minimized to 1.39% when 19 genes are

selected according to our method, but the genes selected by all the test statistics used for classification are not as effective as ours since the classification accuracies maximize to 85% at 70 genes for the Brown-Forsythe test statistic, 71% at 156 genes for ANOVA test statistic, 80.5% at 354 genes for Welch test statistic. From figure 3, the classification error rate minimized to 0% when 21 genes are selected according to our method, but the genes selected by all the test statistics used for classification are not as effective as ours since the classification accuracies maximize to 97.3% at 38 genes for the Welch test statistic, 97.3% at 370 genes for ANOVA test statistic, 94.45% at 105 genes for Brown-Forsythe test statistic.

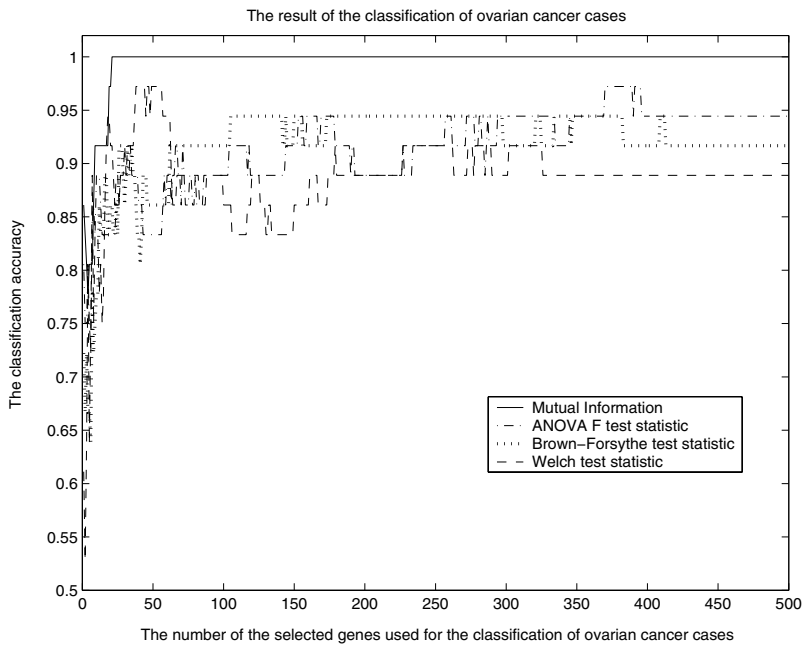


**Fig. 1.** Comparison on the breast cancer cases

Demonstrated by these results, the present method based on the mutual information obviously outperforms the three test statistics. The major reason for the superiority of our method is that mutual information between the genes and the class labels reflects the potential relation and correlation, and thus indicates the discriminability of genes. What's more, there is no assumption about the probability distribution of the microarray data. The three test statistics are based on the default probability distribution, but it is not clear whether microarray data are according to the default probability till now without adequate samples of the cancer cases.



**Fig. 2.** Comparison on the leukemia cancer cases



**Fig. 3.** Comparison on the ovarian cancer cases

## 6 Conclusions

In this paper, contrary to other work managing discriminating one cancer subtype from the other, we present the novel method for the classification of the multi-class cancer subtypes, which will contribute the development of the technology for the research and cure of cancer. In our work, an information theoretic approach is proposed for gene selection algorithm based on the mutual information, which proves promising in the classification of multi-class cancer microarray datasets. The mutual information between the gene expression data and the class label is calculated. And the genes are selected according to the calculated mutual information after removing the redundancy. The successful applications on the breast, as well as ovarian and leukemia cancer datasets prove that our algorithm is effective, robust and appropriate to the classification of the multi-class cancers since it can discovery the informative key genes.

Future work will concentrate on the further research on the method for extracting the key features from gene expression data. And we will try to fully evaluate the performance of the classification by employing SVM and neural network, such as RBF neural network. Furthermore, we will also concentrate on the research of biological significance of the found key genes and try to find the specific feature of the key genes and understand the function of these genes. By doing so, the microarray technology can be fully used.

## Acknowledgement

The authors are grateful to Dechang Chen for sharing the micorarray data sets of breast, ovarian as well as leukemia with us.

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# Gene Selection by Cooperative Competition Clustering

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**Abstract.** Clustering analysis of data from DNA microarray hybridization studies is an essential task for identifying biologically relevant groups of genes. Attribute cluster algorithm (ACA) has provided an attractive way to group and select meaningful genes. However, ACA needs much prior knowledge about the genes to set the number of clusters. In practical applications, if the number of clusters is misspecified, the performance of the ACA will deteriorate rapidly. In fact, it is a very demanding to do that because of our little knowledge. We propose the Cooperative Competition Cluster Algorithm (CCCA) in this paper. In the algorithm, we assume that both cooperation and competition exist simultaneously between clusters in the process of clustering. By using this principle of Cooperative Competition, the number of clusters can be found in the process of clustering. Experimental results on a synthetic and gene expression data are demonstrated. The results show that CCCA can choose the number of clusters automatically and get excellent performance with respect to other competing methods.

## 1 Introduction

In a typical biological system, it is often not clearly known how many genes are sufficient to fully characterize a macroscopic phenotype. However, in practice a working mechanistic hypothesis that is testable and largely captures the biological truth seldom involves more than a few dozens of genes. And knowing the identity of those relevant genes is just as important as finding the grouping of samples they induced [1]. Thus, the selection of the relevant features is key to analyze gene expression microarray data.

So far, several useful approaches have been taken to select the most meaningful genes. One approach is to use a clustering algorithm to group genes into coherent sets and then select representative genes to represent these clusters [3]. This approach only deals with the gene redundancy problem, while it fails to detect non-discriminating genes. Principal component analysis (PCA) may remove non-discriminating genes by restricting attention to so-called eigenfeatures corresponding to the large eigenvalues, but each basis element of the new genes subspace for this method is the linear combination of all the original genes, which make it difficult to identify the important genes[4]. Furthermore, the  $t$ -statistics is widely used to select discriminating genes [5]. It is important to note that the  $t$ -statistics can only be used when the samples are

preclassified and cannot solve the multiclass problem directly. In this paper, we use a two-steps method to select discriminating and meaningful genes, i.e., first using the mutual information between the class label vector and the sample vector to remove most of the non-discriminating genes, then the meaningful genes are selected by using the Cooperative Competition Clustering technique.

Clustering analysis of gene expression microarray data is a key step to understand how the activity of genes varies during biological processes and is affected by disease states and cellular environment. Clustering can be used to group genes according to their expression in a set of samples. There are rich literatures on clustering analysis and various techniques have been developed. Some well-known examples are: k-means algorithm, Attribute Cluster Algorithm [1], Kohonene's self-organizing maps (SOM) [6], and various hierarchical clustering algorithms [7], etc. However, these clustering algorithms need prior knowledge, which is but unknown in practical applications. K-means algorithm, ACA as well as SOM need to in advance know the number of clusters, and hierarchical clustering algorithms need to set a suitable stopping condition. Without prior knowledge, it is hard to find rational results. Recently, some researchers proposed competition clustering algorithm [15] to select cluster model automatically, those algorithms overemphasize the competition and overlook the cooperation between clusters so that some interesting but small cluster will not be found. In this paper, we propose a new clustering algorithm referred to as Cooperative Competition cluster algorithm (CCCA), which can detect the number of clusters automatically also. We suppose that the competition and the cooperation exist at the same time. In the process of competition, winners will move to the centers of clusters and represent clusters gradually while the losers are slowly died out. By this way, true clusters can be found effectively. In some situations, there are some small but interesting clusters. In the competition with other bigger and nearer clusters, those small clusters are in the inferior position and may die out. In order to avoid such situation, we suppose that cooperation exist simultaneously and can help the clusters compete with other clusters. In our experiment, the algorithm can find the suitably interesting and meaningful clusters effectively.

So far, Euclidean distance and Pearson's correlation coefficient have been widely used as the distance measure for clustering analysis. However, when Euclidean distance is applied to measure the similarity between genes, it is not effective to reflect functional similarity such as positive and negative correlation, interdependence as well as closeness in values. In fact, Euclidean distance actually accounts only for the last. In other words, the primary interest of the overall shapes of genes [8] is not well considered. Consequently, some researchers proposed Pearson's correlation coefficient [9]. An empirical study [10] has also shown that Pearson's correlation coefficient is not robust to outliers and it may assign a high similarity score to a pair of dissimilar genes. Recently, some researches [11] proposed using mutual information to measure the similarity between genes. Mutual information has several merits: Firstly, mutual information makes full use of the high-order statistical information contained in the gene expression data. Secondly, there are many missing data in gene expression data, both Euclidean distance and Pearson's correlation coefficient need to estimate those missing data; this operating may induce some extra errors. However, mutual information doesn't need to estimate these missing data. Thirdly, mutual information not only can measure the similarity between genes, but

also the importance of gene by computing the mutual information between gene vector and the class label vector. In our paper, we shall use mutual information to measure the importance of genes and the similarity between genes.

To demonstrate CCCA’s usefulness for mining and analyzing gene expression data and to evaluate its performance, one gene expression data set, colon cancer, are used. We first applied CCCA to each of them, for selecting the most promising genes, then fed the selected genes into several well-known classification algorithms and compared their classification accuracies with those yielded by other gene selection methods. These classification algorithms, including a decision-tree-based algorithm, as well as Multilayer Feedforward Neural Networks (MFNN) and the nearest neighbor approach, are used in this paper. The experimental results demonstrate that CCCA outperforms other algorithms significantly.

## 2 Methods

Gene clustering is the process which finds  $c$  disjoint clusters,  $C_1, C_2 \dots C_c$ , of correlated genes by assigning each genes in  $\{A_1, A_2 \dots A_p\}$  to one of these clusters. Formally, we define gene clustering as the process that  $\forall A_i, i \in \{1, \dots, p\}$ ,  $A_i$  is assigned to a  $C_r, r \in \{1, \dots, c\}$ , where  $C_r \cap C_s = \Phi$ , for all  $s \in \{1, \dots, c\} - \{r\}$ .

To find meaningful clusters, gene clustering is conducted so that genes within a cluster should have high correlation or high interdependence to each other whereas genes in different clusters are less correlated or more independent. Most of the conventional clustering methods use some distance metric to measure the dissimilarity or distance between two objects. In this paper, we use mutual information to measure similarity between two genes, which we believe is more meaningful if interdependent patterns are the most significant characteristics of a cluster reflecting the interrelationship among genes.

### 2.1 The Gene Interdependence Measure

For each continuous fingerprint in gene expression data, its domain is typically discretized into a finite number of intervals for data mining. In this paper, we use an Optimal Class-Dependence Discretization Algorithm (OCDD) [12] to discretize the continuous data. This method uses the normalized mutual information measure, which reflects interdependence between the class label vector and the gene, as the objective function and iterative dynamic programming to find a global optimal solution.

Let us suppose that the domain of  $A_i, i \in \{1, 2 \dots p\}$ , is discretized by OCDD into  $m_i$  intervals. After discretization, the domains of all the attributes in  $R$  can be represented by  $dom(A_i) \in \{v_{i1}, v_{i2} \dots v_{ip}\}$ ,  $i \in \{1, 2 \dots p\}$ , where  $v_{ik} = a_{ik}$ ;  $k = 1, 2 \dots m_i$ , if  $A_i$  is discrete and  $v_{ik} = [b_{ik}, b_{i(k+1)}) \subseteq [l_i, u_i]$ ,  $k = 1, 2 \dots m_i$ ,  $b_{i1} = l_i, b_{i(m_i+1)} = u_i$  if  $A_i$  is a discretized continuous attribute.

Let  $\sigma$  denote the SELECT operation from relational algebra and  $|S|$  denote the cardinality of set S. The probability of a record in R having  $A_i = v_{ik} ; i \in \{1, 2 \dots p\} ; k = 1, 2 \dots m_i$ , is then given by:

$$\Pr(A_i = v_{ik}) = \frac{|\sigma_{A_i=v_{ik}}(R)|}{|\sigma_{A_i \neq NULL}(R)|} \tag{1}$$

and the joint probability of a record in R having  $A_i = v_{ik}$  and  $A_j = v_{jl}, j \in \{1, \dots, p\}, i \neq j, k \in \{1, \dots, m_i\}, l \in \{1, \dots, m_j\}$  is calculated by:

$$\Pr(A_i = v_{ik} \wedge A_j = v_{jl}) = \frac{|\sigma_{A_i=v_{ik} \wedge A_j=v_{jl}}(R)|}{|\sigma_{A_i \neq NULL \wedge A_j \neq NULL}(R)|} \tag{2}$$

For two fingerprints,  $x = \{x_1, \dots, x_p\}$  and  $y = \{y_1, \dots, y_p\}$ , similarity can be measured by the interdependence redundancy measure[1]:

$$R(A_i : A_j) = \frac{I(A_i : A_j)}{H(A_i : A_j)} \tag{3}$$

where  $I(A_i : A_j)$  is the mutual information between  $A_i$  and  $A_j$ , which is given by :

$$I(A_i : A_j) = \sum_{k=1}^{m_i} \sum_{l=1}^{m_j} \Pr(A_i = v_{ik} \wedge A_j = v_{jl}) \log \frac{\Pr(A_i = v_{ik} \wedge A_j = v_{jl})}{\Pr(A_i = v_{ik}) \Pr(A_j = v_{jl})} \tag{4}$$

$H(A_i : A_j)$  is the joint entropy of  $A_i$  and  $A_j$ , which is given by :

$$H(A_i : A_j) = - \sum_{k=1}^{m_i} \sum_{l=1}^{m_j} \Pr(A_i = v_{ik} \wedge A_j = v_{jl}) \log \Pr(A_i = v_{ik} \wedge A_j = v_{jl}) \tag{5}$$

In order to investigate the interdependency of a gene with all the other within a group, we use the multiple interdependency redundancy measure [12]. The multiple interdependence redundancy measure of a gene  $A_i$  within a gene group or cluster,  $C = \{A_j | j = 1, 2, \dots, p\}$ , is defined as:

$$MR(A_i) = \sum_{j=1}^p R(A_i, A_j) \tag{6}$$

where  $R(A_i : A_j)$  is the interdependence redundancy measure between  $A_i$  and  $A_j$ .

We also use the concept of ‘mode’, denoted by  $M_j$ , that is the gene with highest multiple interdependence redundancy in a gene cluster  $C_i = \{A_j \mid j = 1, 2, \dots, p\}$ . So it can be defined as:

$$M(i) = A(j), j = \max_{A_n \in C_i} (MR(A_n)) \tag{7}$$

**2.2 The Cooperative Competition Clustering Algorithm**

To group genes,  $A_1, A_2 \dots A_p$ , into different clusters, we propose a new Cooperative Competition Clustering algorithm. We suppose that cooperation and competition exist simultaneously among clusters in the process of clustering, at the same time, the cooperation, which comes from the nearest cluster, can help the cluster to compete with other clusters. In the competition, winners will move to centers of clusters and represent clusters gradually, while the losers will die out. By this way, true clusters can be found in the end. In some situation, there will be some small but interesting clusters. In the competing with other bigger and nearer clusters, those small clusters are in inferior position and maybe die out. In order to avoid occurring this situation, we suppose that cooperation exist simultaneously in competing, which help the cluster to compete with other clusters.

In many existing algorithms, only the distance information is used to determine which cluster a sample belongs to. But for many practical problems, such as interaction between electric charges, only distance information is not enough to represent the interaction strength, while the masses for two electric charges have to be considered. So, in our proposed Cooperative Competition Clustering algorithm, we introduce a concept of cluster quality to measure the cluster competitive force.

**Definition 1:** The cluster density of a cluster,  $C_i = \{A_j \mid j = 1, 2, \dots, p\}$ , is defined as:

$$D(i) = \frac{\sum_{A_n, A_m \in C_i, n \neq m} R(A_n, A_m)}{N_i(N_i - 1)} \tag{8}$$

where  $R(A_i : A_j)$  is the interdependence redundancy measure between  $A_i$  and  $A_j$ ;  $N_i$  is the number of genes in the cluster,  $C_i$

Nevertheless, in practical applications, only cluster density is not enough to measure the cluster competitive force, the number of genes in the cluster will also impact on the cluster competitive force. So we give the following definition:

**Definition 2:** The cluster quality of a cluster,  $C_i = \{A_j \mid j = 1, 2, \dots, p\}$  is defined as:

$$Q(i) = D(i) * N_i^k \tag{9}$$

where  $D(i)$  is the cluster density of cluster  $C_i$ ;  $N_i$  is the number of genes in the cluster  $C_i$ ;  $k$  is the coefficient which measures the importance of the number of genes in cluster. If  $k = 0$ , the cluster quality is only determined by cluster density, and not related to the number of genes in a cluster; If  $k = 1$ , the cluster density and the number of genes in a cluster have the same impact on the cluster quality; If  $k > 1$ , the number of genes in a cluster is more important to the cluster density; if  $0 < k < 1$ , the number of genes in a cluster is less important to the cluster density. We suppose that the number of genes in a cluster is less important than the cluster density, so we set  $k = 0.5$  in this paper.

In the competition with other bigger clusters, sometimes those small clusters are in inferior position and may die out at beginning of the algorithm. In order to avoid occurring such situation, we suppose that cooperation exist simultaneously in competing, which can help the clusters to compete with other clusters. So we introduce a concept referred to as Inter-cluster aid to measure the strength of cooperation.

**Definition 3:** The Inter-cluster aid of a cluster,  $C_i = \{A_j \mid j = 1, 2, \dots, p\}$ , is defined as:

$$IA(i) = I(M_i, M_j)^2 * Q(j), j = \arg(\max_{n \neq i} (I(M_i, M_n))) \quad (10)$$

where  $Q(j)$  is the cluster quality of cluster,  $c_i$ ,  $M_i$  is the center mode of cluster,  $C_i$ ,  $M_i$  is the center mode of cluster  $C_j$ ;  $I(M_i, M_j)$  is the interdependence redundancy measure between  $M_i$  and  $M_j$ .

The total competitive force of a cluster is thereby composed of the cluster quality of the cluster and the Inter-cluster aid of the cluster. Thus, we introduce the definition of the total competitive force of a cluster.

**Definition 4:** The total competitive force of a cluster,  $C_i = \{A_j \mid j = 1, 2, \dots, p\}$ , is defined as:

$$F(i) = Q(i) + IA(i) \quad (11)$$

where  $Q(i)$  is the cluster quality of cluster  $C_i$ ,  $IA(i)$  is the inter-cluster aid of cluster  $C_i$ .

As a result, the Cooperative Competition Clustering algorithm can be summarized as follows:

Step 1. Initialization. Let us select the number of clusters,  $k$ , where  $k$  is greater than the true number of clusters  $k^*$ . Assume  $k$  genes to be randomly selected as cluster modes  $M_i, i \in \{1, 2, \dots, k\}$ .

Step2. Assigning every gene to one of the clusters. Take a sample  $A_j, j \in \{1, 2, \dots, p\}$  from the data set. For cluster  $i, i \in \{1, 2, \dots, k\}$ , let

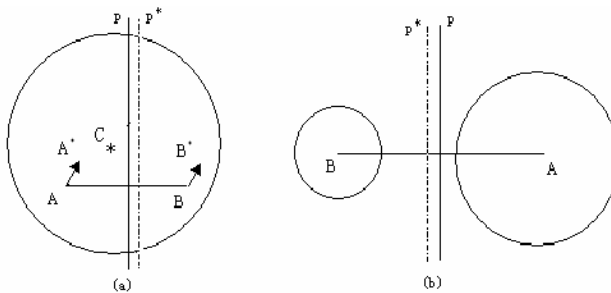
$$f(C_i | A_j) = \begin{cases} 1 & j = \arg(\max(F(i)) * R(A_j, M_i)) \\ 0 & \text{else} \end{cases} \tag{12}$$

where  $F(i)$  is the total competitive force of cluster  $C_i$ ,  $R(A_j, M_i)$  is the interdependence redundancy measure between gene,  $A_j$ , and cluster mode,  $M_i$ .

Step 3. Update cluster modes and the total competitive force for every clusters. Firstly, determine these clusters, in which the number of samples is few, then these clusters should be removed. And then, for every cluster,  $C_i, i \in \{1, 2, \dots, k\}$ , we set the  $M_i = A_j, j = \arg(\max_{A_n \in C_i} (MR(A_n)))$ ; and compute the competitive force for every clusters.

Step 4. Termination. Steps 2 and 3 are repeated until cluster modes  $M_i, i \in \{1, 2, \dots, k\}$  do not change.

In practical applications, how does CCCA work well? There are two hypotheses done: 1). Samples in the same cluster are uniformly distributed. 2). Different clusters are well separated. We can explain the working principle of CCCA by Fig-1. When two (or more) selected cluster modes, say, mode A and B, are in the same true cluster as in Fig-1 (a). At beginning stage, the cluster quality of mode A almost equals to that of mode B and the determination plane, i.e., the plane p, is in the middle of modes A and B. We suppose that mode A is much near to the mode of true cluster, i.e., mode C. Consequently more samples are determined to belong to cluster A so that the cluster quality of cluster A gets much bigger. On the other hand, few samples are determined to belong to cluster B and the cluster quality of cluster B gets much smaller. After that, mode A moves forward to mode C, while mode B moves to the margin of the true cluster and the determination plane move forward to mode B. Finally, mode A moves to mode C and represents the true cluster; while mode B will be removed. When two true clusters are represented by mode A and mode B, respectively, as shown in Fig-1 (b). The cluster quality of cluster A equals to that of cluster B, and the determination plane is in the middle of modes A and B at the beginning stage. We suppose that more samples are near to cluster A and few samples are near to cluster B. Consequently more samples are determined to belong to cluster



**Fig. 1.** A and B are initial mode of cluster A and B, respective. The plane p is the initial determination plane.  $A^*$  and  $B^*$  are new modes of cluster A and B after update, respective. The plane  $p^*$  is the new determination plane after update.

A and the cluster quality of cluster A gets much bigger, while few samples are determined to belong to cluster B and cluster quality of cluster B gets much smaller. In the following update, the determination plane moves forward to mode B for bigger cluster quality of cluster A. However, because the two true clusters are well separated and very few samples in the interspaces between cluster A and cluster B, the moving of the determination plane cannot make cluster A to become much bigger and bigger and the determination plane will be stable finally.

### 3 Experimental Results on Gene Expression Data Sets

We applied CCCA to two widely used gene expression data sets: the colon cancer data set. The colon cancer data set consists of 62 samples and genes. The samples are composed of tumor biopsies collected from tumors and normal biopsies collected from the healthy part of the colons of the same patient. Each sample has been preclassified into one of the two classes: normal and cancer.

It can be evidently that there are so much irrelevant and redundant gene expression data. The data structure of relevant and determinative genes is most important and interesting, while the data structure of irrelevant and non-determinative genes is not. So we removed the most irrelevant genes before using the CCCA by using the interdependence redundancy measure ( $R(F, A_i)$ ) between the class label vector ( $F$ ) and the sample vector  $A_i$ . We selected genes with  $R(F, A_i) > T$ , where  $T$  is a cutoff parameter that controls the strength of selection. To show the efficiency of this selection method, we used the selected genes to do classification tests.

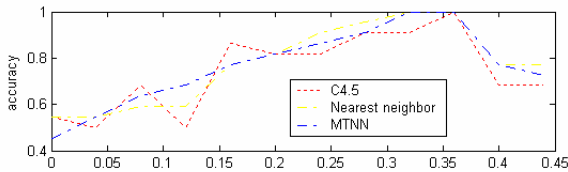


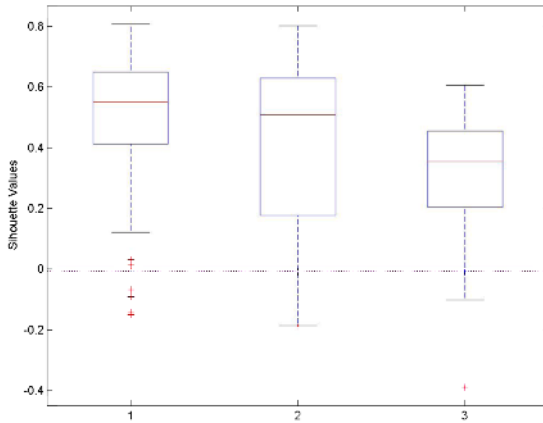
Fig. 2. The performance of classification on selected genes of the colon cancer data set

In the process of evaluating the performance of classification, we employ the leave-one-out cross-validation. We trained C4.5, the nearest neighbor method and Multilayer feedforward neural network (MFNN) with selected genes with the  $R(F, A_i) > T$ . The bigger  $T$  is, the fewer the selected genes are. It can be noticed from experimental results that increasing the features to be considered by a classifier may degrade its performance, if the number of training examples that are used to design the classifier is small relative to the number of features. This paradoxical behavior is termed as the peaking phenomena [13,14]. The explanation stands in the following: If  $T$  is small, non-determinative genes are removed and the classification accuracies increase; on the contrary, if  $T$  is larger, some determinative genes are removed and the classification accuracies decrease. To avoid removing the determinative genes, it is better to select a smaller  $T$ . However, there



will be too many non-determinative genes if  $T$  is too small. In the following experiments, we set  $T$  to 0.1 in colon cancer data set.

We used CCCA to test the colon cancer data set. Initially, we set the number of clusters to be 20. Then, CCCA divides the colon cancer data set into 4 clusters. After that, we selected top  $k$  genes to form every genes cluster, so a total of  $4 \times k$  genes are selected for  $k = 1, 2, 3$  in the colon cancer data set. We then used C4.5, MFNN and nearest neighbor method to build classifiers for testing on the selected genes.



**Fig. 3.** Boxplot of silhouette value of genes in cluster on the breast cancer data set

To evaluate the quality of the clusters formed by CCCA, we used the silhouette measure proposed by Rousseeuw (1987). For computing the silhouette value of a gene  $A_i$ , we first estimated two  $a_i$  and  $b_i$ . Let us denote  $C_r$  as the cluster to which gene belong. The scalar  $a_i$  is average similarity between  $A_i$  and all other genes of  $C_r$ . For any other cluster  $C_s \neq C_r$ , let  $d(A_i, C_s)$  denote the average similarity of gene to all genes of  $C_s$ . The scalar  $b_i$  is the biggest of these  $d(A_i, C_s), r \neq s = 1 \dots K$ , the silhouette value  $S(x_i)$  of gene  $A_i$  is the ratio  $\frac{a_i - b_i}{\max(a_i, b_i)}$ . The silhouette value lies

between  $-1$  and  $1$ . when its value is less than zeros, the corresponding is poorly classified. The Boxplots of the silhouette value are shown for both colon cancer data set and breast cancer data set in Fig 3. It can be seen from Fig 3 that the silhouette values of most genes are bigger than zero. So we can conclude that most genes are well classified and the quality of the clusters found by CCCA is very well.

To evaluate the gene selection performance of CCCA, the selected genes are fed to the same classification algorithms. In literature (Wai et al., 2005), the performance of ACA has been proved better than that of  $k$ -means, Biclustering and SOM. Here, we do not repeat this problem. So in this paper, we only compared the performance of CCCA with that of ACA. The experimental results are showed in Tables 1.

The performance of CCCA almost corresponds to that of ACA, but ACA doesn't have the ability to set  $K$  automatically. ACA needs user to set the  $K$  in advance, If  $K$

**Table 1.** The performance of classification on selected genes of the colon cancer data set

|                  | Number of selected genes | Classification accuracy |       |
|------------------|--------------------------|-------------------------|-------|
|                  |                          | CCCA                    | ACA   |
| C4.5             | 4                        | 83.9%                   | 80.6% |
|                  | 8                        | 85.5%                   | 83.9% |
|                  | 12                       | 85.5%                   | 83.9% |
| Nearest neighbor | 4                        | 90.3%                   | 83.9% |
|                  | 8                        | 85.5%                   | 82.3% |
|                  | 12                       | 85.5%                   | 82.3% |
| MFNN             | 4                        | 91.9%                   | 90.3% |
|                  | 8                        | 91.9%                   | 90.3% |
|                  | 12                       | 91.9%                   | 90.3% |

is not set correctly, the performance of ACA deteriorates rapidly. The performance of classification algorithms on the top genes selected by ACA with different number of clusters is given in Tables 2. It is interesting to find that ACA yields the promising performance with the numbers of cluster determined by CCCA.

**Table 2.** The performance of classification on selected genes by ACA of the colon cancer data set

|      | Number of cluster |       |       |       |       |       |       |       |
|------|-------------------|-------|-------|-------|-------|-------|-------|-------|
|      | 2                 | 3     | 4     | 5     | 6     | 7     | 8     | 9     |
| C4.5 | 77.4%             | 77.4% | 80.7% | 82.3% | 82.3% | 83.9% | 82.3% | 80.7% |
| NN   | 80.7%             | 80.7% | 83.9% | 83.9% | 85.5% | 83.9% | 83.9% | 82.3% |
| MFNN | 80.7%             | 80.7% | 90.3% | 85.5% | 85.5% | 83.9% | 83.9% | 87.1% |

## 4 Conclusions

Even though the Attribute cluster algorithm has been proposed for clustering on gene expression data, the use of this method has been hindered so far by problems associated with the choice of K. Recently many researchers proposes the competition clustering method to solve this problem, but the most of existing competition algorithms overemphasize the competition and overlook the cooperation between clusters so that many small but interesting clusters have been omitted.

In this paper, we proposed a new clustering algorithm known as Cooperative Competition Clustering (CCCA). In this algorithm, we took into account the cooperation between clusters to devise the Cooperative Competition Clustering algorithm. In other words, CCCA uses the idea of cooperative competition: Cooperation and competition exist simultaneously between clusters in the process of clustering and the cooperating, which comes from the nearest cluster, can help the cluster to compete with other clusters. By using this principle of Cooperative Competition, the number of clusters can be found

in the process of clustering efficiently. We devised the experiments on two gene data sets, the colon cancer data set and the breast cancer data set. It can be seen that CCCA can find the  $k$  automatically and select interesting and meaningful genes. The clusters found by the CCCA are well separated and those selected genes can yield very high classification performance on both data sets.

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# Genetic Algorithm and Neural Network Based Classification in Microarray Data Analysis with Biological Validity Assessment

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**Abstract.** Microarrays allow biologists to better understand the interactions between diverse pathologic states at the gene level. However, the amount of data generated by these tools becomes problematic. New techniques are then needed in order to extract valuable information about gene activity in sensitive processes like tumor cells proliferation and metastasis activity. Recent tools that analyze microarray expression data have exploited correlation-based approach such as clustering analysis. Here we describe a novel GA/ANN based method for assessing the importance of genes for sample classification based on expression data. Several different approaches have been exploited and a comparison has been given. The developed system has been employed in the classification of ER+/- metastasis recurrence of breast cancer tumours and results were validated using a real life database. Further validation has been carried out using Gene Ontology based tools. Results proved the valuable potentialities and robustness of similar systems.

## 1 Introduction

Microarrays have gained in this time a great fame . This technology enables the measurement of the levels of mRNA molecules inside a cell and, consequently, the proteins being produced. In this context, the comparison between gene expression patterns through the measurement of the levels of mRNA in healthy versus unhealthy cells can supply important information about pathological states, as well as information that can lead to earlier diagnosis and more efficient treatment.

The real challenge, then, is to find a set of genes, out of the thousands mapped, which can be used to develop a classifier with the highest accuracy [5]. Identification of a set of differentially expressed genes could serve to identify disease subtypes that may benefit from distinct clinical approaches to treatment. This was the primary objective of Foekens et al in [3] and [4]; to predict accurately patient's risk of recurrence is an important aspect of lymph node negative cases treatment planning. Gene signature extracted by Foekens et al consists of 76 genes (60 for ER+ and 16 for ER- cases). In [3] Foekens et al. have employed statistical methods and supervised/unsupervised clustering techniques in order to extract knowledge from a 286 x 22482

array of gene expression values. Although correlation-based approaches have been widely applied in analyzing the patterns of gene expression [1][2], it's commonly believed they may not fully extract the information from data corrupted by high-dimensional noise. Therefore, these ranking based techniques select the genes which individually provide better classification, but they may not result in meaningful gene combinations for an overall classification task. Hence approaches capable of performing an efficient search in high dimensional spaces, such as evolutionary algorithms (EAs), should prove to be ideal candidates. What is more, while high-throughput technology has significantly accelerated the rate at which biological information is acquired, tools that can successfully mine the resulting large data sets are needed. Some research groups have exploited the potentialities of soft computing techniques applied to bioinformatics and some these works were carried out in the field of microarray data analysis [6] [7].

With this work we have tried to address the problem of *gene selection* using a Genetic Algorithm that evolves populations of possible solution and uses an Artificial Neural Network in order to test gene signatures' ability to correctly classify cases belonging to the test set. Therefore, results returned by the GA/ANN based system are then validated using Gene Ontology, a biological validity assessment tool that can show interesting cues of research for biologist and physicians.

This paper firstly gives some details of the problem of classification problem in "post genomic" era. Then a description of the GA and of genetic operators is given. An outlook on the ANN classifier follows. In final paragraphs system results and brief investigations of biological plausibility are exposed.

## 2 Methods

### 2.1 Data Acquisition and Preprocessing

The dataset used to evaluate performances of the system proposed is publicly available and can be downloaded from the Gene Expression Omnibus (GEO) web site. GEO is a data repository of high-throughput gene expressions and hybridization arrays maintained by the National Center for Biotechnology Information. GEO databases have been used in the recent years by researchers of all over the world in order to give publicity to results of specific researches. Each dataset submitted to GEO receives an ID code (a unique identifier) called "Accession Number". Our focus is on the dataset *GSE2034*, submitted by Tim Jatkoe on the February, 23<sup>rd</sup> 2005 and provided to us by the I.R.C.C.S. of Bari, Italy. This dataset collects the results of a multi-center research carried out by Veridex LLC in collaboration with the Department of Medical Oncology, Erasmus MC-Daniel den Hoed of Rotterdam. The research, which involved 286 patients, aimed at discovering gene signatures able to identify patients at high risk of distant recurrence [3]. The ability to identify patients who have a favorable prognosis could, after independent confirmation, allow clinicians to avoid adjuvant systemic therapy or to choose less aggressive therapeutic options.

The data matrix obtained contains quasi-raw data. Gene expression levels, in fact, are characterized by statistical properties that force researchers to apply preprocessing algorithms. In the common practice of microarray data analysis the “normalization” is a key step. Data normalization for microarray experiments is an open field of research and many alternative algorithms have been proposed in order to accomplish this delicate task [9]. Together with normalization, filtering techniques met more and more often the consensus of researcher thanks to their ability to exclude in early stage of the research less meaningful variables that add computational costs to the data mining of similar datasets [10]. Even in this field many different approaches have been proposed. For the peculiarities of the dataset *GSE2034* an “entropy information” based gene filtering has been employed in order to remove genes with low entropy expression values [10]. At the end of these processes a normalised matrix 286 x 20055 have been obtained.

## 2.2 Gene Selection Using Genetic Algorithms

In recent years some research groups have focused their attention on the exploitation of GAs’ potentialities in information extraction from biomedical database. In [11] a multi-objective algorithm has been employed in order to build a reliable classification tool small in size and, at the same time, able to produce as accurate a classification as possible. In [12] the problem of gene assessment and sample classification for gene expression data have been addressed using a Genetic Algorithm and a K-Nearest Neighbor classifier.

The proposed approach is based on a hybrid system that uses a GA to select subsets of genes and an ANN that classifies cases and returns a metric of the error which is used as a fitness function for the selected subset of genes. Given the high variety of approaches reported in literature we have tried herein to carry out a comparative study of the different systems and their results on the chosen dataset.

As known GA, are basically inspired by natural evolution and selection. In biological systems, genetic information is stored in chromosomes. Chromosomes are replicated and passed onto the next generation with selection depending on fitness. Genetic information can, however, also be altered through genetic operations such as mutation and crossover. In GAs, each “chromosome” is a set of genes, which constitutes a candidate solution to the problem. There are four major components of GA:

- Chromosome;
- Fitness;
- Selection;
- Crossover / Mutation.

The modular approach followed in the design phase of the system has allowed to simply evaluating the performances of the other compared classifier systems described below, acting on the fitness function module.

Brief descriptions of particular implementations of the described systems are given below.

### 2.2.1 Chromosome Representation

In this work a 20 genes long chromosome has been used in order to codify a 20 genes long gene signature. A binary codification of the chromosome has been selected.

### 2.2.2 Fitness Function

For the calculation of the fitness function the Sum of the Squared Errors (SSE) error returned by an ANN based classifier has been used. This is a metric of the error made by the ANN in the classification task, other evaluation systems could be simply implemented.

### 2.2.3 Selection Criterion

The selection criterion was the elitistic one. Best performing gene signatures from each population are allowed to pass to the other generation producing offspring.

### 2.2.4 Crossover /Mutation

In the crossover and mutation operators some constraints have been implemented in order to maintain acceptability of the solution (e.g. in order to avoid the repetition of a gene in the same chromosome). Crossover probability has been set to 40% and mutation probability was time dependent.

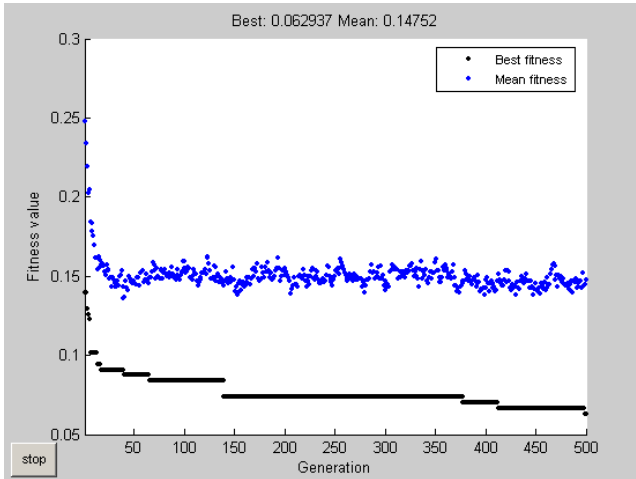
## 2.3 Artificial Neural Network Based Classification

Given the characteristics of the problem and the dimensionality of the dataset, an ANN-Feed-Forward (ANN-FF) has been chosen. Then, for each fitness function evaluation an ANN-FF is trained on 200 cases each of which is defined by 20 parameters (genes selected by the GA and passed to the fitness function for evaluation) and validated. On the basis of results of research described in [14], and having observed high similarity of dimensionality of the two datasets, a three layer ANN has been set up. The selected topology provided for 25 neurons in the first layer, 12 in the hidden layer, and 1 output neuron. Activation functions were: “*tansig*” for the first two layers and “*pure linear*” for the last layer. Stop criterion for the training phase were: 50000 epochs or SSE less than 0.004. Initial learning rate has been set to 0.3 and modified by the descent gradient momentum algorithm. These choices provided a solution able reach a good equilibrium between learning and generalization capabilities of the system.

## 3 Gene Selection

After the preprocessing stage and the system development, the experimentation phase has been carried out. The GA/ANN hybrid system has been set up and executed on the *GSE2034* dataset. The GA/ANN as well as the other compared GA/X hybrid systems were executed 100 times and each GA run accounted for 500 generations. Good convergence ability has been reached with described parameters as can be seen in figure 1.

From a computational standpoint, it's worth noting that statistical classifiers and K-NN based system are characterized by low CPU times when compared to SVM and ANN hybrid solutions. Even though the GA/ANN system showed a computationally intensive behaviour results returned by this system are characterized by an important factor. The amount of variance in the genes extracted, registered along the 100 runs of



**Fig. 1.** Best fitness, in black, and mean fitness values of generations

the GA, is quite low. This particular aspect distinguishes the GA/ANN approach from the others reported as comparison in this work. As it can be seen in the “Results and Comparisons” section, the GA/ANN returns results coherent with the problem; furthermore it has been observed that this system shows a particular ability in extracting relevant genes with a considerably higher probability than other genes.

## 4 Results and Comparisons

Comparative results of the hybrid systems previously described are provided in this section. After 100 executions of the GA a ranking of selected genes has been compiled. This ranking considered selection frequencies for each gene extracted and returned an interesting overview of systems’ performances. It’s worth noting that all of the solutions analyzed selected sets of genes that demonstrated to be overlapping. In table 1, the rankings of the 20 most selected genes for each hybrid system are reported. As it can be seen, a considerable part of the most selected genes are reported by all of the systems analyzed. However GA/ANN system showed lower variability in results returned; this aspect is peculiar of this particular hybrid system only. Genes extracted by the GA/ANN system remained quite the same over all the 100 runs of the algorithm. However, as confirmed by competitive results returned by the other systems, the choice of using a GA in order to extract relevant genes has a considerably positive impact on the overall system accuracy; evidently the sensitivity of GA employment on system’s performances is slightly higher than that of the classifier related choice.

However gene signatures returned by similar techniques are useless until an interpretation is formulated regarding their activities, interaction, and possible involvements in critical contexts (e.g. estrogen synthesis).



**Table 1.** Genes extracted by the compared systems, rank positions for each solution are reported

| <b>Gene ID</b> | <b>GA/ANN<br/>Rank</b> | <b>GA/SVM<br/>Rank</b> | <b>GA/KNN<br/>Rank</b> | <b>GA/Stat<br/>Rank</b> |
|----------------|------------------------|------------------------|------------------------|-------------------------|
| 219340_s_at    | 1                      | 1                      | 1                      | 1                       |
| 217771_at      | 2                      | 2                      | 2                      | 2                       |
| 202418_at      | 3                      | 3                      | 6                      | 4                       |
| 206295_at      | 4                      | 4                      | 4                      | 7                       |
| 200726_at      | 5                      | 5                      | 5                      | 3                       |
| 210314_x_at    | 6                      | 7                      | 3                      | 6                       |
| 219588_s_at    | 7                      | 6                      | 8                      | 8                       |
| 212567_s_at    | 8                      | 8                      | 7                      | 10                      |
| 55081_at       | 9                      | 10                     | 10                     | 18                      |
| 218430_s_at    | 10                     | 9                      | 9                      | 9                       |
| 217404_s_at    | 11                     | 11                     | 12                     | 13                      |
| 205848_at      | 12                     | 12                     | 13                     | 12                      |
| 214915_at      | 13                     | 13                     | 16                     | -                       |
| 202687_s_at    | 14                     | 15                     | 14                     | -                       |
| 221241_s_at    | 15                     | 16                     | 11                     | 11                      |
| 210593_at      | 16                     | 14                     | -                      | -                       |
| 204028_s_at    | 17                     | 17                     | 15                     | -                       |
| 201112_s_at    | 18                     | 19                     | 17                     | -                       |
| 209825_s_at    | 19                     | 18                     | -                      | 16                      |
| 209602_s_at    | 20                     | -                      | 19                     | 14                      |
| 209604_s_at    | -                      | 20                     | -                      | 5                       |
| 201579_at      | -                      | -                      | 18                     | 15                      |
| 210347_s_at    | -                      | -                      | -                      | 17                      |
| 209603_at      | -                      | -                      | 20                     | 19                      |
| 200827_at      | -                      | -                      | -                      | 20                      |

In this work we provide a two-fold validation of the sets of genes. In current research in the bioinformatics field there are two main trends as for the validation of results returned by any kind of computational approach. The first is referred to as “Data-driven” approach which mainly includes statistical tests or validity indices (e.g. Dunn’s index or Silhouette method) applied to the data clustered. The second is referred to as “Knowledge-driven” method [15]. In the Molecular Biology and Bioinformatics field the “Knowledge-base” model has been translated in a set of “genetic ontology” maintained by a specific consortium: the “Gene Ontology Consortium”[16]. Biological validity assessment of gene signatures obtained is given in the next section. In this section “Statistical-Driven” validation is carried out. The focus is obviously on the gene signature extracted by the GA/ANN, however, given the similarities with other gene subsets, similar analyses could be done for the other results. The first gene, “219340\_s\_at”, has been selected 85 times over 100 executions. This gene’s product is a transmembrane protein involved in signal transmission between cells. The putative CLN8 protein gene has been selected as the most statistically meaningful gene even in the work of Foekens[3]. In the following positions in the ranking there is a set of genes “201112\_s\_at”, “202687\_s\_at”,

204028\_s\_at”, “205848\_at”, “206295\_at”, “210314\_x\_at” and “221241\_s\_at” that show frequencies between 62 and 83 and that belong to the same class of genes. In fact all of these genes are involved in the “cell cycle” regulation, included apoptosis that is, the way cells die in an ordered or programmed way. Apoptosis is one of the main types of Programmed Cell Death that allow organism to handle cell proliferation. These mechanisms have been discovered to be strictly correlated to tumor proliferation [18]; in particular down-regulation of apoptosis-related genes can lead to uncontrolled cell proliferation which is a key aspect of cancer.

In order to give a comprehensive outlook on all the techniques involved in this comparative study, table 2 collects computational times required by each system. Measurements refer to an Intel P4 EE 2.8 GHz with 2 GB of DDR RAM memory. An average value of all the measurements made has been calculated, approximated to next integer number and reported.

**Table 2.** Computational times (in seconds) required by each system

| GA/Stat | GA/KNN | GA/SVM | GA/ANN |
|---------|--------|--------|--------|
| 1385    | 9910   | 44500  | 144200 |

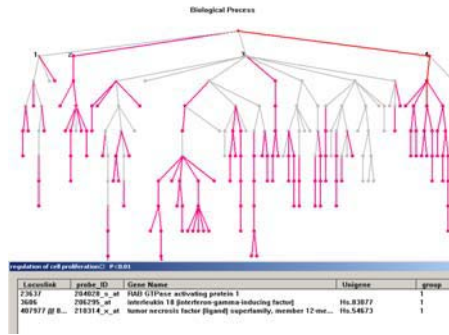
## 5 Biological Validity Assessment

In this section we provide a biological validity assessment of the results obtained in previous steps. Obviously the focus is primarily on the GA/ANN solution, however, given the similarities among the extracted genes subsets, following considerations could be considered applicable even to the other systems.

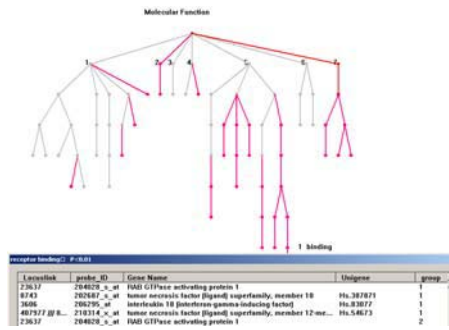
The Gene Ontology (GO) is composed of three related ontologies covering basic areas of biological research: the molecular function of gene products, their role in multi-step biological processes, and their physical structure as cellular components. GO Consortium provides to constantly control and update databases. The GO defines a shared, structured and controlled vocabulary to annotate molecular attributes across models organisms. As shown in figures 2 and 3 each ontology is constructed as a directed acyclic graph. GO is composed by GO terms and each GO term consists of a unique alphanumerical identifier, a common name, and a definition. Terms are classified into only one of the three ontologies. In this way sets of genes, extracted by statistical techniques as well as computational intelligence based systems, could be analyzed in order to observe if there is any “interaction” or involvement in biological path considered critical for the disease or phenomenon examined.

One of the most interesting GO based software is the GO Surfer of the Harvard School of Public Health [15].

Fed with the list of the 20 most selected genes extracted by the GA/ANN hybrid system, GO Surfer puts in evidence quite interesting results. In figure 2 the GO trees of the “biological processes” category are shown. Each node represents an individual GO term and all GO terms at display are associated with at least one out of 20 specific genes. It is remarkable that a great part of these genes belong to GO terms in some way correlated to the regulation of cell life (cellular proliferation, apoptosis and necrosis).



**Fig. 2.** “Biological Process” GO Tree. “Regulation of Cell proliferation” GO Term in evidence.



**Fig. 3.** “Molecular Process” GO Tree. “Receptor binding” GO Term in evidence.

Down-regulation of these genes could result in uncontrolled cell proliferation and then oncogenesis. In figure 3 GO tree of the molecular function is reported. From this standpoint it is interesting to observe that in one of the most meaningful term ( $p < 0.01$ ), the “receptor binding” one, two “tumor necrosis factor” genes are present. Even in this case irregular activity of these genes can bring to dysfunction in cell cycle regulation. In the most interesting of the “cellular component” tree branch ( $p < 0.01$ ) “Cytoskeleton” the “205848\_at” gene is included. This is a growth arrest specific gene, that is to say a gene that could regulate the growth of cells (furthermore in this process the well known P53 onco-suppressor gene is involved). On the basis of all these considerations and observations it can be argued that the research in the field of Breast Cancer should focus on the activity and regulation of “221241\_s\_at”, “202687\_s\_at”, “210314\_x\_at”, “205848\_at” and “55081\_at” genes. As we have previously seen, these genes are not only able to build an accurate classifier, but they are even involved in biological and molecular processes that could be individuated as strictly correlated to typical tumour pattern, just like dysfunction in cell life cycle and receptor activity.

## 6 Concluding Remarks

The development of gene expression data analysis methods is one of the most important challenges of the post-genomic era. With the advent of microarray technology, the scientific community has assisted at the growth of datasets with a peculiar aspect: high disproportion between the two dimensions. This is a critical challenge for both the data miners and the tools they employed.. Machine learning techniques, in this context, have demonstrated to be a powerful tool especially for what concerns clustering and combinatorial optimization problems. These are two of the most active research branch in the bioinformatics field. Soft computing techniques, still, are gaining more and more attention due to their abilities and potentialities in the two fields described. System's performances were tested using a real-world publicly available dataset (*GSE2034*). It is worth noting that the proposed solution shows large applicability: other datasets could be explored with similar results (further experiments were successfully carried out on [19]).

A comparative study of performances of other systems has been given in this paper as additional evaluation tool. As analyzed in previous sections, the results returned by the GA/ANN are quite competitive: the proposed algorithm demonstrated to be robust and be affected by very low variability of results. This is the most interesting characteristics of the system described. In the various experiments carried out the GA/ANN approach selected small subsets of genes with a high frequency; this can be interpreted as the ability of the proposed system, to focus its research on subsets of features and to avoid local minima entrapment. According to the "Knowledge-driven" principles, on the other hand, a Gene Ontology based validity assessment has been carried out. As demonstrated in previous sections validity assessment can be considered to be satisfied both from a statistical and from a biological standpoint. Furthermore we observed that some of the most relevant genes extracted were included in the gene signature proposed by Foekens [3]. Further works will be mainly oriented on the optimization of the classifier. Artificial Immune System (AIS) based approaches are being studied. Given the AIS-ANN theory similarity [20], AIS based systems in the limited resources approach [21] could reveal interesting potentialities, optimizing both classification abilities and resource employment. Further researches have to be carried out but the results in the primary stage are encouraging.

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# Inferring Species Phylogenies: A Microarray Approach

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**Abstract.** The incongruence between the gene trees and species remains a challenge in molecular phylogenetics. In this work, we propose a novel microarray approach to resolve this problem based on our previously proposed phylogenomic mining method. In our microarray approach, we first selected 28 genes from a set of statistically significant housekeeping genes from the *S. cerevisiae* cell cycle time series microarray data. Then we employed the BLAST and synteny criteria to identify homologs and orthologs of the selected genes among the genomes of other species. Finally, we applied the phylogenomic mining method for the aligned genes to infer the species phylogeny. The phylogenetic mining method used the self-organizing map mining, hierarchical clustering and entropy measure to concatenate the phylogenomically informative genes to infer species phylogenies. Compared with the original gene concatenation approach, our method not only overcome the ad-hoc mechanism and prohibitive phylogenetic computing problem of the species inference for the large number of taxa but also first integrated the microarray techniques in the species phylogeny inference.

## 1 Introduction

The gene tree / species tree problem is a fundamental problem in molecular phylogenetics [1,2]. It refers that the gene trees, the phylogenies obtained from individual genes, are incongruent with the species tree. The species phylogeny reflects the true evolution history of species where all lineages are results of speciation and divergence. A gene phylogeny represents the evolutionary history of the gene for a set of organisms. The incongruence between gene trees and species trees can be observed from all levels of taxa. However, the probability of incongruence between the gene trees and species tree is high for a set of closely related species [1,2,3]. Such incongruence may originate from reasons including gene duplication/loss, lineage sorting, horizontal gene transfer and the technical factors including the artifacts of phylogenetic analysis and possible insufficient data sampling [3,4]. Resolving the incongruence among the gene trees and species trees has fundamental impacts on molecular evolution and phylogenetics.

Besides the previous phylogenetic reconciliation models to resolve the gene tree and species tree problem [3], there are currently two recently proposed resolutions to deal with this problem. The first is called the *genome-tree* approach, which uses the complete genome data to build a phylogenetic tree and the final evolutionary tree is a

species tree [5,6]. However, this promising method suffers from naïve phylogenetic computing models and faces the computational hurdle in the genome tree reconstruction. Furthermore, small numbers of relevant genomes are currently available although thousands of genomes are being sequenced [5]. The other method is the genome based gene concatenation method proposed by Rokas *et al.* [7]. This method is widely accepted by biologists for the sake of its simplicity and convenience. The basic idea of their method is to select and align a set of widely distributed orthologous genes from the genomes of multiple species. Then they empirically determine the required number of genes to robustly infer phylogenetic tree by conducting phylogenetic analysis for the randomly selected genes until the final species tree is a phylogeny with the maximum support. In their experiment, they screened 106 orthologous genes from eight yeast genomes and showed the phylogenetic analysis (ML and MP) with at least 20 genes concatenation led to a species tree with the maximum support on each inferred branch [7].

Although the genome based gene concatenation method is easy to use, there are possible problems of this ad hoc approach. First, the gene concatenation number in the method has to be empirically determined for each dataset. Under the situation where large numbers of taxa are available in the species phylogeny inference, the computational burden for the phylogenetic analysis in this method will be prohibitive; Secondly, the random gene concatenation does not consider that some genes may have better phylogenetic information than others in the species phylogeny inference. On the other hand, it assumes all genes in the concatenation are equally phylogenetically informative. Thirdly, if the orthology criterion is not robust in the data collection, then genes used in phylogenetic reconstruction may have different evolutionary histories. The random gene concatenation under such a situation will bring noise signals in the phylogenetic tree reconstruction and the final tree inferred may not be robust or represent the true evolutionary relationships between organisms.

To support our concern about the genome based random gene concatenation method, we create a “worst” case of the random gene concatenation method. The 106 genes in the original dataset are classified into 45 congruent genes (“good” genes) and 61 incongruent genes (“bad” genes) under the Bayesian analysis and maximum likelihood analysis with the Shimodaira-Hasegawa (SH) test [8,9,10]. A congruent (good) / incongruent (bad) gene is a gene whose gene tree is/not the species tree after the Bayesian analysis and maximum likelihood analysis with the SH test. We only concatenate incongruent genes (bad genes) randomly and conduct the Bayesian analysis for the randomly combined bad genes. There are 10 testing trials for each combination case. We found it needed at least 28 genes under this case to reach the satisfactory result; that is, the final tree is a species tree where each inferred branch has the maximum support. On the other hand, the random concatenation experiments are also done for the congruent/good genes and random genes. We found it needed at least 4 congruent genes or at least 15 random genes in the combination to infer a species phylogeny where each inferred branch has the maximum support [11]. From this example, it is clear that different genes have unequal phylogenetic information and the implicitly equal-phylogenetic information assumption for each gene in the random gene concatenation method is improper.

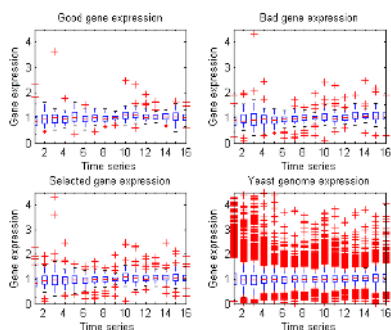
In our previous work, we proposed a phylogenetic mining method to infer the species phylogeny based on the selected 106 orthologous genes to conquer the ad-hoc mechanism [12]. In this work, we propose a novel microarray based approach to infer

the species phylogeny for the same problem under the framework of the phylogenomic mining. This is the first work to resolve the incongruence between gene tree and species tree problem from the point view of the microarray data. In the following sections, section 2 analyzes the characteristics of the gene expression profiles of the 106 selected genes in the *S. cerevisiae* cell cycle time series microarray data. Section 3 presents the microarray based approach to reconstruct the species phylogeny and section 4 describes the details about the phylogenomic mining method. Finally, we discuss the ongoing work and future work in the last section.

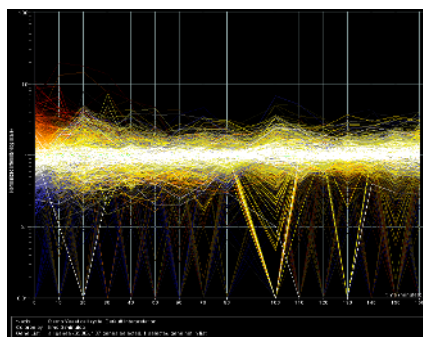
## 2 Gene Expressions of the Selected 106 Genes in the *S. cerevisiae* Microarray Data

According to the data collection criteria in [7], the retained 106 genes are distributed throughout the *S. cerevisiae* genome on all 16 chromosomes of the yeast genome and the synteny method is employed to build orthology before the gene alignments. We believe that the data collection approach is effective but a little bit ad-hoc since many genes can be found widely distributed on all the yeast chromosomes. Before we describe the details of our approach, we check the gene expressions of the selected 106 genes in the *S. cerevisiae* cell cycle time series microarray data.

Figure 1 shows the box plots of the gene expressions of good genes, bad genes, selected 106 genes and whole yeast genome including 6330 genes in *S. cerevisiae* cell cycle microarray data. Figure 2 shows the gene expressions (colored in white) of the 106 selected genes among the gene expressions of the whole yeast genome visualized by the *GeneSpring* 7.2. From the two figures, we can see the selected 106 gene set has the relatively “conservative” expression patterns among the whole yeast genome, that is, the variances of their gene expression data are relatively small compared with those of the whole expression data. We also visualize the gene expression patterns of the good genes and bad genes of the 106 genes. Figure 3 compares the variances of the expression data of the yeast genome, good genes and bad genes of the selected 106



**Fig. 1.** Box plots of the gene expressions of good, bad, selected 106 genes and whole yeast genome



**Fig. 2.** The selected 106 gene expressions (colored in white) among the whole yeast genome



genes, selected 106 genes and two randomly selected 100 genes from the yeast genome. The gene expression data of the selected 106 genes have variance between 0 and 1. This variance is much lower than the variances of expression data of the yeast genome and two randomly selected gene sets! On the other hand, the expression data variances of the good genes are also lower than the expression data variances of the bad genes in the selected 106 genes. Figure 4 compares the expression data means of the yeast genome, good genes, bad genes and the selected 106 genes. It is easy to see that the selected 106 genes have means concentrated around the 1.0 expression level. The good gene expression means are “nearer” the gene expression level 1.0 than the bad gene expression means. From the two sets of results, we can tell that the gene expression levels of the selected genes are more conservative than the average gene expression level of the whole yeast genome. The good gene expression levels are more conservative than the bad gene expression levels among the selected 106 genes. The same conclusion can also be obtained by observing the box plots of the good genes, bad genes, selected 106 genes and whole yeast genome expressions in Figure 1.

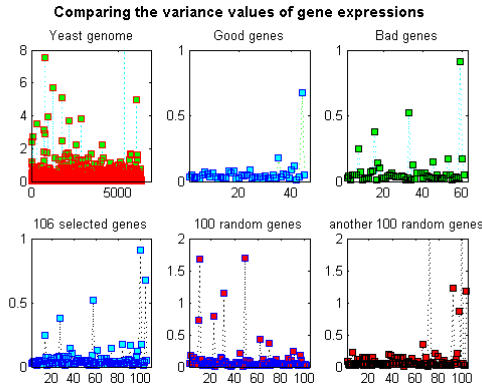


Fig. 3. Compare the gene expression variances of the different gene sets

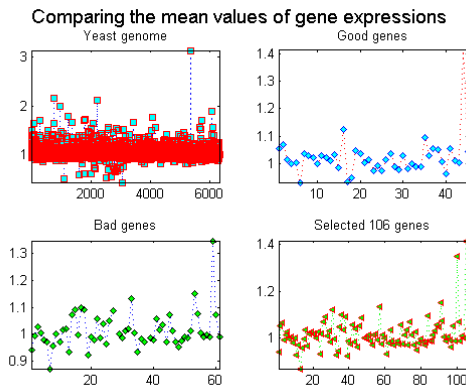


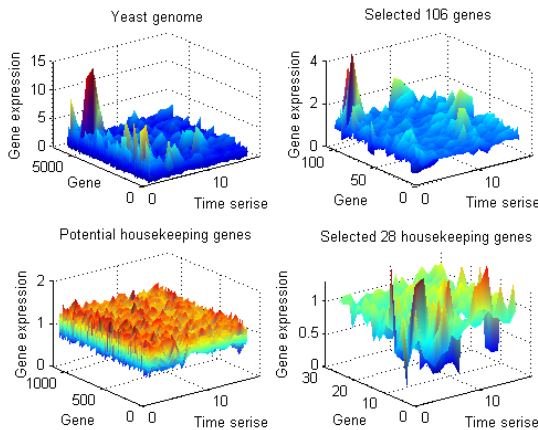
Fig. 4. Compare the gene expression means of the different gene sets

### 3 A Microarray Based Approach to Resolve Incongruence Between the Gene Trees and Species Tress

According to the gene expression analysis results of the congruent, incongruent, 106 selected genes and the whole yeast genome, it's natural to start from the housekeeping genes in the microarray data to collect a new dataset because their gene expressions have the least variations. We start from the *S. cerevisiae* cell cycle time series microarray data to collect housekeeping genes. The housekeeping genes can be viewed as potentially conservative genes in the yeast genome. This is similar to the widely-distributed gene finding in the original data collection [7]. Our microarray based species phylogeny inference method has the following steps.

1. Identify the statistically important house-keeping genes in the *Saccharomyces cerevisiae* cell cycle time series microarray data and select a set of genes from the statistically important house-keeping genes.
2. Use the BLAST and synteny criteria to identify homologs and orthologs for the selected genes.
3. Construct multiple alignments for the selected orthologous genes.
4. Conduct the phylogenomic mining for the aligned genes to infer the species phylogeny.

We first selected 114 statistically significant housekeeping genes from 1014 potential housekeeping genes with the lowest 20 percent variance from the *S. cerevisiae* microarray data by running the *GeneSpring 7.2* software. We then randomly sampled 28 housekeeping genes from the 114 statistically significant housekeeping genes and blasted them to other seven genomes to build an orthologous gene set. In our sampling process, those genes which have gene loss in one species were dropped automatically. The following multiple alignments for each gene are conducted by the *ClustalW* and *MacClade* under a machine running Mac OS X system. After the alignments, the total length of the



**Fig. 5.** The 3D gene expression data visualization of the yeast genome, selected 106 genes, 1014 potential housekeeping genes and selected housekeeping genes

28 aligned genes has 26876 nucleotide sites. In the selected 28 gene set, there are 18 congruent and 10 incongruent genes in this gene sample. The 10 incongruent genes are phylogenetically informative genes according to the SH test; that is, their gene trees have closer distances to the species tree statistically. The SH-test is conducted under the GTR+ $\Gamma$  model with reestimated log likelihoods (RELL) approximation for 21 tree topologies for each gene with 1000 bootstrap replicates [10], Figure 5 shows the gene expression 3D visualization of the yeast genome, 106 selected genes, 1014 potential housekeeping gene sets and the sampled 28 genes from the 114 housekeeping genes. In each sub-figure, the x-axis represents the cell cycle time series, the y-axis represents genes and z-axis represents the gene expression levels.

### 4 Using Phylogenetic Mining to Infer Species Phylogenies

The basic idea of the phylogenomic mining is to discover the phylogenetic knowledge from a gene set  $G$  by the self-organizing map (SOM) mining, hierarchical clustering and entropy based phylogenetically informative gene finding approaches [11,12]. The gene set  $G$  is a set of aligned orthologous genes obtained from the species genome data. The knowledge includes the prototypes of the each species, clustering of genes and the predicted phylogenetically informative genes. After the phylogenetic knowledge discovery, the predicted phylogenetically informative genes are concatenated to be a “super-gene” to conduct the phylogenetic analysis to infer the species phylogenies. A super-gene is the concatenation of phylogenetically informative genes. Figure 6 shows the flowchart of the phylogenetic mining method. It can be sketched as following four steps.

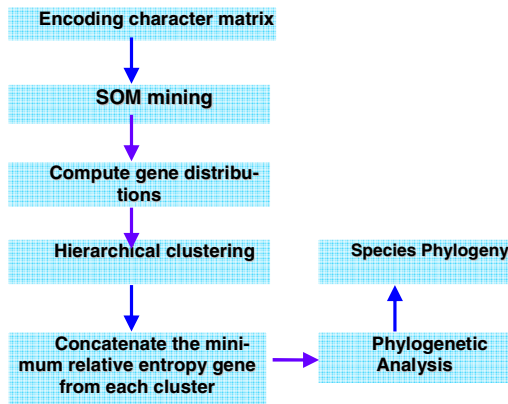


Fig. 6. The phylogenetic mining method to infer species phylogenies

The first step of the phylogenetic mining method is to encode the all the aligned gene data to the numeric data for the convenience of the knowledge discovery. In the data encoding, four nucleotides are encoded as the following orthogonal bases respectively and the missing nucleotides are encoded as a zero vector.

$$\begin{aligned} A &= (1,0,0,0)', \quad T = (0,1,0,0)' \\ C &= (0,0,1,0)', \quad G = (0,0,0,1)' \end{aligned} \tag{1}$$

After the encoding, the 28 selected statistically important housekeeping genes are converted to a 26876×32 numeric matrix where each gene takes certain number of rows in the matrix according to its length.

The second step is to cluster gene sequences by the SOM mining. The SOM based clustering consists of two stages. The first stage is use the SOM mining to obtain the prototypes of the whole gene set and the gene distributions of all genes on the SOM plane [11,12]. The gene distribution of a gene on the SOM plane is an approximation of its probability mass function in the sequence space [12]. In our SOM mining, we implement the *conscience* learning mechanism [13,14] to guarantee that there is a faithful representation of the underlying distribution of the input gene data set. That is, the gene distribution on the SOM plane is a faithful approximation of the probability mass function of a gene in the sequence space. The second stage is to cluster all the genes by hierarchically clustering their gene distributions on the SOM plane. The gene distribution on the SOM plane for each gene is computed by retracing the projection of each gene site on the SOM plane [12].

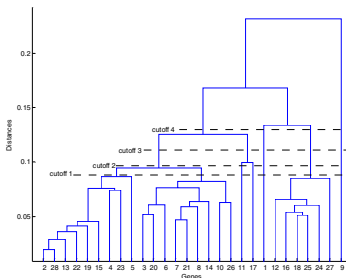
It is proved that the complexity of the SOM learning scales linearly with the number of data sample  $m$  if the number of map units  $k$  is chosen to be proportional to the  $\sqrt{m}$  [15]. According to this result, in our SOM mining, the SOM takes an input/output plane with  $k = 169 (13 \times 13)$  neurons for the 26876×32 input data matrix. Our SOM mining employs the *conscience* learning, which is a sequence learning algorithm. The sequence learning is not prone to trap in the local minimum in the learning than the batch map learning, although the latter is generally faster than the former [13,14]. The reference vectors associative with neurons on the SOM plane are initialized by the principal component analysis (PCA) instead of the random initialization for the sake of fast convergence. The neighborhood kernel function used in the SOM training is the Gaussian function. In the following hierarchical clustering, we decide the cutoff of the clustering by computing the U-matrix on the SOM plane [12,14]. For this 28 housekeeping dataset, we have 7 identified clusters in the hierarchical clustering (Figure 7).

The third step in the phylogenomic mining is to identify the phylogenetically informative genes in the gene set. It also consists of two steps. The first step is to identify the most conservative gene by finding the minimum entropy gene in the gene set. The second step is to find the genes with mostly similar sequence patterns with respect to the most conservative gene. This is equivalent to computing the relative entropy, also called the K-L distance, for all the genes with respect to the most conservative gene. The minimum entropy gene among the 28 housekeeping genes is the gene *YPR165W*. The five genes with the nearest K-L distances with the minimum entropy gene are {*YIL142*, *YOR259C*, *YPL117C*, *YLR243W*, *YIR002C*}. Among the five minimum relative entropy genes with respect to the minimum entropy gene, the gene *YLR243W* is a phylogenetically informative gene according to the SH-test, although it is not convergent under the Bayesian analysis and other four genes are convergent genes.

The fourth step is to build a “super-gene” by concatenating the phylogenetically informative genes and use the “super-gene” to infer the species phylogeny. The

“super-gene” can be constructed by concatenating genes with the nearest K-L distances in the gene set or by picking the minimum relative entropy gene from each cluster and combining them together. We already proved that the genes with nearer K-L distance to the minimum entropy gene were more likely to be phylogenetically informative by the SH-test. We concatenated the seven minimum relative entropy genes including the gene *YER165W* itself. The final tree from the Bayesian and ML analysis was a species tree with the maximum support on each branch (Figure 8). We also built the super-gene by concatenating the seven minimum relative entropy genes from each cluster. Similarly, the phylogenetic tree reconstructed from the seven minimum relative entropy gene selected from each cluster was also the species tree with the maximum support on each inferred branch. We also changed the cutoff in the hierarchical clustering for the number of clusters to 6,5,4 and built super-genes by concatenating the minimum relative entropy from each cluster. We obtained the same species tree with the maximum supports in the phylogenetic reconstruction! Figure 8 shows the species tree with maximum support in the phylogenomic mining method.

Compared with the original random gene concatenation approach [7], our method achieves even better results than the just good gene combination case! The microarray based approach not only overcomes the ad-hoc mechanism in the original method but also provides a systematic resolution to the species tree reconstruction problem from the initial data collection to phylogenetically informative gene selection before the phylogenetic analysis. Our method is easy to extend to other dataset and can avoid the prohibitive phylogenetic computing problem of the species phylogeny inference of the large number of taxa because of the phylogenetically informative gene selection mechanism.



**Fig. 7.** Hierarchical clustering of 28 housekeeping genes



**Fig. 8.** The species tree with the maximum support

## 5 Conclusions

In this work, we showed our microarray based species tree inference approach was a robust and systematic approach to infer species phylogenies than the random gene concatenation method under a same problem [7]. In the on-going work, we are integrating few more microarray datasets other than the current microarray data to select statistically important housekeeping genes for the phylogenomic mining. In the future

work, we are going to compare the clustering results between the SOM based clustering in the phylogenomic mining and the SOM clustering of microarray data themselves for the same set of genes. The SOM based clustering is a sequence based clustering and the latter SOM clustering is expression data based clustering. The comparison of two clustering results can give make the gene clustering analysis more representative and robust.

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# Penalized Independent Component Discriminant Method for Tumor Classification

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**Abstract.** This paper proposes a new method for tumor classification using gene expression data. In this method, we first employ independent component analysis (ICA) to model the gene expression data, then apply optimal scoring algorithm to classify them. To show the validity of the proposed method, we apply it to classify two DNA microarray data sets involving various human normal and tumor tissue samples. The experimental results show that the method is efficient and feasible.

## 1 Introduction

A reliable and precise classification of tumors is essential for successful diagnosis and treatment of cancer. Current methods for classifying human malignancies are mostly rely on a variety of morphological, clinical, and molecular variables. Despite the progress recently made, there are still many uncertainties in diagnosis.

With the wealth of gene expression data from microarrays being produced, more and more new prediction, classification and clustering techniques are being used for analysis of the data. Up to now, several studies have been reported on the application of microarray gene expression data analysis for molecular classification of cancer [1,2,4,6,18,19,20].

One feature of microarray data is that the number of tumor samples collected tends to be much smaller than the number of genes. The number for the former tends to be on the order of tens or hundreds, while microarray data typically contain thousands of genes on each chip. In statistical terms, it is called “large p, small n” problem [17], i.e., the number of predictor variables is much larger than the number of samples. To overcome this difficult, Ghosh [5] proposed a methodology using regularized regression models for the classification of tumors. In this literature, he focused on three types of regularized regression models, i.e., ridge regression, principal components regression and partial least squares regression. One drawback of these techniques is that only second-order statistical information of the gene data is used. However, in the task such as classification, much of the important information may be contained in the high-order relationships among samples. And thus, it is important to investigate whether or not

the generalizations of PCA, which are sensitive to high-order relationships (not just second-order relationships), are advantageous. Usually, independent component analysis (ICA) [2,15] is one of such generalizations. In this paper, we shall employ FastICA, which was proposed by Hyvärinen [10] and proven successful in many applications, to address the problems of tumor classification.

## 2 Methods

### 2.1 Independent Component Analysis

Considering an  $n \times p$  data matrix  $\mathbf{X}$ , whose rows  $\mathbf{r}_i$  ( $i = 1, \dots, n$ ) correspond to observational variables and whose columns  $\mathbf{c}_j$  ( $j = 1, \dots, p$ ) are the individuals of the corresponding variables, the ICA model of  $\mathbf{X}$  can be written as:

$$\mathbf{X} = \mathbf{A}\mathbf{S} \tag{1}$$

Without loss of generality,  $\mathbf{A}$  is an  $n \times n$  mixing matrix, and  $\mathbf{S}$  is an  $n \times p$  source matrix subject to the condition that the rows of  $\mathbf{S}$  are as statistically independent as possible. Those new variables contained in the rows of  $\mathbf{S}$  are called as ‘independent components’, i.e., the observational variables are linear mixtures of independent components. The statistical independence between variables can be quantified by mutual information  $I = \sum_k H(s_k) - H(S)$ , where  $H(s_k)$  is the marginal entropy of the variable  $s_k$ , and  $H(S)$  is the joint entropy. Estimating the independent components can be accomplished by finding the right linear combinations of the observational variables, since we can invert the mixing matrix as:

$$\mathbf{U} = \mathbf{S} = \mathbf{A}^{-1}\mathbf{X} = \mathbf{W}\mathbf{X} \tag{2}$$

There are a number of algorithms for performing ICA. In this paper, we shall employ the FastICA algorithm, which was proposed by Hyvärinen [10], to address the problems of tumor classification. In this algorithm, the mutual information is approximated by a ‘contrast function’:

$$J(s_k) = (E\{G(s_k)\} - E\{G(v)\})^2 \tag{3}$$

where  $G$  is an any nonquadratic function and  $v$  is a normally distributed variable. The interested readers can refer to literature [10] for further details.

Like PCA, ICA can remove all linear correlations. By introducing a non-orthogonal basis, it also takes into account higher-order dependencies in the data. Particularly, ICA is in a sense superior to PCA, which are just sensitive to second-order relationships of the data. And, the ICA model usually leaves some freedom of scaling and sorting by convention, the independent components are generally scaled to unit deviation, while their signs and orders can be chosen arbitrarily.



### 2.2 ICA Models of Gene Expression Data

Now let the  $n \times p$  matrix  $\mathbf{X}$  denote the gene expression data (generally speaking,  $n \ll p$ ),  $x_{ij}$  is the expression level of the  $j$ th gene in the  $i$ th assay.  $\mathbf{r}_i$  (a  $p$ -dimensional vector), the  $i$ th row of  $\mathbf{X}$ , denotes the snapshot of the  $i$ th assay (cell sample)<sup>1</sup>. Alternatively,  $\mathbf{c}_j$  (an  $n$ -dimensional vector), the  $j$ th column of  $\mathbf{X}$ , is the expression profile of the  $j$ th gene. We suppose that the data have already been preprocessed and normalized, i.e., every sample has mean zero and standard deviation one.



**Fig. 1.** The second gene expression data synthesis model. Each gene profile in the data matrix was considered to be a linear combination of underlying basis expression profiles (eigengenes) in the matrix  $\mathbf{A}$  (the columns in  $\mathbf{A}$ ). Each of the basis expression profiles was associated with a set of independent “causes (coefficient)”, given by a vector of coefficients in  $\mathbf{S}$ . The basis profiles were estimated by  $\mathbf{A} = \mathbf{W}^{-1}$ , where  $\mathbf{W}$  is the learned ICA weight matrix.

Regardless of which algorithm is used to compute ICA, we can apply ICA to model gene expression data as shown in Fig 1. In this model, the gene expression profiles (columns of  $\mathbf{X}$ ) can be regarded as points in a multidimensional space with dimensions corresponding to the number of samples. The linear ICA model  $\mathbf{X} = \mathbf{A}\mathbf{S}$  represents the gene expression profiles (the columns of  $\mathbf{X}$ ) by a new set of basis vectors (the columns of  $\mathbf{A}$ , Fig. 1). This idea is based on the assumptions that, first, the gene expression profiles are determined by a combination of hidden regulatory variables, which were called ‘expression modes’. Second, the genes’ responses to these variables can be approximated by linear functions [9,11]. Expression mode  $k$  is characterized by its profile over the samples ( $k$ th column of  $\mathbf{A}$ ) and by its linear influences on the genes ( $k$ th row of  $\mathbf{S}$ ).

### 2.3 Penalized Regression Models

In this section, we briefly outline two types of regularized regression models, i.e., ridge regression and principal component regression.

#### 2.3.1 Ridge Regression

Consider the standard regression model:

$$\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \boldsymbol{\varepsilon} \tag{4}$$

<sup>1</sup> In the gene data literature, the problem is usually formulated using the transposed matrix  $\mathbf{X}^T$ .

where  $\mathbf{y}$  is an  $n$ -dimensional response vector;  $\mathbf{X}$  is an  $n \times p$  predictor matrix;  $\boldsymbol{\beta}$  is a  $p$ -dimensional vector of unknown regression parameters;  $\boldsymbol{\varepsilon}$  is a random vector with zero mean and one variance. In this paper, because  $n$  is smaller than  $p$ , the usual ordinary least squares estimator will not be well-defined. An alternative is to use the ridge regression estimator of  $\boldsymbol{\beta}$  in equation (4):

$$\hat{\boldsymbol{\beta}} = (\mathbf{X}^T \mathbf{X} + \lambda \mathbf{I})^{-1} \mathbf{X}^T \mathbf{y} \tag{5}$$

where  $\mathbf{I}$  is a  $p \times p$  identity matrix, and  $\lambda$  a constant. The parameter  $\lambda$  controls the amount of shrinkage in the data.

### 2.3.2 Principal Component Regression

The method of principal components regression can be traced back to the literature [12]. To use this method, we first perform a singular value decomposition (SVD) of the gene data  $\mathbf{X}$ :

$$\mathbf{X} = \mathbf{U} \mathbf{D} \mathbf{V}^T \tag{6}$$

where  $\mathbf{U}$  is the  $n \times n$  singular value decomposition matrix, and it has both orthonormal rows and columns. The diagonal matrix  $\mathbf{D}$  contains the ordered eigenvalues of  $\mathbf{X} \mathbf{X}^T$  on the diagonal elements so that  $\mathbf{D} = \text{diag}(d_1, d_2, \dots, d_n)$ , where  $d_1 > d_2 > \dots > d_n > 0$ .  $\mathbf{V}$  is a  $p \times n$  matrix with orthonormal columns. Plugging this decomposition into equation (4), we have:

$$\mathbf{y} = \mathbf{X} \boldsymbol{\beta} + \boldsymbol{\varepsilon} = \mathbf{U} \mathbf{D} \mathbf{V}^T \boldsymbol{\beta} + \boldsymbol{\varepsilon} = \mathbf{H} \boldsymbol{\gamma} + \boldsymbol{\varepsilon} \tag{7}$$

where  $\mathbf{H} = \mathbf{U} \mathbf{D}$  and  $\boldsymbol{\gamma} = \mathbf{V}^T \boldsymbol{\beta}$ . We can fit the model in equation (4) using ordinary least squares and get an estimate of  $\boldsymbol{\beta}$  by multiplying  $\mathbf{V}$  to the least squares estimator of  $\boldsymbol{\gamma}$  in equation (7).

### 2.4 Optimal Scoring

In the previous section, we have described two penalized regression models that have been used successfully in other applications such as in chemometrics. However, in this paper, the goal for our interest is classification. Thus, we should firstly re-express the classification problem as a regression problem. This is done using the optimal scoring algorithm. The point of optimal scoring is to turn categorical variables into quantitative ones by assigning scores to classes (categories).

Let  $g_i$  denote the tumor class for the  $i$ th sample ( $i = 1, \dots, n$ ), we assume that there are  $G$  tumor classes so that  $g_i$  takes values  $\{1, \dots, G\}$ . We first convert  $\mathbf{g} = [g_1, \dots, g_n]^T$  into an  $n \times G$  matrix  $\mathbf{Y} = [Y_{ij}]$ , where  $Y_{ij} = 1$  if the  $i$ th sample falls into class  $j$ , and 0 otherwise. Let  $\boldsymbol{\theta}_k(\mathbf{g}) = [\theta_k(g_1), \dots, \theta_k(g_n)]^T$  ( $k = 1, \dots, G$ ) be the  $n \times 1$  vector of quantitative scores assigned to  $\mathbf{g}$  for the  $k$ th class. The optimal scoring problem involves

finding the coefficients  $\beta_k$  and the scoring maps  $\theta_k$  that minimize the following average squared residual:

$$ASR = \frac{1}{n} \sum_{k=1}^G \sum_{i=1}^n (\theta_k(g_i) - \mathbf{X}_i^T \beta_k)^2 \tag{8}$$

Let  $\Theta_{G \times J}$  ( $J \leq G - 1$ ) be a matrix of  $J$  score vectors for the  $G$  classes, i.e., its  $k$ th row is the scores,  $\theta_k(\bullet)$ . Assume that the minimization of equation (12) is subject to the constraint  $n^{-1} \|\mathbf{Y}\Theta\|^2 = 1$ , then, as mentioned by [8], the minimization of this constrained optimization problem leads to the estimates of  $\beta_k$  that are proportional to the discriminant variables in linear discriminant analysis. The interested readers can refer to the literatures[7,8].

### 2.5 Penalized Optimal Scoring for Classification

So far, we have outlined the components necessary for the implementation of our procedure. In this section, we give out our algorithm for classifying the tumor samples.

We propose to use ICA for regularizing the gene expression data and then use a penalized optimal scoring procedure for classification. The outline of our method is shown as follows:

*Step 1:* Using the ICA model  $\mathbf{X} = \mathbf{A}\mathbf{S}$  to present the gene expression data, i.e., using ICA and consensus sources algorithm to calculate the eigengenes (columns of  $\mathbf{A}$ ) and the independent coefficients (rows of  $\mathbf{S}$ ).

*Step 2:* Choose an initial score matrix  $\Theta_{G \times J}$  with  $J \leq G - 1$  satisfying  $\Theta^T D_p \Theta = I$ , where  $D_p = \mathbf{Y}^T \mathbf{Y} / n$ . Let  $\Theta_0 = \mathbf{Y}\Theta$ .

*Step 3:* Fit a multivariate penalized regression model of  $\Theta_0$  on  $\mathbf{A}$ , yielding the fitted values  $\hat{\Theta}_0$  and the fitted regression function  $\hat{\eta}_0(\mathbf{A})$ . Let  $\hat{\eta}(\mathbf{X}) = S^+ \hat{\eta}_0(\mathbf{A})$  be the vector of the fitted regression function on  $\mathbf{X}$ , where  $S^+$  is the pseudoinverse of  $\mathbf{S}$ .

*Step 4:* Obtain the eigenvector matrix  $\Phi$  of  $\Theta_0^T \hat{\Theta}_0$ , and hence the optimal scores  $\Theta_1 = \Theta\Phi$ .

*Step 5:* Let  $\eta(\mathbf{X}) = \Phi^T \hat{\eta}(\mathbf{X})$ .

What should be explained is that the objective function we are minimizing in *Step 3* is the following expression:

$$ASR = \frac{1}{n} \sum_{k=1}^G \sum_{i=1}^n (\theta_k(g_i) - \mathbf{A}_i^T \gamma_k)^2 \tag{9}$$

where  $\mathbf{A}_i$  is the  $i$ th column of  $\mathbf{A}$ ,  $\gamma_k = \mathbf{S}\beta_k$ . Another problem is how to choose the initial values for  $\Theta$ . Readers can refer to the discussions about this problem in literature [8]. In fact, our algorithm is somewhat similar to the algorithm proposed by Ghosh [5], except that we replace principal components with independent components.

Once the algorithm has been run, we now have a discriminant rule for classifying new samples. We use the nearest centroid rule to form the classifier, i.e., assign a new sample  $\mathbf{X}_{new}$  to the class  $j$  that minimizes:

$$\delta(\mathbf{X}_{new}, j) = \|\mathbf{D}(\eta(\mathbf{X}_{new}) - \bar{\eta}^j)\|^2 \tag{10}$$

where  $\bar{\eta}^j = \frac{\sum_{g_i=j} \eta(\mathbf{X}_i)}{n_j}$  denotes the fitted centroid of the  $j$ th class.  $\mathbf{D}$  is a matrix with diagonal element:

$$D_{kk} = \left(\frac{1}{\lambda_k^2(1 - \lambda_k^2)}\right)^{1/2} \tag{11}$$

where  $\lambda_k$  is the  $k$ th largest eigenvalue calculated in Step 4 of the algorithm.

### 3 Results

In this section, we shall demonstrate the efficiency and effectiveness of the proposed methodology described above by classifying two data sets with various human tumor samples.

#### 3.1 Datasets

In this study, two publicly available microarray datasets are used to study the tumor classification problem. They are colon cancer data [1], and High-grade glioma data [13], respectively. In these datasets, all data samples have already been assigned to a training set or test set.

An overview of the characteristics of all the datasets can be found in Table 1. Pre-processing of this dataset was done by setting threshold and log-transforming on the original data, similar as in the original publication. Threshold technique is generally achieved by restricting gene expression levels to be larger than 20. In other words, the expression levels which are smaller than 20 will be set to 20. Regarding the log-transformation, the natural logarithm of the expression levels usually is taken. In addition, no further preprocessing is applied to the rest of the datasets.

**Table 1.** Summary of the datasets for the two binary cancer classification problems. (Explanation of the abbreviations used in Table 1: D, datasets; TR, training set; TE, test set; C1, class 1; C2, class 2; Levels, the number of genes; M, microarray technology; T1, oligonucleotide; 1. Colon cancer data; 2. High-grade glioma data).

| D | TR |    | TE |    | Levels | M  |
|---|----|----|----|----|--------|----|
|   | C1 | C2 | C1 | C2 |        |    |
| 1 | 14 | 26 | 8  | 14 | 2000   | T1 |
| 2 | 21 | 14 | 14 | 15 | 12625  | T1 |

### 3.2 Experiments Results

We now use the proposed methodology to classify the tumor data. Since all data samples in these four datasets have already been assigned to a training set or test set, we built the classification models using the training samples, and estimated the classification correct rates using the test set.

**Table 2.** The summary of the results of the numerical experiments on four datasets

| Experiments |                                            | Colon data   |             |
|-------------|--------------------------------------------|--------------|-------------|
| No.         | Methods                                    | Training set | Test set    |
| 1           | LS-SVM linear kernel                       | 99.64±0.87   | 82.03±7.49  |
| 2           | LS-SVM RBF kernel                          | 98.33±2.36   | 81.39±9.19  |
| 3           | LS-SVM linear kernel (no regularization)   | 49.40±8.93   | 51.73±12.19 |
| 4           | PCA + FDA (unsupervised PC selection)      | 90.95±5.32   | 80.30±9.65  |
| 5           | PCA + FDA (supervised PC selection)        | 95.24±5.56   | 76.84±7.41  |
| 6           | kPCA lin + FDA (unsupervised PC selection) | 90.95±5.32   | 80.30±9.65  |
| 7           | kPCA lin + FDA (supervised PC selection)   | 95.24±5.56   | 76.84±7.41  |
| 8           | kPCA RBF + FDA (unsupervised PC selection) | 87.86±11.24  | 75.11±15.02 |
| 9           | kPCA RBF + FDA (supervised PC selection)   | 100.00±0.00  | 64.07±1.94  |
| 10          | P-RR                                       | 97.75±2.36   | 83.88±6.53  |
| 11          | P-PCR                                      | 91.25±2.02   | 85.54±4.45  |
| 12          | P-ICR                                      | 93.63±2.05   | 85.95±5.16  |
| 13          | PAM                                        | 91.50±4.29   | 83.63±5.82  |

Because the gene numbers of the last three data sets are so great that our computer (CPU: 2 GHz Pentium IV) can not process them using ridge regression model, we have not classified Glioma data using ridge regression model. On the contrary, ICA and PCA have the ability of compressing the gene expression data (as shown in Method Section), so we can use principal component regression or independent component regression to deal with large scale data.

To obtain reliable experimental results showing comparability and repeatability for different numerical experiments, this study not only uses the original division of each data set in training and test set, but also reshuffles all datasets randomly. In other words, all numerical experiments were performed with 20 random splitting of the two original datasets. And, they are also stratified, which means that each randomized training and test set contains the same amount of samples of each class compared to the original training and test set.

We used penalized independent component regression (P-ICR) proposed in this paper to analyze the four gene expression data sets. For comparison, we also used penalized ridge regression (P-RR), penalized principal component regression (P-PCR) proposed in[5], and PAM [16] to do the same tumor classification experiment.

**Table 2.** The summary of the results of the numerical experiments on four datasets (*continued*)

| Experiments |                                            | Glioma data  |             |
|-------------|--------------------------------------------|--------------|-------------|
| No.         | Methods                                    | Training set | Test set    |
| 1           | LS-SVM linear kernel                       | 90.02±14.16  | 61.25±11.75 |
| 2           | LS-SVM RBF kernel                          | 98.41±7.10   | 69.95±8.59  |
| 3           | LS-SVM linear kernel (no regularization)   | 50.79±12.75  | 48.93±10.88 |
| 4           | PCA + FDA (unsupervised PC selection)      | 92.29±7.12   | 68.72±7.24  |
| 5           | PCA + FDA (supervised PC selection)        | 92.97±10.14  | 65.52±11.01 |
| 6           | kPCA lin + FDA (unsupervised PC selection) | 92.52±6.98   | 68.31±6.78  |
| 7           | kPCA lin + FDA (supervised PC selection)   | 95.24±8.57   | 67.32±11.04 |
| 8           | kPCA RBF + FDA (unsupervised PC selection) | 94.78±9.05   | 64.20±11.19 |
| 9           | kPCA RBF + FDA (supervised PC selection)   | 96.15±7.29   | 58.13±12.24 |
| 10          | P-RR                                       |              |             |
| 11          | P-PCR                                      | 93.33±8.16   | 70.35±8.19  |
| 12          | P-ICR                                      | 91.10±9.87   | 74.30±7.30  |
| 13          | PAM                                        | 98.57±2.17   | 67.24±6.58  |

The classification results for tumor and normal tissues using our proposed penalized methods are displayed in Table 2. For each classification problem, the experimental results gave the statistical means and standard deviations of accuracy on the original data set and 20 randomizations as described above. Since the random splits for training and test set are disjoint, the results given in Table 2 are unbiased and can in general also be too optimistic.

To show the efficiency and feasibility of the method proposed in this paper, the results using other 9 methods (Methods 1-9) are also listed in Table 2 for comparison. These 9 methods can be subdivided in two steps: dimensionality reduction and classification. For dimensionality reduction, classical PCA as well as kernel PCA (with linear or RBF kernel) are used. Fisher discriminant analysis (FDA) and least squares support vector machine (LS-SVM) are then used for classification. Note that these methods and results were ever reported in literature[14], where the divisional method of each training and test data set is the same as ours. Readers can see the details about the first 9 methods from literature [14].

From Table 2 depicted above we can see that our proposed method is indeed efficient and feasible.

## 4 Conclusions

In this paper, we presented independent component analysis methods for the classification of tumors based on microarray gene expression data. The methodology involves regularizing gene expression data using ICA, followed by the classification applying penalized discriminant method. We have compared the experimental results of our method with other 12 methods, which show that our method is effective and efficient in predicting normal and tumor samples from four human tissues. Furthermore, these results hold under re-randomization of the samples.

In future works, we will in deep study the ICA model of gene expression data, how to apply the method proposed in this paper to solving multiclass problems of tumor classification, and also study how to make full use of the information contained in the gene data to restrict ICA models so that more exact prediction of tumor class can be achieved.

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# Practical Linear Space Algorithms for Computing String-Edit Distances

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**Abstract.** String-edit operations consist of insertion of a symbol, deletion of a symbol, and substituting one symbol with another. String-edit distances have been applied in problems of error correction and pattern recognition. In this paper, two practical algorithms for computing the edit distance between two strings are presented. The space complexity for the first is  $m + n + O(1)$ , where  $m$  and  $n$  are the lengths of the input strings. The second requires only  $\min(m, n) + O(1)$ .

**Keywords:** String-edit distance, time and space complexities, algorithms.

## 1 Introduction

The string-editing problem that we are dealing with here is well-known in the fields of pattern recognition [1–4], file comparison [5], spelling correction and genome study [6]. A lower bound on time-complexity was established [7]. We are given a finite set of symbols, called the alphabet, and a finite set of edit operations. Each operation is the insertion, deletion, or substitution of one symbol and each operation has a cost which is a non-negative real number. Then, given two strings generated from the alphabet, we want to find the minimum total cost of a sequence of operations to transform one string into the other by these edit operations. This minimum total cost is known as the distance between the two input strings.

Using dynamic programming approach, Wagner and Fischer [8] described Algorithm A (see below) to find the edit distance in  $O(mn)$  space as well as time, where  $m$  and  $n$  are the numbers of symbols in the first and the second input string respectively. In this paper, two practical linear-space algorithms are presented to find the distance between two strings. Algorithm B runs in  $O(m + n)$  space and  $O(mn)$  time but in actual CPU time units, it runs faster than Algorithm A. Algorithm C requires only  $O(\min(m, n))$  space, not counting the storage locations for the input strings. It runs in  $O(mn)$  time and in practice, it runs slightly faster than Algorithm A.

Edit distances has been applied to spelling correction software to identify a misspelled word's closest neighbors. For example, assuming all edit operations have the same cost of 1, the distance between the strings *December* and *ecema* is 4. It costs

1 to delete the  $D$ , 1 to change the  $b$  to  $a$ , and 2 to delete  $er$ . The total cost is 4 to change *December* to *ecema*.

In bioinformatics, a gene sequence is often coded simply as a string from the alphabet  $\{A, T, G, C\}$  of the 4 standard nucleotide bases. Human genes vary in size from a few hundred bases to more than 2 million bases. In this case, the saving in space from quadratic to linear would be tremendous. The algorithms presented here can be used to find homologous genes. Two sequences are homologous (related to each other through evolution) when they share a lot of similar subsequences. In pattern recognition, chromosomes are often represented by strings. Chan [9] used edit distance to distinguish between median and telocentric chromosomes.

## 2 Algorithm A

Let  $\Sigma$  be a finite set of symbols, i.e., the alphabet;  $\text{del}(a), a \in \Sigma$ , be a non-negative real number representing the cost of deleting  $a$  from a string;  $\text{ins}(a), a \in \Sigma$ , be a non-negative real number representing the cost of inserting  $a$  into a string; and  $\text{sub}(a, b), a, b \in \Sigma$ , be a non-negative real number representing the cost of substituting  $a$  for  $b$ . Now given two strings  $A$  and  $B$ , generated from the alphabet, find the minimum total cost to transform  $A$  into  $B$  by a sequence of these edit operations. Let  $A[i] \in \Sigma, 1 \leq i \leq m$ , be the  $i$ th symbol of  $A$  and similarly for  $B[j]$ . Wagner and Fischer described a quadratic time and space algorithm to find the distance as follows:

Algorithm A

Global inputs: del, ins, sub

Inputs: A, B

Output:  $D[m, n]$

1.  $m := \text{length}(A)$
2.  $n := \text{length}(B)$
3.  $D[0, 0] := 0$
4. for  $j := 1$  to  $n$  do  $D[0, j] := D[0, j - 1] + \text{ins}(B[j])$
5. for  $i := 1$  to  $m$  do  $D[i, 0] := D[i - 1, 0] + \text{del}(A[i])$
6. for  $i := 1$  to  $m$  do
  7. for  $j := 1$  to  $n$  do begin
  8.  $m1 := D[i - 1, j - 1] + \text{sub}(A[i], B[j])$
  9.  $m2 := D[i - 1, j] + \text{del}(A[i])$
  10.  $m3 := D[i, j - 1] + \text{ins}(B[j])$
  11.  $D[i, j] := \min(m1, m2, m3)$
  12. end
13. end

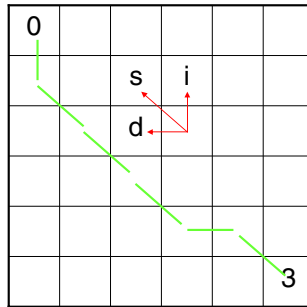
In practice, to satisfy the metric axioms, the insertion and deletion costs are the same for the same symbol, so we only need one function *indel* for both *ins* and *del*; also  $\text{sub}(a, b) = \text{sub}(b, a)$ , and  $\text{sub}(a, a) = 0$ , i.e., the distance between  $a$  and  $b$  is the same as the distance between  $b$  and  $a$ , and the distance between  $a$  and  $a$  must be zero. From the implementation point of view, if we represent a symbol by an integer which is an index to the alphabet set, we can conveniently implement  $A$  and  $B$  as

1-dimensional integer arrays of length  $m$  and  $n$  respectively and we can implement `indel` as a real vector and `sub` as a real matrix. For example, if there are five symbols in the alphabet, then the integers 1, 2, 3, 4, and 5 can represent the five symbols and `indel` is a 1-dimensional array of length 5 containing non-negative real numbers, while `sub` is a 5 by 5 symmetric matrix with 0's on the main diagonal. An APL implementation can be found in [10] with its CPU time summary statistics.

Algorithm A takes  $O(mn)$  space because the matrix  $D$  has exactly  $(m + 1)(n + 1)$  cells. Line 3 initializes the cell  $D[0, 0]$ . Line 4 is a loop initializing the rest of the cells in the 0th row. Line 5 is a loop initializing the rest of the cells in the 0th column. Lines 6 to 12 contain the double loop that fills out the remaining cells of  $D$  one by one in row-major order. Note that at any given point inside the double loop, the calculation of  $D[i, j]$  depends only on the cell directly above, on the cell directly to the north-west corner, and on the cell directly to the left. It is precisely because of this observation that linear space algorithms are possible. Fig. 1 shows this.

## Alignment Cost

- Fill out an  $(m+1) \times (n+1)$  matrix.
- $O(mn)$  time and space complexity
- Local alignment has same complexity
- $O(mn)$  space



**Fig. 1.** Initial cost is 0. Final distance is 3;  $d$  is for deletion,  $s$  for substitution, and  $i$  for insertion.

### 3 Algorithm B

Algorithm B below takes advantage of the ideas that we do not need to store the whole matrix  $D$  to calculate the distance, and that insertion and deletion are symmetric operations.

Algorithm B

Global inputs: `indel`, `sub`

Inputs:  $A, B$

Output:  $d[n]$

1.  $m := \text{length}(A)$
2.  $n := \text{length}(B)$
3.  $q := m$
4.  $d[q] := 0$
5. for  $j := 1$  to  $n$  do begin

```

6. q := q + 1
7. d[q] := d[q - 1] + indel(B[j])
8. end
9. p := m
10. for i := 1 to m do begin
11. p := p - 1
12. q := p
13. d[q] := d[q + 1] + indel(A[i])
14. for j := 1 to n do begin
15. q := q + 1
16. m1 := d[q] + sub(A[i], B[j])
17. m2 := d[q + 1] + indel(A[i])
18. m3 := d[q - 1] + indel(B[j])
19. d[q] := min(m1, m2, m3)
20. end
21. end

```

## 4 Proof of Correctness of Algorithm B

Wagner and Fischer [8] proved that Algorithm A correctly computes the edit distance between strings A and B. The correctness of Algorithm B can be proved by showing that  $d[q]$  in statement 19 of Algorithm B has the same value as  $D[i, j]$  in statement 11 of Algorithm A.

Lemma. In Algorithm B,  $q = m - i + j$ .

Proof. There are four cases which need to be considered.

First, when  $i = j = 0$ , from statement 3, we have  $q = m = m - 0 + 0$ .

Second, when  $i = 0$  and  $j > 0$ , we can see from the single loop, i.e., statements 5 to 8, that every time  $j$  is incremented by 1,  $q$  also is incremented by 1 so that  $q = m + j = m - 0 + j$ .

Third, when  $i > 0$  and  $j = 0$ , we can see from the outer loop, specifically statements 9 to 12, that every time  $i$  is incremented by 1,  $q$  is decremented by 1 so that  $q = m - i = m - i + 0$ .

Fourth, when  $i > 0$  and  $j > 0$ , we can see from statements 14 and 15 that every time  $j$  is incremented by 1,  $q$  is also incremented by 1. From the third case, we know that in statement 12,  $q = m - i$  so that in statement 15,  $q = m - i + j$ . Hence, in Algorithm B,  $q = m - i + j$  as stated in the lemma.

Theorem. For every assignment to  $D[i, j]$  in Algorithm A, there is a corresponding assignment to  $d^i[q]$  in Algorithm B, where  $q = m - i + j$  and  $d^i[q]$  is the value of  $d[q]$  at the  $i$ th pass.

Proof. There are four cases.

First, in statement 3 of Algorithm A, when  $i = j = 0$ ,  $D[0, 0] := 0$ . This is translated as statement 4 in Algorithm B as  $d[q] := 0$  where  $q = m - i + j$ .

Second, in statement 4 of Algorithm A, when  $i = 0$  and  $j > 0$ , we have

$$D[0, j] := D[0, j - 1] + \text{ins}(B[j]).$$

This is translated in the single loop, as statement 7 of Algorithm B, when  $i = 0$  and  $j > 0$ , which reads

$$d[q] := d[q - 1] + \text{indel}(B[j]).$$

Since the two lines of codes here have the same  $i$  and  $j$ , by the lemma,  $D[0, j]$  corresponds to  $d[q]$ . We know that  $\text{ins}(B[j]) = \text{indel}(B[j])$ . It remains only to be shown that  $d^0[q - 1] = D[0, j - 1]$  in order to establish  $d^0[q] = D[0, j]$ . By the lemma,  $[0, j - 1]$  maps to  $m - 0 + j - 1 = m + j - 1 = q - 1$  so that  $d^0[q - 1] = D[0, j - 1]$ . The correctness of the value in  $d^0[q - 1]$  is inherited from the correctness of the value in  $D[0, j - 1]$ . Alternatively, the correctness of the value in  $d[q - 1]$  can be seen from analyzing the single loop in Algorithm B. Each time through the  $j$  loop,  $d[q - 1]$  is simply the value of the previous calculation.

Third, when  $i > 0$  and  $j = 0$ , we compare statement 5 of Algorithm A with statement 13 of Algorithm B. The proof for this case is analogous to case two. We need only to show that  $[i - 1, 0]$  maps to  $m - (i - 1) + 0 = m - i + 1 = q + 1$ .

Lastly, we have the double loops, when  $i > 0$  and  $j > 0$ . Comparing statement 8 of Algorithm A with statement 16 of Algorithm B, we can show that  $[i - 1, j - 1]$  maps to  $m - (i - 1) + j - 1 = m - i + 1 + j - 1 = q$ . Comparing statement 9 of Algorithm A with statement 17 of Algorithm B, we can show that  $[i - 1, j]$  maps to  $m - (i - 1) + j = m - i + 1 + j = q + 1$ . Comparing statement 10 of Algorithm A with statement 18 of Algorithm B, we can show that  $[i, j - 1]$  maps to  $m - i + j - 1 = m - i + j - 1 = q - 1$ . Now we have proved the correctness of Algorithm B by finding a mapping that relates every  $[i, j]$  to  $q$  and proving that for every  $D[i, j]$  there is a corresponding identical value  $d^i[q]$ .

## 5 Space and Time Analysis of Algorithm

Apart from storage for the two input strings, the dominating data structure is the 1-d array  $d$ , which has exactly  $1 + m + n$  words. In fact, the algorithm takes  $m + n + K$  words where  $K$  is a constant independent of  $m$  and  $n$ . So the space complexity is  $O(m+n)$  which is substantially better than that of  $O(mn)$  for Algorithm A.

The most time-consuming part of the algorithm is the inner loop which is executed exactly  $mn$  times. So the time complexity is  $O(mn)$  which is the same as that of Algorithm A. But a closer analysis reveals that Algorithm B has a lower multiplier in the quadratic term, so that, in practice, Algorithm B actually takes less CPU time than Algorithm A. For Algorithm A, each time through the inner loop, there are four 2-d array indexings. For Algorithm B, each time through the inner loop, there are four 1-d array indexings plus one extra addition and one more assignment operation (statement 15).

## 6 Algorithm C

Observe that in Algorithm B, the single loop basically initializes the 0th row of  $D$  and packs it to the right end of  $d$  starting at location  $d[m]$  ending at location  $d[m + n]$ ; then at the  $i$ th pass through the double loop, it packs the  $i$ th row of  $D$  starting at location

$d[m - i]$  ending at location  $d[m - i + n]$ . At any point in time, we need only  $n+1$  words to store the current row of  $i$  plus one word for temporary storage. This observation gives rise to the following algorithm that uses a ring structure  $dd$  instead of a simple 1-d array  $d$  to calculate the values in place.

Algorithm C

Global inputs:  $indel, sub$

Inputs:  $A, B$

Output:  $z$

1.  $m := \text{length}(A)$
2.  $n := \text{length}(B)$
3. if  $m > n$  then begin
4.    $m \ n := n \ m$
5.    $A \ B := B \ A$
6. end
7.  $dd[0] := 0$
8. for  $j := 1$  to  $n$  do  $dd[j] := dd[j - 1] + indel(B[j])$
9.  $n2 := n + 2$
10.  $r := n$
11. for  $i := 1$  to  $m$  do begin
12.    $r := \text{mod}(r + 1, n2)$
13.    $dd[r] := dd[\text{mod}(r + 1, n2)] + indel(A[i])$
14.   for  $j := 1$  to  $n$  do begin
15.      $r := \text{mod}(r + 1, n2)$
16.      $m1 := dd[r] + sub(A[i], B[j])$
17.      $m2 := dd[\text{mod}(r + 1, n2)] + indel(A[i])$
18.      $m3 := dd[\text{mod}(r - 1, n2)] + indel(B[j])$
19.      $dd[r] := \min(m1, m2, m3)$
20.   end
21. end
22.  $z := dd[\text{mod}(r, n2)]$

The proof of correctness for Algorithm C is again an exercise in index mapping. It is similar to that for Algorithm B and is omitted.

## 7 Space and Time Analysis of Algorithm C

Apart from storage for the two input strings, the only data structure that depends on the input strings is the ring  $dd$  which has exactly  $n + 2$  words. Lines 3 to 6 make sure  $B$  is the shorter input string. Thus, the space complexity is  $O(\min(m, n))$ .

By inspection the time complexity is  $O(mn)$ . Experiments demonstrate that it takes about the same number of CPU seconds as that of Algorithm A.

Algorithm C takes slightly more CPU time than Algorithm B, but uses less space.

As a special case, this ring idea can also be applied to Hirschberg's Algorithm B [11] for calculating the length of maximal common subsequences. The improved version will reduce the actual local storage requirements from Hirschberg's  $2(n + 1)$  to  $n + 2$  while keeping the actual CPU time about the same.

# Edit distance

- Edit operations
  - Insert
  - Delete
  - Replace
- Edit distance: minimum number of edit operations

- AATTGGAC
- | | | |
- ACATGGAT
  
- A-ATTGGAC
- | | | |
- ACAT-GGAT

Fig. 2. Two examples of alignment

## 8 Applications

National Institute of Health (NIH), US Department of Health and Human Services, provides a service called GenBank. It contains all publicly available DNA sequences. As of April 2004, there are over 38,989,342,565 bases in 32,549,400 sequence records. Pekso [12] mentioned that “Genome sequence now accumulate so quickly that, in less than a week, a single laboratory can produce more bits of data than Shakespeare managed in a lifetime, although the latter make better reading.”

The following is a sample record. It is the *Saccharomyces cerevisiae* TCP1-beta gene. There are 1510 a’s, 1074 c’s, 835 g’s, and 1609 t’s.

```

1 gatcctccat atacaacggt atctccacct caggtttaga tctcaacaac gaaccattg
61 ccgacatgag acagttaggt atcgtcgaga gttacaagct aaaacgagca tagtcagct
121 ctgcatctga agccgctgaa gttctactaa ggggtgataa catcatccgt caagaccaa
181 gaaccgcaa tagacaacat atgtaacata tttaggatat acctcgaaaa aataaacg
241 ccacactgtc attattataa ttagaacag aacgcaaaaa ttatccacta ataattcaa
.
.
.
4921 ttttcagtgt tagattgctc taattctttg agctgttctc tcagctcctc atatTTTTc
4981 tgccatgact cagattctaa ttttaagcta ttcaatttct ctttgatc

```

Use edit distance to calculate dissimilarity between AATTGGAC and ACATGGAT. The first alignment requires change the second A from the first string to a C, a T to an A, and finally a C to T. A total of 3 edit operations are needed. The

second alignment requires deleting the C from the second string, deleting the second T from the first string and finally change the last C to T. The total costs also is 3 edit operations.

Another application is the parity string problem. Some examples of odd parity strings are 01, 010, 1011. The total number of 1's in the string is odd. Some examples of even parity strings are 000, 1111, 010100. The total number of 1's in the string is even.

The pattern language is simply the set of bit strings. There are exactly two classes: even parity and odd parity. The only edit operation we need is the substitution of a bit by another bit, where a bit can be a 1, a 0, or the empty string.

Step 1: For patterns  $p_1, p_2 \in P$ ,

let  $\Delta_1(p_1, p_2) =$  the minimum number of substitutions needed to transform  $p_1$  into  $p_2$ .

E.g., 1000 can be transformed into 0001 by deleting

the 1 at the begining and inserting an 1 at the end, so that  $\Delta_1(1000, 0001) = 2$ .

Step 2: The average intra-group distance for  $\check{Q}_1 = \{\check{q}_1, \check{q}_2, \dots, \check{q}_{n_1}\}$  is

$$\rho(\Delta_w) = \frac{2}{n_1(n_1 - 1)} \sum_{i=2}^{n_1} \sum_{j=1}^{i-1} \Delta_w(\check{q}_i, \check{q}_j).$$

Step 3: The average inter-group distance between groups  $\check{Q}_1$  and  $\check{Q}_2$  is

$$v(\Delta_w) = \frac{1}{n_1 n_2} \sum_{i=1}^{n_1} \sum_{j=1}^{n_2} \Delta_w(\check{q}_i, \check{r}_j), \text{ where } \check{Q}_2 = \{\check{r}_1, \check{r}_2, \dots, \check{r}_{n_2}\}.$$

Step 4: Stability quotient is  $Z(\Delta_w) = \frac{\rho(\Delta_w)}{v(\Delta_w)}$ .

Stability optimization minimizes  $Z(\Delta_w)$

$$\text{subject to the constraint that } \sum_{i=1}^m w_i = 1.$$

Figure 3 shows the first training set consists of two examples: 01 and 10101. The second training set consists of 11 and 00. The distance between the two set is 1/3. The cost for inserting (or deleting because of symmetry) a 0 is 0, for a 1 is 1/3, for a string 00 is 0, for 01 is 1/3, for 10 is 1/3, and for 11 is 0. So we can see that inserting or deleting 0s is free while inserting or deleting a string that contains a 1 costs 1/3 unless there are two 1s. In order to distinguish between even and odd parity strings, it makes sense that if there is an even number of 1s, the cost is free. This scheme will give the optimal objective function value of 0 as shown in Figure 3.



# Parity Answer

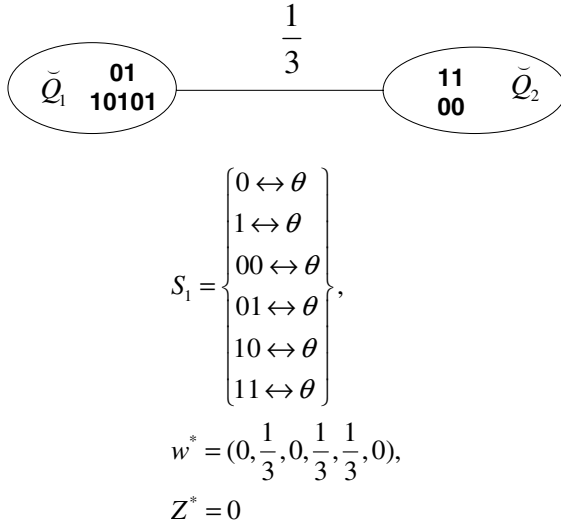


Fig. 3. Parity problem: optimal weights

## 9 Conclusion

Two useful algorithms are presented to reduce the quadratic space complexity of Wagner and Fischer’s edit distance algorithm to linear. One idea was that instead of calculated the entries of a matrix in a row-after-row order, we did it in a diagonal-after-diagonal order. Another idea to further reduce the space requirement was to treat a diagonal not as a linear array but as a ring structure. These ideas were implemented and tested in the APL language and the resulting programs were applied to the recognition of chromosomes.

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# Prediction of Protein Complexes Based on Protein Interaction Data and Functional Annotation Data Using Kernel Methods

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**Abstract.** Prediction of protein complexes is a crucial problem in computational biology. The increasing amount of available genomic data can enhance the identification of protein complexes. Here we describe an approach for predicting protein complexes based on integration of protein-protein interaction (PPI) data and protein functional annotation data. The basic idea is that proteins in protein complexes often interact with each other and protein complexes exhibit high functional consistency/even multiple functional consistency. We create a protein-protein relationship network (PPRN) via a kernel-based integration of these two genomic data. Then we apply the MCODE algorithm on PPRN to detect network clusters as numerically determined protein complexes. We present the results of the approach to yeast *Saccharomyces cerevisiae*. Comparison with well-known experimentally derived complexes and results of other methods verifies the effectiveness of our approach.

## 1 Introduction

Cellular organization and function are carried out through gene/protein interactions. With ever-increasing different types of genomic data such as DNA sequences, gene expression measurement, protein-protein interaction, and protein phylogenetic profiles, reconstruction of biological machinery from these genomic data is a crucial problem. Protein complex is a group of proteins that often interact with each other, forming a special biological chemical machinery. However, despite recent advances in detection technologies of protein interactions, only a very few of many possible protein complexes has been experimentally determined [1]. Then prediction of protein complexes is a key problem in computational biology. One of such work has been done within the PPI networks [2,3,4]. Proteins in a complex often interact with each other, so protein complexes generally correspond to dense subgraphs in the PPI networks. Recently, three approaches to network clustering including the MCODE (Molecular Complex Detection) algorithm [2], restricted neighborhood search clustering (RNSC) [3], and local clique merging algorithm (LCMA) [4] have been applied to predict protein complexes.

The MCODE algorithm utilizes connectivity values in PPI networks to identify complexes, a shortcoming of which is that its resulted clusters may be too sparse. While RNSC partitions the PPI networks using a cost function. It is a random algorithm and relatively fewer complexes can be predicted by this algorithm. LCMA algorithm which is based on local clique merging has been shown more efficient than MCODE algorithm preliminarily. It should be noted that proteins in known complexes often correspond to consistent functional annotation [2,3], so the relatively abundant functional annotation information can be employed to identify protein complexes. In the study of ref.[3], functional homogeneity has been used as a necessary condition for prediction of protein complexes.

Kernel representation of heterogeneous genomic information has already been proven to be very useful tool in computational biology [5,6]. Each type dataset can be represented by means of a kernel function, a real-valued function  $K(x, y)$ , which defines similarities between pairs of objects (genes, proteins and so on)  $x$  and  $y$ . Evaluating the kernel on all pairs of data objects yields a symmetric, positive semi-definite matrix  $\mathbf{K}$  known as the kernel matrix. The distinguished characteristic is that all types of data are represented in the unified framework even though they might be different in nature. Various kernels have been developed for various genomic data integration [5,6]. For example, the linear kernel and Gaussian kernel are natural choice for datasets which are represented by vectors, while diffusion kernel [7] has proven to be very effective for describing network data. In this study, a simple kernel representation which captures the functional consistency or even multiple functional consistency of protein complexes properly is defined naturally for the protein functional annotation data.

Here we propose an integrated approach that attempts to identify protein complexes using protein interaction data and functional annotation information. We create an integrated protein-protein relationship network (PPRN) by using the kernel methods to integrate these two genomic data. Then the network clustering method called MCODE algorithm is applied to the created PPRN network to detect numerically derived complexes. The MCODE algorithm is developed for detecting complexes in protein interaction networks and it can detect overlapping modules. So they are also suitable for finding complexes in our networks. This approach was applied to yeast *Sacchomyces cerevisiae*. The computed protein complexes show good consistency with well-known yeast protein complexes. Comparison with other methods such as the MCODE algorithm applied on PPI network directly shows the effectiveness of our approach.

## 2 Systems and Methods

### 2.1 Materials

We use yeast-related genomic data to predict protein complexes as it is currently the organism with the most comprehensive experimental datasets available publicly.

**Protein Interaction Data.** A physical network of 4713 yeast *Sacchomyces cerevisiae* proteins containing 14848 protein interactions is used in our work.

The protein-protein interactions were downloaded from the DIP database as of July 2004 and predominantly included data from large-scale experiments [8,9,10,11].

**Functional Annotation Data.** To employ the functional consistency of protein complexes, we utilize the functional annotation of *Saccharomyces cerevisiae* genes in MIPS Functional Catalog (FunCat) [12] database. FunCat is an annotation scheme for the functional description of proteins from various biology and consists of 28 main functional categories (or branches). The main branches exhibit a hierarchical, tree like structure with up to six levels of increasing specificity and 1307 functional categories are included in total. Here we utilize the functional annotation at the second levels of 68 categories (to the 4713 proteins), so that each protein corresponds to a vector of dimension 68 in which 1 or 0 represents a protein belonging to or not belonging to a category.

**Gold Standard Complex Data.** To evaluate the effectiveness of our approach for predicting protein complexes, we compare the predicted complexes of the yeast data with known protein complexes in MIPS yeast complex database [13]. In order to removing/filtering the experimentally predicted protein complexes from the dataset to a certain extent, we only use manually annotated complexes derived from literature scanning and the known Gavin benchmark data [10] as our gold standard dataset. Finally, a set  $M$  of 439 yeast complexes is used as known complexes set. Its biggest protein complex contains 88 proteins and the average size of it is 9.11.

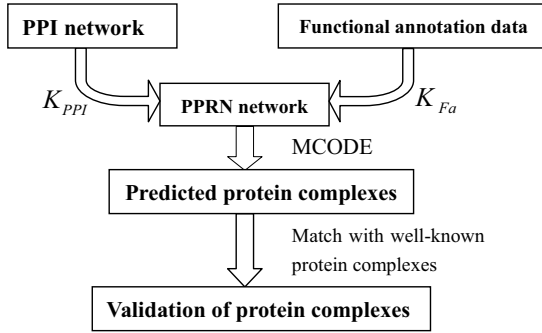
## 2.2 Methods

The outline of our method is shown in Figure 1. Two genomic datasets are represented by two kernel matrices respectively. Then a protein-protein relationship network (PPRN) is produced by integration of these two kernels. A powerful tool of detecting network modules is applied to PPRN network. The resulting modules are our numerically detected protein complexes which constitute the predicted complex set  $P$ . Validation of these complexes and comparison with related methods verifies our idea that functional annotation information is helpful for the detection of protein complexes.

**Kernel Representation and Data Integration.** In order to represent each type of genomic information uniformly, kernel representation is an efficient method [5,6]. PPI network can be represented using the diffusion kernel [7]. Let  $A$  denote the adjacency matrix of the PPI network and  $D$  denote the diagonal matrix of degrees of nodes. So the Laplacian matrix of this network is  $L = D - A$ . Then the diffusion kernel is defined as

$$K = \text{expm}(-\beta L), \quad (1)$$

where  $\text{expm}$  is a matrix exponential operation and  $\beta$  is a parameter to control



**Fig. 1.** The schematic diagram of our method for detection of protein complexes

the degree of diffusion. Then the diffusion kernel is normalized so that its all diagonal elements are one:

$$K_{PPI} = \frac{K_{ij}}{\sqrt{K_{ii}K_{jj}}}. \tag{2}$$

Functional annotation data is represented by means of liner kernel:

$$K_{fa}(i, j) = x_i \cdot x_j, \quad K_{Fa} = \frac{K_{fa}}{\max(K_{fa})}, \tag{3}$$

where  $\cdot$  means the inner product and  $\max()$  means the maximal value of the matrix.

These two kernels measure the similarity of proteins with respect to every genomic data. A new kernel defined as the sum of the two kernels:

$$K_{Int} = \frac{K_{PPI} + K_{Fa}}{2}, \tag{4}$$

is a simple approach of data integration. Although more complex kernel operation can be employed to create new integrating method, this simple kernel has been used comprehensively [5].

**Protein-Protein Relationship Network (PPRN):** Kernels describe some implicit similarity of proteins, so any protein kernel matrix  $K$  can denote a weighted/unweighted network  $G(V, E, W)/G(V, E)$  of protein-protein relationship. The nodes set  $V$  consists of all proteins, the matrix  $W$  is the value of corresponding kernel matrix which denotes the weights of the edges, and the edge set of such network is defined as:

$$E = \{(i, j) | K_{ij} \geq c\}, \tag{5}$$

where  $c$  is a parameter to control the density of the network. We denote the network of kernel  $K_{Int}$  as our protein-protein relationship network (PPRN). We

believe that a group of proteins which have large enough kernel mutually likely corresponds to a protein complex.

**MCODE Algorithm:** Bader and Hogue [2] have developed a novel graph theoretic clustering algorithm, i.e., so-called MCODE algorithm (<http://cbio.mskcc.org/bader/software/mcode/index.html>), which utilizes connectivity values in PPI networks to detect protein complexes. This algorithm is based on vertex weighting according to its local neighborhood density and then outward traversal from a dense seed protein with a high weighting value to recursively include neighboring vertices whose weight satisfies some given threshold. Here we also apply it on our PPI network and PPRN networks to evaluate our idea that functional annotation can improve the ability of prediction of complexes.

### 3 Experiments and Results

#### 3.1 Validation of Protein Complexes

We assess the precision of results of applying MCODE algorithm on our PPRN networks by using evaluation metric used in [2,4]. They used the overlap score:

$$OS(p, m) = \frac{k^2}{n_1 \times n_2} \quad (6)$$

to determine matching between a predicted complex  $p \in P$  and a known complex  $m \in M$ , where  $k$  is the size of overlap of  $p$  and  $m$  and  $n_1, n_2$  are the sizes of  $p$  and  $m$  respectively. Given a predicted complex  $p$  and a known complex  $m$ , they are considered to be matching if  $OS(p, m) \geq 0.2$ , where 0.2 is an experientially determined threshold used in [2] firstly and also was used in [4]. And then we refer the notation in [4] to define the set of true positives ( $TP$ ) as  $TP = \{p | \exists m, OS(p, m) \geq 0.2, p \in P, m \in M\}$ , and the set of false positives ( $FP$ ) as  $FP = P - TP$ . Naturally, the set of false negatives ( $FN$ ) is defined as  $FN = \{m | \forall p, OS(p, m) < 0.2, p \in P, m \in M\}$ , and the matched gold-standard complex set  $MS$  can be defined as  $MS = M - FN$ , which contains known complexes matched by predicted complexes. Then the recall (sensitivity) and precision (specificity) are defined as  $|TP|/(|TP| + |FN|)$  and  $|TP|/(|TP| + |FP|)$  respectively. The so-called F-measure which is defined as

$$F = \frac{2 \times Precision \times Recall}{Precision + Recall} \quad (7)$$

adopted in [4] is used to evaluate the performance of our approach. Just as the authors have pointed that F-measure of every method only can be taken as comparative measures rather than their real values for the incompleteness of known complexes set.

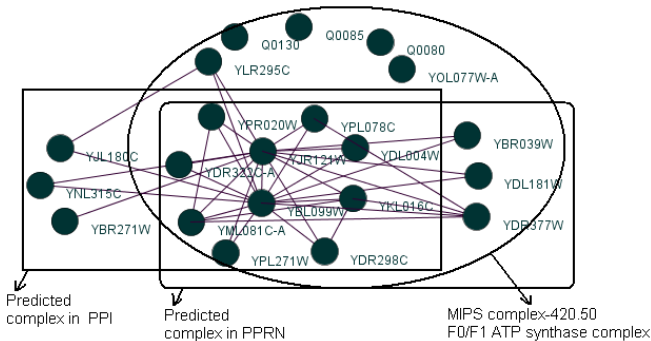
In order to further test our approach, we consider another index which measures the coverage of predicted protein complexes:

$$Cov(p, m) = \frac{k}{n_2}, \quad C_q = \{m | \exists p, Cov(p, m) \geq q, p \in P, m \in M\}, \quad (8)$$

where  $q$  is a real number between 0 and 1, the set  $C_q$  contains the known complexes whose members appear in a predicted complex above the degree  $q$ .

### 3.2 Experimental Results

Since the noise and incompleteness of known protein interaction data, our approach aims to detect more complexes through integrating functional annotation data to current protein interaction data with high recall and precision. The effectiveness of kernel methods employs the functional consistency of proteins and implicit relationship of interacting proteins. The functional annotation information can complement the absence of existing interactions and correct some false interactions. So integration of the two genomic data can enhance the robustness of network clustering method against only the high noise protein interaction data. Figure 2 shows an example of MIPS complex of size 18 and two matching complexes both of size 13 in PPI and PPRN network respectively by means of MCODE algorithm. Table 1 shows the functional annotation of proteins in Figure 2 (only the functional annotation that is labeled by at least three proteins has been shown). The predicted complex in PPRN network (with  $c = 0.24$ , see below) is contained within the known complex while for the predicted complex in PPI network only ten proteins are included in it. We can see that all the proteins in the given MIPS complex (the first 18 proteins in table 1) show high multiple functional consistency, while three proteins (the last three proteins labeled in black font) that are included in the predicted complex in PPI network but not included in the given MIPS complex do not show such multiple consistent functional annotation information. This shows our idea that known functional annotation information/functional annotation consistency is helpful for detecting complexes.



**Fig. 2.** An example: MIPS complex (MIPS-420.50)-F0/F1 ATP synthase complex and the matching complex predicted in PPI network and PPRN network respectively

In all the study, the diffusion kernel of protein interaction network is computed with  $\beta = 3$ . And then we choose  $c = 0.25$  and  $0.24$  experientially for producing two PPRN networks with 14423 and 16413 edges respectively. We



**Table 1.** Functional annotation of proteins in Figure 2

|                  |       |       |          |       |       |             |          |          |          |             |
|------------------|-------|-------|----------|-------|-------|-------------|----------|----------|----------|-------------|
| <i>Q0080</i>     | 02.11 | 02.13 | 02.45.15 |       |       | 20.01.01.01 | 20.01.15 | 20.03.22 | 20.09.04 | 34.01.01.03 |
| <i>Q0085</i>     | 02.11 | 02.13 | 02.45.15 | 14.10 | 16.07 | 20.01.01.01 | 20.01.15 | 20.03.22 | 20.09.04 | 34.01.01.03 |
| <i>Q0130</i>     | 02.11 | 02.13 | 02.45.15 | 14.10 | 16.07 | 20.01.01.01 | 20.01.15 | 20.03.22 | 20.09.04 | 34.01.01.03 |
| <i>YOL077W-A</i> | 02.11 | 02.13 | 02.45.15 |       |       | 20.01.01.01 | 20.01.15 |          | 20.09.04 |             |
| <i>YLR295C</i>   | 02.11 | 02.13 | 02.45.15 |       |       | 20.01.01.01 | 20.01.15 | 20.03.22 | 20.09.04 | 34.01.01.03 |
| <i>YBL099W</i>   | 02.11 | 02.13 | 02.45.15 |       |       | 20.01.01.01 | 20.01.15 | 20.03.22 | 20.09.04 | 34.01.01.03 |
| <i>YBR039W</i>   | 02.11 | 02.13 | 02.45.15 |       |       | 20.01.01.01 | 20.01.15 | 20.03.22 | 20.09.04 | 34.01.01.03 |
| <i>YDL004W</i>   | 02.11 | 02.13 | 02.45.15 |       |       | 20.01.01.01 | 20.01.15 | 20.03.22 | 20.09.04 | 34.01.01.03 |
| <i>YDL181W</i>   | 02.11 |       | 02.45.15 |       |       |             | 20.01.15 |          |          |             |
| <i>YDR298C</i>   | 02.11 | 02.13 | 02.45.15 |       | 16.07 | 20.01.01.01 | 20.01.15 | 20.03.22 | 20.09.04 | 34.01.01.03 |
| <i>YDR322C-A</i> | 02.11 | 02.13 | 02.45.15 | 14.10 | 16.07 |             | 20.01.15 | 20.03    | 20.09.04 |             |
| <i>YDR377W</i>   | 02.11 | 02.13 | 02.45.15 | 14.10 |       | 20.01.01.01 | 20.01.15 |          |          |             |
| <i>YJR121W</i>   | 02.11 | 02.13 | 02.45.15 |       |       | 20.01.01.01 | 20.01.15 | 20.03.22 | 20.09.04 | 34.01.01.03 |
| <i>YKL016C</i>   | 02.11 | 02.13 | 02.45.15 | 14.10 | 16.07 | 20.01.01.01 | 20.01.15 | 20.03.22 | 20.09.04 | 34.01.01.03 |
| <i>YML081C-A</i> | 02.11 | 02.13 | 02.45.15 |       |       | 20.01.01.01 | 20.01.15 |          |          |             |
| <i>YPL078C</i>   | 02.11 | 02.13 | 02.45.15 |       | 16.07 | 20.01.01.01 | 20.01.15 | 20.03.22 | 20.09.04 | 34.01.01.03 |
| <i>YPL271W</i>   | 02.11 | 02.13 | 02.45.15 |       |       | 20.01.01.01 | 20.01.15 | 20.03.22 | 20.09.04 | 34.01.01.03 |
| <i>YPR020W</i>   | 02.11 | 02.13 | 02.45.15 |       | 16.07 |             | 20.01.15 |          |          |             |
| <b>YJL180C</b>   |       |       |          | 14.10 |       |             |          |          |          |             |
| <b>YNL315C</b>   |       |       |          | 14.10 |       |             |          |          |          |             |
| <b>YBR271W</b>   |       |       |          |       |       |             |          |          |          |             |

apply the MCODE algorithm on the two networks to predict protein complexes. For comparison, we also apply it on the original protein interaction network to show the effectiveness of integration of two genomic information using kernel methods. The MCODE algorithm needs two important parameters  $w$  and  $f$  to control the number and size of resulting clusters. With respect to different networks, the optimal results will be produced by different parameter pairs [2]. We choose some parameter pairs to optimize the biological relevance.

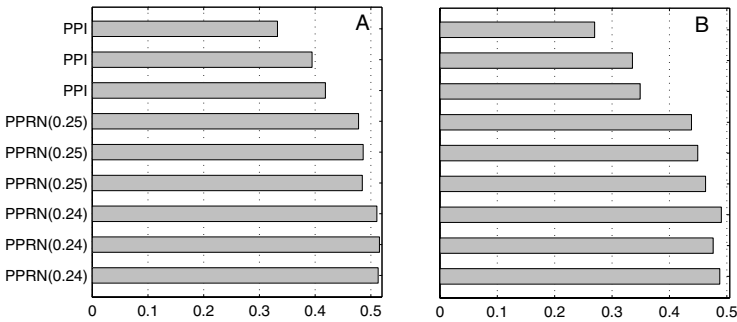
Some of the predicted complexes are of size 3, while complex with size 3 is less statistical significant, since it is easy to produce in a random graph. So we discuss two cases: one is that the predicted complex set includes complexes size of 3 and the other is not. Table 2 and Figure 3 show that the optimal results with respect to the largest F-measures with three groups  $w$  in three networks. The results show the integration of functional annotation information with PPI data can enhance the prediction results largely. More complexes are detected using the same network clustering method, and the F-measures of the two PPRN networks are also clearly higher than that of only PPI network used. For example, the F-measures of two PPRN networks are able to achieve 15.85%/22.62% higher than that of PPI networks and 32.66%/39.74% higher in two cases with  $w = 0.1$ .

We test coverage of predicted complexes, i.e., the degree to which entire complexes appear in the same predicted complexes [16]. Figure 4 shows the large improvement of our results for varying values of  $q$  in two cases respectively. For example, in our two PPRN networks, there are 139/140 gold-standard complexes (with  $w = 0.1$  and  $f = 0$ ) for which 50% or more of their members appeared in the same predicted complex, compared only 70 in the predicted results of PPI network.

King *et al.*[3] applied RNSC algorithm to predict complexes from protein interaction networks. But they only predicted 45 complexes which match 30 MIPS complexes. A new recent system LCMA algorithm based on local clique merging has been reported to be more efficient than MCODE algorithm. But we do not

**Table 2.** List of various protein-protein networks and its related results, where  $P_3$  and  $P_4$  represent predicted complexes set with minimum size 3 and 4 of their predicted complexes respectively

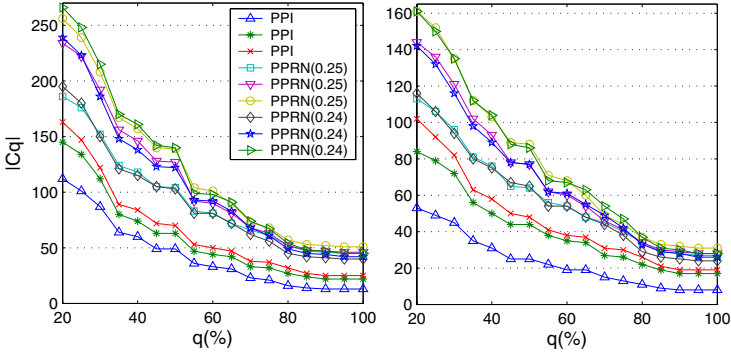
| Protein-Protein network | para( $c, \langle w, f \rangle$ ) | $ P_3 $ | $ TP $ | $ MS $ | para( $c, \langle w, f \rangle$ ) | $ P_4 $ | $ TP $ | $ MS $ |
|-------------------------|-----------------------------------|---------|--------|--------|-----------------------------------|---------|--------|--------|
| PPI (MCODE)             | (no, (0.00, 0.00))                | 157     | 104    | 74     | (no, (0.00, 0.20))                | 147     | 82     | 60     |
| PPI (MCODE)             | (no, (0.05, 0.00))                | 237     | 143    | 94     | (no, (0.05, 0.10))                | 235     | 121    | 74     |
| PPI (MCODE)             | (no, (0.10, 0.00))                | 305     | 169    | 105    | (no, (0.10, 0.25))                | 268     | 130    | 92     |
| PPRN (Int+MCODE)        | (0.25, (0.00, 0.00))              | 371     | 216    | 122    | (0.25, (0.00, 0.10))              | 357     | 192    | 112    |
| PPRN (Int+MCODE)        | (0.25, (0.05, 0.00))              | 510     | 260    | 139    | (0.25, (0.05, 0.00))              | 360     | 204    | 95     |
| PPRN (Int+MCODE)        | (0.25, (0.10, 0.00))              | 591     | 284    | 142    | (0.25, (0.10, 0.00))              | 405     | 225    | 97     |
| PPRN (Int+MCODE)        | (0.24, (0.00, 0.30))              | 377     | 239    | 119    | (0.24, (0.00, 0.30))              | 330     | 216    | 104    |
| PPRN (Int+MCODE)        | (0.24, (0.05, 0.00))              | 526     | 286    | 141    | (0.24, (0.05, 0.00))              | 368     | 223    | 93     |
| PPRN (Int+MCODE)        | (0.24, (0.10, 0.00))              | 633     | 318    | 150    | (0.24, (0.10, 0.00))              | 435     | 248    | 105    |



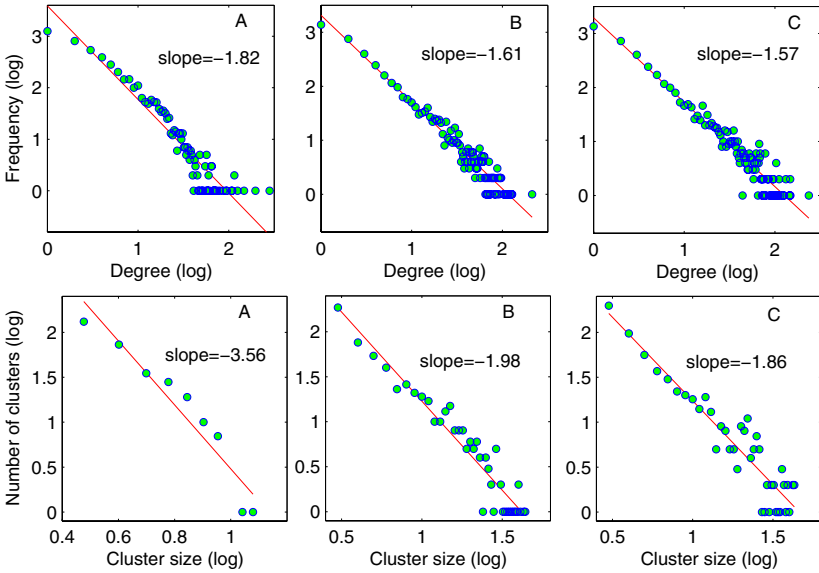
**Fig. 3.** Comparison of F-measures of applying the MCODE algorithm on various networks with various selective parameters

do direct comparison for the lack of their system, and we emphasize that our contribution is that we complement the incomplete PPI data with functional annotation information by means of kernel methods which well exploit the functional homogeneity of protein complexes or even multiple functional consistency of proteins. Our approach also predicted complexes that do not match current protein complexes set just like other methods have done. Since the known complex set is largely incomplete, these new unmatched complexes could be real complexes likely. So the actual precision of our approach would be higher than current results.

Recent studies have well shown that biological networks (eg. metabolic network, physical interaction networks) show the characteristic of scale-free networks just like many natural networks [14]. Here, we examined the scale-free characteristic of protein-protein relationship networks and size distribution of predicted complexes based on the PPI network and the two PPRN networks. On the top of Figure 5, plots A,B,C show that the probability  $P(k)$  of a node with degree in these three networks follows power law:  $P(k) \propto k^{-\gamma}$ , and at the bottom of Figure 5, plots B,C show that the size distribution of clusters (modules) of two PPRN networks also follow power law clearly, while that of PPI networks has a high slope ( $\gamma = 3.56$ )(see in plot A).



**Fig. 4.** Complex coverage:  $|C_q|$  represents the number of complexes whose member proteins appear in the same predicted complex for various  $q$  values. The left figure plots the results with all the predicted complexes including complexes of size 3, while the right removing complexes of size 3.



**Fig. 5.** On the top of the figure, plots show the degree distribution of PPI network and two PPRN networks, and at the bottom of the figure, plots show size distribution of these networks by MCODE algorithm with parameter  $w = 0.1$  and  $f = 0$

### 4 Conclusion and Discussion

In this paper, we develop a method of predicting protein complexes based on integration of two important genomic data (physical interaction data and protein

functional annotation data) by means of kernel methods. Group of genes/proteins which may correspond to functional modules have been detected comprehensively in physical interaction data [15]. However, it is often hard to conclude that these clusters/modules must have such properties. One reason is that these data is very noisy and incomplete. Prediction of protein complexes has been done based on protein interaction data such as MCODE algorithm [2], RNSC algorithm [3] and recent LCMA algorithm [4]. Detection of molecular pathways/functional modules also have been done based on integration of physical interaction data and another important genomic data—gene expression data [16]. Here, we introduce the functional annotation data to improve the limitation of the physical interaction data and this approach will employ the functional consistency of protein complexes. Kernel representation has been proven to be very useful for various types data, e.g. string, trees, network and so on. Its merit has been comprehensively used in bioinformatics, e.g. inference of biological network [5]. In this study, we will exploit the characteristic of kernel methods and combine these two data. The experimental results with yeast data show the effectiveness of our proposed method. Compared with the results of only using protein interaction data, our predicted complexes match or contain more known experimentally protein complexes. More novel predicted complexes may help biologists to detect new protein complexes experimentally. We can conclude that the combination of these two data sources can produce more better results than only using protein interaction data.

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# Prediction of Transmembrane Proteins from Their Primary Sequence by Support Vector Machine Approach

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**Abstract.** Prediction of transmembrane (TM) proteins from their sequence facilitates functional study of genomes and the search of potential membrane-associated therapeutic targets. Computational methods for predicting TM sequences have been developed. These methods achieve high prediction accuracy for many TM proteins but some of these methods are less effective for specific class of TM proteins. Moreover, their performance has been tested by using a relatively small set of TM and non-membrane (NM) proteins. Thus it is useful to evaluate TM protein prediction methods by using a more diverse set of proteins and by testing their performance on specific classes of TM proteins. This work extensively evaluated the capability of support vector machine (SVM) classification systems for the prediction of TM proteins and those of several TM classes. These SVM systems were trained and tested by using 14962 TM and 12168 NM proteins from Pfam protein families. An independent set of 3389 TM and 6063 NM proteins from curated Pfam families were used to further evaluate the performance of these SVM systems. 90.1% and 86.7% of TM and NM proteins were correctly predicted respectively, which are comparable to those from other studies. The prediction accuracies for proteins of specific TM classes are 95.6%, 90.0%, 92.7% and 73.9% for G-protein coupled receptors, envelope proteins, outer membrane proteins, and transporters/channels respectively; and 98.1%, 99.5%, 86.4%, and 98.6% for non-G-protein coupled receptors, non-envelope proteins, non-outer membrane proteins, and non-transporters/non-channels respectively. Tested by using a significantly larger number and more diverse range of proteins than in previous studies, SVM systems appear to be capable of prediction of TM proteins and proteins of specific TM classes at accuracies comparable to those from previous studies. Our SVM systems – SVMProt, can be accessed at <http://jing.cz3.nus.edu.sg/cgi-bin/svmprot.cgi>.

## 1 Introduction

Transmembrane (TM) proteins play important roles for signaling, transport, recognition and interaction with extracellular molecules [1,2,3,4]. Many TM proteins, such as G-protein coupled receptors and channels, have been explored as

therapeutic targets [5,6,7]. Membrane-bound transporters are responsible for absorption and excretion of drugs as well as cellular molecules [8,9]. Thus prediction of TM proteins is important for facilitating functional study of genomes, understanding molecular mechanism of diseases, and for searching new therapeutic targets.

Although TM proteins can be determined by experimental methods such as antibody-binding analysis and C-terminal fusions with indicator proteins [10,11], the number of experimentally determined TM proteins is significantly smaller than the estimated TM proteins in genomes [12,13,14]. Thus computational methods have been developed for facilitating the prediction of TM sequences [13,14,15,16,17,18]. These methods are capable of achieving high prediction accuracy for TM proteins and they can satisfactorily distinguish between TM and globular proteins and between TM and signal peptides. A study of 14 TM protein prediction methods using 270 helical TM chains, 1,418 signal peptides and 616 globular proteins showed that  $\sim 95\%$  TM helices are correctly predicted as TM proteins and  $\sim 92\%$  of globular proteins are correctly predicted as non-membrane (NM) proteins by the best methods [13]. A more recent study showed that  $\sim 95\%$  of the 125 TM proteins and  $\sim 99\%$  of the 526 soluble proteins can be correctly predicted by using a modified algorithm [18].

These methods have been developed and tested by using a few hundred to several hundred TM sequences and a slightly higher number of NM proteins. Our search of Swissprot database <http://www.expasy.ch/sprot> (Swissprot release 44.1, [19]) showed that there are 18358 TM protein sequences and over 134,000 NM proteins. Thus these methods may preferably need to be more adequately tested and trained by using a more diverse set of proteins. Previous studies also revealed that some TM prediction methods tend to predict proteins with more than 5 TM helices at a lower accuracy [13], which affects their prediction capability for such therapeutically and biologically relevant TM proteins as G-protein coupled receptors and certain types of channels and transporters [20]. Some methods have been found to be less capable of distinguishing between signal peptides and membrane helices [13,14]. Therefore, it is useful to evaluate the performance of TM protein prediction methods on specific therapeutically and biologically important classes of TM proteins.

The performance of a statistical learning method, support vector machine (SVM), for the prediction of TM proteins was evaluated in this work by using a diverse set of TM proteins and NM proteins. It was also tested on specific classes of TM proteins. SVM is a relatively new and promising algorithm for binary classification by means of supervised learning and it appears to be more superior than other statistical learning methods [21]. SVM has been applied to the prediction of TM proteins [15,17] and a specific TM class of G-protein coupled receptors [22] as well as other proteins [23,24,25,26,27,28,29,30,31]. These SVM TM protein prediction systems were not trained and tested by using a sufficiently diverse set of TM and NM proteins. Therefore, in this work, a large number of TM and NM proteins were used to train and test a SVM system. SVM systems were also trained and tested for the prediction of therapeutically and biologically

important individual classes of TM proteins including G-protein coupled receptors, envelope proteins, outer membrane proteins, and transporters/channels.

Many of the proteins in these four classes either contain more than 5 TM helices or have non-helix TM segments. For instance, G-protein coupled receptors contain 7 TM helices as well as intracellular and extracellular domains. Envelope proteins are located in viral lipoprotein membranes which form the outermost layer of the virion in certain viruses. Outer membrane proteins are located in the outer membrane of organelles like mitochondria, chloroplasts and some eubacteria which are surrounded by a double membrane. Almost all TM transport processes are mediated by integral TM proteins, sometimes functioning in conjunction with extracytoplasmic receptors or receptor domains as well as with cytoplasmic energy-coupling and regulatory proteins or protein domains. Thus the four classes of TM proteins have their own characteristics and they are useful for testing the performance of SVM classification.

## 2 Methods

### 2.1 Selection of Transmembrane Proteins and Non-membrane Proteins

All TM proteins used in this study were from a comprehensive search of Swissprot database (Swissprot release 44.1, TrEMBL release 27.1, [19]). A total of 18,358 TM protein sequences were obtained, which include 8,457 G-protein coupled receptors, 450 envelope proteins, 1,492 outer membrane proteins, and 980 transporters and channels. All distinct members in each group were used to construct positive samples for training, testing and independent evaluation of SVM classification system. Multiple entries for a distinct protein were evenly distributed to the training, testing, and independent evaluation set.

The negative samples, i.e. NM proteins, for training and testing our SVM classification systems were selected from seed proteins of the more than 3886 curated protein families in the Pfam database [32] that have no TM protein as a family member. Each negative set contains at least one randomly selected seed protein from each of the Pfam families. For each sub-group of non-G-protein coupled receptor, non-envelope protein, non-out membrane protein, or non-transporter/non-channel, distinct members in the other four sub-groups were added to the negative samples of each of the training, testing and independent evaluation set. For instance, distinct members of envelope proteins, out membrane proteins, transporters and channels are added into the negative samples of the G-protein coupled receptors. It is expected that the number of negative samples in each of these sub-groups may be higher than that in the group of negative samples for all TM proteins.

Training sets of both positive and negative samples were further screened so that only essential proteins that optimally represent each group are retained. The SVM training system for each group was optimized and tested by using separate testing sets of both positive and negative samples composed of all the remaining distinct proteins of a group and those outside the group respectively. The performance of



SVM classification was further evaluated by using independent sets of both positive and negative samples composed of all the remaining proteins of a group and those outside the group respectively. No duplicate protein entry was used in the training, testing and independent evaluation set for each group. For those with sufficient number of distinct members, multiple entries were assigned into each set. For those with less than three distinct members, the proteins were assigned in the order of priority of training, testing and independent evaluation set.

The number of positive and negative samples for each of the training, testing and independent evaluation set for each group of TM proteins is given in Table 1. The training set is composed of 2,105 TM and 2,563 NM proteins, 927 G-protein coupled receptors and 1,320 non-G-protein coupled receptors, 177 envelope proteins and 1,999 non-envelope proteins, 602 outer membrane proteins and 1,539 non-outer membrane proteins, and 485 transporters/channels and 3,511 non-transporters/non-channels. The testing set is comprised of 12,857 TM and 9,605 NM proteins, 4,998 G-protein coupled receptors and 13,216 non-G-protein coupled receptors, 123 envelope proteins and 7,932 non-envelope proteins, 547 outer membrane proteins and 8,385 non-outer membrane proteins, and 335 transporters/channels and 5,632 non-transporters/non-channels. The independent evaluation set is made of 3,389 TM and 6,063 NM proteins, 2,532 G-protein coupled receptors and 7,244 non-G-protein coupled receptors, 150 envelope proteins and 4,952 non-envelop proteins, 343 outer membrane proteins and 4,948 non-outer membrane proteins, and 160 transporters/channels and 3,963 non-transporters/non-channels.

## 2.2 Feature Vector Construction

Construction of the feature vector for a protein was based on the formula for the prediction of protein-protein interaction [33] and protein function prediction [23,24,25,26]. Details of the formula can be found in the respective publications and references therein. Each feature vector was constructed from encoded representations of tabulated residue properties including amino acids composition, hydrophobicity, normalized van der Waals volume, polarity, polarizability, charge, surface tension, secondary structure and solvent accessibility.

There is some level of overlap in the descriptors for hydrophobicity, polarity, and surface tension. Thus the dimensionality of the feature vectors may be reduced by principle component analysis (PCA). Our own study suggests that the use of PCA reduced feature vectors only moderately improves the accuracy. It is thus unclear to which extent this overlap affects the accuracy of SVM classification. It is noted that reasonably accurate results have been obtained using these overlapping descriptors in various protein classification studies [23,24,25,26,33,34,35,36].

## 2.3 Support Vector Machine

SVM is based on the structural risk minimization (SRM) principle from statistical learning theory [21]. SVM constructs a hyperplane that separates two different classes of feature vectors. A feature vector  $x_i$  represents the structural

and physico-chemical properties of a protein. There are a number of hyperplanes for an identical group of training data. The classification objective of SVM is to separate the training data with maximum margin while maintaining reasonable computing efficiency. SVM maps feature vectors into a high dimensional feature space using a kernel function  $K(\mathbf{x}_i, \mathbf{x}_j)$  followed by the construction of OSH in the feature space [36]. Gaussian kernel function:  $K(\mathbf{x}_i, \mathbf{x}_j) = e^{-\frac{\|\mathbf{x}_i - \mathbf{x}_j\|^2}{2\sigma^2}}$  was used in this work because it consistently gives better results than other kernel functions [35]. Linear support vector machine is applied to this feature space and then the decision function is given by:

$$f(\mathbf{x}) = \text{sign}\left[\sum_{i=1}^l \alpha_i^0 y_i K(\mathbf{x}, \mathbf{x}_i) + b\right], \tag{1}$$

where the coefficients  $\alpha_i^0$  and  $b$  are determined by maximizing the following Langrangian expression:

$$\sum_{i=1}^l \alpha_i - \frac{1}{2} \sum_{i=1}^l \sum_{j=1}^l \alpha_i \alpha_j y_i y_j K(\mathbf{x}_i, \mathbf{x}_j), \tag{2}$$

under conditions

$$\alpha_i \geq 0 \quad \text{and} \quad \sum_{i=1}^l \alpha_i y_i = 0. \tag{3}$$

Positive or negative value from Eq.(1) indicates that the vector  $\mathbf{x}$  belongs to the positive or negative class respectively. To further reduce the complexity of parameter selection, hard margin SVM with threshold was used in our own SVM program SVM\* [36].

As in the case of all discriminative methods [37], the performance of SVM classification can be measured by the quantity of true positives  $TP$ , true negatives  $TN$ , false positives  $FP$ , false negatives  $FN$ , sensitivity  $SE = TP/(TP + FN)$ , specificity  $SP = TN/(TN + FP)$ , the overall accuracy ( $Q$ ) and Matthews Correlation Coefficient ( $MCC$ ) [25] are given below:

$$Q = (TP + TN)/(TP + FN + TN + FP), \tag{4}$$

$$MCC = \frac{TP \bullet TN - FN \bullet FP}{\sqrt{(TP + FN)(TP + FP)(TN + FN)(TN + FP)}}. \tag{5}$$

### 3 Results and Discussion

The number of training and testing proteins and prediction results of specific class of TM proteins and the corresponding NM proteins are given in Table 1. In this Table, TP stands for true positive (correctly predicted TM protein of a specific TM class), FN stands for false negative (protein from a specific class

of TM proteins incorrectly predicted as a non-class-member), TN stands for true negative (correctly predicted non-class-member), and FP stands for false positive (non-class-member incorrectly predicted as a member of a specific class of TM proteins). The predicted accuracies for TM proteins, G-protein coupled receptors, envelope proteins, outer membrane proteins, and transporters/channel are 90.1%, 95.6%, 90.0%, 92.7% and 73.9% respectively. The predicted accuracies for NM proteins, non-G-protein coupled receptors, non-envelope proteins, non-outer membrane proteins, and non-transporters/non-channels are 86.7%, 98.1%, 99.5%, 86.4%, and 98.6% respectively.

**Table 1.** Prediction accuracies and the number of positive and negative samples in the training, test, and independent evaluation set of transmembrane proteins (Tr), G-protein coupled receptors (Gp), Envelope proteins (En), Outer Membrane proteins (OM), and Transporters and Channels (TC). Predicted results are given in  $TP$ ,  $FN$ ,  $TN$ ,  $FP$ , accuracy for positive samples  $SE$ , accuracy for negative samples  $SP$ , overall accuracy  $Q$  and Matthews correlation coefficient  $MCC$ . The number of positive or negative samples in the training set is  $P$  or  $N$  respectively. The number of positive or negative samples in the test and independent evaluation sets is  $TP + FN$  or  $TN + FP$  respectively. PF represents Protein Family.

| PF | Training Set |      | Test Set |      |       |      | Independent Set |      |      |      |             |             |            |       |
|----|--------------|------|----------|------|-------|------|-----------------|------|------|------|-------------|-------------|------------|-------|
|    | $P$          | $N$  | $TP$     | $FN$ | $TN$  | $FP$ | $TP$            | $FN$ | $TN$ | $FP$ | $SE$<br>(%) | $SP$<br>(%) | $Q$<br>(%) | $MCC$ |
| Tr | 2105         | 2563 | 11135    | 1722 | 8237  | 1368 | 3054            | 335  | 5254 | 809  | 90.1        | 86.7        | 87.9       | 0.749 |
| Gp | 927          | 1320 | 4993     | 5    | 13212 | 4    | 2421            | 111  | 7104 | 140  | 95.6        | 98.1        | 97.4       | 0.933 |
| En | 177          | 1999 | 112      | 11   | 7904  | 28   | 135             | 15   | 4927 | 25   | 90.0        | 99.5        | 99.2       | 0.867 |
| OM | 602          | 1539 | 547      | 0    | 8384  | 1    | 318             | 25   | 4276 | 672  | 92.7        | 86.4        | 86.8       | 0.499 |
| TC | 485          | 3511 | 331      | 4    | 5628  | 4    | 127             | 33   | 3909 | 54   | 73.9        | 98.6        | 97.8       | 0.735 |

A direct comparison with results from previous protein studies is inappropriate because of the differences in the specific aspects of proteins classified, dataset, descriptors and classification methods. Nonetheless, a tentative comparison may provide some crude estimate regarding the level of accuracy of our method with respect to those achieved by other studies. With the exception of and transporters/channels, the accuracies for various TM classes are comparable to those of  $\sim 95\%$  obtained from previous studies [13,18]. The prediction accuracy for transporters and channels is substantially lower primarily because the collected proteins in this class are not sufficiently diverse to adequately train the corresponding SVM classification system. There are 250 identified families of transporters and 115 families of channels, some of which contain substantial number of distinct proteins [20]. Thus the collected 980 transporters and channels are not enough to fully represent all of the identified families.

The prediction accuracy for the NM proteins and those of negative samples of individual TM classes is comparable to the level of  $92\% \sim 99\%$  obtained from previous studies. Unlike that of the positive samples, the prediction accuracy

for the negative samples of transporters and channels is comparable to those of other classes and those from other studies. This is because the corresponding SVM system was trained by using a diverse set of negative samples that include all representative NM proteins and proteins from other TM classes.

## 4 Conclusion

SVM appears to be capable of prediction of MP proteins and proteins in specific TM classes from a large number and diverse range of proteins at accuracies comparable to those from other studies. The prediction accuracy of SVM may be further enhanced with the improvement of SVM algorithms particularly the use of multi-class prediction models, more adequate training for distantly related proteins, and the use of the expanded knowledge about specific classes of TM proteins such as transporters and channels. To assist their evaluation and exploration, our SVM classification systems – SVMProt, can be accessed at <http://jing.cz3.nus.edu.sg/cgi-bin/svmprot.cgi>.

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# Protein Subcellular Location Prediction Based on Pseudo Amino Acid Composition and Immune Genetic Algorithm

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**Abstract.** Protein subcellular location prediction with computational method is still a hot spot in bioinformatics. In this paper, we present a new method to predict protein subcellular location, which based on pseudo amino acid composition and immune genetic algorithm. Hydrophobic patterns of amino acid couples and approximate entropy are introduced to construct pseudo amino acid composition. Immune Genetic algorithm (IGA) is applied to find the fittest weight factors for pseudo amino acid composition, which are crucial in this method. As such, high success rates are obtained by both self-consistency test and jackknife test. More than 80% predictive accuracy is achieved in independent dataset test. The result demonstrates that this new method is practical. And, the method illuminates that the hydrophobic patterns of protein sequence influence its subcellular location.

## 1 Introduction

In eukaryotic cell, newly proteins play their biological roles only if they are targeted to the correct subcellular compartments. Firstly, Nakia and Kanehisa [1] put forward computational method to predict the protein subcellular location. Recently, several approaches have been introduced on this topic, such as neural networks [2], markov chain models [3], support vector machine [4-7].

Chou and Elrod proposed covariant discriminant algorithm to predict the subcellular locations of protein from amino acid composition. Shortly after, Chou presented the concept of pseudo amino acid composition. Several powerful prediction algorithms are developed based on the concept. The most important difference among these methods is how to construct pseudo amino acid composition. Pan et al [8] used digital signal processing; Cai and Chou [9] employed domain composition; Xiao et al [10] applied complexity measure factor. Wang et al. [11] studied the problem of membrane protein type prediction by using amino acid order effect.

Here, we introduce a new method which based on pseudo-amino acid composition and immune genetic algorithm. The pseudo-amino acid composition is constructed by amino acid composition, hydrophobic patterns and approximate entropy (ApEn) [14] of protein sequence. According to the theory of Lim [12], amino acid residue hydrophobic patterns incline to occur in second structure of a protein sequence. The amino acid

residue hydrophobic value represents the major driving force behind protein folding [13]. Proteins take different functions in different subcellular. So amino acid residue hydrophobic pattern can reveal amino acid sequence. ApEn is used to evaluate the complexity of sequence.

The weight factors of pseudo amino acid composition are crucial to predict subcellular locations. In the reported literature, the method of decision weight factors is test. However, it is difficult to find all appropriate weight factors through just several tests. Here, we apply the immune genetic algorithm (IGA) to find the fittest weight factors. IGA has some new functions than simple genetic algorithm (SGA), for instance, antigen recognition, memory, and adjustment. It promotes the viability of some individuals in population by vaccination. Compared with SGA, IGA not only provides better solution, but also enhances the algorithm convergent speed.

## 2 Methods

### 2.1 Datasets

Two datasets constructed by Chou [16] are adopted to test our approach. The training dataset consists of 2191 proteins and independent dataset consists of 2494 proteins. Training dataset includes 145 chloroplast, 571 cytoplasm, 34 cytoskeleton, 49 endoplasmic reticulum, 224 extracellular, 25 golgi apparatus, 37 lysosome, 84 mitochondria, 272 nucleus, 27 peroxisome, 699 plasma membrane, and 24 vacuole. While, Independent dataset includes 112 chloroplast, 761 cytoplasm, 19 cytoskeleton, 106 endoplasmic reticulum, 95 extracellular, 4 golgi apparatus, 31 lysosome, 163 mitochondria, 418 nucleus, 23 peroxisome, and 762 plasma membrane.

### 2.2 Hydrophobic Value and Hydrophobic Patterns

There are 20 kinds of amino acid in organism which represented by characters as A, C, D, E, F, G, H, I, K, L, M, N, P, Q, R, S, T, V, W, and Y. The characters in protein sequence cannot be used to calculate the characteristic of protein sequence in mathematical computation. The protein sequence has to be described in quantitative way and each element has its corresponding numerical value. The hydrophobic value of amino acid can reflect the amino acid tends to occur in the surface of protein or in the core of protein. We select the hydrophobic value of 20 amino acids to present digitized protein sequence.

Hydrophobic patterns ( $i, i+2$ ;  $i, i+3$ ;  $i, i+2, i+4$ ;  $i, i+5$ ;  $i, i+3, i+4$ ;  $i, i+1, i+4$ ), which based on the theory of Lim[12], are classified into three types to construct pseudo amino acid composition. The hydrophobic patterns ( $i, i+2$ ) and ( $i, i+2, i+4$ ) occur more frequently in beta-sheets while the patterns ( $i, i+3$ ), ( $i, i+3, i+4$ ) and ( $i, i+1, i+4$ ) tend to occur more often in alpha-helices. The concept ( $i, i+5$ ) is an extension of the concept of the “helical wheel” or amphipathic alpha-helix[17], where the helix has a hydrophilic side with amino acid side chains extending into the solvent and a hydrophobic side where side chains extend into the non-polar core of the protein. The occurrence frequencies of three types in protein represent the folding pattern.



**Table 1.** The hydrophobic value of 20 amino acids

| Amino acid | Hydrophobic value | Amino acid | Hydrophobic value |
|------------|-------------------|------------|-------------------|
| A          | 0.62              | M          | 0.64              |
| C          | 0.29              | S          | -0.18             |
| D          | -1.05             | N          | -0.85             |
| E          | -0.87             | T          | -0.05             |
| F          | 1.19              | P          | 0.12              |
| G          | 0.48              | V          | 1.08              |
| H          | -0.4              | Q          | -0.78             |
| I          | 1.38              | W          | 0.81              |
| K          | -1.35             | R          | -1.37             |
| L          | 1.06              | Y          | 0.26              |

The selection of hydrophobic amino acids is based on the theory of Rose [18]. The amino acids that have a mean fractional area loss (on transfer from the standard state to the folded protein) of greater than 80% are included. These amino acids tend to be buried in the hydrophobic core of a protein. Seven amino acids meet this criterion: Val (V), Leu (L), Ile (I), Met (M), Cys (C), Phe (F), and Trp (W). The method of calculation occurrence frequencies of three types in protein is described as below:

Step 1: A protein sequence  $R$  is expressed by

$$R = R_1R_2R_3\dots R_N \tag{1}$$

where,  $R_i$  is the  $i$ -th residue in protein sequence.

Step 2: If the conditions  $R_i \in \Psi$  and  $R_{(i+2)} \in \Psi$  are satisfied simultaneously,

$C_{(i,i+2)} = C_{(i,i+2)} + 1$ , where  $\Psi = \{V, L, I, M, C, F, W\}$ .  $C_{(i,i+2,i+4)}$ ,  $C_{(i,i+3)}$ ,  $C_{(i,i+3,i+4)}$ ,  $C_{(i,i+1,i+4)}$ , and  $C_{(i,i+5)}$  are computed according to the rule mentioned above.

Step 3:

$$F(\alpha) = \sum_{i=1}^{i=N-2} C_{(i,i+2)} + \sum_{i=1}^{i=N-4} C_{(i,i+2,i+4)} \tag{2}$$

$$F(\beta) = \sum_{i=1}^{i=N-2} C_{(i,i+3)} + \sum_{i=1}^{i=N-4} C_{(i,i+3,i+4)} + \sum_{i=1}^{i=N-4} C_{(i,i+1,i+4)} \tag{3}$$

$$F(\gamma) = \sum_{i=1}^{i=N-2} C_{(i,i+5)} \tag{4}$$

where,  $F(\alpha)$ ,  $F(\beta)$ ,  $F(\gamma)$  denote the occurrence frequencies of alpha-helices, beta-sheets, and amphipathic alpha-helix, respectively.

### 2.3 Approximate Entropy (ApEn)

Approximate entropy is a non-negative number that denotes the complexity of time series [14]. It has been successfully applied to the field of EEG and cognition. Pincus

[15] introduced ApEn, a set of measures of system complexity closely related to entropy, which is easily applied to clinical cardiovascular and other time series. The algorithm which is described in his paper is low efficiency and slow speed. Hong et al. [19] improve the algorithm and the speed is almost enhanced by five times. We apply the new algorithm in the study. Suppose a digitized protein sequence  $X$  is expressed by  $X = u_1u_2u_3..u_N$ .

The approximate entropy can be calculated through the following steps:

Step 1: m-D (dimensional) vector  $X(i)$  is composed by sequence  $u(i)$  according to its order. Assume that  $m=2$ .

$$X(i) = [u(i), u(i + 1), \dots, u(i + m - 1)] \quad i = 1 \sim N - m + 1 \tag{5}$$

Step 2: Assume a threshold  $r$ , if both the distance  $d_{ij} = u(i) - u(j)$  and the distance  $d_{(i+1)(j+1)} = u(i + 1) - u(j + 1)$  less than  $r$  then  $C_i^m = C_i^m + 1$ . Assume  $r=0.25SD(u)$  (SD: standard difference) in calculate procedure.

$$C_i^m(r) = \sum_{j=1}^{N-m+1} d_{ij} \cap d_{(i+1)(j+1)} \tag{6}$$

$$C_i^{m+1}(r) = \sum_{j=1}^{N-m} d_{ij} \cap d_{(i+1)(j+1)} \cap d_{(i+2)(j+2)} \tag{7}$$

Step 3: Make the average value of the logarithm of  $C_i^m$  and  $C_i^{m+1}$ , the results are signed as  $\Phi^m(r)$  and  $\Phi^{m+1}(r)$

$$\Phi^m(r) = \frac{1}{N - m + 1} \sum_{i=1}^{N-m+1} \ln C_i^m(r) \tag{8}$$

$$\Phi^{m+1}(r) = \frac{1}{N - m} \sum_{i=1}^{N-m} \ln C_i^{m+1}(r) \tag{9}$$

Step 4: Approximate entropy is the difference between  $\Phi^m(r)$  and  $\Phi^{m+1}(r)$

$$ApEn(m,r) = \Phi^m(r) - \Phi^{m+1}(r) \tag{10}$$

### 2.4 Immune-Genetic Algorithm

According to the description by Chou [20], a protein can be expressed by a 24-D vector that is composed by 20 amino acid frequency and 4 characteristics of digital amino acid sequence: 3 hydrophobic patterns and ApEn value.

$$X = [x_1, x_2, \dots, x_{20}, x_{21}, x_{22}, x_{23}, x_{24}]^T \tag{11}$$

where

$$x_k = \begin{cases} \frac{f_k}{\sum_{i=1}^{20} f_i + \sum_{j=1}^4 w_j p_j} & (1 \leq k \leq 20) \\ \frac{w_k p_k}{\sum_{i=1}^{20} f_i + \sum_{j=1}^4 w_j p_j} & (21 \leq k \leq 24) \end{cases} \tag{12}$$

In Eq. (12),  $f_k$  is the normalized occurrence frequency of the 20 amino acid in the protein,  $p_i$  is the additional characteristic parameter, and  $w_i$  is the weight factor for the parameter  $p_i$ . In this study, the weight factors are calculated by IGA. The IGA is described as follows:

**Step 1: Initialization**

Generate  $N$  individuals and set search spaces for each parameter, then assign uniform random numbers within search space to each parameter of all individuals. Each individual is an antibody. The fitness function is the antigen.

**Step 2: Evaluation**

Calculate fitness  $F$  for each individual. The results are sorted. If the stop criterion is satisfied, then output the result.

**Step 3: Stopping criterion**

The implementation will be stopped if the conditions are satisfied:

The value for  $\Delta F$  does not change for several generations.

$$\Delta F(i) = F(i) - F(i-1) \tag{13}$$

where,  $F(i)$  is the fitness value for the  $i$ -th generation,  $F(i-1)$  is the fitness value for the  $(i-1)$ -th generation.

2) The number of generation reaches to upper limit  $G_{max}$

**Step 4: Update memory set**

At the first time, the memory set is empty.  $m$  individuals with the highest fitness are saved into the memory set. The memory set is composed of  $m$  individuals. In the current population, the  $d$  individuals with highest fitness are selected to replace the  $d$  individuals in memory set that are the lowest.

**Step5: Crossover and mutation**

The methods of crossover and mutation are the same as traditional genetic algorithm. After the new  $N$  individuals are generated, let the  $m$  individuals in the memory set replace the  $m$  new individuals. The new population is generated. Return to Step 2.

### 3 Results and Discussion

Evaluating an algorithm, the success prediction rate and the reliability of prediction should be considered together. Three indexes are applied to evaluate the prediction accuracy: Sensitivity ( $S_n$ ), personality ( $S_p$ ), correlation coefficient (CC).

$$S_n = \frac{t_p}{t_p + f_n} \tag{14}$$

$$S_p = \frac{t_p}{t_p + f_p} \tag{15}$$

$$CC = \frac{S_n + S_p}{2} \tag{16}$$

where,  $t_p$  is the protein number of right prediction in a subcellular group,  $f_n$  is the protein number of wrong prediction in a subcellular group,  $f_p$  is the number of the proteins in other groups to be predicted in this group. Sensitivity ( $S_n$ ) represents the accuracy, and personality ( $S_p$ ) represents the reliability in procedure of prediction.

Three methods are applied to examine the prediction quality: the self-consistent test, the jackknife test, and independent data set test. In the self-consistent test, the prediction rates for 12 subcellular locations are obtained.  $S_n$ ,  $S_p$  and  $CC$  are calculated respectively.

**Table 2.** Accuracy rate by the self-consistency test for training data set

| Subcellular location  | Sn               | Sp     | CC     |
|-----------------------|------------------|--------|--------|
| Chloroplast           | 0.8690           | 0.6774 | 0.7732 |
| Cytoplasmic           | 0.8266           | 0.8444 | 0.8355 |
| Cytoskeleton          | 1.0000           | 0.7391 | 0.8696 |
| Endoplasmic reticulum | 0.9388           | 0.6479 | 0.7933 |
| Extracellular         | 0.7009           | 0.8263 | 0.7636 |
| Golgi apparatus       | 1.0000           | 1.0000 | 1.0000 |
| Lysosomal             | 1.0000           | 0.8810 | 0.9405 |
| Mitochondrial         | 0.7976           | 0.6381 | 0.7179 |
| Nuclear               | 0.7794           | 0.8760 | 0.8277 |
| Peroxisomal           | 1.0000           | 1.0000 | 1.0000 |
| Plasma membrane       | 0.9270           | 0.9614 | 0.9442 |
| Vacuolar              | 1.0000           | 1.0000 | 1.0000 |
| Total accuracy        | 1875/2191=85.58% |        |        |

IGA is used to calculate the weight factors in Eq. 12. The fitness is a key in IGA. A prediction algorithm cannot be deemed as a good one if the self-consistency is poor. So we select overall accuracy rate of self-consistency as fitness  $F$ . Generate 20 individuals and assign uniform random numbers in search space  $[0, 1.0]$  for 4 weight factors. The crossover rate is 0.90 and the mutation rate is 0.2. When the number of generations reaches the upper limit 20, the biggest fitness  $F$  and the weight factors are obtained:  $F=0.8594$

$$\begin{cases} w_1 = 0.0050 \\ w_2 = 0.0933 \\ w_3 = 0.0612 \\ w_4 = 0.0555 \end{cases}$$

The sensitivity ( $S_n$ ), personality ( $S_p$ ), and correlation coefficient ( $CC$ ) of 12 subcellular locations are listed in Table 2. In training data set, 1875 proteins are correctly predicted and 316 proteins are incorrectly done. From the Table 2, we can see that the accuracy ( $S_n$ ) and the reliability ( $S_p$ ) are satisfied. It can be testified by the correlation coefficient ( $CC$ ).

The Jackknife test and independent data set test are the methods often used for cross-validation in statistical prediction. The jackknife is deemed as the most effective and objective method [21, 22]. Chou [23] discussed the mathematical principle of jackknife test. Accordingly, the accuracy rate of jackknife test should be calculated to measure the new predictor algorithm. The independent data set test can be used to examine the practical application of new approach. An independent data set is applied to test the new algorithm. The overall accuracy rate of jackknife on training data set and independent data set test are filled in Table 3, which are 79% and 80.27%, respectively. The results of three other test methods on same data sets are also listed in Table 3. From the table 3, we can see that the overall success rates obtained by current approach are higher than those of Cedano [24] and Pan [8], while almost the same as that of Xiao [10]. However, the accuracy rate of independent data set test is higher than that of Xiao. The accuracy rate of independent data set test obtained by the new algorithm is highest among the algorithm already known.

**Table 3.** Overall success rates by different test methods and different algorithms

| Algorithm      | Test method      |                  |                  |
|----------------|------------------|------------------|------------------|
|                | Self-consistency | Jackknife        | Independent set  |
| ProtLock       | 1006/2191=45.9%  | 971/2191=44.3%   | 1018/2491=40.8%  |
| Digital signal | 1785/2191=81.5%  | 1483/2191=67.7%  | 1842/2494=73.9%  |
| Complexity     | 1884/2191=86.0%  | 1612/2191=73.6%  | 1990/2494=79.9%  |
| This work      | 1875/2191=85.58% | 1573/2191=71.80% | 2002/2494=80.27% |

We test the accuracy rates when the number of subcellular location is reduced from 12 ( $S^{12}$ ) to seven ( $S^7$ ) and five ( $S^5$ ). The results are filled in Table 5. When the small subsets are reduced, the overall accuracy rate decreases in the self-consistency test and independent data set test. The accuracy rates of small subsets are almost 100% in self-consistency and independent data set test, such as cytoskeleton, endoplasmic reticulum, Golgi apparatus, lysosome, peroxisome, and vacuole. But in the jackknife test, the accuracy rates increase with the decreasing of subsets with little proteins number. We can see that the accuracy rate changes from 71.79% ( $S^{12}$ ) to 76.37% ( $S^7$ ) and 80.9% ( $S^5$ ). This because that the protein number in training data set is little. If the training data set is enlarged, the difference between the self-consistency test and jackknife test will be erased.

The aim of this study is to find a new method to predict protein subcellular location based on the concept of pseudo amino acid composition. Hydrophobic of amino acids determine the folding pattern of protein. Therefore, the occurrence frequencies of hydrophobic patterns in protein sequence can reflect the function of protein in some respects. The result obtained in this study proves that the new approach is practical.

**Table 4.** Overall accuracy rates by different data sets and different test methods

| Measures         | S12              | S7               | S5               |
|------------------|------------------|------------------|------------------|
| Self-consistency | 1875/2191=85.58% | 1731/2044=84.69% | 1657/1911=86.71% |
| Jackknife        | 1573/2191=71.79% | 1561/2044=76.37% | 1546/1911=80.9%  |
| Independent set  | 2002/2494=80.27% | 1924/2417=79.60% | 1766/2216=79.69% |

## 4 Conclusions

Different compartments of a cell have different physic-chemical environments. So the physic-chemical environments of the compartments of a cell will determine the subcellular location of proteins with special surface physic-chemical characteristic. The amino acid composition might carry a 'signal' in subcellular location. The additional components of pseudo amino acid composition are defined from view of surface physic-chemical characteristic of protein folding. The introduction of frequencies of alpha-helices, beta-sheets, and amphipathic alpha-helix in protein sequence as the pseudo amino acid composition can effectively reflect the sequence feature of a protein. Approximate entropy reflects the complexity of the whole protein sequence. We obtain a higher accuracy rate in predicting the subcellular location by self-consistency test, jackknife test, and independent data set test, especially the result obtained by independent data set test. As such, our new approach is quite promising and practical.

## Acknowledgments

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# SPDBS: An SBML-Based Biochemical Pathway Database System\*

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**Abstract.** Biochemical pathways such as metabolic, regulatory, or signal transduction pathways can be viewed as a complicated network of interactions among molecular species in the cell. As the amount of pathway information for various organisms is increasing very rapidly, performing various analyses on the full network of pathways for even multiple organisms can be possible and therefore developing an integrated database for storing and analyzing pathway information is becoming a critical issue. However, analyzing these networks is not easy because of the nature of the existing pathway databases, which are often heterogeneous, incomplete, and/or inconsistent. To solve this problem, SBML (Systems Biology Markup Language) – a computer-readable format for representing various biochemical pathways – has been adopted by the most of the SW packages in systems biology. We developed an SBML-based Biochemical Pathway Database System (SPDBS) that supports (1) efficient integration of the heterogeneous and distributed pathway databases, (2) prediction of the metabolic pathways for a given (non-annotated) genome sequence, (3) dynamic visualization/simulation of the pathways, (4) starting from the detailed pathway graph, build networks at different levels of representation, (5) imports/exports of SBML documents for the simulation and/or exchange of the biochemical pathways in various applications. To evaluate the system, we applied the system to the construction of pathways from its genome sequences. For the *E. coli* genome sequence, SPDBS estimates the same metabolic pathways as the original well-known *E. coli* pathway. We are applying our system to the pathway prediction of *S. chungbukensis* DJ77 and *Vibrio vulnificus* CMCP6.

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## 1 Introduction

There are three kinds of *Biochemical pathways*, metabolic, regulatory, or signal transduction pathways. The pathways can be viewed as interconnected processes including an intricate network of interactions between molecular compounds in the cell[1]. *Metabolic pathways* are responsible for carrying out the chemical reactions that provide basic biological functions (DNA, RNA, protein synthesis and degradation, energy metabolism, fatty acid synthesis, and many others). *Regulatory pathways* are responsible for converting genetic information into proteins (gene products). *Signal transduction pathways* are concerned with coordinating metabolic processes with transcription and protein synthesis. Each of these pathways has been kept in a separate (independent) database with distinct attributes even though they are related each other.

*Pathway databases* contain data of biochemical pathways which consist of two kinds of information: *biochemical components* (e.g., substrates, enzymes, products) and *their interactions* [1]. Most existing pathway databases focus on specific types of pathways rather than an integrated one: e.g., *Transpath*[2] for protein-DNA interactions, *KEGG*[5] for metabolic pathways, *EcoCyc* and *MetaCyc*[6] for *E. coli* and other organisms' metabolic pathways, *BIND*[2] for signal transduction pathways, *PathFinder*[3], *WIT*[14], *PathMAPA*[15], *BioJAKE*[17], and *MPW*[18] for metabolic pathways. Pathway databases raise many important and challenging computational and bioinformatics issues, such as querying, navigation, and visualization of the pathways; seamless integration/analysis of the heterogeneous pathway data distributed in diverse sources.

*Systems Biology Markup Language (SBML)* is a computer-readable format for representing models of various biochemical pathways[4,21]. SBML has been evolving since mid-2000 through the efforts of an international group of software developers and users. Various knowledge on the metabolic, regulatory, and signal transduction pathways can be represented in the unified SBML data model[4,21]. Recently, KEGG and EcoCyc export SBML files for the metabolic pathways, and more than 90 software products support SBML as a standard data format.

We propose an SBML-based integrated pathway database system, called *SPDBS(SBML-based Biochemical Pathway Database System)*, can access the system from <http://database.cbnu.ac.kr/SPDBS/CBPathway.jnlp>), for the integration and management of heterogeneous biochemical pathways. We adopt an object database for implementing SBML data model. Object model has been regarded as a strong tool for integrating metabolic, regulatory, and signal transduction pathways, removing the (artificial) barrier between 3 kinds of biochemical pathways, and allowing analysis of the whole pathways[1]. In SPDBS, the result of a query can be visualized dynamically and the users can edit or simulate the result pathways by using various simulation tools. For gene list or (non-annotated) sequence data, SPDBS provides dynamic pathway reconstruction or estimation by using an orthologous database[12]. Orthologous database provides useful information for estimating the function of unknown genes. To remove ambiguity in the data integration or query, gene ontology(GO)[23] has been utilized. GO guarantees consistent terminologies in the description of biological entities.

To evaluate SPDBS, we applied the system to the reconstruction of various pathways from their genome sequences or particular genes. In Section 4, we describe pathway reconstruction procedure for *E. coli* genome sequence. The result shows that SPDBS estimates the same metabolic pathways as the original one. And we reconstructed TCA cycle of *S. chungbukensis* DJ77 from non-annotated sequences using SPDBS. We verify the reconstructed pathway biologically with biologists.

The paper is organized as follows. In Section 2, we present related work. In Section 3, we describe the system architecture of the SPDBS. In Section 4, we present key functions of SPDBS and evaluation results for *E. coli* genome sequence. In Section 5, we conclude our paper.

## 2 Related Work

In this section, we discuss SBML documents, conventional pathway database systems, and orthologous databases as related issues.

The *SBML*(*Systems Biology Markup Language*) has been developed by the systems biology community[4]. It is a free and open language designed as computer readable format for representing models of biochemical reaction networks. It uses XML as its description language and UML for modeling the components. Recently, the utility *KEGG2SBML* has been released for converting metabolic pathways in KEGG (text file with pathway image) to the SBML documents[4]. SBML will be popular in the description of the pathways and protein interaction databases because there are over 90 software packages supporting SBML including KEGG and EcoCyc[4].

A wide variety of *pathway database systems* exist for the storage and retrieval of pathway information. The most widely used system is KEGG [5]. While KEGG uses static approaches for the pathway data visualization, its value lies primarily in the breadth of its content coverage. The benefits of the first-generation systems such as WIT [13], MPW [17] and EcoCyc [6], which perform limited dynamic visualization, comes mainly from their content. General purpose systems for pathway rendering include BioJake [15], PathDB [9], PathFinder [3], Pathways Database System [7], PaVESy [10], and VitaPad [11]. However, none of these systems import/export SBML documents into/from the database. Furthermore, they do not provide useful tools such as integration of the various pathways into a database, query/navigation/ modification of the pathway database, estimation/reconstruction of the pathways from gene-list or (non-annotated) genome sequence, and visualization of the pathways.

The genes that have evolved directly from an ancestral gene [12], [13] are called *orthologous genes*. They are most likely to share the function and similar sequence [18]. Therefore, orthologous genes are useful to predict the functions of unknown genes [19]. In SPDBS, orthologous genes are used in the estimation of the pathways from genome sequence in which unknown genes are included. For this purpose, we have developed an orthologous database for 88 species [12].

### 3 SPDBS: An SBML-Based Biochemical Pathway Database System

In this section, we present the system architecture of the SBML-based biochemical pathway database system (SPDBS). SPDBS has 4 layers as shown in Fig. 1; a database construction system, a local pathway database, an analysis system, and a user interface. We will introduce each layer one by one.

(a) *Database Construction System (DCS)*: DCS constructs a unified integrated database from external pathway databases. It has two kinds of tools – *SBML Converter* and *Mediators* – for the integration of heterogeneous pathway databases. The *SBML Converter* transforms SBML documents from external sources into the local object database. The *Mediator* receives various kinds of biochemical pathway data and converts them into the local object database. We have developed several mediators for various external data sources.

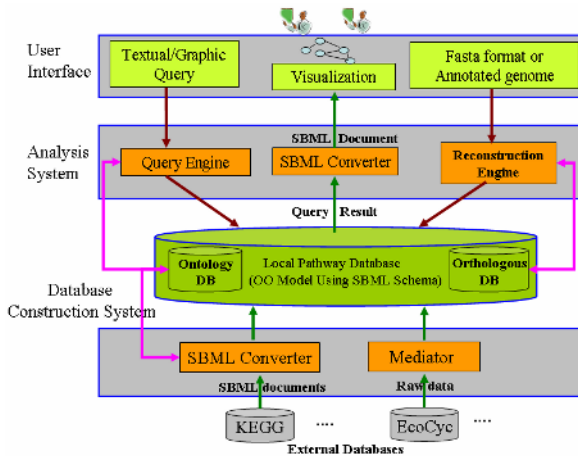


Fig. 1. System Architecture

(b) *Local Pathway Database*: It consists of an *ontology database*<sup>1</sup>, an *orthologous database* [12], and a *biochemical pathway database*. The *ontology database* is used for removing terminology ambiguity in the database construction and queries. The *orthologous database* is used for estimating the function of the unknown genes in the genome sequence. The *biochemical pathway database* stores and manages pathway information in an object data model. Although various graph-based data models (such as compound graphs, reaction graphs, bipartite graph, hyper-graphs etc.) have been proposed for representing pathway information, object data model can be seen as a generalization of the graph-based data models [1], and thus it can be regarded as a unified data model for

<sup>1</sup> Gene ontology solves terminology ambiguity problems in the database integration and query. For example, 'EC number 4.1.2.13' is represented as 'FbaA' in KEGG. But, it is represented as 'FBABSYN-MONOMER' in EcoCyc. This leads to ambiguity.



Second, user can find the pathways for given enzyme. If a user input the enzyme ‘D-ribulokinase’, then SPDBS provides corresponding pathways. User can get visualized pathway by selecting the pathway from the result panel.

Third, SPDBS constructs pathways for a given gene-list. Since multiple pathways can be generated for a single gene-list, SPDBS provides multiple visualization panels. Comparison of the result pathways can be done in the multiple visualization panels.

Fourth, SPDBS estimates pathways for genome sequence in which unknown genes are included (i.e., non-annotated genome sequence). For the genome sequence, the system searches the top-hit scored gene by using the BLAST. For the selected genes, orthologous genes are used for the prediction of their pathways. In the next section, we will describe this service in detail.

Fifth, A metabolic pathway for an increasing number of organisms reveals that even small networks can contain thousands of reactions and chemical compounds. The intimate connectivity between components complicates their decomposition into biologically meaningful sub-pathway. So, SPDBS provides a graph abstraction function. Users can make a group some nodes to an abstract node.

Sixth, SPDBS can export the result pathways into the SBML documents. From the SBML documents, the user can modify the initial quantities and kinetic laws for the pathway, and the result can be exported into the SBML documents. For the result SBML documents, simulation can be done with the help of public simulation software such as Gepasi[22] or COPASI[24].

### 4.2 Pathway Reconstruction System

For a non-annotated genome sequence, SPDBS estimates the functions of the unknown genes by using orthologous database [12] and dynamically generates metabolic pathways in a graphical form (dynamic visualization). Note that most of the existing systems including KEGG and Boehringer Mannheim support static visualization of metabolic pathways [3], [5]. This not only limits the usefulness of the systems, but also increases maintenance cost.

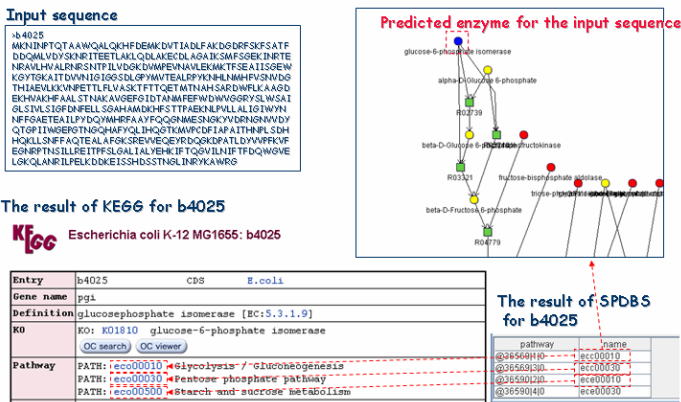


Fig. 3. Evaluation of SPDBS through comparison the results with KEGG



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22. <http://www.gepasi.org>
23. <http://www.geneontology.org>
24. COPASI, <http://www.copasi.org>

# Supervised Inference of Gene Regulatory Networks by Linear Programming

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**Abstract.** The development of algorithms for reverse-engineering gene regulatory networks is boosted by microarray technologies, which enable the simultaneous measurement of all RNA transcripts in a cell. Meanwhile the curated repository of regulatory associations between transcription factors (TF) and target genes is available based on bibliographic references. In this paper we propose a novel method to combine time-course microarray dataset and documented or potential known transcription regulators for inferring gene regulatory networks. The gene network reconstruction algorithm is based on linear programming and performed in the supervised learning framework. We have tested the new method using both simulated data and experimental data. The result demonstrates the effectiveness of our method which significantly alleviates the problem of data scarcity and remarkably improves the reliability.

**Keywords:** Systems biology, gene regulatory network, linear programming.

## 1 Introduction

Microarray technologies have produced tremendous amounts of gene expression data [1]. For example the Stanford Microarray Database (SMD) has deposited data for 60,222 experiments, from 302 labs and 36 organisms, as of March, 2006. It is necessary and important to understand gene expression and regulation through mining these data. A straightforward way on microarray data analysis is the reconstruction of gene regulatory network, which aims to find the underlying network of gene-gene interactions from the measured dataset of gene expression [2]. A wide variety of approaches have been proposed to infer gene regulatory networks from time-course data [3, 4, 5] or perturbation experiments [6], such as discrete models of Boolean networks and Bayesian networks, and



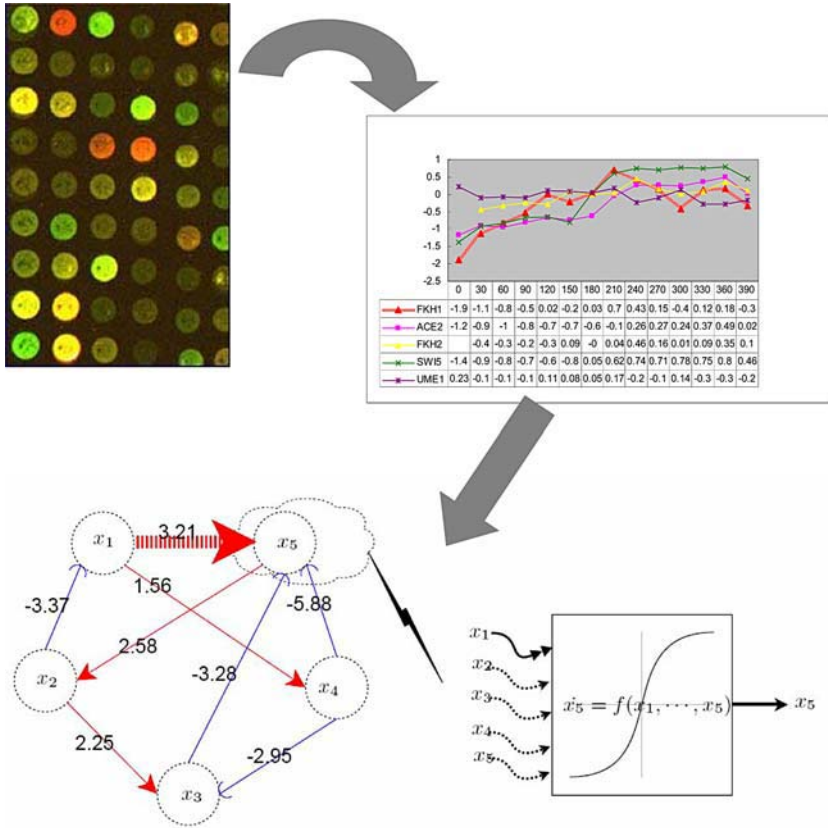
continuous models of neural networks, difference equations [1] and differential equations [7, 8].

The common problem for all these models is scarcity of data [9]. Since a typical gene expression dataset consists of relatively few time points (often less than 20) with respect to a large number of genes (generally in thousands). In other words, the number of genes far exceeds the number of time points for which data are available, making the problem of determining gene regulatory network structure a difficult and ill-posed one.

In this paper we propose a novel method to combine computational analysis of microarray dataset and biological experiment results together for inferring gene regulatory network with the consideration of sparsity of connections. We develop a supervised gene network reconstruction algorithm by linear programming based on the differential equation model [9]. The original idea of supervised learning is to incorporate the known documented interactions between genes into the parameter estimation by keeping sparsity, because many regulatory associations have been identified and recorded in literatures or databases, which are valuable information for the inference of gene networks. For example, YEASTRACT (Yeast Search for Transcriptional Regulators And Consensus Tracking, <http://www.yeasttract.com/>) is a curated repository of more than 12,500 regulatory associations between transcription factors (TF) and target genes in *Saccharomyces cerevisiae*, based on more than 900 bibliographic references. All the information in YEASTRACT will be updated regularly to match the recent literature on yeast regulatory networks. In this paper, the supervised information is adopted in the inference procedure by exploiting the general solution form of arbitrary Jacobian matrix for gene regulatory network. The proposed method theoretically ensures the derivation of feasible network structure with respect to the used dataset, thereby not only significantly alleviating the problem of data scarcity but also remarkably improving the reliability. Specifically, it can be expected that the information of documented regulatory interactions considered will lead to biologically plausible results.

## 2 Methods

In general, one can represent a gene regulatory network model as a directed graph. In this paper the graph is mathematically expressed by a set of linear differential equations. The regulatory influence between genes are formulated as a matrix and obtained as the general solution of differential equations [9]. The supervised learning information is added in the procedure of seeking general solution from particular solution by solving a linear programming problem. Fig. 1 illustrates the schematic of the proposed method. The experiment data obtained by microarray technology is analyzed and normalized, then the time course data of gene expression are collected as a matrix. The dynamic properties of the gene regulatory network are described by ordinary differential equation model. To infer the relationships between genes, previously known regulatory interactions in the network are picked as supervised information. Then novel influences (or



**Fig. 1.** Graph depiction of the strategy to construct the network by supervised learning. The experimenter measures the expression (concentration) of many or all RNA transcripts in the cells by microarray. Then time course data are collected as a matrix by normalization. The ordinary differential equation is used to infer the relationship between genes. In the network previously known regulatory influences are marked in bold and special line, novel influences (or false positives) are marked in common line. Arrows and arcs denote activation and repression, respectively.

false positives) are obtained by linear programming inference algorithm as a result. Noticed that the network structure inferred with or without supervision are all solutions of the ordinary differential equation. They differ only in that the supervised one learns the known correct information in the inference procedure and the results tend to be more consistent with the known literatures.

## 2.1 Gene Regulatory Network

The model is based on relating the changes in gene transcript concentration to each other and to the external perturbation [10]. The external perturbation means an experimental treatment that can alter the transcription rate of the genes in the cell. An example of perturbation is the treatment with

a chemical compound, or a genetic perturbation involving over-expression or down-regulation of particular genes. The ordinary differential equation is used to represent the rate of synthesis of a transcript as a function of the concentrations of every other transcript in a cell and the external perturbation:

$$\dot{x}(t) = Jx(t) + pc(t), \quad t = t_1, \dots, t_m \tag{1}$$

Where  $x(t)$  is expression level (mRNA concentrations) of gene at time point  $t$ ,  $J = (J_{ij})_{n \times n} = \partial f(x)/\partial x$  is an  $n \times n$  Jacobian matrix or connectivity matrix. Here  $p$  represents the effort of perturbation on  $x$  and  $c(t)$  represents the external perturbation at time  $t$ . By introducing  $p$  as a variable in inference, the approach can be a powerful methodology for the drug discovery process. Since it would be able to identify the compound mode of action via a time course gene expression profile and the feasibility is proved by reconstruct the SOS system in the bacteria *Escherichia coli* [6, 10].

Writing the equation (1) in a compact form for all time points using matrix notation as

$$\dot{X} = JX + PC \tag{2}$$

where  $X = (x(t_1), \dots, x(t_m))$  and  $\dot{X} = (\dot{x}(t_1), \dots, \dot{x}(t_m))$  are all  $n \times m$  matrices with the first derivative of mRNA concentration  $\dot{x}_i(t_j) = [x_i(t_{j+1}) - x_i(t_j)]/[t_{j+1} - t_j]$  for  $i = 1, \dots, n; j = 1, \dots, m$ . Suppose that there are  $s$  times external perturbation, then  $C = (c(t_1), \dots, c(t_m))$  is a  $s \times m$  matrix representing the  $s$  perturbations. The unknowns to calculate are connectivity matrix  $J$  and  $P$ .  $J$  is an  $n \times n$  connectivity matrix, composed of elements  $J_{ij}$ , which represents the influence of gene  $j$  on gene  $i$  with a positive, zero or negative sign indicating activation, no interaction and repression respectively.  $P$  is an  $n \times s$  matrix representing the effect of  $s$  perturbations on the  $n$  gene system. A non-zero element  $P_{ij}$  of  $P$  implies that the  $i$ th gene is a direct target of the  $j$ th perturbation. The equation (2) can be reformed as:

$$\dot{X} = [J \ P] \begin{bmatrix} X \\ C \end{bmatrix} \tag{3}$$

By adopting SVD to  $\begin{bmatrix} X \\ C \end{bmatrix}$ , i.e.,

$$\begin{bmatrix} X \\ C \end{bmatrix}_{m \times (n+s)}^T = U_{m \times (n+s)} E_{(n+s) \times (n+s)} V_{(n+s) \times (n+s)}^T \tag{4}$$

where  $U$  is a unitary  $m \times (n + s)$  matrix of left eigenvectors,  $E = \text{diag}(e_1, \dots, e_{(n+s)})$  is a diagonal  $(n + s) \times (n + s)$  matrix containing the  $(n + s)$  eigenvalues and  $(V)^T$  is the transpose of a unitary  $(n + s) \times (n + s)$  matrix of right eigenvectors. Then we can have a particular solution with the smallest  $L_2$  norm for the Jacobian matrix  $\hat{J} = (\hat{J}_{ij})_{n \times n}$  and  $\hat{P} = (\hat{P}_{ij})_{n \times s}$  as

$$[\hat{J} \ \hat{P}] = (\dot{X})U(E)^{-1}V^T \tag{5}$$

where  $E^{-1} = \text{diag}(1/e_i)$  and  $1/e_i$  is set to be zero if  $e_i = 0$ . Thus, the general solution of the Jacobian matrix  $J = (J_{ij})_{n \times n}$  and  $P = (P_{ij})_{n \times s}$  are

$$[J P] = [\hat{J} \hat{P}] + YV^T \quad (6)$$

$Y = (y_{ij})$  is an  $n \times (n + s)$  matrix. Solutions of (6) represent all of the possible networks that are consistent with the perturbation microarray dataset, depending on arbitrary  $Y$ . Then given the gene of interest, the supervised information can be incorporated during the process of getting the sparse structure of  $J$  by similarly solving linear programming as described in 2.2.

## 2.2 Supervised Learning by Linear Programming

With the general solution expression of (6), the next step is to pick a biologically meaningful solution by determining variable  $Y$ . In [11], the objective is to make the zero elements of  $J$  as much as possible. Though the inferred network is sparse in some sense, it is still a heuristic idea and cannot be biologically ensured. In this paper we add the supervised information during the inference process of the network structure. This strategy will drive the network toward the direction in a more biological meaning way.

Suppose that the known information of gene regulatory network is expressed by  $K$ , which is an  $n \times n$  sparse matrix. If the element  $K_{ij}$  is nonzero, it means that gene  $j$  has regulatory influence (the activation or depression depends on the sign of  $K_{ij}$ ) on gene  $i$  and this interaction is assumed to be revealed by biological experiments. We will discuss how to incorporate these valuable information in the inference of whole network by linear programming formulation.

The  $\hat{J}$  is the particular solution of the microarray dataset by SVD. The information of  $K$  is incorporated in the general solution  $J = (J_{ij})_{n \times n}$  by a proper  $Y$  such that

$$[J P] = [\hat{J} \hat{P}] + YV^T, \quad (7)$$

and at the same time the following conditions are satisfied

$$(J_{ij})_{n \times n} = (K_{ij})_{n \times n}, \quad K_{ij} \neq 0 \quad (8)$$

Considering the  $L_1$  problem:

$$\min_Y |[ (K - \hat{J}) \hat{P} ] + Y^k V^T | \quad (9)$$

where  $\hat{J}$ ,  $K$ ,  $\hat{P}$  and  $V^T$  are given. Without loss of generality, the problem is expressed as the standard form

$$\min_X |AX - B| \quad (10)$$

where the coefficient  $A$  is an  $n \times (n + s) \times nl$  matrix, and  $l$  is the number of zero elements in  $E^{-1}$  in (4).  $X$  and  $B$  are  $l \times n$  and  $(n + s) \times n$  matrices, respectively. In fact we Do not need to solve such a large LP problem. Observing that  $A$  has a special structure as

$$A = \begin{bmatrix} A_1 & & & \\ & A_2 & & \\ & & \dots & \\ & & & A_n \end{bmatrix}$$

The size of  $A_i, i = 1, 2, \dots, n$  is  $(n + s) \times l$ . With the correspondingly decomposing  $X = [X_1, X_2, \dots, X_n]$  and  $B = [B_1, B_2, \dots, B_n]$ , the solution of the raw problems (10) can be obtained by solving the following  $n$  small problems:

$$\min_{X_i} |A_i X_i - B_i| \quad i = 1, 2, \dots, n \tag{11}$$

where the dimensions of  $A_i, X_i$  and  $B_i$  are  $n \times l, l \times 1$  and  $n \times 1$ , respectively. Clearly the decomposition scheme reduces the storage space from about  $O(n^4)$  to  $O(n^2)$  and requires  $O(n^4)$  computations. Furthermore, it provides the formulation for parallel computation so as to rapidly find regulatory relationship of the interested gene in a high priority. i. e. the regulatory influence relationship of a designated gene can be obtained independently by solving a small scale L1 problem. Without loss of generality, only gene  $i$  is to be considered in the following inference algorithm.

Noticing that  $B_i = -\hat{J}_i + K_i$  ( $B_i, \hat{J}_i$  and  $K_i$  are the  $i$ th row of the matrix  $B, \hat{J}$  and  $K$ , respectively), let  $I = \{j | K_{ij} \neq 0\}$  and  $|I| = q$ , by introducing  $2(n - q)$  slack variables  $u_j, v_j, j \in \{1, 2, \dots, n\} \setminus I$ , the L1 problem

$$\min_{x_{ij}} \sum_{j=1}^n |\sum_{k=1}^l a_{ik} x_{ik} - \hat{J}_{ij} + K_{ij}| \tag{12}$$

is equivalent to the linear programming model as follows:

$$\begin{aligned} \min_{x_{ij}, u_j, v_j} \quad & \sum_{j \in I} (u_j + v_j) & (13) \\ \text{s.t.} \quad & \sum_{k=1}^l a_{ik} x_{ik} - \hat{J}_{ij} + K_{ij} = u_j - v_j, \quad j \in \{1, 2, \dots, n\} \setminus I \\ & \sum_{k=1}^l a_{ik} x_{ik} = \hat{J}_{ij}, \quad j \in I \\ & u_j, v_j \geq 0, \quad j \in \{1, 2, \dots, n\} \setminus I \\ & x_{ij} \in R, \quad j \in \{1, 2, \dots, n\} \end{aligned}$$

The variables need to be solved are  $x_{i1}, x_{i2}, \dots, x_{il}, u_1, v_1, \dots, u_{n-q}, v_{n-q}$  and the total number is  $2n - 2q + l$ . There are  $n$  equality constraints and  $2(n - q)$  inequality constraints. The LP problem for such a scale can be dealt directly by simplex method.

In the above linear programming formulation, the supervised information is incorporated through the first  $n - q$  equality constraints. If a little supervised information is added ( $q$  is small), the LP will generally give the unique solution which is a particular solution and satisfies  $(J_{ij})_{n \times n} = (K_{ij})_{n \times n}, K_{ij} \neq 0$ . But when much supervised information is applied to the gene regulatory system ( $q$  is large), the LP will give an approximate solution due to redundant constraints. In this case the system is over-determined and not all  $(J_{ij})_{n \times n} = (K_{ij})_{n \times n}, K_{ij} \neq 0$  are satisfied. The answer of how much supervised information should be incorporated in the inference depends on the inherent degree of freedom depicted by

*l*. For example in a large-scale gene network, the time course data is relatively scarce ( $l \approx n$ ) and much supervised information can be added. As reported in [11] for a large system, the smallest number of time points needed is  $O(\log n)$  to reconstruct the  $n \times n$  connectivity matrix for an  $n$ -gene network. Hence, the proper incorporation of known information of interactions in the inference algorithm will alleviate the requirement and dependence on high quality microarray data greatly.

Next we want to further address how to set values for matrix  $K$  from know information. In our model the knowledge of gene regulatory network is expressed and incorporated by matrix  $K$ . If the element  $K_{ij}$  is nonzero, it means that gene  $j$  has regulatory influence on gene  $i$ . The activation or depression role differs on the sign of  $K_{ij}$ . It is better to provide the quantitative strength of the know regulatory interactions, but many constraints are basically all qualitative instead of quantitative in the databases or literatures though it is true that they are readily available. You may know gene  $i$  activates gene  $j$ , but the quantitative relationship as described by the  $K_{ij}$  is not known. The feasible way is to assign a constant to  $K_{ij}$  and use its sign to indicate activation or depression relationship. Since in some meaning, the major function of element  $k_{ij}$  is to introduce constraints in the linear programming and this function can be preformed by keeping it a constant. In the long run, a systematic search/protocol or a soft (boundary) constraint can be developed. In this paper, The  $k_{ij} = 1$  or  $k_{ij} = -1$  are simply set to know activation or regression regulatory interaction in our experiments using biological microarray data.

### 3 Results

In this section, we first report on simulated numerical test that we have designed to benchmark our method by using supervised inference strategy. Then we will describe the gene regulatory network inference using yeast microarray gene expression data. As analyzed in Methods section, when no supervised information is applied, our method is similar to the method of [11], which can recover the network connectivity from gene expression measurements in the presence of noise by singular value decomposition (SVD) and regression. With supervised information, we can further infer the network structure in a more accurate and robust manner. In this section, only preliminary results are given for incorporating supervised information by single microarray dataset, the experiments of gene network inference by perturbation dataset and multiple datasets can be conducted similarly.

#### 3.1 Simulated Data

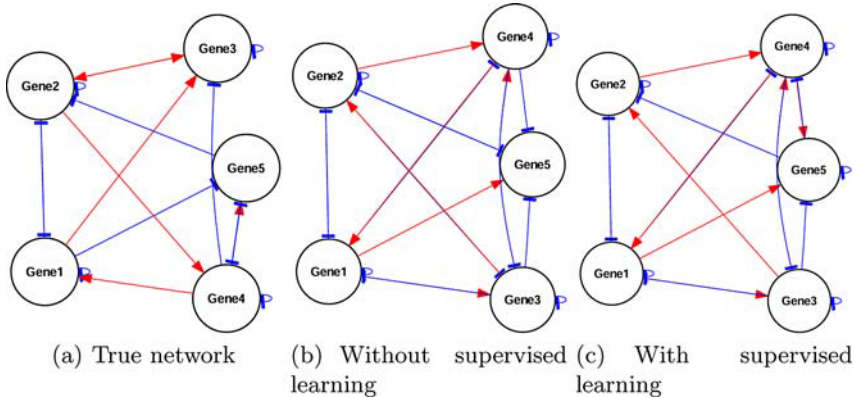
The first example is a small simulated network with five genes governed by

$$\begin{aligned}\dot{x}_1(t) &= -x_1(t) - 0.2x_2(t) + 0.5x_4(t) + \xi_1(t), \\ \dot{x}_2(t) &= -0.8x_1(t) - 1.5x_2(t) + x_3(t) - 0.5x_5(t) + \xi_2(t), \\ \dot{x}_3(t) &= 0.6x_1(t) + 0.2x_2(t) - x_3(t) - 0.3x_4(t) + \xi_3(t), \\ \dot{x}_4(t) &= 0.9x_2(t) - x_4(t) - 1.5x_5(t) + \xi_4(t), \\ \dot{x}_5(t) &= -0.2x_1(t) + 0.7x_4(t) - 1.5x_5(t) + \xi_5(t),\end{aligned}$$

where  $x_i$  reflects the expression level of the gene- $i$  and  $\xi_i(t)$  represents noise for  $i = 1, 2, 3, 4, 5$ .

To test our method, we randomly choose the initial condition of the system and take several points of  $x$  as a measured time-course dataset. In our simulated example, we obtained a dataset with 4 time points, and applied our method to reconstruct the connectivity matrix or the Jacobian matrix  $J$ . We set all of noises  $\xi_i(t), i = 1, 2, 3, 4, 5$  obeying normal distribution in the simulated example with noise level of  $N(0, 0.005)$ . And the supervised information  $K$  is incorporated by fixing  $K_{2,5} = -0.5$  and  $K_{5,4} = 0.7$ , which means the depression influence of gene 5  $\rightarrow$  gene 2 and the activation influence of gene 4  $\rightarrow$  gene 5 are measured and known.

The numerical results are depicted in Figure 2, which shows the reconstructed networks without and with supervised information, respectively. Clearly with the supervised information, it infers the network more accurately. Without supervised information (Fig. 2 (b)), the strong self repressive relation of gene  $x_5$ , the activation relation between gene  $x_4$  and gene  $x_5$  are neglected. When the supervised information is used, the topology of the network becomes correct and the predicted connectivity matrix, which represents the strengths among gene interactions, is very close to the true one (Fig. 2 (c)). Such results imply that our method is able to infer the solution of the highly under-determined problem in an accurate manner when a sufficient number of known interactions are available even although the microarray dataset has only a few time points.

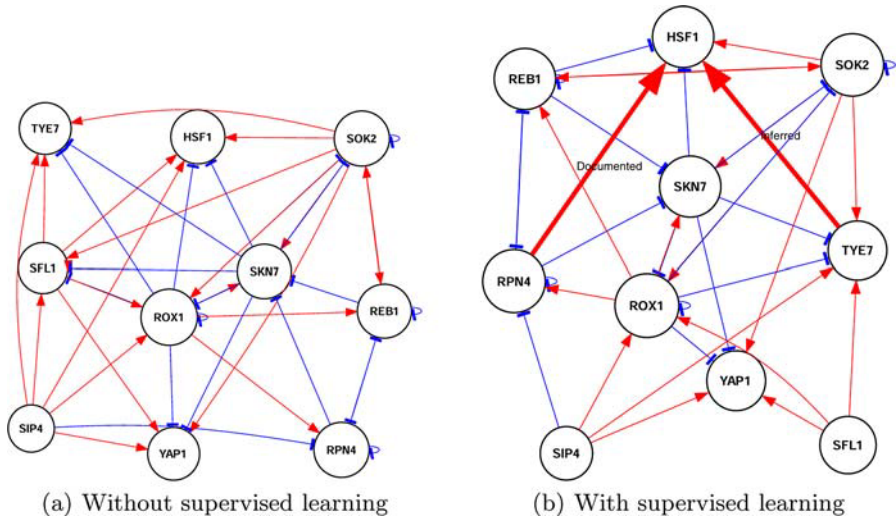


**Fig. 2.** Regulatory network reconstruction for the simulated example with 5 genes. Activation is shown in red arrow and repression in blue arc.

### 3.2 Application to Experimental Data

We applied our method using experimental data. To ensure high quality of the data, we only used microarray experimental data generated from whole genome Affymetrix chips, instead of any oligo or cDNA array data. The experiments are conducted to test our method using a small number of genes of Heat-Shock

Response data for yeast. We created an input dataset for 10 transcription factors related to heat-shock response in yeast *Saccharomyces cerevisiae*. 2 out of the 10 transcription factors (HSF1 and SKN7) are known to be directly involved in heat shock response. HSF1 and SKN7 each are known to regulate 4 other transcription factors among the ten.  $\text{TYE7} \rightarrow \text{HSF1}$  and  $\text{RPN4} \rightarrow \text{HSF1}$  are documented known regulation. This information was obtained from YEASTRACT (<http://www.yeasttract.com/index.php>). For the 10 transcription factors, we used microarray dataset at the Stanford Microarray Database (<http://smd.stanford.edu/>) (y14, with 5 time points) for gene expression under heat shock conditions. We applied the proposed method to this dataset. As indicated in 2.2 subsection, the  $k_{ij} = 1$  or  $k_{ij} = -1$  are simply set to know regulatory interaction in our real data experiments. As shown in Fig. 3, the prediction succeeded in reconstructing 2 edges of the network which are identical with the documented known regulation (see subfigure (b) in Fig. 3). But these regulation information can not be obtained without the supervised learning procedure (see the subfigure (a) in Fig. 3).



**Fig. 3.** Regulatory network reconstruction for a set of 10 transcription factors for heat shock response microarray data y14. Activation is shown in red arrow and repression in blue arc. The confirmed edges are shown in bold arrows with labels.

## 4 Discussion and Conclusion

Microarray gene expression data become increasingly common data source that can provide insights into biological processes at a system-wide level. In contrast to the conventional methods suffering the dimensionality problem, the main contribution of this paper is development of a methodology to reconstruct gene regulatory network by using existing interaction information of genes from database.



In other words, we provide a general framework to handle the microarray data by fully considering the accumulative biological experiment results, which not only makes the inferred results more accurate, but also alleviates the problem of dimensionality or data scarcity greatly. We have tested our approach to both simulated small-size problems and experimental biological data in this paper, which verified the efficiency and effectiveness of our algorithm.

In this paper, the supervised learning strategy is incorporated in the network inference. These approaches are called “supervised” because the model is learned from a training data consisting of a set of system responses. In our method, the training data are collected from the known transcription relationship from YEASTRACT, which allows the identification of documented or potential transcription regulators of a given gene and documented or potential regulatory for each transcription factor. Compared with the supervised learning strategy in [6], our method has advantages in simplifying the design of experiments and requiring less expensive computation. In our method, only time-course data of gene expression is utilized. While in [6] the perturbations around steady state are used. The reverse engineering algorithm implemented by linear programming in our method simplifies the complexity of network inference greatly. The strategy in [6] to fix the number of interaction of every gene and to enumerate all the cases by greedy algorithm is expensive and time consuming compared with the simplex algorithm for linear programming.

To examine causal relation among genes, a major source of errors comes from the noises of the gene expression data intrinsic to microarray technologies. To reduce the defect of unreliable data, a feasible method is to combine multiple microarray gene expression datasets together to get the more consistent network. Our supervised strategy in inferring gene regulatory network is ready to generalized in multiple datasets case. The more simulations and experiments are in progress.

The tendency is clearly that more and more data of gene interaction will be experimentally measured, reported and deposited in the literatures or databases. Meanwhile the quality of these data and microarray data keeps improving. It is reasonable to expect that our inference method will continue to prove valuable in analyzing and predicting the behavior or gene regulatory networks.

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# Double Optimization for Design of Protein Energy Function

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**Abstract.** We propose an automated protocol for designing the energy landscape suitable for the description of a given set of protein sequences with known structures, by optimizing the parameters of the energy function. The parameters are optimized so that not only the global minimum-energy conformation becomes native-like, but also the conformations distinct from the native structure have higher energies than those close to the native one, for each protein sequence in the set. In order to achieve this goal, one has to sample protein conformations that are local minima of the energy function for given parameters. Then the parameters are optimized using linear approximation, and then local minimum conformations are searched with the new energy parameters. We develop an algorithm that repeats this process of parameter optimization based on linear approximation, and conformational optimization for the current parameters, ultimately leading to the optimization of the energy parameters. We test the feasibility of this algorithm by optimizing a coarse grained energy function, called the UNRES energy function, for a set of ten proteins.

## 1 Introduction

According to the thermodynamic hypothesis [1], proteins adopt native structures that minimize their free energies. Therefore, obtaining energy function that accurately describes proteins would lead not only to the prediction of three-dimensional structures, but also to the understanding of folding mechanism [2,3].

Energy functions are generally parameterized from quantum mechanical calculations and experimental data on model systems. However, such calculations and data do not determine the parameters with perfect accuracy. The residual errors in energy functions may have significant effects on simulations of macromolecules such as proteins where the total energy is the sum of a large number of interaction terms. Moreover, these terms are known to cancel each other to

a high degree, making their systematic errors even more significant. Thus it is crucial to refine the parameters of a energy function before it can be successfully used to study protein folding.

In this work, we develop an automated protocol for the parameter optimization, where the parameters are modified so as to make conformations with larger values of root-mean-square deviation (RMSD) have higher values of energy relative to those with smaller values of RMSD. This goal is achieved by repeating two distinct optimization procedures, sampling local minimum-energy conformations for a given parameter set, and parameter optimization using linear approximation. The parameter optimization based on linear approximation is performed by supernodal Cholesky factorization method [4], a Linear Programming algorithm, and the local minimum-energy conformations with low energies for a given parameter are sampled using the conformational space annealing method [5,6,7,8].

We show the feasibility of this algorithm by successfully optimizing the UNRES energy function [9,10], for a set of ten proteins. Our work is an improvement over previous works [3,11,12,13,14,15,16], where either primitive methods of parameter optimization were used, or the optimization was performed for the training set of a small number of protein sequences, at most four of them.

## 2 Methods

### 2.1 Constrained and Unconstrained Conformational Searches

In order to check the performance of a energy function for a given set of parameters, one has to perform two types of conformational search, the constrained and unconstrained conformational searches. In the constrained search, the backbone angles of the conformations are fixed to the values of the native conformations, and only the side-chain angles are minimized with respect to the energy. We call the resulting conformations the super-native. The other conformations are obtained from unconstrained conformational search. The conformations obtained from the constrained and unconstrained searches are added to the structural database of local minimum-energy conformations for each protein. The search algorithm we use is the conformational space annealing (CSA) method [5,6,7,8]. The CSA method can be considered as a genetic algorithm that enforces a broad sampling in its early stages and gradually allows the conformational search to be focused into narrow conformational space in its later stages. As a consequence, many low-energy local minima including the GMEC of the benchmark protein can be identified for a given parameter set.

### 2.2 Parameter Refinement Using Linear Programming

The changes of energy gaps are estimated by the linear approximation of the energy function in terms of parameters. Among the conformations with non-zero RMSD values in the structural database, 50 (an arbitrary number) conformations with the smallest RMSD values are selected as the native-like conformations,

while the rest are considered as the non-native ones. Since an energy function can be considered to describe the nature correctly if native-like structures have lower energies than non-native ones, the parameters are optimized to minimize the energy gaps  $E_{\text{gap}}^{(1)}$  and  $E_{\text{gap}}^{(2)}$ ,

$$\begin{aligned} E_{\text{gap}}^{(1)} &= E^{\text{N}} - E^{\text{NN}} \\ E_{\text{gap}}^{(2)} &= E^{\text{SN}} - E^{\text{NN}} \end{aligned} \quad (1)$$

for each protein in the training set, where  $E^{\text{N}}$  and  $E^{\text{SN}}$  are the highest energies of the native-like and super-native conformations, respectively, and  $E^{\text{NN}}$  is the lowest energy of the non-native conformations. The energies are the modified ones that are weighted with the RMSD values of the conformations:

$$E_{\text{modified}} = E + 0.3 \text{ RMSD}. \quad (2)$$

Weighting the energies with the RMSD values makes the large RMSD conformations have high energies compared to ones with small RMSD values. The parameter optimization is carried out by minimizing the energy gaps  $E_{\text{gap}}^{(1)}$  and  $E_{\text{gap}}^{(2)}$  of each protein in turn, while imposing the constraints that all the other energy gaps, including those from the other proteins, do not increase.

In this work, we adjust the 715 linear parameters of the UNRES energy function [9,10], a coarse-grained protein energy function. The energy of a local minimum-energy conformation can be written as:

$$E = \sum_j p_j e_j(\mathbf{x}_{\text{min}}) \quad (3)$$

where  $e_i$ 's are the energy components evaluated with the coordinates  $\mathbf{x}_{\text{min}}$  of a local minimum-energy conformation. Since the positions of local minima also depend on the parameters, the full parameter dependence of the energy gaps are nonlinear. However, if the parameters are changed by small amounts, the energy with the new parameters can be estimated by the linear approximation:

$$E^{\text{new}} \approx E^{\text{old}} + \sum_i (p_i^{\text{new}} - p_i^{\text{old}}) e_i(\mathbf{x}_{\text{min}}) \quad (4)$$

where the  $p_i^{\text{old}}$  and  $p_i^{\text{new}}$  terms represent the parameters before and after the modification, respectively. The parameter dependence on the position of the local minimum can be neglected in the linear approximation, since the derivative in the conformational space vanishes at a local minimum. The additional term 0.3 RMSD of Eq.(2) vanishes in these expressions due to the same reason. The changes of the energy gaps are estimated as:

$$\begin{aligned} \Delta E_{\text{gap}}^{(1)} &= E_{\text{gap}}^{(1)}(\{p_j^{\text{new}}\}) - E_{\text{gap}}^{(1)}(\{p_j^{\text{old}}\}) \\ &= (E^{\text{N}}(\{p_j^{\text{new}}\}) - E^{\text{NN}}(\{p_j^{\text{new}}\})) - (E^{\text{N}}(\{p_j^{\text{old}}\}) - E^{\text{NN}}(\{p_j^{\text{old}}\})) \\ &= \sum_j (e_j^{\text{N}} - e_j^{\text{NN}})(p_j^{\text{new}} - p_j^{\text{old}}) \end{aligned} \quad (5)$$

$$\begin{aligned}
 \Delta E_{\text{gap}}^{(2)} &= E_{\text{gap}}^{(2)}(\{p_j^{\text{new}}\}) - E_{\text{gap}}^{(2)}(\{p_j^{\text{old}}\}) \\
 &= (E^{\text{SN}}(\{p_j^{\text{new}}\}) - E^{\text{NN}}(\{p_j^{\text{new}}\})) - (E^{\text{SN}}(\{p_j^{\text{old}}\}) - E^{\text{NN}}(\{p_j^{\text{old}}\})) \\
 &= \sum_j (e_j^{\text{SN}} - e_j^{\text{NN}})(p_j^{\text{new}} - p_j^{\text{old}}) \tag{6}
 \end{aligned}$$

The magnitude of the parameter change  $\delta p_j \equiv p_j^{\text{new}} - p_j^{\text{old}}$  is bounded by a certain fraction  $\epsilon$  of  $p_j^{\text{old}}$ . We use  $\epsilon = 0.01$  in this study. First, the vector  $\delta p_j$  is chosen within the bound to decrease the energy gap  $\Delta E_{\text{gap}}^{(1)}$  of the selected protein as much as possible while imposing the constraints that any positive values among  $E_{\text{gap}}^{(2)}$  and the energy gaps of the other proteins do not increase and negative values do not become positive. Denoting the energy gaps of the  $k$ -th protein as  $E_{\text{gap}}^{(p=1,2)}(k)$  and assuming the  $i$ -th protein is selected for the decrease of the energy gap, this problem can be phrased as follows:

**Minimize**

$$\Delta E_{\text{gap}}^{(1)}(i) = \sum_j (e_j^{\text{N}}(i) - e_j^{\text{NN}}(i))(p_j^{\text{new}} - p_j^{\text{old}})$$

**with constraints**

$$|\delta p_i| \leq \epsilon$$

$$\Delta E_{\text{gap}}^{(2)}(i) = \sum_j (e_j^{\text{SN}}(i) - e_j^{\text{NN}}(i))(p_j^{\text{new}} - p_j^{\text{old}}) \leq \begin{cases} 0 & \text{if } E_{\text{gap}}^{(2)}(i) > 0 \\ -E_{\text{gap}}^{(2)}(i) & \text{otherwise} \end{cases}$$

$$\Delta E_{\text{gap}}^{(p=1,2)}(k \neq i) = \sum_j (e_j^{(\text{S})\text{N}}(k) - e_j^{\text{NN}}(k))(p_j^{\text{new}} - p_j^{\text{old}}) \leq \begin{cases} 0 & \text{if } E_{\text{gap}}^{(p)}(k) > 0 \\ -E_{\text{gap}}^{(p)}(k) & \text{otherwise} \end{cases}$$

This is a global optimization problem where the linear parameters  $p_j$  are the *variables*. The object function to minimize, and the constraints, are all linear in  $p_j$ . This type of the optimization problem is called the Linear Programming. It can be solved exactly, and many algorithms have been developed for solving the Linear Programming problem. We use the primal-dual method with supernodal Cholesky factorization [4] in this work, which finds an accurate answer with reasonably computational costs.

After minimizing  $\Delta E_{\text{gap}}^{(1)}(i)$ , we solve the same form of linear programming where now  $\Delta E_{\text{gap}}^{(2)}(i)$  is the objective function and the other energy gaps become constrained. Then we select another protein and repeat this procedure (300 times in this work) of minimizing  $\Delta E_{\text{gap}}^{(1)}$  and  $\Delta E_{\text{gap}}^{(2)}$  in turn.

The algorithm of parameter optimization based on linear approximation, using repeated Linear Programming, is summarized in algorithm 1.

### 2.3 Re-minimization and New Conformational Search

Since the procedure of the previous section was based on the linear approximation Eqs.(5) and (6), we now have to evaluate the true energy gaps using the newly obtained parameters. The breakdown of the linear approximation may

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**Algorithm 1.** Parameter optimization for conformations in the structural database, using linear programming

---

```

1: N_p = Number of protein sequences in the dataset (constant)
2: N_{it} = Maximum number of iteration (300 in this work)
3: $\mathbf{p}^{(i)}$ = The initial parameters at the start of this sub-algorithm
4: for $i = 0$ to N_{it} do
5: Calculate energy gaps $E_{\text{gap}}^{(1)}(p)(p = 1, \dots, N_p)$
6: for $p = 1$ to N_p do
7: minimize $\Delta E_{\text{gap}}^{(1)}(p)$, while constraining the other energy gaps (Linear Programming)
8: minimize $\Delta E_{\text{gap}}^{(2)}(p)$, while constraining the other energy gaps (Linear Programming)
9: end for
10: if Energy gaps are negative for all of the N_p proteins then
11: End this sub-algorithm, since parameters are optimized for the conformations in the structural database.
12: end if
13: end for

```

---

come from two sources. First, the conformations corresponding to the local minima of the energy for the original set of parameters are no longer necessarily so for the new parameter set. For this reason, we reminimize the energy of these conformations with the new parameters. Since super-native conformations are not local minimum-energy conformations, even with the original parameters, the unconstrained reminimization of these conformations with the new parameters may furnish low-lying local minima with small values of RMSD. Second, the local minima obtained from conformational searches with the original parameter set may constitute only a small fraction of low-lying local minima. After the modification of the parameters, some of the local minima which were not considered due to their relatively high energies, can now have low energies for the new parameter set. It is even possible that entirely distinct low-energy local minima appear. Therefore these new minima are taken into account by performing subsequent conformational searches with the newly obtained parameter set.

## 2.4 Update of the Structural Database and Iterative Refinement of Parameters

The low-lying local energy minima found in the new conformational searches are added into the energy-reminimized conformations to form a structural database of local energy minima. The conformations in the database are used to obtain the energy gaps, which are used for the new round of parameter refinement. As the procedure of [conformational search  $\rightarrow$  parameter refinement  $\rightarrow$  energy reminimization] is repeated, the number of conformations in the structural database increases. This iterative procedure is continued until sufficiently good native-like conformations are found from the unconstrained conformational search. The whole procedure is summarized in algorithm 2.

---

**Algorithm 2.** The algorithm for protein energy function parameter optimization

---

```

1: N_p = Number of protein sequences in the dataset (constant)
2: N_{it} = Maximum number of iteration (constant)
3: $\mathbf{p}(i)$ = the initial parameters
4: for $i = 0$ to N_{it} do
5: for $p = 1$ to N_p do
6: For the protein sequence p , sample low-lying local minimum-energy conformations with no constraints, and save their coordinates and energy components.
7: For the protein sequence p , sample low-lying local minimum-energy native-like conformations (constrained sampling), and save their coordinates and energy components
8: end for
9: if Low-lying conformations found from unconstrained search are native-like for all of the N_p sequences then
10: Parameter optimization accomplished. End the algorithm.
11: end if
12: if $i == 0$ then
13: structural database \leftarrow low-lying conformations obtained from unconstrained search + low-lying native-like conformations obtained from constrained search (coordinates and energy components)
14: else
15: structural database \leftarrow structural database + low-lying conformations obtained from unconstrained search + low-lying native-like conformations obtained from constrained search (coordinates and energy components)
16: end if
17: Optimize parameters using Linear Programming, so that the energy gap $E_g = E_{na} - E_{nn}$ between the maximum energy among native-like conformations, E_{na} , and the minimum energy among non-native conformations, E_{nn} (See alg. 1), is minimized for each of the N_p sequences in the training set $\Rightarrow \mathbf{p}(i + 1)$ (new parameters)
18: Reinitialize structural database with respect to the energy function with the new parameters
19: end for

```

---

### 3 Results and Discussions

#### 3.1 Ten Proteins in the Training Set and Two Proteins in the Test Set

We apply our protocol to the optimization of UNRES energy function, for a training set consisting of ten proteins, that belong to the structural class of  $\alpha$  proteins. The PDB codes of these proteins are, 1BBA(36), 1BDD(60), 1EDI(56), 1EDK(56), 1HNR(47), 1IDY(54), 1PRB(53), 1PRU(56), 1VII(36), and 1ZDB(38), where the number inside parentheses are the lengths of these proteins. The initial parameter set is the one used in CASP3[17,18]. The optimized parameter set obtained using the training set above, is useful for the protein folding study of an  $\alpha$  protein, including the tertiary structure prediction, where the secondary structure content



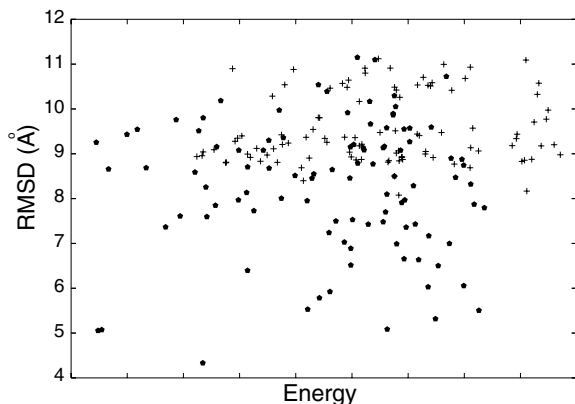
**Table 1.** The  $C_\alpha$  RMSD of GMEC, for the ten proteins in the training set and the two proteins in the test set. The number in parantheses are the smallest RMSD values found in the fifty low-energy conformations.

|                      |            |            |            |           |           |           |
|----------------------|------------|------------|------------|-----------|-----------|-----------|
|                      | 1BBA       | 1BDD       | 1EDI       | 1EDK      | 1HNR      | 1L2Y      |
| initial parameters   | 8.9 (8.1)  | 9.8 (7.2)  | 7.8 (5.0)  | 7.6 (4.9) | 9.9 (6.6) | 6.5 (4.6) |
| optimized parameters | 9.3 (4.3)  | 3.9 (2.9)  | 3.8 (2.4)  | 3.9 (2.4) | 9.4 (5.3) | 3.6 (3.1) |
|                      | 1IDY       | 1PRB       | 1PRU       | 1VII      | 1ZDB      | 1F4I      |
| initial parameters   | 11.2 (6.9) | 10.1 (7.5) | 11.5 (6.9) | 6.3 (4.9) | 7.7 (6.7) | 6.8 (5.1) |
| optimized parameters | 10.1 (4.9) | 6.2 (5.9)  | 6.7 (5.8)  | 5.3 (3.5) | 7.6 (3.0) | 5.4 (4.2) |

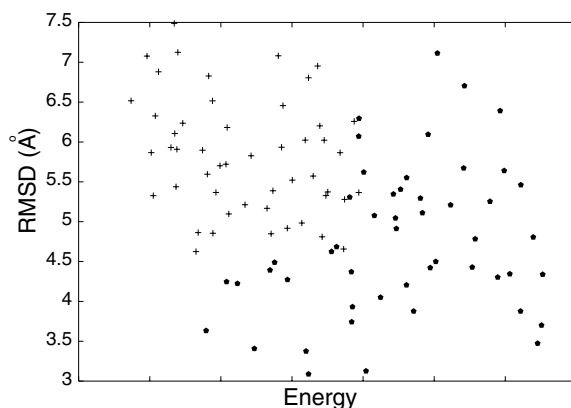
can be determined relatively easily using experimental methods such as Circular Dichroism (CD) or Nuclear Magnetic Resonances (NMR). It is of course possible to obtain energy function parameters suitable for the general description of proteins regardless of their structural classes, using training set consisting of proteins that belong to diverse structural classes[13,14].

The performance of UNRES energy function with the optimized parameters was tested, by sampling low-energy conformations of two  $\alpha$  proteins not included in the training set, 1F4I(40) and 1L2Y(20).

For proteins both in training and test sets, fifty conformations were sampled in each conformational search. The RMSDs of  $C_\alpha$  coordinates from those of native structures for the global minimum-energy conformations (GMEC) are shown in Table 1, along with the smallest values of RMSD found among the fifty low-energy conformations, obtained with the initial and optimized parameters. Five iterations of linear optimization were performed in order to obtain the optimized parameter set. The energies are not displayed since their numerical



**Fig. 1.** Plots of the energy and  $C^\alpha$  RMSD values of fifty low-energy conformations for the protein 1BBA, obtained using the initial (*plus signs*) and the optimized parameters (*filled circles*). Although the RMSD of the GMEC is smaller for conformations obtained with the initial parameters, much more native-like low-energy conformations are obtained with the optimized parameters.



**Fig. 2.** Plots of the energy and  $C^\alpha$  RMSD values of fifty low-energy conformations for the protein 1L2Y, obtained using the initial (*plus signs*) and the optimized parameters (*filled circles*). The GMEC found with the optimized parameters has smaller RMSD value than that found with the initial parameters. Also, much more native-like low-energy conformations are obtained with the optimized parameters.

values have no physical meaning, due to the fact that the overall scale of the linear parameters is not fixed in our protocol. We see from the data that after five iteration, the parameters are indeed optimized for the ten proteins in the training set. The smallest RMSD values found among the fifty low-energy conformations decreased for all of the proteins in the training set, and the RMSD values of the GMECs also decreased for all of them except 1BBA. Since the native structure of a protein is usually predicted by constructing several models, rather than selecting just one GMEC, GMEC not being native-like is not a serious problem, as long as there are sufficient number of native-like conformations in the final set of low-energy conformations obtained by the sampling algorithm. In fact, even for 1BBA where RMSD value of the GMEC increased, those of the second and third lowest energy conformations all decreased, and there are much more native-like low-energy conformations obtained with the optimized parameters, as can be seen in Fig. 1 where the RMSD values of the fifty low-energy conformations are plotted against their energy values.

We see that also for the two proteins in the test set, the lowest RMSD value found from the fifty low-energy conformations, as well as that of GMEC, decrease as the parameters are optimized. Again, the low-energy conformations become more native-like overall, as can be seen from the plot of RMSD against energy values for 1L2Y (Fig. 2). The result suggests that the optimized parameters are transferable to  $\alpha$  proteins not included in the training set, and can be used for the study of protein folding of such proteins.

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# Efficient Solution of Bidomain Equations in Simulation of Cardiac Excitation Anisotropic Propagation

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**Abstract.** Bidomain equations are used to characterize myocardial physiological activation and propagation. Their numerical solution is costly computation because of the higher temporal and spatial discretization requirements, especially in three dimensions. In most previous studies, the heart was supposed to be homogeneous isotropic medium, and thus can use the monodomain equation instead of the bidomain equations to simulate the heart excitation propagation. Simulation of heart excitation anisotropic propagation in three-dimensional large tissue size by solving bidomain equations has not been implemented yet. In this paper, we present an efficient solution of bidomain equations in simulation of heart excitation anisotropic propagation by combining some numerical techniques such as non-standard finite difference (NSFD), domain decomposition and multigrid methods. The results show that the proposed method can successfully be used to simulate heart excitation anisotropic propagation in three-dimensional large tissue size, and it suggests that such method may provide a good basis for heart simulation research in a more physiologically way.

## 1 Introduction

Computational models of activation and propagation in virtual cardiac tissues are now becoming an established research tool for investigating mechanisms of normal and abnormal heart activation [1]. More recently, on the basis of anisotropic bidomain theory [2], reaction-diffusion equations have been used to characterize myocardial physiological propagation and electrical behavior generated by ionic movements in myocardial cell by coupling with myocardial cell model which is composed of a large number of ordinary differential equations (ODEs).

However, the bidomain equations are computationally very expensive. Most researchers simplify heart as homogeneous isotropic medium, thus the bidomain equations can be replaced by the monodomain equation in which an operator splitting approach and adaptive time step can be used to solve parabolic equation and avoid the solution of a large non-linear PDE system (PDEs) at every time step. Huiskamp [3] created a model of the ventricles that was composed of 810546 elements and used a biophysically based membrane model in a monodomain framework to simulate the spread of excitation. Gulrajani et al [4] created a cardiac model with 12 million cell

units by using an equal anisotropy assumption to simplify the system to a monodomain model and performed the computations on a large parallel shared memory computer. All these models of cardiac propagation are far less expensive computationally than the bidomain frameworks, but they fail to provide an avenue for introducing extracellular stimulation nor do they produce extracellular potentials that can be compared directly with experimental recordings. Recently, some researchers have adopted bidomain framework to model different aspects of cardiac activation, but only implement in simplified and segmental 3D anatomical heart geometry for limitation of computational capacity. Most bidomain implementations are based around a finite difference solution technique but the finite element method has also been used [5], as well as the finite volume technique [6].

Since the heart is a heterogeneous 3-D object with anisotropic properties, we have to solve another elliptic equation, which is actually to solve an algebra equation  $Ax=b$ . Since the number of the grid units in heart propagation model maybe millions, inverting the matrix  $A$  is infeasible for the common iterate methods, such as Gauss-Siedel iteration or C-G iteration, and even for the multigrid method [7], and that elliptic equations are known to yield matrices that become progressively more ill-conditioned as the spatial resolution is increased. In this paper, we present an efficient solution of bidomain equations in simulation of heart excitation anisotropic propagation by combining some numerical techniques such as non-standard finite difference (NSFD) [8], domain decomposition [9] and multigrid methods, which can drastically reduce the overall time of simulation.

## 2 Methods

### 2.1 The Bidomain Model and Cardiac Cell Model

The bidomain model applied in heart is:

$$\frac{\partial V_m}{\partial t}(\underline{x}, t) = \frac{1}{C_m} \left[ - \sum I_{ion}(\underline{x}, t) - I_{app}(\underline{x}, t) - \frac{1}{\beta} \nabla \cdot (D_e(\underline{x}) \nabla \phi_e(\underline{x}, t)) \right] \quad (1)$$

$$\nabla \cdot ((D_i(\underline{x}) + D_e(\underline{x})) \nabla \phi_e(\underline{x}, t)) = - \nabla \cdot (D_i(\underline{x}, t) \nabla V_m(\underline{x}, t)) \quad (2)$$

The parabolic (1) and elliptic (2) equations are the governing equations of the bidomain model. The main variables  $V_m$  and  $\phi_e$  are the transmembrane potential and the extracellular potential,  $I_{ion}$  is the current density flowing through the ionic channels,  $I_{app}(\underline{x}, t)$  is an applied stimulus current per unit area,  $\beta$  is a geometrical constant,  $C_m$  is the capacitance of the cell membrane,  $D_i$  and  $D_e$  are conductivity tensors which is used to describe the anisotropic nature of the cardiac microstructure,  $\underline{x}$  is the spatial position. They can be simplified by the assumption of equal anisotropy, treating heart as homogeneous isotropic medium.

$$D_t(\underline{x}) = \frac{1}{k} D_e(\underline{x}) \tag{3}$$

$$\frac{\partial V_m}{\partial t}(\underline{x}, t) = \frac{1}{C_m} \left[ -\sum I_{ion}(\underline{x}, t) - I_{app}(\underline{x}, t) + \frac{1}{\beta} \left( \frac{k}{k+1} \right) \nabla \cdot (D_t(\underline{x}) \nabla V_m(\underline{x}, t)) \right] \tag{4}$$

where  $k$  is the anisotropy ratio. The resulting parabolic equation is known as the monodomain equation (4), details about bidomain theory can see Ref. [1].

The electrophysiological behavior of single cell can be described by the following differential equations which constitute the non-linear parts of the PDEs:

$$\begin{aligned} dV_m / dt = & -(1/C_m)(I_{Na} + I_{NaL} + I_{CaL} + I_{to} + I_{Kr} + I_{Ks} + I_{K1} \\ & + I_{NaK} + I_{NaCa} + I_{pCa} + I_{pK} + I_{bCa} + I_{bNa} + I_{stim}) \end{aligned} \tag{5}$$

$$I_x = G_x \cdot (V_m - E_x) \tag{6}$$

where  $I_x$  is the current flow through the ion channel  $x$ ,  $G_x$  is the conductance of the channel and  $E_x$  is the reversal potential for the channel which is the Nernst potential for the ion or ions. The conductance is the maximal conductance  $g_x$  multiplied by the state of the channel which is modeled with a set of gating variables. For a channel with  $m$  different gates, each with  $n_i$  sub-units per gate, the model of the channel conductance is given by ODEs of the form:

$$G_x = g_x \prod_{i=1}^m x_i^{n_i} \tag{7}$$

$$\frac{dx_i}{dt} = \alpha_{x,i}(V_m) \cdot (1 - x_i) - \beta_{x,i}(V_m) \cdot x_i, \quad \text{or} \quad \frac{dx_i}{dt} = \frac{x_{i,\infty}(V_m) - x_i}{\tau_{x,i}(V_m)} \tag{8}$$

$$\tau_{x,i}(V_m) = \frac{1}{\alpha_{x,i}(V_m) + \beta_{x,i}(V_m)}, x_{i,\infty}(V_m) = \frac{\alpha_{x,i}(V_m)}{\alpha_{x,i}(V_m) + \beta_{x,i}(V_m)} \tag{9}$$

where  $x_{i,\infty}$  represents the steady state behavior of the gate. The  $\alpha_{x,i}(V_m)$  and  $\beta_{x,i}(V_m)$  coefficients are known as rate constants and are voltage dependent.

In this study, the Tusscher et al.'s ionic model of human ventricular tissue [10] is used since it includes a high level of electrophysiological detail while maintaining a low computational cost. There are thirteen ionic currents in the ten Tusscher et al.'s ionic model [10], fourteen gating parameters in total. These ODEs for gating parameters are coupled with an ODE for the calcium concentration in the cell and an ODE for the membrane voltage, making sixteen ODEs in total.

### 2.2 Boundary Conditions

In order to specify the boundary conditions, let the closed surface  $S_H$  be a boundary separating bidomain region  $H$  and surrounding volume conductor  $B$ , and let the closed

surface  $S_B$  bound region  $B$ .  $\mathbf{n}$  denotes the unit outward normal to  $S_H$  and  $S_B$ .  $\Phi_o$  is the extracardiac potential and  $D_i$  is the isotropic scalar conductivity outside of  $H$ .

$$\phi_o = \phi_e, \quad \mathbf{n} \cdot D_o(\underline{x}) \nabla \phi_o = \mathbf{n} \cdot (D(\underline{x}) \nabla \phi_e(\underline{x}, t) + D_i(\underline{x}) \nabla V_m(\underline{x}, t)) \quad \text{on } S_H \tag{10}$$

$$\mathbf{n} \cdot \sigma_o \nabla \phi_o = 0 \quad \text{on } S_B \tag{11}$$

Since the sources in  $H$  are related to the presence of intracellular medium, which is absent in  $B$ , we may assume that the vector  $D_i \nabla V_m$  in Eq.(10) is tangent to the surface  $S_H$ ; this becomes an boundary condition:

$$\mathbf{n} \cdot D_i(\underline{x}) \nabla V_m(\underline{x}, t) = 0 \quad \text{on } S_H \tag{12}$$

$$\mathbf{n} \cdot D_i(\underline{x}) \nabla \phi_e(\underline{x}, t) = 0 \quad \text{on } S_H \tag{13}$$

### 2.3 Numerical Considerations

The equations of bidomain model can be solved with different time steps and at different spatial resolutions as a decoupled system, a system of a parabolic PDE, an elliptic PDE and a nonlinear system of ODEs. First, we introduce a temporal discretization of the time intervals  $t \in (0, t_N]$ . Let  $\Delta t$  be the global time step or the time interval between each integration process  $\Delta t = t_N/N$  and  $M$  be an even number of fractional time steps. Define  $\Delta t' = \Delta t/M$  as the fractional diffusion time step. In the spatial direction, we use rectangular blocks the domain ( $H$ ), which can be partitioned into a set of smaller, simpler elements to generate computational matrices. Both the parabolic PDE and the nonlinear ODEs system are solved via the explicit forward-Euler scheme with an operator splitting technique [1]. The equations can be solved in the following steps:

1. Assume we know the value of  $x^n, y^n, V_m^n$  and  $\Phi_e^n$  at  $t^n$ .
2. Compute  $V_m^{n+1/2}$  in  $H$  by solving the parabolic equation (Eq.(1), or (4)) using a step size  $\Delta t'$  repeated  $M/2$  times. ( Eq.(14) for bidomain, Eq.(15) for monodomain)

$$V_m^{n+1/2} = V_m^n + \frac{\Delta t'}{C_m} \left[ -\sum I_{ion}^n - I_{app}^n - \frac{1}{\beta} \nabla \cdot (D_e \nabla \phi_e^n) \right] \tag{14}$$

$$V_m^{n+1/2} = V_m^n + \frac{\Delta t'}{C_m} \left[ -\sum I_{ion}^n - I_{app}^n + \frac{1}{\beta} \left( \frac{k}{k+1} \right) \nabla \cdot (D_i \nabla V_m^n) \right] \tag{15}$$

3. Compute  $x^{n+1}, y^{n+1}$  by solving the ODEs of the cell model using nonstandard finite difference scheme, in which  $x^{n+1}$  represents gating variables,  $y^{n+1}$  represents  $I_{ion}$ .

$$x^{n+1} = x_\infty(V_m^{n+1/2}) + (x^n - x_\infty(V_m^{n+1/2})) e^{\left( \frac{-\Delta t}{\tau_i(V_m^{n+1/2})} \right)} \tag{16}$$

$$y^{n+1} = y^n + \Delta t \cdot f(V_m^{n+1/2}, x^n) \tag{17}$$

4. Compute  $V_m^{n+1}$  in  $H$  by solving the parabolic equation (Eq.(1), or (4)) using a step size  $\Delta t'$  repeated  $M/2$  times again. (same as step 2)
5. Compute  $\Phi_e^{n+1}$  in  $H$  by solving the elliptic equation (Eq.(2)) using domain decomposition and multigrid methods:

$$\nabla \cdot ((D_i + D_e) \nabla \phi_e^{n+1}) = -\nabla \cdot (D_i \nabla V_m^{n+1}) \quad \text{only for bidomain model} \quad (18)$$

### 2.4 Efficient ODE-Solvers

Generally, the ODEs system is solved using forward Euler method, but it has to take small step-size to maintain the stable computation. Here we take advantage of the linear equations (Eq.(8)) of the ODEs governing the gating variables by making use of discrete derivative (Eq.(19)) from the exact solution as part of a NSFD scheme [8], to update gating variables,

$$x_{n+1} = x_\infty + (x_n - x_\infty) e^{-\left(\frac{\Delta t}{\tau_x}\right)} \quad (19)$$

where  $x_\infty$  and  $\tau_x$ , are defined previously and can be evaluated explicitly using the value of  $V_m$  from the previous time step. It leaves the ODEs only for membrane potential ( $V_m$ ) and calcium concentration ( $[Ca^{2+}]_i$ ) which can solved numerically by forward Euler method. In this way, the system is no longer stiff. A larger step-size can now be used.

### 2.5 Efficient Parabolic Equation-Solvers

Most studies [1] used the conventional Euler method to integrate the PDEs by using a very small time step to keep numerical stability and accuracy, which makes the computation much slow. Here, we solve the PDEs for cardiac excitation propagation by using the well-known operator splitting and adaptive time step methods, which can speed up the computation and maintain the accuracy as well. The operator-splitting scheme can then be symbolically represented as:

$$y^{n+1} = D_{\Delta t'}^M R_{\Delta t} D_{\Delta t'}^M y^n \quad (20)$$

where  $y^{n+1}$  and  $y^n$  are solutions at  $t^{n+1}$  and  $t^n$  respectively,  $R_{\square t}$  represents the stiff integration of the reaction term over a step size  $\Delta t$  (see step.3).  $D_{\Delta t'}$  represents the integration of the diffusion term using a step size  $\Delta t'$  and the superscript indicates this integration is to be repeated  $M$  times (see step.2, step.4). This construct enables the global time step ( $\Delta t = M\Delta t'$ ) to become significantly larger than the diffusion stability limit, resulting in an improved computational performance.

### 2.6 Efficient Elliptic Equation-Solvers

We decompose  $H$  into some subdomains:  $H := \bigcup_{i=1}^n H_i$  with non-overlapping decomposition. Then a smaller linear system can be computed in each subdomain separately:



$$\nabla \cdot ((D_i + D_e) \nabla \phi_{e,i}^{n+1,k}) = -\nabla \cdot (D_i \nabla V_{m,i}^{n+1}) \quad \text{in } H_i \tag{21}$$

$$B_{i,j} \phi_{e,i}^{n+1,k} = B_{i,j} \phi_{e,j}^{n+1,k-1} \quad \text{on } \partial H_i \cap \bar{H}_j, \quad B_{i,j} = \frac{\partial}{\partial n_i} + c_1 + c_2 \frac{\partial}{\partial \tau_i} + c_3 \frac{\partial^2}{\partial \tau_j^2} \tag{22}$$

$$\partial_n \phi_{e,i}^{n+1,k} = 0 \quad \text{on } \partial H_i \cap \partial H \tag{23}$$

where  $B_{i,j}$  is artificial boundary condition (ABC) on the boundary of  $H_i$  intercepted by  $H_j$ ,  $\tau_i$  is the tangential derivative along the interface,  $n_i$  is the normal, and the coefficient  $c_1, c_2, c_3$  is used to minimize the convergence rate of the Schwarz algorithm [11, 12].

It is well known that classical relaxation methods such as the Jacobi or Gauss-Seidel methods, applied to the iterative solution of the resulting linear system, can quickly damp the high frequencies of the error. However, they do not allow for an efficient treatment of the low frequency components, so we use the multigrid method in subdomain. The basic idea of the multigrid grid is to transfer the partially solved solution on a coarser grid in order to transform the low frequencies of the fine grid solution in high frequencies, which can be efficiently damped by the standard relaxation methods. In the subdomain, let  $\tilde{\phi}_{e,j,h}^{n+1,k}$  (subscript h denotes in fine grid) be the approximate iterative solution by classical relaxation methods:

$$\nabla \cdot ((D_i + D_e) \nabla v_h) = r_h \tag{24}$$

where  $r_h = -\nabla \cdot (D_i \nabla V_{m,i,h}^{n+1}) - \nabla \cdot ((D_i + D_e) \nabla \tilde{\phi}_{e,i,h}^{n+1,k})$  is the residual; since  $v_h$  is smooth, Eq.(24) can be approximated on the coarser grid with mesh spacing  $H > h$  by

$$\nabla \cdot ((D_i + D_e) \nabla v_H) = I_h^H r_h \tag{25}$$

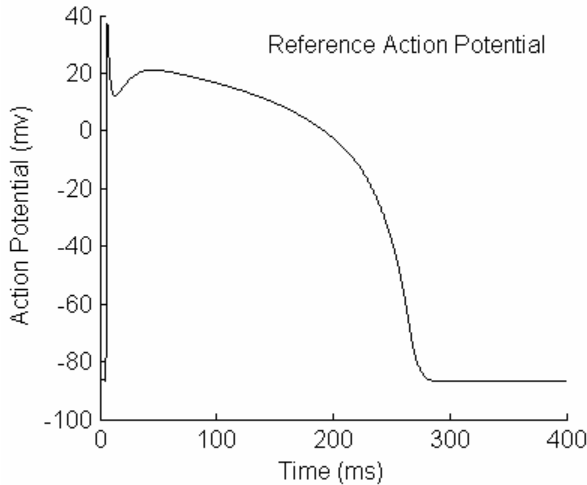
The function  $I_h^H$  is to interpolate the value in fine grid to coarser grid ( $I_H^h$  is the opposite). Then after working out  $v_H$  from Eq.(25), we can re-interpolate it to the finer grid, and added to the previous approximate solution  $\tilde{\phi}_{e,i,h}^{n+1,k+1} = \tilde{\phi}_{e,i,h}^{n+1,k} + I_H^h v_H$ . Actually, the higher level multigrid method may be more feasible, since it brings more accuracy while only increasing a little more computation (see [7]). The procedure is similar to the two level multigrid, just to reuse the two level multigrid when solve the equation in coarser grid and then resort it for the more coarser grid. In addition, there are many cases of the multi-level multigrid method. The most important cases in practice are V-cycle, and W-cycle. For more details, see [7, 13].

### 3 Results

#### 3.1 Numerical Results for Single Cell Experiments with NSFD Scheme

By using of Matlab7.0's ode15s function with setting both absolute and relative tolerances (*atol* and *rtol*, respectively) to  $10^{-10}$  which is a variable step-size stiff solver for ODEs, which is based on a family of linear multistep methods, we get the reference solution of the membrane voltage  $V_m^{ref}$  which is shown in Fig.1.

The relative root-mean square error ( $E_{RMS}$ ) between the numerical solution  $V_m$  and the reference  $V_m^{ref}$  can be computed using Eqs. (26) to give a more intuitive sense of the error between solutions (Table 1). As we know, the ODEs governing the gating variables are linear, so we make use of their known exact solution as part of a non-standard finite difference scheme to update gating variables, so that the stiffness of the ODEs system of ionic model is reduced and a larger step-size can be used.



**Fig. 1.** Reference solution generated for the membrane voltage  $V_m^{ref}$

$$E_{RMS} = \sqrt{\frac{\sum_{i=1}^N (V_i - V_i^{ref})^2}{\sum_{i=1}^N V_i^{ref}}} \tag{26}$$

#### 3.2 Validation of the Model on Simple and Anatomical Geometry

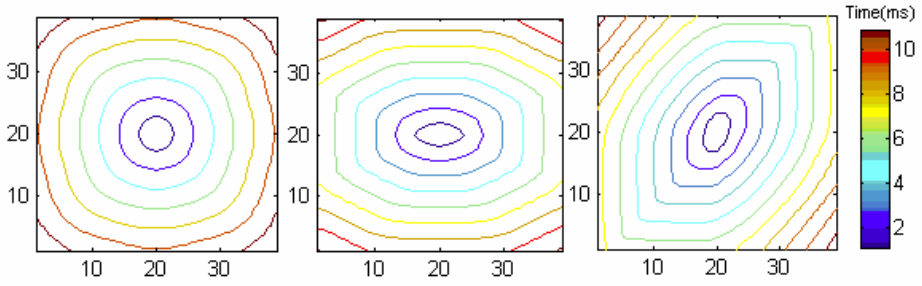
First, we simulate isotropy and anisotropic propagation inside a homogeneous virtual tissue composed of uniform cell units (40×40), in which the fiber direction was kept constant and anisotropic conductivity tensors  $Dl = 0.45\text{cm}^2/\text{ms}$  ( $l$  for longitudinal),

**Table 1.**  $R_{RMS}$  values for the NSFD scheme for some step sizes  $\Delta t$ 

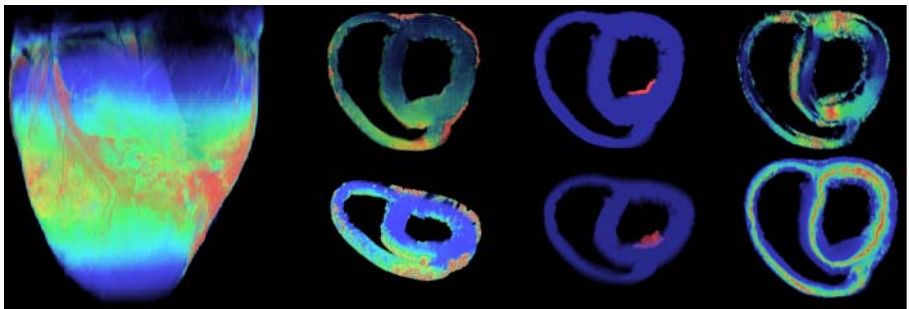
| $\Delta t(\text{ms})$ | $E_{RMS}$ |
|-----------------------|-----------|
| 0.005                 | 0.0086    |
| 0.01                  | 0.0236    |
| 0.05                  | 0.0392    |
| 0.1                   | 0.0423    |
| 0.2                   | 0.0496    |
| 0.3                   | 0.0654    |

$D_t = 0.13 \text{ cm}^2/\text{ms}$  ( $t$  for transversal). The stimulus current is applied at the center of the region and  $\Delta t = 10\mu\text{s}$ ,  $M=20$ ,  $D_x=0.39\text{mm}$ . Fig.2 shows the equal anisotropy propagated isochrones agree with theoretical predictions very well, i.e., the ratio of the longitudinal and transversal axes of isochrone is proportional to the square-root of the conductivities in the corresponding directions [14].

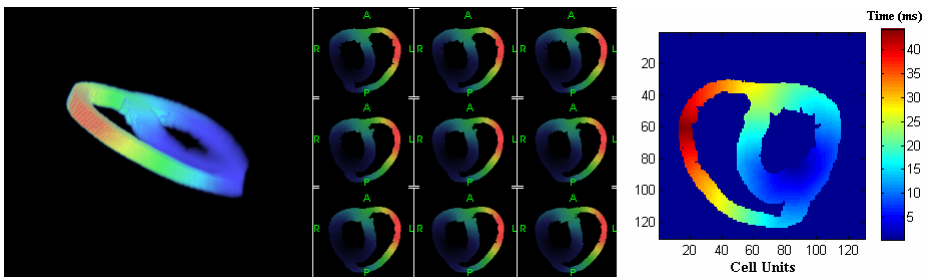
Second, we test the proposed method on the heart model with real anatomical structure. A dog ventricle data set, composed of the volume image and tensor eigenvector reconstructed from diffusion tensor magnetic resonance imaging developed by Edward [15], is used as the domain for simulating normal activation. We chose ten slices of the cardiac tissue for simulation test. The spatial matrix size is  $12 \times 130 \times 130$  which corresponds to pixel size of  $0.78 \times 0.78 \times 0.78 \text{ mm}$ . Initial activation points (Purkinje–myocardial junction sites) and Fiber angles are shown in Fig. 3 at a representative section perpendicular to the long axis of our heart model. We set the discretization parameters as  $\Delta t = 10\mu\text{s}$ ,  $M=20$ ,  $D_x=0.39\text{mm}$  and the tolerance for the elliptic solve is set to  $10^{-6}$ . All the simulation are performed on Dual-Core Intel® Xeon® processors Dell Precision WorkStation 670 System (2R) with 4Gb physical RAM, cost 17 hrs and 40 mins for 55ms excitation propagation simulation. Fig. 4 shows the activation isochrones, the wave front radiates from the points of stimulation, initially from the two sites in the left ventricle. This initiates a wave of depolarization that spreads concentrically around the left ventricle. After about 50 ms the wave fronts merge in the posterior part of the right ventricle, which is a little different from the real physiological condition. The reason is that, there are more activation points in a real heart, but here it is a segmental 3D model and only activation points lying in the vicinity of the tissue were included. In physiological condition wave fronts originating from other sites lying outside the selected segment could depolarize tissue inside the segment before the wave front comes from our activation points. This possible effect is not included in the present simulation.



**Fig. 2.** Activation isochrones from simulations in uniformly isotropy and anisotropic virtual slab tissue. The left panel shows view of isotropy propagation, the middle and right display views of anisotropic propagation simulation with fiber directions of  $0^\circ$  and  $60^\circ$ ; the slab are 40 cells in each direction.



**Fig. 3.** Anatomical model of the dog ventricle. The left panel shows 3D view of the whole ventricle, and the next displays view of the selected part of the cardiac tissue for simulation. After that displays the initial activation points (*Purkinje–myocardial junction sites*). The right view displays the fiber angles (*above is azimuth angles, bottom is colatitude angles*).



**Fig. 4.** Isochrones of simulated normal activation of the ventricles. The left panel shows 3D isochrones in selected part of ventricle, and the right view displays the activation isochrones on the first slice of the tissue. The middle panels display views of the activation in other slices.

## 5 Conclusion

In this paper, we combine the advantage of domain decomposition and multigrid methods to give a better scheme for solving large scale algebra equation that arise from elliptic problems, which can significantly speed up integration while preserving accuracy. The results show that the proposed method can successfully be used to simulate heart excitation anisotropic propagation in three-dimensional large tissue size, and it suggests that such method may provide a good basis for heart simulation research in a more physiologically way.

Since the action potential varies greatly on the wave front of excitation propagation, the adaptive multigrid may supply an inexpensive switching criterion, with which adaptive smoother terminates when the (scaled) residuals have become small, thus effectively decrease the iteration steps. Furthermore, the multilevel scheme of elliptic partial differential equations can be combined with adaptive mesh refinement. However, the adaptive choice of the discretization order is difficult, which will be a good topic for future research.

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# Analysis of Numerical Solutions to Stochastic Age-Dependent Population Equations

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**Abstract.** In this paper, stochastic age-dependent population equations, one of the important classes of hybrid systems, are studied. In general, most of stochastic age-dependent population equations do not have explicit solutions. Thus numerical approximation schemes are invaluable tools for exploring their properties. The main purpose of this paper is to develop a numerical scheme and show the convergence of the numerical approximation solution to the true solution.

## 1 Introduction

We consider the convergence of stochastic age-dependent population equation of the form

$$\frac{\partial P}{\partial t} + \frac{\partial P}{\partial a} = -\mu(t, a)P + f(t, P) + g(t, P)\frac{dW_t}{dt},$$

or

$$d_t P = [-\frac{\partial P}{\partial a} - \mu(t, a)P + f(t, P)]dt + g(t, P)dW_t, \quad (1)$$

where  $P(t, a)$  denotes the population density of age  $a$  at time  $t$ ,  $\beta(t, a)$  denotes the fertility rate of females of age  $a$  at time  $t$ ,  $\mu(t, a)$  denotes the mortality rate of age  $a$  at time  $t$ .  $f(t, P)$  denotes effects of external environment for population system.  $g(t, P)$  is a diffusion coefficient.

There has been an increasing interest in the study of age-dependent population equations. For example, Cushing [1] investigated hierarchical age-dependent populations with intra-specific competition or predation when  $g(t, P) = 0$ . Allen and Thrasher [2] considered vaccination strategies in age-dependent populations in the case of  $g(t, P) = 0$ . Existence, uniqueness and stability of strong solutions equation (1) were discussed in [3]. Pollard [4] studied the effects of adding stochastic terms to discrete-time age-dependent models that employ Leslie matrices. Using Lyapunov functional, numerical analysis for stochastic age-dependent population equation (1) has been studied by Zhang[5]. Abia [6] gave the numerical solution for non-linear age-dependent population models basing second-order finite difference schemes; explicit schemes of first-order were considered by Kostova [7] for a model describing interacting population dynamics; explicit two-step

second-order methods based on the central-difference operator along characteristics were studied by Milner and Rabbio [8] for the Gurtin- MacCamy model but assuming that the fertility rate in Eq.(1) is independent of the total size of the population. In this paper, by virtue of a direct approach quite different from those mentioned above, we shall prove that the numerical solutions converge to the exact solutions and provide the order of convergence. We give an example to show the efficiency of our numerical method.

## 2 Preliminaries and Approximation

Let

$$V = H^1([0, A]) \equiv \{\varphi | \varphi \in L^2([0, A]), \frac{\partial \varphi}{\partial x_i} \in L^2([0, A]),$$

where  $\frac{\partial \varphi}{\partial x_i}$  is generalized partial derivatives\}.

V is a Sobolev space.  $H = L^2([0, A])$  such that

$$V \hookrightarrow H \equiv H' \hookrightarrow V'.$$

$V'$  is the dual space of V. We denote by  $\|\cdot\|, |\cdot|$  and  $\|\cdot\|_*$  the norms in  $V, H$  and  $V'$  respectively; by  $\langle \cdot, \cdot \rangle$  the duality product between  $V, V'$ , and by  $(\cdot, \cdot)$  the scalar product in  $H$ . For an operator  $B \in \mathcal{L}(M, H)$  be the space of all bounded linear operators from  $M$  into  $H$ , we denote by  $\|B\|_2$  the Hilbert-Schmidt norm, i.e.

$$\|B\|_2^2 = tr(BWB^T).$$

Let  $(\Omega, \mathcal{F}, P)$  be a complete probability space with a filtrations  $\{\mathcal{F}_t\}_{t \geq 0}$  satisfying the usual conditions (i.e., it is increasing and right continuous while  $\mathcal{F}_0$  contains all  $P$ -null sets).

Let  $C = C([0, T]; H)$  be the space of all continuous function from  $[0, T]$  into  $H$  with sup-norm  $\|\psi\|_C = \sup_{0 \leq s \leq T} |\psi|(s)$ ,  $L_V^p = L^p([0, T]; V)$  and  $L_H^p = L^p([0, T]; H)$ .

Consider stochastic age-dependent population equation of the form

$$\begin{cases} d_t P = [-\frac{\partial P}{\partial a} - \mu(t, a)P + f(t, P)]dt + g(t, P)dW_t, & \text{in } Q = (0, T) \times (0, A), \\ P(0, a) = P_0(a), & \text{in } [0, A], \\ P(t, 0) = \int_0^A \beta(t, a)P(t, a)da, & \text{in } [0, T]. \end{cases} \tag{2}$$

where  $T > 0, A > 0, f(t, \cdot) : L_H^2 \rightarrow H$  be a family of nonlinear operators,  $\mathcal{F}_t$ -measurable almost surely in  $t. g(t, \cdot) : L_H^2 \rightarrow \mathcal{L}(M, H)$  is the family of nonlinear operator,  $\mathcal{F}_t$ -measurable almost surely in  $t.$

The integral version of Eq.(2) is given by the equation

$$P_t = P_0 - \int_0^t \frac{\partial P_s}{\partial a} ds - \int_0^t \mu(s, a)P_s ds + \int_0^t f(s, P_s) ds + \int_0^t g(s, P_s) dW_s, \tag{3}$$

here  $P_t = P(t, a).$



For system (2) the discrete approximate solution on  $t = 0, \Delta t, 2\Delta t, \dots, N\Delta t$  is defined by the iterative scheme

$$Q_t^{n+1} = Q_t^n - \frac{\partial Q_t^n}{\partial a} \Delta t - \mu(t, a) Q_t^n \Delta t + f(t, Q_t^n) \Delta t + g(t, Q_t^n) \Delta W_n, \quad (4)$$

with initial value  $Q_t^0 = P(0, a)$ ,  $Q^n(t, 0) = \int_0^A \beta(t, a) Q_t^n da$ ,  $n \geq 1$ . Here,  $Q_t^n$  is the approximation to  $P(t_n, a)$ , for  $t_n = n\Delta t$ , the time increment is  $\Delta t = \frac{T}{N} \ll 1$ , Brownian motion increment is  $\Delta W_n = W(t_{n+1}) - W(t_n)$ .

For convenience, we shall extend the discrete numerical solution to continuous time. We first define the step function

$$Z_t = Z(t, a) = \sum_{k=0}^{N-1} Q_t^k \mathbf{1}_{[k\Delta t, (k+1)\Delta t)}, \quad (5)$$

where  $\mathbf{1}_G$  is the indicator function for the set  $G$ . Then we define

$$Q_t = P_0 - \int_0^t \frac{\partial Q_s}{\partial a} ds - \int_0^t \mu(s, a) Z_s ds + \int_0^t f(s, Z_s) ds + \int_0^t g(s, Z_s) dW_s, \quad (6)$$

with  $Q_0 = P(0, a)$ ,  $Q(t, 0) = \int_0^A \beta(t, a) Q_t da$ ,  $Q_t = Q(t, a)$ . It is straightforward to check that  $Z(t_k, a) = Q_t^k = Q(t_k, a)$ .

The key contribution of this paper is to show that the approximate solution  $Q_t$  will converge to the true solution  $P_t$  of stochastic age-dependent population equation (2) under the given conditions. Because  $Q_t$  interpolates the discrete numerical solution, this will immediately give a convergence for  $Q_t^k$ .

As the standing hypotheses we always assume that the following conditions are satisfied:

- (i)  $f(t, 0) = 0, g(t, 0) = 0$ ;
- (ii) (Lipschitz condition) there exists a positive constant  $K$  such that  $x, y \in C$

$$|f(t, y) - f(t, x)| \vee \|g(t, y) - g(t, x)\|_2 \leq K \|y - x\|_C, \quad a.e.t; \quad (7)$$

- (iii)  $\mu(t, a), \beta(t, a)$  are continuous in  $\bar{Q}$  such that

$$0 \leq \mu_0 \leq \mu(t, a) \leq \bar{\alpha} < \infty, \quad 0 \leq \beta(t, a) \leq \bar{\beta} < \infty. \quad (8)$$

*Notes* It is known (cf.[3]) that Eq.(2) has a unique strong solution on  $t \in [0, T]$  under conditions (i)–(iii).

### 3 The Main Results

In this section, we will prove the convergence of  $Q_t$ . Throughout the following analysis we use  $C_1, C_2, \dots$  to denote generic constants that depend upon  $K, T$ , but not upon  $\Delta t$ . The precise values of these constants may be determined via the proofs.

In order to prove the convergence of  $Q_t$ , we first give several lemmas. our first lemma shows that the continuous approximation has bounded second moments in a strong sense.

**Lemma 1.** *Under the assumptions above, then*

$$E \sup_{t \in [0, T]} |Q_t|^2 \leq C_1. \tag{9}$$

*Proof.* From (6), one can obtain

$$dQ_t = -\frac{\partial Q_t}{\partial a} dt - \mu(t, a)Z_t dt + f(t, Z_t)dt + g(t, Z_t)dW_t. \tag{10}$$

Applying Itô formula to  $|Q_t|^2$  yields

$$\begin{aligned} |Q_t|^2 &= |Q_0|^2 + 2 \int_0^t \left\langle -\frac{\partial Q_s}{\partial a} - \mu(s, a)Z_s, Q_s \right\rangle ds + 2 \int_0^t (f(s, Z_s), Q_s) ds \\ &\quad + 2 \int_0^t (Q_s, g(s, Z_s) dW_s) + \int_0^t \|g(s, Z_s)\|_2^2 ds \\ &\leq |Q_0|^2 - 2 \int_0^t \left\langle \frac{\partial Q_s}{\partial a}, Q_s \right\rangle ds - 2\mu_0 \int_0^t (Z_s, Q_s) ds + 2 \int_0^t (f(s, Z_s), Q_s) ds \\ &\quad + \int_0^t \|g(s, Z_s)\|_2^2 ds + 2 \int_0^t (Q_s, g(s, Z_s) dW_s). \end{aligned}$$

Since

$$\begin{aligned} &-\left\langle \frac{\partial Q_s}{\partial a}, Q_s \right\rangle \\ &= -\int_0^A Q_s d_a(Q_s) = \frac{1}{2} \left( \int_0^A \beta(s, a) Q_s da \right)^2 \\ &\leq \frac{1}{2} \int_0^A \beta^2(s, a) da \int_0^A Q_s^2 da \\ &\leq \frac{1}{2} A^2 \bar{\beta}^2 |Q_s|^2. \end{aligned}$$

Therefore, we get that

$$\begin{aligned} |Q_t|^2 &\leq |Q_0|^2 + A^2 \bar{\beta}^2 \int_0^t |Q_s|^2 ds + 2 \int_0^t |Q_s| |f(s, Z_s)| ds \\ &\quad + 2\mu_0 \int_0^t |Q_s| |Z_s| ds + \int_0^t \|g(s, Z_s)\|_2^2 ds + 2 \int_0^t (Q_s, g(s, Z_s) dW_s). \end{aligned}$$

Now, it follows that for any  $t \in [0, T]$

$$\begin{aligned}
 & E \sup_{0 \leq s \leq t} |Q_s|^2 \\
 & \leq E|Q_0|^2 + (A^2\bar{\beta}^2 + 2 + \mu_0) \int_0^t E \sup_{0 \leq s \leq t} |Q_s|^2 ds + \int_0^t E|f(s, Z_s)|^2 ds \\
 & \quad + \int_0^t E\|g(s, Z_s)\|_2^2 ds + 2E \sup_{0 \leq s \leq t} \int_0^s (Q_r, g(r, Z_r) dW_r).
 \end{aligned}$$

Using condition (ii) yields

$$\begin{aligned}
 & E \sup_{0 \leq s \leq t} |Q_s|^2 \\
 & \leq E|Q_0|^2 + (A^2\bar{\beta}^2 + 2 + \mu_0) \int_0^t E \sup_{0 \leq s \leq t} |Q_s|^2 ds \tag{11} \\
 & \quad + 2K^2 \int_0^t E\|Z_s\|_C^2 ds + 2E \sup_{0 \leq s \leq t} \int_0^s (Q_r, g(r, Z_r) dW_r).
 \end{aligned}$$

We can argue in a similar manner as Zhang did in paper[5]. Hence our claim is proved.

Next, we show that the continuous time approximation remains close to the step function  $Z_t$  in a strong sense.

**Lemma 2.** *Assume the preceding hypotheses hold, then*

$$E \sup_{0 \leq t \leq T} |Q_t - Z_t|^2 \leq C_3 \Delta t. \tag{12}$$

*Proof.* For  $\forall t \in [0, T]$ , there exists an integer  $k$  such that  $t \in [k\Delta t, (k + 1)\Delta t)$ . We have

$$\begin{aligned}
 & Q_t - Z_t \\
 & = Q_t - Q_t^k \\
 & = - \int_{k\Delta t}^t \frac{\partial Q_s}{\partial a} ds - \int_{k\Delta t}^t \mu(s, a) Z_s ds + \int_{k\Delta t}^t f(s, Z_s) ds \\
 & \quad + \int_{k\Delta t}^t g(s, Z_s) dW_s.
 \end{aligned}$$

Thus,

$$\begin{aligned}
 & |Q_t - Z_t|^2 \\
 & \leq 4 \left| \int_{k\Delta t}^t \frac{\partial Q_s}{\partial a} ds \right|^2 + 4 \left| \int_{k\Delta t}^t \mu(s, a) Z_s ds \right|^2 + 4 \left| \int_{k\Delta t}^t f(s, Z_s) ds \right|^2 \\
 & \quad + 4 \left| \int_{k\Delta t}^t g(s, Z_s) dW_s \right|^2.
 \end{aligned}$$

Now, the Cauchy-Schwarz inequality and the assumptions give

$$\begin{aligned}
 & |Q_t - Z_t|^2 \\
 & \leq 4\Delta t \int_{k\Delta t}^t \|Q_s\|^2 ds + 4\bar{\alpha}^2 \int_{k\Delta t}^t |Q_s|^2 ds + 4\Delta t \int_{k\Delta t}^t |f(s, Z_s)|^2 ds \\
 & \quad + 4 \left| \int_{k\Delta t}^t g(s, Z_s) dW_s \right|^2 \\
 & \leq 4\Delta t \int_0^T \|Q_s\|^2 ds + 4\bar{\alpha}^2 \int_{k\Delta t}^t |Q_s|^2 ds + 4K^2 \Delta t \int_0^T |Q_s|^2 ds \\
 & \quad + 4 \left| \int_{k\Delta t}^t g(s, Z_s) dW_s \right|^2.
 \end{aligned}$$

Hence

$$\begin{aligned}
 & E \sup_{t \in [0, T]} |Q_t - Z_t|^2 \\
 & \leq 4\Delta t \int_0^T E \|Q_s\|^2 ds + 4\bar{\alpha}^2 C_1 \Delta t + 4K^2 \Delta t T C_1 \\
 & \quad + 4E \sup_{t \in [0, T]} \max_{k=0, 1, \dots, N-1} \left| \int_{k\Delta t}^t g(s, Z_s) dW_s \right|^2.
 \end{aligned}$$

Using the Doob inequality and (7), (9) yield

$$\begin{aligned}
 & E \sup_{t \in [0, T]} |Q_t - Z_t|^2 \\
 & \leq 4\Delta t \int_0^T E \|Q_s\|^2 ds + 4\bar{\alpha}^2 C_1 \Delta t + 4K^2 \Delta t T C_1 \\
 & \quad + 4 \max_{k=0, 1, \dots, N-1} \int_{k\Delta t}^{(k+1)\Delta t} E |g(s, Z_s)|^2 ds \\
 & \leq 4\Delta t \int_0^T E \|Q_s\|^2 ds + 4\bar{\alpha}^2 C_1 \Delta t + 4K^2 \Delta t T C_1 + 4K^2 C_1 \Delta t,
 \end{aligned}$$

Invoking lemma 3.2 of Zhang[5], we obtain the result (12).

We are now in a position to prove a strong convergence result.

**Theorem 1.** *Under the assumptions in Lemma 2, then*

$$E \sup_{0 \leq t \leq T} |P_t - Q_t|^2 \leq C_4 \Delta t. \tag{13}$$

*Proof.* Combining (3) with (6) has

$$\begin{aligned}
 & P_t - Q_t \\
 & = - \int_0^t \frac{\partial(P_s - Q_s)}{\partial a} ds - \int_0^t \mu(s, a)(P_s - Z_s) ds \\
 & \quad + \int_0^t (f(s, P_s) - f(s, Z_s)) ds + \int_0^t (g(s, P_s) - g(s, Z_s)) dW_s.
 \end{aligned}$$

Therefore using Itô formula, along with the Cauchy-Schwarz inequality and (7) yields,

$$\begin{aligned}
 & d|P_t - Q_t|^2 \\
 &= -2\langle P_t - Q_t, \frac{\partial(P_t - Q_t)}{\partial a} \rangle dt - 2(P_t - Q_t, \mu(t, a)(P_t - Z_t))dt \\
 &\quad + 2(P_t - Q_t, f(t, P_t) - f(t, Z_t))dt + \|g(t, P_t) - g(t, Z_t)\|_2^2 dt \\
 &\quad + 2(P_t - Q_t, (g(t, P_t) - g(t, Z_t))dW_t) \\
 &\leq A^2\bar{\beta}^2|P_t - Q_t|^2 dt + 2\bar{\alpha}|P_t - Q_t||P_t - Z_t|dt \\
 &\quad + 2K|P_t - Q_t||P_t - Z_t|_C dt + K^2\|P_t - Z_t\|_C^2 dt \\
 &\quad + 2(P_t - Q_t, (g(t, P_t) - g(t, Z_t))dW_t).
 \end{aligned}$$

Hence, for any  $t \in [0, T]$ ,

$$\begin{aligned}
 & E \sup_{s \in [0, t]} |P_s - Q_s|^2 \\
 &\leq (A^2\bar{\beta}^2 + \bar{\alpha} + K) \int_0^t E \sup_{r \in [0, s]} |P_r - Q_r|^2 ds \\
 &\quad + \bar{\alpha}E \int_0^t |P_s - Z_s|^2 ds + K(K + 1)E \int_0^t \|P_s - Z_s\|_C^2 ds \\
 &\quad + 2E \sup_{s \in [0, t]} \int_0^s (P_s - Q_s, (g(s, P_s) - g(s, Z_s))dW_s) \tag{14} \\
 &\leq (A^2\bar{\beta}^2 + 3\bar{\alpha} + 3K + 2K^2) \int_0^t E \sup_{r \in [0, s]} |P_r - Q_r|^2 ds \\
 &\quad + 2\bar{\alpha}E \int_0^t |Q_s - Z_s|^2 ds + 2K(K + 1)E \int_0^t \|Q_s - Z_s\|_C^2 ds \\
 &\quad + 2E \sup_{s \in [0, t]} \int_0^s (P_s - Q_s, (g(s, P_s) - g(s, Z_s))dW_s).
 \end{aligned}$$

By Burkholder-Davis-Gundy’s inequality, we have

$$\begin{aligned}
 & E \sup_{s \in [0, t]} \int_0^s (P_s - Q_s, (g(s, P_s) - g(s, Z_s))dW_s) \\
 &\leq k_1 E \left[ \sup_{0 \leq s \leq t} |P_s - Q_s| \left( \int_0^t \|g(s, P_s) - g(s, Z_s)\|_2^2 ds \right)^{1/2} \right] \tag{15} \\
 &\leq \frac{1}{4} E \left[ \sup_{0 \leq s \leq t} |P_s - Q_s|^2 \right] + k_2 \int_0^t E \|P_s - Z_s\|_C^2 ds,
 \end{aligned}$$

where  $k_1, k_2$  are two positive constants. Therefore inserting (15) into (14) has

$$\begin{aligned} & E \sup_{s \in [0,t]} |P_s - Q_s|^2 \\ & \leq (A^2 \bar{\beta}^2 + 3\bar{\alpha} + 3K + 2K^2 + 2k_2) \int_0^t E \sup_{r \in [0,s]} |P_r - Q_r|^2 ds \\ & \quad + 2(\bar{\alpha} + K + K^2 + k_2) \int_0^t E \sup_{s \in [0,t]} |Q_s - Z_s|^2 ds \\ & \quad + \frac{1}{2} E \sup_{s \in [0,t]} |P_s - Q_s|^2. \end{aligned}$$

Applying Lemma 2 we obtain a bound of the form

$$E \sup_{s \in [0,t]} |P_s - Q_s|^2 \leq D_1 \Delta t + D_2 \int_0^t E \sup_{r \in [0,s]} |P_r - Q_r|^2 ds,$$

where

$$\begin{aligned} D_1 &= 4(\bar{\alpha} + K + K^2 + k_2)TC_3, \\ D_2 &= 2(A^2 \bar{\beta}^2 + 3\bar{\alpha} + 3K + 2K^2 + 2k_2). \end{aligned}$$

The result (14) then follows from the continuous Gronwall inequality with

$$C_4 = D_1 \exp(D_2 T).$$

It is easy to deduce that the following theorem is satisfied.

**Theorem 2.** *Assume the preceding hypotheses hold, the approximate solution (6) will converge to the true solution of Eq. (2) in the sense*

$$\lim_{\Delta t \rightarrow 0} E \left[ \sup_{0 \leq t \leq T} |P_t - Q_t|^2 \right] = 0. \tag{16}$$

### 4 One Example

Let us consider a stochastic age-dependent population equation of the form

$$\begin{cases} d_t P = \left[ -\frac{\partial P}{\partial a} - \frac{1}{2(1-a)^2} P - \frac{1}{2} t P \right] dt + P dB_t, & \text{in } Q = (0, T) \times (0, 1), \\ P(0, a) = \frac{1}{2} \exp\left(-\frac{1}{1-a}\right), & \text{in } [0, 1], \\ P(t, 0) = \int_0^1 \frac{1}{2(1-a)^2} P(t, a) da, & \text{in } [0, T]. \end{cases} \tag{17}$$

Here  $B_t$  is a real standard Brownian motion (so,  $M = R$  and  $W = 1$ ). We can set this problem in our formulation by taking  $H = L^2([0, 1])$ ,

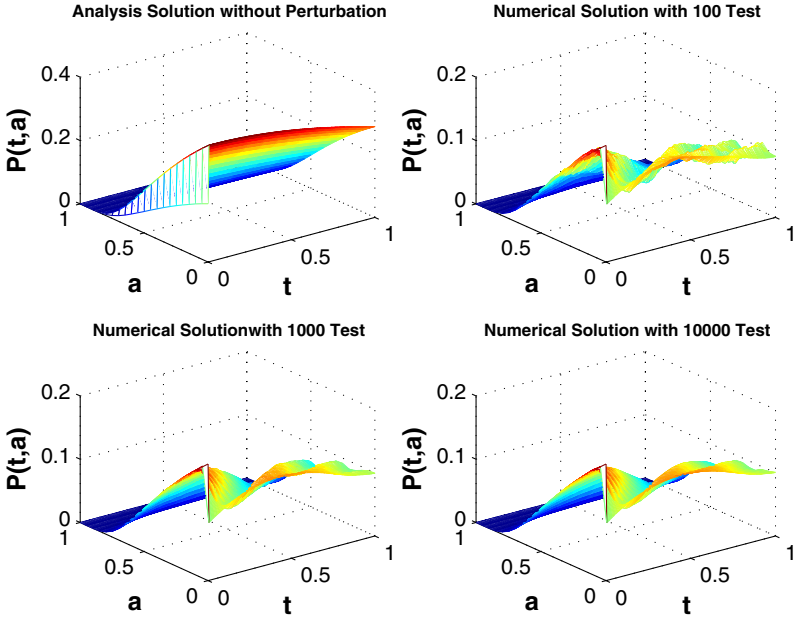


Fig. 1. Numerical Simulations of Stochastic Population Equation

$V = W_0^1([0, 1])$  (a Sobolev space with elements satisfying the boundary conditions above),  $\mu(t, a) = \beta(t, a) = \frac{1}{2(1-a)^2}$ ,  $f(t, P) = -\frac{1}{2}tP$ , and  $g(t, P) = P$ ,  $P_0(a) = \frac{1}{2}\exp(-\frac{1}{1-a})$ .

Clearly, the system (17) satisfy conditions (i)-(iii). Consequently, the approximate solution will converge to the true solution of (17) for any  $(t, a) \in (0, T) \times (0, 1)$  in the sense of Theorem 2

Take  $T = 1$  in Eq.(17). Fig.1 gives the pictures above with fixed step sizes  $\Delta t = 0.005$ ,  $\Delta a = 0.05$ . The Upper in the left is the explicit solution to Eq.(17) without perturbation, that is  $EP(t, a) = \exp(-\frac{1}{1-a} - \frac{t^2}{4})$ . The other three pictures are numerical simulations of the stochastic age-dependent population equations with 100, 1000 and 10000 experiments respectively, where  $EQ(t, a) = \frac{1}{n} \sum_{k=1}^n Q_k(t, a)$ . It clearly reveals the fact that the numerical approximation will tend to the true solution in the mean sense.

It is difficult to obtain the true explicit solution to Eq.(17), so the explicit solution  $P(t, a)$  to Eq.(17) can be replaced by  $\exp(-\frac{1}{1-a} - \frac{t^2}{4})(1 + \Delta B_t)$ . The Fig.2 shows the computer simulation for the difference between  $\exp(-\frac{1}{1-a} - \frac{t^2}{4})(1 + \Delta B_t)$  and the Euler approximation solution  $Q(t, a)$ . The maximum value of the error square is not greater than 0.05. Clearly the numerical approximation will tend to the true solution in the mean square sense.

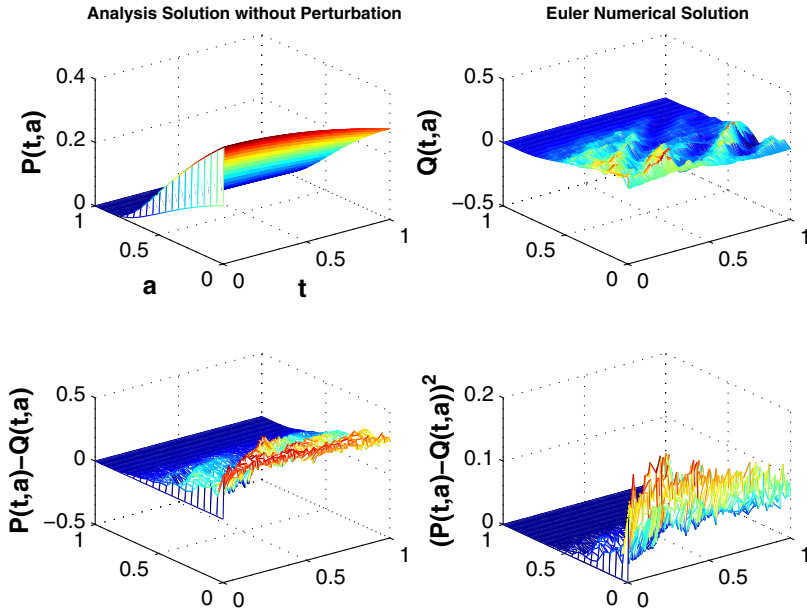


Fig. 2. Error Simulation of Stochastic Population Equation

## 5 Conclusion

In general, most of stochastic age-dependent population equations do not have explicit solutions, thus numerical approximation schemes are invaluable tools for exploring their properties. Using the Doob inequality and Burkholder-Davis-Gundy's inequality, the main purpose of this paper is to develop a numerical scheme and show the convergence of the numerical approximation solution to the true solution. We give an example to show the efficiency of our numerical method.

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# Classifying G-Protein Coupled Receptors with Hydropathy Blocks and Support Vector Machines

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**Abstract.** This paper develops a new method for recognizing G-Protein Coupled Receptors (GPCRs) based on features generated from the hydropathy properties of the amino acid sequences. Using the hydropathy characteristics, namely hydropathy blocks, the protein sequences are converted into fixed-dimensional feature vectors. Subsequently, the Support Vector Machine (SVM) classifier is utilized to identify the GPCR proteins belonging to the same families or subfamilies. The experimental results on GPCR datasets show that the proteins belonging to the same family or subfamily can be identified using features generated based on the hydropathy blocks.

## 1 Introduction

G-protein coupled receptors (GPCRs) is a superfamily of proteins that play key role in the signaling network which regulates the basic cellular processes: neurotransmission, cellular metabolism, secretion, inflammatory and immune response, taste and vision, etc [1]. Because of their crucial role in signal transduction, many researchers are focusing on understanding their structure and function. At present, more than 50% of drugs available on the market act through GPCRs [2]. However, their tertiary structures remain mostly unresolved, because of their difficult crystallization. To date, only the structure of one GPCR (bovine rhodopsin) has been solved [3]. On the other hand, the amino acid sequences of more than 1000 GPCR-related proteins have been determined. Therefore, it is strongly desired to develop an efficient and reliable method to predict the structure and function of GPCRs from sequence data.

One way towards this task is to classify the GPCRs into known families to induce its structural and functional features. In the literature, a variety of

approaches, e.g. PSI-BLAST [4], Hidden Marked Models (HMM) [5], and so forth, have been developed for classifying protein sequences by searching against protein databases with annotations of structure and function. However, these methods will not work when query proteins lack significant sequence similarity to the database sequences [2]. Recently, a machine learning method, namely Support Vector Machine (SVM) [6] [7], has been successfully applied to classifying GPCRs and shown the superiority to other methods [3] [2].

Most of the methods described above for classifying GPCR proteins depend on alignment or the similarities between protein sequences. Generally, the similarities can be characterized by the physicochemical properties of amino acids in protein sequences, such as polarity, solubility, hydrophathy, and so forth. Among these physicochemical properties, hydrophathy (the patterns of hydrophilicity and hydrophobicity) is known to be well conserved. In the literature, many methods have been developed for explaining the folding of proteins. Since the hydrophobicity profile of a membrane protein is conserved much better than the amino acid sequence itself during the evolution process, the hydrophathy profile has been used to identify the membrane proteins in various classical methods [8] [9] [10]. Furthermore, the hydrophathy patterns presenting in the protein sequences are used to develop reduced amino acid alphabets for protein secondary structure prediction [11] [12]. Recently, Panek et al. has developed a new method for identification of protein families based on hydrophathy distributions in proteins [13]. In the method developed by Panek et al., the number of segments must be optimally estimated in advance and the length of the protein sequence is not taken into account.

In this paper, we present a new method for classifying the GPCRs based on the hydrophathy blocks. Using the hydrophathy characteristics within the three hydrophathy subsets (strongly hydrophilic, strongly hydrophobic and weakly hydrophilic or weakly hydrophobic), we generate a number of  $k$ -tuples, called hydrophathy blocks here. Instead of dividing the protein sequences into segments and counting the number of hydrophathy characters in each segment, the frequencies of the hydrophathy blocks occurring in the protein sequence are calculated and used to generate fixed-dimensional vectors. Having obtained the feature vectors, the Support Vector Machine (SVM) classifier is utilized to classify the protein sequences into known families. Experiments on classifying GPCRs show the promising results.

The remainder of this paper is organized as follows. Section 2 describes the methods for feature extraction and presents an overview of Support Vector Machine. The experimental results and discussions are reported in Section 3. Finally, a conclusion is drawn in Section 4.

## 2 Methods

### 2.1 Feature Extraction

A protein sequence  $S$ , of length  $n$ , is defined as a linear succession of  $n$  symbols from the 20-letter amino acid alphabet  $\{A, C, D, E, F, G, H, I, K, L, M, N, P, Q,$

R, S, T, V, W, Y }. According to the hydropathy scale, the 20 amino acids can be grouped into 3 hydropathy sets: strongly hydrophilic (POL), strongly hydrophobic (HPO) and weakly hydrophilic or weakly hydrophobic (Ambi) (Table 1) [2]. Here, the abbreviations, i.e. POL, HPO and Ambi, for hydropathy characteristics used by Panek et al. are adopted. Proline and glycine are not classified into any hydropathy set because of their unique backbone properties, and Cysteine is excluded from any set because it has polarizable properties [14].

**Table 1.** Hydropathy Characteristics [13]

| Hydropathy characteristics                           | Abbreviation | Amino acids   |
|------------------------------------------------------|--------------|---------------|
| Strongly hydrophilic (polar)                         | POL          | r,d,e,n,q,k,h |
| Strongly hydrophobic                                 | HPO          | l,i,v,a,m,f   |
| Weakly hydrophilic or weakly hydrophobic (ambiguous) | Ambi         | s,t,y,w       |

In this paper, the 2 – tuples [15] generated from the 3 hydropathy sets instead the alphabet of 20 amino acids are used to generate feature vectors. The 2 – tuples extract various patterns of two consecutive residues with the same hydropathy characteristics in the protein sequence  $S$  and counts the number of occurrences of the 2 – tuples with overlapping. Here, the 2-tuples generated from the 3 hydropathy sets are called hydropathy blocks (abbreviated as 2-HBs) because they consist of successive residues with the same hydropathy characteristics just like the BLOCKS presenting in the protein sequences. Since the amino acids are grouped into 3 sets: POL, HPO and Ambi, we need to generate the 2-HBs for each set, respectively. The union of 2-HBs belonging to the POL set is noted as POL2, and the size of POL2 will be  $7^2 = 49$ . Similarly, the union of the 2-HBs belonging to the HPO set is noted as HPO2 and the union of the 2-HBs belonging to the Ambi set is noted as Ambi2. The size of HPO2 is  $6^2 = 36$ , and the size of Ambi2 is  $4^2 = 16$ .

One can count the number of the occurrences of 2-HBs by taking a 2 – letter sliding window that is run through the sequences, from position 1 to  $n - 2 + 1$ . Consequently, the number of occurrences of the 2-HBs in protein sequence  $S$  can be represented as:

$$\begin{aligned}
 POL_2 &= \{POL_2_1^S, POL_2_2^S, \dots, POL_2_i^S, \dots, POL_2_{49}^S\} \\
 HPO_2 &= \{HPO_2_1^S, HPO_2_2^S, \dots, HPO_2_j^S, \dots, HPO_2_{36}^S\} \\
 Ambi_2 &= \{Ambi_2_1^S, Ambi_2_2^S, \dots, Ambi_2_m^S, \dots, Ambi_2_{16}^S\}
 \end{aligned}$$

where  $POL_2_i^S$  represents the number of the  $i$ th 2-HB of POL2 occurring in sequence  $S$ ,  $HPO_2_j^S$  represents the number of the  $j$ th 2-HB of HPO2 occurring in sequence  $S$ , and  $Ambi_2_m^S$  represents the number of the  $m$ th 2-HB of Ambi2 occurring in sequence  $S$ . For example, for protein sequence

$S = \{STWPVERKHLVIVITN\}$ ,  $n=16$ , the counting determined by taking a 2-letter sliding window for  $n - 2 + 1 = 15$  times would be:

$$\begin{aligned} W_2^{POL} &= \{ER, RK, KH\} \\ W_2^{HPO} &= \{LV, VI, IV, VI\} \\ W_2^{Ambi} &= \{ST, TW\} \end{aligned}$$

and the number of 2-HBs occurring in  $S$  is:

$$\begin{aligned} POL_2 &= \{1, 1, 1\} \\ HPO_2 &= \{1, 2, 1\} \\ Ambi_2 &= \{1, 1\} \end{aligned}$$

In the above countings, those HBs not presented in  $S$  are not listed. Hence, the protein sequence can be represented as a linear succession of the 2-HBs, i.e.,  $V = [POL_2, HPO_2, Ambi_2]$ .

For a protein sequence  $S$ , suppose the size of  $POL_2$  be  $L_{POL_2}$ , the size of  $HPO_2$  be  $L_{HPO_2}$ , the size of  $Ambi_2$  be  $L_{Ambi_2}$ , and  $X = [X_{POL_2}^S, X_{HPO_2}^S, X_{Ambi_2}^S]$ , with

$$X_{POL_2_i}^S = \frac{C_i^{POL}}{\sum_{i=1}^{L_{POL_2}} C_i^{POL}}, \quad i = 1, \dots, L_{POL_2} \tag{1}$$

$$X_{HPO_2_j}^S = \frac{C_j^{HPO}}{\sum_{j=1}^{L_{HPO_2}} C_j^{HPO}}, \quad j = 1, \dots, L_{HPO_2} \tag{2}$$

$$X_{Ambi_2_m}^S = \frac{C_m^{Ambi}}{\sum_{m=1}^{L_{Ambi_2}} C_m^{Ambi}}, \quad m = 1, \dots, L_{Ambi_2} \tag{3}$$

where  $X_{POL_2_i}^S$  is the frequency of the  $i$ -th 2-HB of  $POL_2$  occurring in  $S$ , and  $C_i^{POL}$  is the times of the  $i$ -th 2-HB of  $POL_2$  occurring in  $S$ , and so forth. Consequently, the protein sequence  $S$  can be converted into a 101 dimensional vector:

$$v = \frac{X}{\sqrt{\text{length}(S) - 1}} \tag{4}$$

where  $\text{length}(S)$  is the length of protein sequence  $S$ .

### 2.2 Construction of Support Vector Machine

After converting the protein sequences into feature vectors, the next step is to classify the protein sequences into certain families. Many pattern recognition methods have been developed for protein sequence classification, among which the Support Vector Machine shows superior to other methods because of its good generality and strong statistical theory ground.

Support Vector Machine (SVM) is a class of supervised learning algorithms introduced by Vapnik [6], which is based on the well developed statistical learning theory. An important feature of SVM is that due to Mercer’s conditions on the kernels, the corresponding optimization problems are convex and hence have no local minima [16].

Given a set of labelled training vectors  $\mathbf{x}_i, i = 1, \dots, l$ , from two classes, labelled by  $y_i \in \{-1, +1\}, i = 1, \dots, l$ , SVM maps the input vectors  $\mathbf{x} \in R^n$  into a high dimensional feature space  $H$  by a mapping function  $\Phi(\cdot)$  and finds a hyperplane, which maximizes the margin, i.e., the distance between the hyperplane and the nearest data points of each class in the space  $H$ . The decision function implemented by SVM can be written as:

$$f(\mathbf{x}) = \text{sgn}\left(\sum_{i=1}^l y_i \alpha_i \cdot K(\mathbf{x}_i, \mathbf{x}) + b\right) \tag{5}$$

with

$$K(\mathbf{x}_i, \mathbf{x}) = \langle \Phi(\mathbf{x}_i), \Phi(\mathbf{x}) \rangle \tag{6}$$

where  $\alpha_i$ s are the coefficients obtained by solving the following optimization problem:

$$\begin{aligned} &\text{maximize} \quad \sum_{i=1}^l \alpha_i - 1/2 \sum_{i=1}^l \sum_{j=1}^l \alpha_i \alpha_j \cdot y_i y_j \cdot K(\mathbf{x}_i, \mathbf{x}_j) \\ &\text{subject to} \quad 0 \leq \alpha_i \leq C \\ &\quad \quad \quad \sum_{i=1}^l \alpha_i y_i = 0 \quad i = 1, 2, \dots, l. \end{aligned}$$

where  $C$  is a regularization parameter, which controls the trad-off between the margin and the misclassification error.

To construct the SVM classifier, we need to tune two parameters: the capacity, and the choice of kernel. The capacity generally allows us to control how much tolerance for the errors in the classification we allow. Hence, the capacity will affect the generalization ability of the SVM classifier and prevent it from overfitting the training set. On the other hand, the kernel function allows the SVM classifier to create a hyperplane in high dimensional space that effectively separates the training data. In this paper, the Gaussian kernel is employed for all the classifiers and the capacity is set to 1000.

### 3 Experimental Results and Discussions

We investigated the performance of our proposed method on identifying the families(classes) and subfamilies of the G protein-coupled receptors (GPCRs). Following the same three steps described in [3] and [2], we first discriminate the GPCRs from the non-GPCRs, then discriminate the five major classes of GPCR, and finally identify the subfamilies of ClassA of GPCRs.

Initially, we applied our proposed method (note as SVM-HB hereinafter) to identifying the GPCRs from the non-GPCRs. The dataset used here was obtained from <http://www.soe.ucsc.edu/research/compbio/gpcr/>. It consisted of 778 GPCRs from the five major GPCR classes and was used as the positive examples. Another dataset, which consisted of 99 decoy negative examples and 2425 negative examples obtained from SCOP version 1.37 PDB90 domain data, was used as the negative examples. Our proposed method was compared with GPCRpred developed by Raghava et al. [2], where SVMs were trained and tested using features generated from the dipeptide compositions. The performance was evaluated by 5-fold cross validations. Furthermore, four parameters - sensitivity, specificity, accuracy and Matthews' correlation coefficient (MCC)- were used to measure the performance of the two methods. The results were summarized in Table 2.

**Table 2.** The performance of SVM-HB and GPCRpred in differentiating GPCRs from non-GPCRs by 5-fold cross-validation

| Method                | Sensitivity (%) | Specificity (%) | ACC (%) | MCC  |
|-----------------------|-----------------|-----------------|---------|------|
| SVM-HB                | 100.00          | 100.00          | 99.96   | 0.99 |
| GPCRpred <sup>a</sup> | 98.60           | 99.80           | 99.50   | 0.99 |

*a.* The results were obtained from [2].

It can be seen from Table 2 that our proposed SVM-HB can differentiate GPCRs from non-GPCRs with accuracy of 99.96% and MCC of 0.9992, outperforms GPCRpred. The results suggest that using features generated from the hydropathy blocks, the SVM classifier can get better results in differentiating GPCRs from non-GPCRs than the one using features generated from the dipeptide components.

Subsequently, our proposed method was used to identify the five major classes of the GPCRs. According to the GPCRDB information system, the GPCR superfamily can be divided into five major classes: Class A (receptors related to rhodopsin and adrenergic receptors), Class B (receptors related to calcitonin and parathyroid hormone (PTH) receptors), Class C (receptors related to metabotropic receptors), Class D (receptors related to pheromone receptors) and Class E (receptors related to cAMP receptors). The datasets for the five classes were obtained from the work of Karchin et al. [3], and they were also used by Raghava et al. [2].

To predict the class of GPCRs, a series of binary SVMs were constructed, which were trained and tested using the feature vectors generated from hydropathy blocks. Our proposed SVM-HB was also compared with GPCRpred. Both SVM-HB and GPCRpred were evaluated by 2-fold cross-validation because of the low number of sequences. The performance was measured by the recognition rates (ACC) and MCC. The performance of the SVM-HB and GPCRpred is summarized in Table 3. It can be seen that SVM-HB can discriminate between all the GPCR classes exactly except for Class D. As pointed out in [2], the poor results were obtained due to the lower number of sequences for training. It was

**Table 3.** The performance of SVM-HB and GPCRpred in discriminating the five major GPCR classes

| GPCR classes                                       | Seq | SVM-HB |      | GPCRpred <sup>b</sup> |      |
|----------------------------------------------------|-----|--------|------|-----------------------|------|
|                                                    |     | ACC(%) | MCC  | ACC(%)                | MCC  |
| Rhodopsin and andrenergic-like receptors (Class A) | 692 | 100.00 | 1.00 | 98.10                 | 0.80 |
| Calcitonin and PTH-like receptors (Class B)        | 56  | 100.00 | 1.00 | 85.70                 | 0.84 |
| Metabotropic-like receptors (Class C)              | 16  | 100.00 | 1.00 | 81.30                 | 0.81 |
| Pheromone-like receptors (Class D)                 | 12  | 94.90  | 0.88 | 36.40                 | 0.49 |
| cAMP-like receptors (Class E)                      | 3   | 100.00 | 1.00 | 100.00                | 1.00 |

*b.* The results were obtained from [2].

readily found from Table 3 that our proposed SVM-HB performs significantly better than the GPCRpred method.

Generally, the determination of GPCR function is crucial for pharmaceutical research. To determine GPCR function from sequence information, we need to discriminate the GPCR subfamilies instead of superfamilies. Although superfamily discrimination can be achieved by various methods that generalize features shared by a diverse group of examples, it is usually difficult to discriminate the examples belonging to different subfamilies because they may differ only slightly [3]. The problem of recognizing GPCR subfamilies lies in the fact that the subfamily classification in GPCRDB is defined chemically (according to which ligand the receptor binds) rather than by sequence homology [3]. Here, we applied our proposed SVM-HB to classifying the subfamilies of the rhodopsin-like family. The datasets were obtained from <http://www.soe.ucsc.edu/research/compbio/gpcr/>, and the 14 datasets used in this experiment were the same ones used by Raghava et al.

The performance of our proposed method was evaluated using 2-fold cross-validation and compared with CPGRpred. The performance of SVM-HB and GPCRpred in terms of recognition rates (ACC) and MCC is shown in Table 4. It can be seen from that all subfamilies can be discriminated exactly using SVM-HB except Amine and Rhodopsin, and the performance of SVM-HB is much better than GPCRpred. The overall recognition rate and MCC for the 14 subfamilies of the rhodopsin-like family using SVM-HB are 99.93% and 0.9986, respectively. Poor results were obtained due to the lower number of sequences for training.

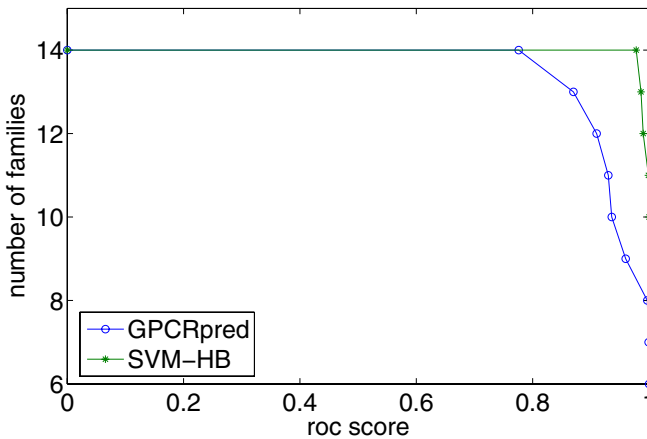
Furthermore, the ROC scores were also used to estimate the performance of the GPCRpred and SVM-HB methods in identifying subfamilies of the rhodopsin-like family of GPCR. The experimental results are shown in Fig.1, where a higher curve corresponds to a more accurate classification result. It can



**Table 4.** The performance of SVM-HB and GPCRpred in identifying subfamilies of the rhodopsin-like family of GPCR

| GPCR classes                   | SVM-HB |      | GPCRpred <sup>c</sup> |      |
|--------------------------------|--------|------|-----------------------|------|
|                                | ACC(%) | MCC  | ACC(%)                | MCC  |
| Amine                          | 99.10  | 0.99 | 99.10                 | 0.99 |
| Peptide                        | 100.00 | 1.00 | 99.70                 | 0.95 |
| Hormone proteins               | 100.00 | 1.00 | 100.00                | 1.00 |
| Rhodopsin                      | 99.96  | 0.99 | 98.90                 | 0.99 |
| Olfactory                      | 100.00 | 1.00 | 100.00                | 0.99 |
| Prostanoid                     | 100.00 | 1.00 | 100.00                | 0.99 |
| Nucleotide-like                | 100.00 | 1.00 | 85.40                 | 0.92 |
| Cannabis                       | 100.00 | 1.00 | 100.00                | 1.00 |
| Platelet activating factor     | 100.00 | 1.00 | 100.00                | 1.00 |
| Gonadotropin releasing hormone | 100.00 | 1.00 | 100.00                | 1.00 |
| Thyrotropin releasing hormone  | 100.00 | 1.00 | 85.70                 | 0.93 |
| Melatonin                      | 100.00 | 1.00 | 100.00                | 1.00 |
| Viral                          | 100.00 | 1.00 | 33.30                 | 0.58 |
| Lysospingolipids               | 100.00 | 1.00 | 58.80                 | 0.76 |
| Overall                        | 99.93  | 0.99 | 97.30                 | 0.97 |

c. The results were obtained from [2].



**Fig. 1.** Relative performance of the SVM-HB method and the GPCRpred method, where the curves show the number of families vs a ROC score threshold for the two methods

be seen from Fig.1 that using the hydropathy blocks, the SVM classifiers can better discriminate GPCR subfamilies than using the features generated from

the dipeptide compositions. The results in Table 4 and Fig.1 show again that using the hydropathy blocks, we can extract more biological information than using the dipeptide compositions.

## 4 Conclusions

Hydropathy is one of important physicochemical properties of amino acids, and is better conserved than protein sequences in evolution. In this paper, we introduce a new method for identifying families or subfamilies of GPCR in a set of proteins using information extracted from protein sequences based on hydropathy blocks. Our proposed method has been applied to differentiating GPCR proteins from non-GPCR proteins, identifying the five major GPCR classes, and discriminating subfamilies of rhodopsin-like family of GPCR. Experimental results show that our proposed method using hydropathy blocks is indeed efficient and outperforms the method based on dipeptide composition in classifying GPCRs.

## Acknowledgments

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# HSPPIP: An Online Tool for Prediction of Protein–Protein Interactions in Humans

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**Abstract.** Recently, protein-protein interaction prediction (PPIP) has been emerging as an appealing question. Although several *in silico* approaches have been developed to delineate the potential protein-protein interaction (PPI), there are few online tools of human PPIP for further experimental design. Here we present an online service, hsPPIP (Protein-Protein Interaction Predicting of Homo Sapiens), to predict or evaluate the potential PPIs in human. The annotations of functional domain (Interpro) and GO (Gene Ontology) for proteins are employed as two informative features, and are integrated by the naïve Bayesian approach. The prediction accuracy is comparable to the existing tools. Based on the hypothesis that the features correlated with PPIs are conserved in different organisms, the web server hsPPIP is established and could predict the PPIs of human dynamically. hsPPIP is implemented in PHP+MySQL and can be freely accessed at: <http://973-proteinweb.ustc.edu.cn/hspip/>.

## 1 Introduction

Dissecting the Protein-Protein Interaction (PPI) network in a cell is the foundation for elucidating all kinds of cellular mechanisms. *In vivo* or *in vitro* PPI identifications are usually time-consuming and labour intensive. Although high-throughput approaches have generated many data sets of PPIs, they are fairly noisy and need further confirmation by *in vivo* or *in vitro* experiments. So for its statistical accuracy and convenience, *in silico* PPI prediction (PPIP) might be a great help and insightful for further experimental consideration.

In this work, we have developed an easy-to-use online tool, hsPPIP (Protein-Protein Interaction Predicting of Homo Sapiens), to predict or evaluate the potential PPIs of human. We choose the annotations of functional domain (Interpro) [1] and GO (Gene Ontology) [2] for proteins as two features associated with PPIs. The naïve Bayesian approach is adopted to integrate the features together to improve the prediction accuracy. Since there is increasing evidence that interacting protein pairs are usually co-conserved through evolution and the PPI network structures are also conserved in different organisms [3, 4], we hypothesize that the features correlated with PPIs are also conserved in different organisms. So we might predict human PPIs

based on the associated features from budding yeast. hsPPIP is especially fast and convenient for the construction of small scale human PPI networks. Although there have been several other web servers or databases for human PPIP, we propose that hsPPIP could be a useful tool for the experimentalists.

## 2 Materials and Methods

### 2.1 Training Data Set

The PPI data set for training was collected from six public PPI database, the MIPS CYGD (Comprehensive Yeast Genome Database) PPI (Mar. 2004) [11], BIND (Biomolecular Interaction Network Database) (Apr. 2004) [12], GRID (General Repository for Interaction Database) (Mar. 2004) [13], SGD (Saccharomyces Genome Database) (Apr. 2004) [14], MINT (Molecular INTERaction database) (Apr. 2004) [15], and Database of Interacting Proteins (DIP) (Mar. 2004) [16]. We only used budding yeast PPI data in the current analysis. The PPI information of each PPI database is listed in table 1. We combined the six PPI data sets into a non-redundant PPI data set including 21, 295 unique protein pairs. We also manually validated the data set.

### 2.2 Gold Standards and Testing Data

To test our method, we adopt both positive and negative control data sets reported previously [5]. The positive control contains protein pairs from the same MIPS complex (pos\_MIPS), and the negative control is protein pairs with different subcellular localization and couldn't be found in verified PPI list (L\_neg). As in the literature [5], the positive control is regarded as the set of positive PPIs ( $P$ ), and the negative control is regarded as the set of negative PPIs ( $N$ ).

For comparison, we also randomly generate 200, 000 protein pairs (Random200K), in which the real PPIs are expected to be only a small fraction. The gold standard and testing data sets are listed in table 1.

### 2.3 Collection of Human and Yeast Proteins

The protein sequences were downloaded from ExPASy (<ftp://cn.expasy.org>). The hsPPIP used the protein accession numbers as standard entries for prediction. All accession numbers of human and yeast proteins are retrieved and stored in the local MySQL database for further processing.

### 2.4 Protein Annotation by Functional Domain (Interpro) and Gene Ontology (GO)

Interpro is an integrated resource of annotation for protein families, functional domains and motifs [1]. Gene Ontology Consortium [2] is to produce a controlled vocabulary as the knowledge of gene and protein roles in cells. We downloaded the files containing all Interpro and GO annotations for the proteins from the EBI repository (<ftp://ftp.ebi.ac.uk/pub/databases/>), and mapped the Interpro and GO

annotations to human and yeast proteins, respectively. The information is also stored in our local MySQL database and could be searched and browsed. Users could search or browse our local database for each protein entry in human or yeast.

We excluded three GO annotations from the analysis: GO:0000004 (biological\_process unknown), GO:0008372 (cellular\_component unknown), and GO:0005554 (molecular\_function unknown), since such unknown and ambiguous assignments might introduce noises into the analysis.

**Table 1.** The total data sets we used for this work. Training data set is retrieved and combined from six public PPI databases into a non-redundant PPI data set, including 21, 295 protein pairs. The gold standard is taken from the previous work [5] with both positive and negative control. We also randomly generate 200, 000 protein pairs as an additional testing data set.

| Data type      | Data set                           | # Protein pairs                        | Used for ... |
|----------------|------------------------------------|----------------------------------------|--------------|
| Training data  | CYGD (MIPS) (2004-03-21)           | 11,862                                 | Training     |
|                | BIND (2004-04-01)                  | 5,875                                  |              |
|                | GRID (2004-03-18)                  | 19,038                                 |              |
|                | SGD (2004-04-01)                   | 4,624                                  |              |
|                | MINT (2004-04-01)                  | 14,014                                 |              |
|                | DIP (2004-03-07)                   | 15,393                                 |              |
|                | TOTAL (non-redundant PPI data set) | 21,295                                 |              |
| Gold standards | Positive                           | Protein pair in the same MIPS complex  | 8,617        |
|                | Negative                           | Protein pair separated by localization | 2,705,844    |
| Testing data   | Random                             | Random PPI (200K)                      | 200,000      |

### 2.5 Algorithm

PPIP (protein-protein interaction prediction) with functional domain-based strategies is widely used [17, 18, 19, 20]. In this work we adopt the Naïve Bayesian approach to integrate two features, functional domains and GO annotations, for PPIP. We considered if two proteins  $P_i, P_j$  have  $a, b$  Interpro annotations and  $c, d$  GO annotations respectively, then the probability of  $P_i$  and  $P_j$  to be interacting pair is shown below:

$$P(PPI_{ij} = 1) = 1 - \prod_{(I_a, I_b) \in (P_i \times P_j)} (1 - P(I_{ab} = 1)) \times \prod_{(G_c, G_d) \in (P_i \times P_j)} (1 - P(G_{cd} = 1)) \tag{1}$$

$PPI_{ij}=1$ : Protein  $P_i$  interacts with Protein  $P_j$ .

$I_{ab}= 1$ : Interpro annotation  $I_a$  and  $I_b$  are interacting functional domain.

$G_{cd}= 1$ : GO annotation  $G_c$  and  $G_d$  are functional associated.

$a, b$ : Numbers of Interpro annotations in  $P_i$  and  $P_j$ , respectively.

$c, d$ : Numbers of GO annotations in  $P_i$  and  $P_j$ , respectively.

$(I_a, I_b) \in (P_i \times P_j)$ : Interpro pair  $(I_a, I_b)$  is included in protein pair  $P_i \times P_j$ .

$(G_c, G_d) \in (P_i \times P_j)$ : GO pair  $(G_c, G_d)$  is included in protein pair  $P_i \times P_j$ .

The  $P(I_{ab} = 1)$  and  $P(G_{cd} = 1)$  could be obtained from training our non-redundant PPI data set. And the equation for calculating the two probabilities could be proposed as:

$$P(I_{ab} = 1) = \frac{Int_{ab}}{N_{ab}} \tag{2}$$

$$P(G_{cd} = 1) = \frac{Int_{cd}}{N_{cd}} \tag{3}$$

$Int_{ab}$ : Number of PPIs that include  $(I_a, I_b)$ ;

$N_{ab}$ : Number of all potential PPIs that include  $(I_a, I_b)$ .

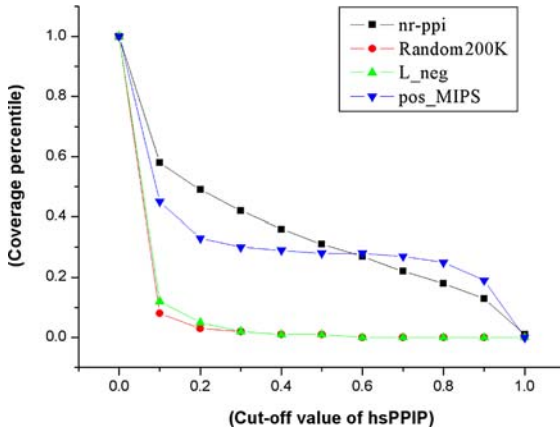
$Int_{cd}$ : Number of PPIs that include  $(G_c, G_d)$ ;

$N_{cd}$ : Number of all potential PPIs that include  $(G_c, G_d)$ .

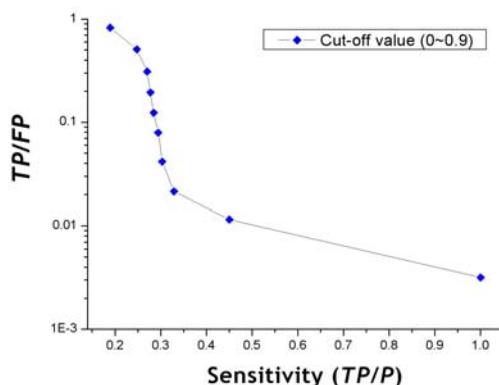
### 3 Results and Discussion

#### 3.1 Testing the Accuracy of hsPPIP

Table 1 gives the basic information about the PPI data sets used in this work. We test our approach with four data sets: our training data set (nr\_ppi), random PPI (Random200K), positive control (pos\_MIPS) and negative control (L\_neg). For random PPI, we randomly pick out two proteins of budding yeast to form 200,000 pairs. Obviously, this data set contains some real PPI, but its overall characteristics should be similar to the negative control. The cut-off value of hsPPIP is changed from 0-0.9 with per 0.1 per step. The result is diagramed in figure 1.



**Fig. 1.** Prediction accuracy of hsPPIP. We use four data sets to test the prediction accuracy: the training data set (nr-ppi), positive control (pos\_MIPS), random PPIs (Random200K) and negative control (L\_neg). It's clear that the positive control is much similar with the training data. And both the negative and random PPIs get little hits. The default cut-off value of hsPPIP is taken as 0.3.



**Fig. 2.** The curve of TP/FP vs. Sensitivity (TP/P) under certain cut-off value of hsPPIP. We change the cut-off value of hsPPIP from 0-0.9 with per 0.1 per step. With the cut-off value of hsPPIP as 0.3, the TP/FP is 0.041 and Sensitivity (TP/P) is about 30.32%. If the cut-off value is taken as 0.7, the TP/FP is 0.309 and Sensitivity (TP/P) is about 27.04%, which could be comparable with the previous work.

**Fig. 3.** The prediction page of hsPPIP WWW server. For convenience, hsPPIP supports PPIP in both budding yeast and human. The default cut-off value is taken as 0.3. Two accessing methods are provided. The first is Complex Prediction, which gives out all the potential PPIs among the given list of proteins with the predicted probabilities higher than the cut-off. The second is PPI Verification, which verifies the given list of PPIs with the predicted probabilities higher than the cut-off. Users could either choose Interpro & GO or one of the two features for PPIP.



It's obvious that the training data set gets the best accuracy. And the curve of positive control is much similar with the training data set. The curves of both the negative control and random PPI are similar and very different to our positive control and training data set. So we propose that hsPPIP could distinguish true positive PPIs from random PPIs accurately. The curve of the positive inclines to smooth when *cut-off value* is greater than 0.3. And even when *cut-off value* is great than 0.9, our approach could still predict ~20% PPIs in positive control properly. For convenience, we set the default *cut-off value* of hsPPIP as 0.3. Users could choose their favorite *cut-off value*.

We also perform an additional test with *TP/FP* vs. Sensitivity (*TP/P*) and compare the prediction results with previous work [5]. The *P* is total positive PPIs and *TP* is true positive PPIs which hsPPIP could predict properly. The *FP* is false positive predictions from hsPPIP. We change the *cut-off value* of hsPPIP from 0-0.9 with per 0.1 per step. The result is diagramed in figure 2.

With the *cut-off value* of hsPPIP as 0.3, the *TP/FP* is ~0.041 and Sensitivity (*TP/P*) about 30.32%. If the *cut-off value* is taken as 0.7, the *TP/FP* is ~0.309 and Sensitivity (*TP/P*) about 27.04%, which could be comparable with the previous work (Ref. 5, Figure 2C, *TP/FP*: ~0.3-0.4, Sensitivity (*TP/P*): ~27%).

### 3.2 The Implementation of Web Server

The web server of hsPPIP has been implemented in PHP+MySQL. The web server is developed mainly for human PPIP. But for convenience, we also include the PPIP of budding yeast. In our system, only protein's Swissprot accession numbers are available. In addition, the information for proteins included in hsPPIP could be visited by either searching or browsing. The correlated probabilities of two features associated with PPIs, Interpro and GO annotations, are pre-computed and stored in a MySQL database. There are two approaches to access hsPPIP. Firstly, for complex prediction, users could submit a list of their required proteins with the Swissprot accession numbers. hsPPIP will find all the potential PPIs among the given list of proteins with predicted probabilities higher than the cut-off. Secondly, for PPI verification, users could submit a list of protein pairs, and hsPPIP will find all the potential PPIs whose probabilities are higher than the cut-off. The prediction page of hsPPIP is shown in Figure 3.

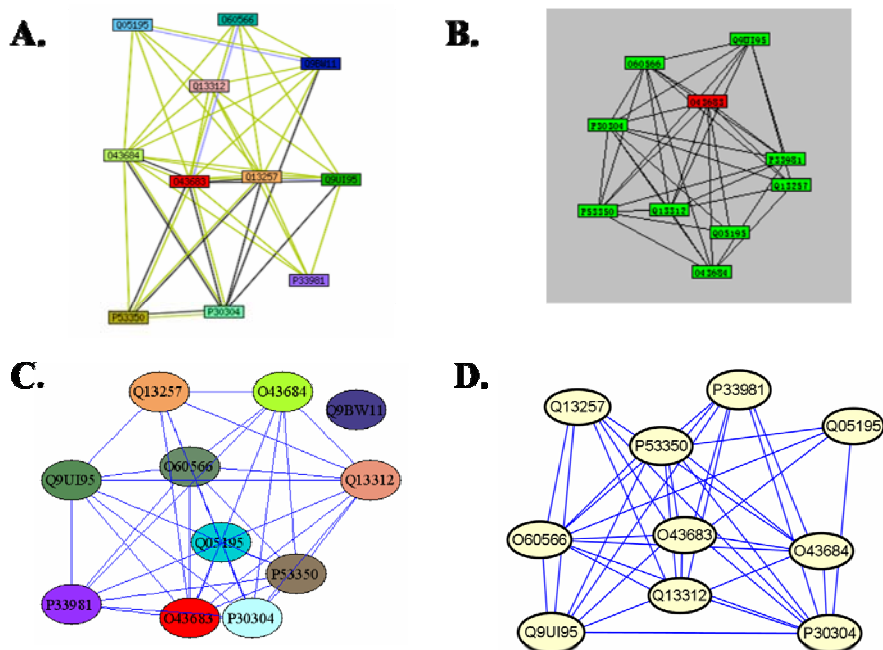
The hsPPIP could export the prediction results into multiple file formats. The plain text format could be downloaded and viewed locally. The .dot format file could be imported into the professional graphic software Graphviz (<http://www.research.att.com/sw/tools/graphviz/>) to get a publication-quality figure. Users could modify the color setting for nodes (proteins) and edges (interactions) of the .dot file. Moreover, the .sif format file could be generated for Cytoscape [6]. We also adopt a Java applet program [7] (a modified version for hsPPIP) to visualize the prediction results directly in the web browser.

### 3.3 An Example of Usage

Here we use human Bub1 protein (Swissprot accession number: O43683) and its putative interacting partners as an instance to diagram the usage of hsPPIP. Human Bub1 protein is one of the spindle checkpoint components localized to kinetochore during mitosis, blocking the onset of anaphase until all chromosomes are attached to

microtubules properly [8]. Aberrant organization of spindle checkpoint complex will contribute the genomic instability and aneuploidy, which could induce a variety of cancers with high rate [9]. Although many experimental studies were performed to depict the PPIs implicated in spindle checkpoints, it's still unclear how many proteins will interact with Bub1 and Bub1-related sub-network.

Firstly, we used STRING web server [10] to get the putative interacting partners of human Bub1 with default parameters (see in figure 4A). The sub-network contains eleven human proteins that interact with each other. Then we retrieve the Swissprot accession number of the eleven proteins and input them into hsPPIP for Complex Prediction. The default *cut-off value* for hsPPIP is 0.3. And the prediction results are visualized by Java applet in figure 4B. Only protein with at least one interaction with other proteins is shown. Moreover, the .dot file of prediction results from hsPPIP is modified directly and imported into Graphviz with the output format .png (see in figure 4C). In addition, .sif file format could be visualized by Cytoscape (see in figure 4D). By comparing the prediction results of hsPPIP to STRING, we find the prediction results of hsPPIP are similar with of STRING. Some putative PPIs are existed in STRING while missed by hsPPIP, such as Mxd3 protein (Q9BW11) with its binding partners. But there are several putative PPIs not existed in STRING but



**Fig. 4.** Predicted sub-network for human Bub1 protein (O43683). (A) The prediction results of STRING, one of the most popular web servers for PPIP. (B) The prediction results of hsPPIP is visualized by java applet online. (C) The prediction results of hsPPIP is modified directly and then imported to Graphviz for visualization. (D) The prediction results of hsPPIP is viewed in Cytoscape.

predicted by hsPPIP. For instance, another spindle checkpoint protein human BubR1 (O60566) is predicted to interact with MAD (Q05195) by hsPPIP, but STRING doesn't find this potential interaction. And the predicted PPIs for human Bub1 may be insightful and needs the further experimental verification.

## 4 Conclusions

In this work, we provide a web server hsPPIP for protein-protein interaction prediction in human. For convenience, the hsPPIP could also predict the PPIs in budding yeast. The prediction results could be downloaded, modified locally, or visualized online directly. We also use human Bub1 protein to predict its potential PPIs and construct its sub-network by hsPPIP. Compared to another popular web server STRING, the prediction results are similar. Users could submit their favorite proteins in a list to predict the PPIs among them. The prediction results from hsPPIP may be helpful and insightful for further experimental design.

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# Prediction of Ribosomal -1 Frameshifts in the *Escherichia coli* K12 Genome

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**Abstract.** Ribosomal frameshifting at a particular site can yield two protein products from one coding sequence or one protein product from two overlapping open reading frames. Many organisms are known to utilize ribosomal frameshifting to express a minority of genes. However, finding ribosomal frameshift sites by a computational method is difficult because frameshift signals are diverse and dependent on the organisms and environments. There are few computer programs available for public use to identify frameshift sites from genomic sequences. We have developed a web-based application program called FSFinder2 for predicting frameshift sites of general type. We tested FSFinder2 on the *Escherichia coli* K12 genome to detect potential -1 frameshifting genes. From the genome sequence, we identified 18,401 frameshift sites following the X XXY YYZ motif. 11,530 frameshift sites out of the 18,401 sites include secondary structures. Comparison with the GenBank annotation produced 11 potential frameshift sites, including 3 known frameshift sites. The program is useful for analyzing frameshifts of various types and for discovering new genes expressed by frameshifts.

## 1 Introduction

Ribosomes in general terminate translation at three kinds of stop codons (UAG, UGA and UAA), but some ribosomes continue to decode after the stop codons. This alternative translational event is called 'recoding'. Recoding events include frameshifting, read-through and bypassing [1-3]. In frameshifting, ribosomes shift reading frame by one or more nucleotides at a specific mRNA signal between overlapping genes [4]. Frameshifts are classified into different types depending on the number of nucleotides shifted and the shifting direction. The most common type is a -1 frameshift, in which the ribosome slips a single nucleotide in the upstream direction. -1 frameshifting requires a frameshift cassette that consists of a slippery site, a stimulatory RNA structure and a spacer. +1 frameshifts are much less common than -1 frameshifts, but have been observed in diverse organisms [1].

No program exists to predict general types of frameshift. In addition, existing computational models predict too many false positives. In previous work we developed a program called FSFinder (Frameshift Signal Finder) for predicting -1 and +1

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frameshift sites [5]. That program is written in Microsoft C# and is executable on Windows systems only. To remove these limitations and to handle frameshifts of general type, we developed a new web-based application called FSFinder2. Users can predict frameshift sites of any type online from any web browser and operating system.

In previous experimental results of testing FSFinder2 on ~190 genomic and partial DNA sequences showed that it predicted frameshift sites efficiently and with greater sensitivity and specificity than other programs, because it focused on the overlapping regions of ORFs and prioritized candidate signals (For -1 frameshifts, sensitivity was 0.88 and specificity 0.97; for +1 frameshifts, sensitivity was 0.91 and specificity 0.94) [5-7].

Using the web service of the FSFinder2, we analyzed the *Escherichia coli* (*E. coli*) K12 genome sequence to find the -1 frameshifting genes with high probability. From the *E. coli* K12 genome sequence, we found 18,401 frameshift sites after the X XXY YYZ motif. Among these sequences, 11,530 frameshift sites included secondary structure such as pseudoknots or stem-loops. Using the GenBank description we found 312 overlapping regions of two genes with more than 1 base. Using FSFinder we found 309 overlapping regions with more than 30 bases. After removing redundant ones, we obtained 195 overlapping regions and found 66 potential frameshift sites in the 195 overlapping regions. Among these sites, 11 sites including 3 known frameshift sites were considered significant based on the gene length, shape and the length of overlapping region. We believe that at least 4 new frameshift sites are highly likely to be frameshift sites.

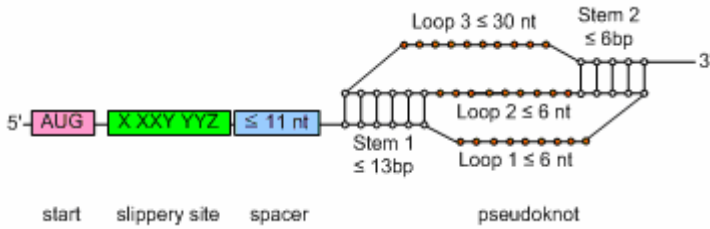
## 2 Analyzing Method

### 2.1 Finding Frameshift Motifs

The cassettes of -1 frameshift consist of three parts: slippery site, spacer and secondary structure. The slippery site is usually a heptameric sequence in the form X XXY YYZ (in the incoming 0-frame), where X, Y and Z can be same nucleotides [5-7]. The spacer is a short sequence of 5 to 11 nucleotides separating slippery site and the downstream secondary structure. The downstream structure is usually a pseudoknot or simple stem-loop, as shown in Fig. 1.

For analyzing frameshift sites in the *E. coli* genome sequence, we detected heptameric sequence with a secondary structure. In previous work by others [5-7], frameshift sites have two constraints. In slippery site X XXY YYZ, X is any nucleotide, Y is A or U, and Z is either A, U or C. However, in our work, any kind of nucleotide with secondary structure can be located in the slippery sequence.

Fig. 2 shows the parameters for the FSFinder web service. The web service and web application of FSFinder2 were implemented using XML, XSLT and JavaScript. If the user sends a query to the FSFinder2 server after setting parameters or defining a new model, all the computations are done on the server side. After computation, the server sends the results to the user.



**Fig. 1.** A programmed -1 ribosomal frameshift signal with H-type pseudoknot. Stem 1 has 11 base pairs, stem 2 has 6 base pairs, and both loops of the pseudoknot have 6 nucleotides. In particular, any nucleotide can be located in the slippery site not the same as previous work.

The screenshot shows the FSFinder web service interface. Section A, '1. Select option', includes radio buttons for target genes (dnaX, oaz, prfB, other genes in bacteria, genes in viruses), size of sequence (Full genome, Partial sequence <3000bp), and direction (+ strand, - strand). Section B, '2. Edit model', shows a model list with '-1 frameshift signal' selected and a context menu with options: Add new model, Add default model, Delete model. Section C, 'Edit components', shows the model name '-1 frameshift signal', a checked '-1 frame' option, and search settings (Find first). The 'Pattern' section includes 'X,XXY,YYZ' and 'NNN'. The 'spacer' is set to '4~11 nt'. The 'RNA structure' section has checked 'Stem' and 'Pseudoknot', with lengths: Stem1 < 13, Stem2 < 6, Loop1 < 6, Loop2 < 6, Loop3 < 30. At the bottom, there are fields for 'Insert or delete components' and 'Select the component type' (Pattern type).

**Fig. 2.** The input page of the FSFinder web service. (A) The select option lets the user choose the type of genes expressed via frameshifts, the size of the sequence and its direction. (B, C) The user can define a new model by specifying its components and their locations. To analyze *E. coli* genome, we set the selection option as other genes in bacteria, partial sequence and +1 strand. Because we focused on -1 frameshift model, we made a model which is the general motif X XXY YYZ of the -1 frameshift. There was no limitation of frameshift site, thus any kind of nucleotide can be located in the frameshift site. For downstream secondary structure, the length of the stems and loops set by default.

```

<FSFinder_run xmlns="http://wilab.inha.ac.kr/WSFSFinder/">
 <FSFinder_Input xmlns:xsd=http://www.w3.org/2001/XMLSchema
 xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance">
 <Sequence_information>
 <Target_gene>other genes in bacteria</Target_gene>
 <Sequence_size>Patial</Sequence_size>
 <Sequence_direction>Plus strand</Sequence_direction>
 <Sequence>input sequence</Sequence>
 <Sequence_name>E. coli K-12</Sequence_name>
 </Sequence_information>
 <FSFinder_Model_List>
 <FSFinder_Model Find_first="0" Overlap_with="-1">
 <Model_name>-1 frameshift signal</Model_name>
 <Components>
 <Pattern_type Spacer="0">
 <Pattern>X,XXY,YYZ</Pattern>
 <Pattern_match>NNN</Pattern_match>
 </Pattern_type>
 <RNA_structure_type Spacer="4~11" Structure=
 "StemLoop;Pseudoknot">
 <Stem1_size_max>13</Stem1_size_max>
 <Stem2_size_max>6</Stem2_size_max>
 <Loop1_size_max>6</Loop1_size_max>
 <Loop2_size_max>6</Loop2_size_max>
 <Loop3_size_max>30</Loop3_size_max>
 </RNA_structure_type>
 </Components>
 </FSFinder_Model>
 </FSFinder_Model_List>
 </FSFinder_Input>
</FSFinder_run>

```

**Fig. 3.** XML schema with the parameters shown in Fig. 2. If the user sets the parameters of a model in the web page of the FSFinder web service, the parameters are converted to XML. After the request of a web service is sent to the FSFinder server, all the computations are done on the server side.

To analyze *E. coli* genome, we set the selection option as other genes in bacteria, partial sequence and + strand (Fig. 2A). Because we focused on -1 frameshift sites (Fig. 2B), we defined a signal that fits all kinds of motif X XXY YYZ of the -1 frameshift. There was no limitation of frameshift site, thus any kind of nucleotide can be located in the frameshift site. Thus we set the match type as NNN (N is any nucleotide) and no exception of arrangement. That is, frameshift site can occur even at A AAA AAA or U UUU UUU. Default values were used for the lengths of the stems and loops in the downstream secondary structure (Fig. 2C). Fig. 3 shows the XML schema for the parameters of FSFinder2. When the user sets the parameters of a



model in the web page of the FSFinder web service, the parameters are converted to XML. After the request of a web service is sent to the FSFinder server, all the computations are done on the server side.

## 2.2 Finding Overlapping Regions of Genes

Fig. 4 shows the frameshift site of the genome of SARS corona virus (NC\_004718). ORF1a (265..13398) and ORF1b (13398..21485) partially overlap each other. U UUA AAC is the slippery sequence and the secondary structure is a pseudoknot [8]. In the GenBank description, the overlapping region of ORF1a and ORF1b has only one 1 nucleotide. ORF1b starts from codon AAA instead of a regular start codon. The start codon of ORF2 (red triangle) exists outside the overlapping region. Frameshifting can occur even in overlapping regions with 1 nucleotide. To solve these problems, finding an overlapping region is divided into two processes: finding motifs and finding overlapping regions.

### 2.2.1 Finding Overlapping Regions Using FSFinder

The shape of an overlapping region is considered to find an overlapping region. As shown in Fig. 5, the overlapping region is extended from stop codon 1 of open reading frame 2 to stop codon 2 of open reading frame 1 (green color). The minimum length of both genes should be longer than 100 nucleotides, and the length of the overlapping region should be longer than 30 nucleotides. In addition, the location of the start codon of ORF2 does not matter. As in the SARS corona virus, the start codon is not always located in the overlapping region of frameshifting genes.

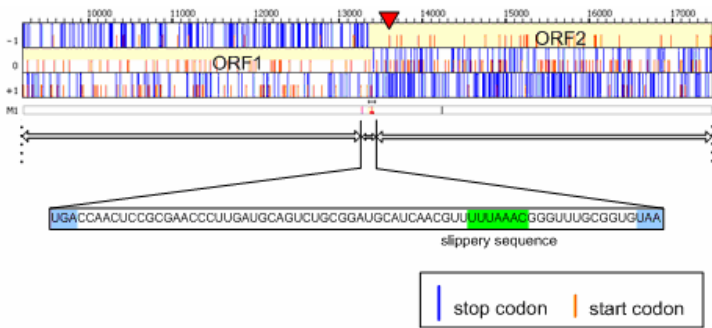
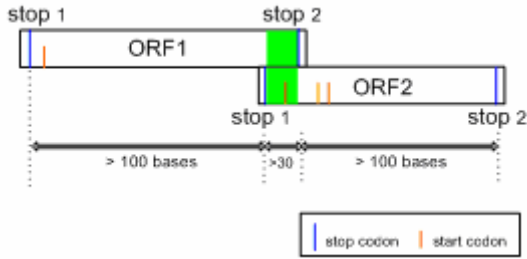


Fig. 4. The frameshift site of the SARS corona virus (the slippery sequence UUUAAAC shown in green background)

### 2.2.2 Finding Overlapping Regions Using the GenBank Description

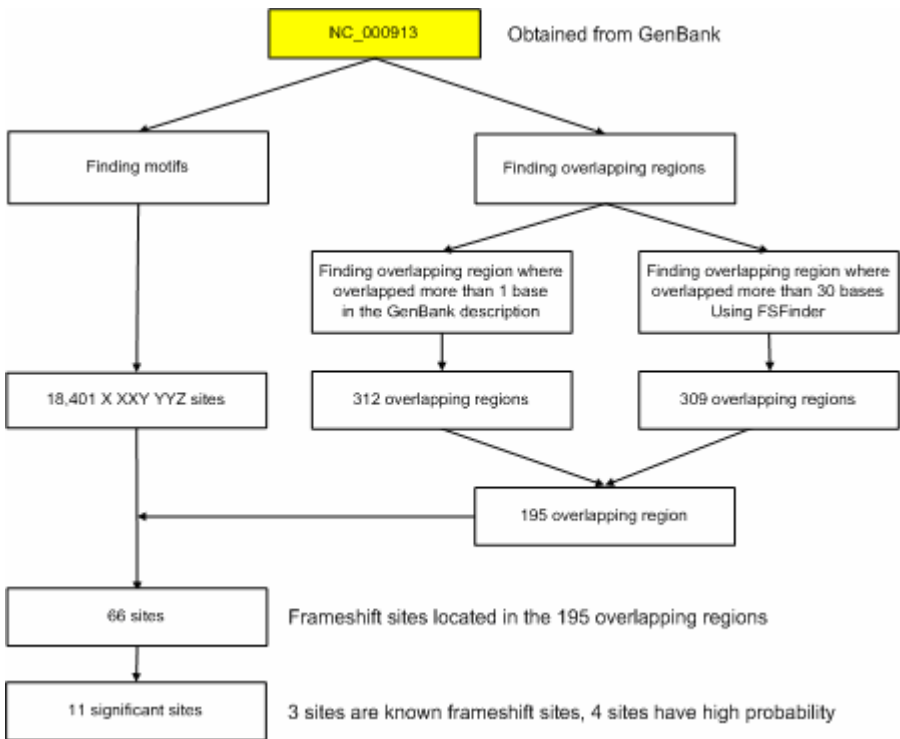
Additional method to find overlapping regions is to use the description of the GenBank file. If more than 1 nucleotide is overlapped, we consider two open reading frames as a candidate of partially overlapping genes. Finally, the overlapping regions found both by FSFinder and by the GenBank description are used for further analysis.



**Fig. 5.** Finding overlapping regions by FSFinder. Unlike general overlapping regions, FSFinder extends the overlapping region from stop codon 1 of open reading frame 2 to stop codon 2 of open reading frame 1 (green color). The length of both ORFs should be longer than 100 nucleotides and the length of the overlapping region should be longer than 30 nucleotides.

### 3 Results and Discussion

The *E. coli* K12 genome sequence (NC\_000913) was obtained from GenBank. As shown in Fig. 6, all the heptameric sequences that follow X XXY YYZ motif were



**Fig. 6.** The prediction process of frameshift sites from the *Escherichia coli* K 12 genome sequence

examined. As a result of this process 18,401 sites were found. Whether these sites are located in the overlapping region or not was not considered when finding these sites.

For overlapping regions of ORFs, we found 312 candidate regions that were partially overlapped more than 1 base according to the GenBank description and 309 candidate regions that were overlapped more than 30 bases using the FSFinder web service. After removing redundant sites, we obtained 195 overlapping regions. From these regions, heptameric sequences that were not located in the overlapping region were filtered out. Just 66 sites remained in the overlapping regions. From the gene length, shape and the length of the overlapping region, 11 sites including 3 known frameshift sites were identified as significant candidates.

This process consists of two sub-processes: finding motifs and finding overlapping regions. The *E. coli* K 12 genome sequence (NC\_000913) was obtained from the GenBank. To find motifs, all the heptameric sequences that follow X XXY YYZ motif were found. 18,401 sites were detected. According to the GenBank description, there were 312 candidate overlapping regions that were partially overlapped more than 1 base in. The FSFinder web service found 309 candidate overlapping regions that were overlapped more than 30 bases. After removing redundant sites, we obtained 195 overlapping regions. After further removing heptameric sequences that were not located in the overlapping region, 66 sites remained in the overlapping regions. Considering the gene length, shape and length of the overlapping region, 11 frameshift sites including 3 known sites were considered significant candidates.

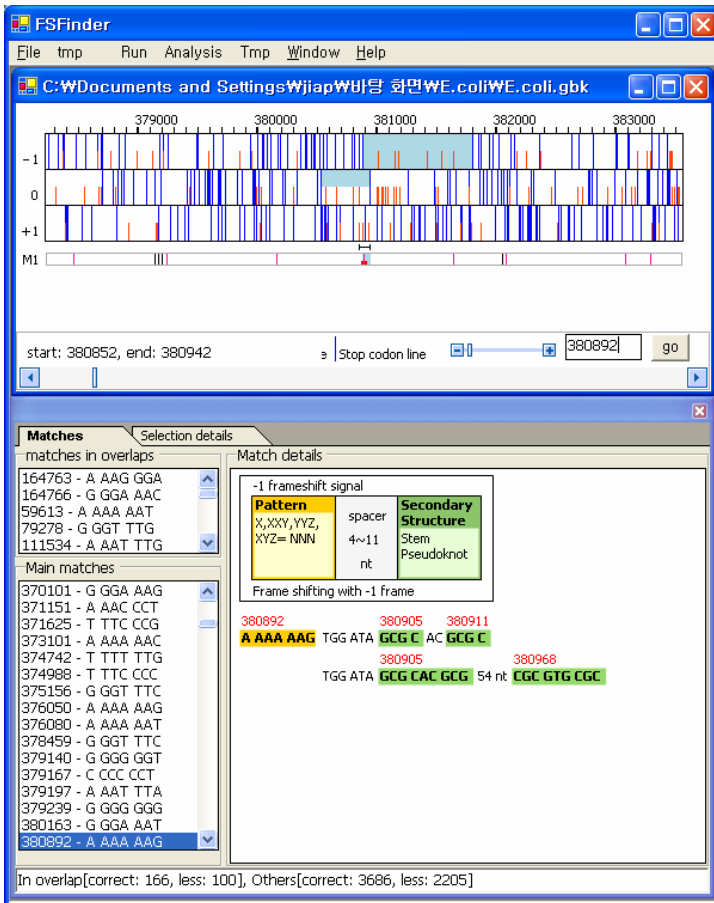
Table 1 shows the names of overlapping genes, the locations of the slippery sites, slippery sequences and number of overlapped nucleotides from our analysis. The three genes, yi21\_1-yi22\_1, yi21\_5-yi22\_5, yi21\_6-yi22\_6, are known genes expressed via -1

**Table 1.** The predicted frameshift sites in the *E. coli* K 12 genome sequence. The first three genes marked with \* symbol are those with known frameshift sites. PK represents a pseudoknot.

| Gene name       | Slippery site | Slippery sequence + secondary structure | # bases in the overlapping region found by FSFinder | # bases in the overlapping region based on GenBank |
|-----------------|---------------|-----------------------------------------|-----------------------------------------------------|----------------------------------------------------|
| yi21_1..yi22_1* | 380892        | A AAA AAG + PK                          | 61                                                  | 43                                                 |
| yi21_5..yi22_5* | 3184526       | A AAA AAG + PK                          | 61                                                  | 43                                                 |
| yi21_6..yi22_6* | 4496612       | A AAA AAG + PK                          | 61                                                  | 43                                                 |
| insA_6..insB_6  | 3581757       | A AAA AAC +PK                           | 103                                                 | 82                                                 |
| entB..entA      | 627723        | A AAC CCG + PK                          | 76                                                  | 1                                                  |
| tehA..tehB      | 1499529       | G GGA AAA + PK                          | 154                                                 | 4                                                  |
| xdhB..xdhC      | 3001496       | G GGG GGA + stem                        | 37                                                  | 4                                                  |
| mhpD..mhpF      | 372127        | C CCA AAA only                          | 61                                                  | 4                                                  |
| fliM..fliN      | 2019082       | U UUA AAU only                          | 40                                                  | 4                                                  |
| atoS..atoC      | 2319873       | G GGA AAU only                          | 85                                                  | 4                                                  |
| yijC..yijD      | 4159773       | G GGA AAU only                          | 46                                                  | 1                                                  |

frameshifts. These three genes and insA\_6-insB\_6 are insertion sequences. We believe that entB-entA, tehA-tehB, and xdhB-xdhC have a high probability using frameshift events. All these seven genes have either pseudoknot or stem loop as a downstream secondary structure. The rest four genes, mhpD-mhpF, fliM-fliN, atoS-atoC and yijC-yijD, have no downstream secondary structures and have a lower probability of frameshifting than the other 7 genes.

There exist previous works similar to our approach. Hammell *et al.* [7] studied -1 ribosomal frameshift signals in the large databases. Using their well-established model, they found that -1 frameshifts occur with frequencies from two- to six-fold greater than random. They considered the nucleotides of a frameshift site, spacer, and pseudoknot. However, they focused on the -1 frameshifts only. Bekaert *et al.* [6] performed a computational method similar to Hammell’s approach. From their model, they designed a model for -1 eukaryotic frameshifting. But these two programs are not available for public use.



**Fig. 7.** Frameshift site of overlapping genes i21\_1..yi22. FSFinder2 found the sequences of the frameshift cassettes and locations of the slippery site.

The FreqAnalysis [9] is an application program available for public use. FreqAnalysis was implemented in the Java language and can find putative translational frameshift from probabilistic calculation. In fact, Shah *et al.* [9] found putative frameshift sites from the *Sacharomyces cerevisiae* ORFs. But FreqAnalysis does not consider the X XXY YYZ frameshift motif. Thus it is hard to compare the results of FreqAnalysis with ours directly.

Fig. 7 shows the result of the FSFinder2. Two rectangles filled with sky blue color in the upper window represent i21\_1 and yi22\_1, respectively. The i21\_1 gene located in 0 frame and the yi22\_1 gene located in -1 frame are partially overlapped. When translational frameshift occurs, translation continues past the stop codon at 380,938 until the stop codon at 381,801.

## 4 Conclusion

Ribosomal frameshifting is unusual event which is known to affect producing heterogeneous proteins, auto-regulation. Prediction of frameshift sites is very difficult. On the other hand if prediction is possible, this is very useful to understand of biological phenomenon. And unveiling of unknown protein production mechanisms can be realized. For this valuable advantage, we develop a web application and serve web service for prediction of frameshift sites.

Using the FSFinder, we analyzed *Escherichia coli* K 12 genome sequence to detect potential -1 frameshifting genes. From the E. coli K 12 genome sequence, we have got 18,401 frameshift sites followed X XXY YYZ motif. Among these sequences, 11,530 frameshift sites included secondary structure. Comparing with GenBank description, we have got 11 sequences including 3 known frameshift sites. Among these sequences, we believe that at least 4 sequences have a high probability to use frameshift event and all these 4 sites have a downstream secondary structure such as pseudoknot and stem loops. Other 4 gene do not have downstream structure, but we believe that these sequences have less probabilities than above 7 genes but significant.

## Acknowledgements

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# Using a Stochastic AdaBoost Algorithm to Discover Interactome Motif Pairs from Sequences

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**Abstract.** Protein interactome is an important research focus in the post-genomic era. The identification of interacting motif pairs is essential for exploring the mechanism of protein interactions. We describe a stochastic AdaBoost approach for discovering motif pairs from known interactions and pairs of proteins that are putatively not to interact. Our interacting motif pairs are validated by multiple-chain PDB structures and show more significant than those selected by traditional statistical method. Furthermore, in a cross-validated comparison, our model can be used to predict interactions between proteins with higher sensitivity (66.42%) and specificity (87.38%) comparing with the Naive Bayes model and the dominating model.

## 1 Introduction

With the finishing of genome sequencing projects, the protein level functional annotation of the entire genome has been a major goal in the post-genomic era. Furthermore, the relationships between proteins play more important role than the function of individual proteins since proteins interact and regulate each other in most biological process. Many experimental and computational methods are developed to identify protein-protein interactions (PPIs).

The traditional genetic, biochemical or biophysical techniques such as protein affinity chromatography, immunoprecipitation, sedimentation and gel-filtration [1] are not suitable for genome-wide interaction detection. Several high-throughput methods have being developed to identify protein-protein interactions in parallel [2–7]. However, the high throughput experiment methods suffer from both high false positives and false negatives[8]. As a result, computational (*in silico*) methods are required to complete the interactome and explore the interacting mechanisms.

The computational approaches for protein interaction discovery have been developed over the years. Earlier methods focus on predicting genome-wide functional linkages by phylogenetic profiles [9, 10], gene fusion information[11, 12] or conservation of gene neighborhoods and gene orders[13, 14]. With the high-throughput interaction data, several machine learning approaches have been developed to predict protein interactions in the domain level [15–29] or motif level

[20]. The central point of those works is interaction prediction. Most of them considered protein domain interactions as the mediate of protein interaction. Gomez [20] tried to show predicting ability of short tuple pairs. Actually, the classifier used by Gomez was a modified Bayes model. To avoid the independent assumption, only the most informative feature was included in the joint probability computing, which is equivalent to dominating Bayes model with uniform prior distribution. In fact, protein interaction motifs themselves are very important for drug and protein design, often referred as protein contact interfaces or binding sites. Interactome motif finding would be of considerable value. Protein-protein interaction data provide more information of motif pairs [30, 31] than one-side interaction motifs [32]. But both Sprinzak's [30] and Wang's [31] works are based on known one-side motifs from database such as PROSITE [33]. We want to discover hidden motif pairs behind the interaction data. In our previous work [34], statistical significant motif pairs set was selected and successfully validated in several ways. But in this paper we will show that statistical significant is not equivalent to biological functional.

In this study, we use an AdaBoost [35] strategy to study the protein-protein interactions in the motif level. Starting from protein sequences and known protein interactions only, the predicting effective motif pairs are identified as the signatures of the protein-protein interactions. By validating them on PDB structure, our interacting motif pairs are more significant than those selected by traditional statistical method. Furthermore, we predict genome-wide protein-protein interactions with higher sensitivity and specificity comparing with Gomez's dominating Bayes model [20] and the Naive Bayes model as a benchmark baseline.

## 2 Methods

### 2.1 Data

Protein-protein interaction data and corresponding protein sequences for *Saccharomyces cerevisiae*(yeast) were collected from the DIP (Database of Interacting Proteins) [36]. The data was obtained on July 31, 2005 containing 15529 interactions among 4786 proteins. Since negative interaction data are not available, several methods have been proposed to construct negative interaction data set. The two most popular approaches are described as follows. In the first approach, proteins in separate subcellular compartments are considered as negatives[37]. The shortcoming of this approach is that there is no information showing whether proteins can bind with each other if they are being put together. Different subcellular locations only indicates that the proteins have no chance to bind. The second approach assumes that two proteins do not interact if there is no positive evidence of interaction[20]. The huge false negative data set is not acceptable for computing. We defined a negative PPI pair as the one proposed in our previous work [34]. A negative PPI pair is a pair of proteins that have chance to interact with each other but fail to be observed in the interaction map. To be precise, we first built a protein interaction graph with proteins as nodes and



positive interactions as edges with equally weights. Then all pairs among nodes in connected graph with shortest path length greater than a cutoff were treated as putative negative protein-protein interactions. The cutoff was selected to balance the sample sizes of positive and negative training data. For example, when cutoff = 7, we obtained 26605 negative protein-protein interactions.

To estimate the reliability of our results, 135 protein complex structures were obtained from PDB (RCSB Protein Data Bank ) [38] on October 31, 2005 with following conditions:

1. Contains RNA Chain(s): No;
2. Contains Carbohydrate Chain(s): No;
3. Number of Chains (min.): 2;
4. Contains Enzyme Chain(s): Yes
5. Contains DNA/RNA Hybrid Chain(s): No
6. Contains Glycoprotein Chain(s): Yes
7. Contains DNA Chain(s): No

The PDB data contain the 3-dimension coordinates of all amino acid atoms, which are direct evidences for protein-protein interactions. The protein complex structures allow us to find out the protein contact interface by simply calculating the Euclidean distances between atoms. The shortcoming of PDB structures is lack of data compared to sequences due to difficulty of biological wet experiments.

## 2.2 Feature Vectors Extraction

Feature vectors extraction used in this work is similar to the one discussed in Gomez's study [20]. 20 amino acids were divided into six categories of biochemical similarity [{IVLM}, {FYW}, {HKR}, {DE}, {QNTP} and {ACGS} [39]]. After the reduction, there are  $M = \binom{6^4}{2} + 6^4 = 840456$  possible 4-tuple pairs in total if the two 4-tuples are exchangeable. Each pair of interaction (positive or negative) could be represented by a binary vector of length  $M$ , in which each bit indicated whether the corresponding 4-tuple pair occurred in the interaction. These  $M$  4-tuple pairs are considered as the interacting motif pair candidates.

## 2.3 Algorithm

Our method is a boosting approach on regulated stochastic linear-threshold classifier. AdaBoost is not a classifier but a procedure to learn a voting ensemble of many weak classifier. The procedure is shown in Table 1. The only missing things in AdaBoost strategy is a system complexity parameter  $T$  and a weak classifier with sample weights. In each step, a error adjustment method was performed on the sample weights. Usually, the larger  $T$  leads to more computation and risk of overfitting. In our experiment, the factors of weak classifiers were convergence to zero after four rounds, so  $T$  was fixed to 4.

Given the sample weights calculated by each boosting round, our goal was mining the different effects of each vector component. Furthermore, we used a regulated stochastic WINNOWER2 (in Table 2, with  $R = 200,000$ ) as the weak

**Table 1.** The AdaBoost procedure.  $T$  weak classifier are constructed according to its accuracy in previous round. The final classifier is a weighted linear combination of the  $T$  weak classifier.

- Given training data:  $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$  where  $y_i = 1, -1$  for positive and negative samples respectively.
- Initialize weight  $D_1(i) = 1/n$  for  $i = 1, 2, \dots, n$ .
- For  $t = 1, \dots, T$ :
  1. Train weak learner using distribution  $D_t$  and get back a weak classifier  $h_t : \{0, 1\}^M \rightarrow \{1, -1\}$ .
  2. Calculate the error rate with respect to  $D_t$ :  $r_t = \sum_i D_t(i)h_t(x_i)y_i$ .
  3. Update the weights:  $D_{t+1}(i) = D_t(i)\exp(-\alpha_t h_t(x_i)y_i)$ , where  $\alpha_t = \frac{1}{2} \log\left(\frac{1+r_t}{1-r_t}\right)$ .
  4. Normalize the weights  $D_{t+1}$  into a probability distribution.
- The final strong classifier is:  $H(x) = \text{sign}(\sum_{t=1}^T \alpha_t h_t(x))$ .

**Table 2.** The regulated stochastic WINNOWN2. The algorithm is applied according to the sample weights. Feature factors are regulated to capture the effective components.

- Given training data  $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$  and its corresponding weights  $D_t(1), D_t(2), \dots, D_t(n)$ .
- Initialize learner factor  $\omega_i = 1$  for  $i = 1, 2, \dots, M$ , threshold  $\theta = M/2$
- For  $r = 1, \dots, R$ :
  1. Draw a sample  $(x_k, y_k)$  according to the sample weights, we denotes vector  $x_k$  as  $(x_{k1}, x_{k2}, \dots, x_{kM})$ .
  2. The learner responds as follows:
    - $h = 1$ , if  $\sum_{i=1}^M \omega_i x_{ki} > \theta$
    - $h = -1$ , if  $\sum_{i=1}^M \omega_i x_{ki} \leq \theta$
  3. Update learner factors  $\omega_i := \omega_i 2^{(1-x_{ki})(y-h)/2}$
- We define regulated classifier at level  $c$ ,  $h(c)$ , as follows:
  - $h(c) = 1$ , if  $\sum_{i=1}^M \omega_{i,c} x_{ki} > \theta$ ,
  - $h(c) = -1$ , if  $\sum_{i=1}^M \omega_{i,c} x_{ki} \leq \theta$ ,
 where  $\omega_{i,c} = 0$ , if  $\omega_i \geq c$  and  $\omega_{i,c} = \omega_i$ , if  $\omega_i < c$ .
- let  $N_c$  denotes the number of positive prediction on the training data with classifier  $h(c)$ . Output the classifier  $h(C)$  where  $C = \text{argmax}(c : N_c = N_0)$ , where  $N_0$  is the number of positive prediction at the cutoff level  $c=0$ .
- The features with non-zero factor  $w_{i,c}$  are identified as effective components.

classifier, which was somewhat a error adjustment method on the feature weights. The original version of WINNOWN2 was introduced by Littlestone [40]. The major difference of our version from the original one is that our sample weights are not equal. The sample for next learning round was drawn according to the sample weights. Finally, an additional regulation step was applied to discover

the effective components. The features with large enough factor were identified as effective components. The union of effective components in these  $T$  rounds were considered as the motif pairs of the protein-protein interactions.

## 2.4 Cross-Validation and Structural Validation

The performance of classifier was measured using five-fold cross-validation. The data were divided into five subsets. The classifier was trained on four subsets and tested on the remaining one. Then the average sensitivity and specificity across all five trails were computed and compared with Naive Bayes classifier (described in appendix) and dominating Bayes model [20].

The reliability of identified motif pairs sets was estimated by bootstrap of PDB protein complex structures validation. A motif pair is verifiable is defined as follows:

**Definition 1.** *Motif pairs verifiable: Given two protein chains with 3-D structural coordinates and a motif pair ( $Motif_A, Motif_B$ ),  $Motif_A$  occurs in one protein chain and  $Motif_B$  occurs in the other and at least one atom from  $Motif_A$  and one from  $Motif_B$  contact.*

*Atoms contacting if and only if  $dist(Atom_A, Atom_B) < \varepsilon$ , where  $dist(\cdot, \cdot)$  is the Euclidean distance, and  $\varepsilon$  is an empirical threshold  $5\text{\AA}$ .*

For a given motif pairs set  $S$ , the bootstrap method for p-value estimation is applied as follows. We repeatedly drawn the same number of 4-tuple pairs randomly as set  $R_1, R_2, \dots, R_m$ . If  $m$  is large enough, the p-value of the set  $S$  can be estimated as  $P(S) = \#(V(R_i) \geq V(S))/m$ , where  $V(S)$  denotes the number of verifiable motif pairs in set  $S$ .

The results were compared with  $\chi^2$  feature selection method (described in appendix).

## 3 Results

At the motif level, we combined the five-fold information together as follows:  $M_i = \{\text{motif pairs identified in at least } i \text{ folds}\}$ , where  $i = 2, 3, 4, 5$ . Let  $M_{all}$  denote the motif pairs set identified with all training data. Table 3 shows the results of 100,000 times bootstrap of PDB structure validation comparing with  $\chi^2$  feature selection.

It is a shock that more statistical conserved motif pairs are less structural verifiable. Noting the fact that the totally random selection should have average p-value of 0.5, the number of verifiable motif pairs in the most conserved set selected by  $\chi^2$  method is only a little more than that of random pairs. Whereas all motif pairs sets identified by our AdaBoost algorithm are significantly verifiable.

At the protein interaction level, with threshold at zero, our AdaBoost model achieves 87.38% in specificity and 66.42% in sensitivity in average. The sensitivities comparison with comparable fixed specificity at approximately 87.38% are shown in Table 4. It is clearly shown that AdaBoost outperforms the others in prediction accuracy.

**Table 3.** Motif validation. the  $V(\text{Set})$  column and the  $V(\text{Stat})$  column are the verifiable number of the Set and the same size set selected by  $\chi^2$  method, respectively. p-values are estimated by 100,000 times bootstrap method described above.

| Set       | number of motif pairs in Set | $V(\text{Set})$ | p-value | $V(\text{Stat})$ | p-value |
|-----------|------------------------------|-----------------|---------|------------------|---------|
| $M_{all}$ | 660                          | 77              | 6.43e-3 | 73               | 2.49e-2 |
| $M_2$     | 775                          | 87              | 1.13e-2 | 84               | 2.76e-2 |
| $M_3$     | 490                          | 58              | 1.16e-2 | 50               | 0.147   |
| $M_4$     | 307                          | 45              | 2.67e-4 | 28               | 0.424   |
| $M_5$     | 157                          | 27              | 1.93e-4 | 15               | 0.374   |

**Table 4.** Accuracy Comparison. the Sensitivity and Specificity of three methods with comparable fixed specificity.

|             | AdaBoost | Dom-Bayes | Naive Bayes |
|-------------|----------|-----------|-------------|
| Sensitivity | 66.42%   | 54.85%    | 32.08%      |
| Specificity | 87.38%   | 87.14%    | 87.38%      |

## 4 Conclusion and Discussion

This work describes a stochastic AdaBoost method for discovering the interactome motif pairs and predicting protein-protein interactions from sequences. To apply the machine learning procedure, the putative negative protein-protein interactions were generated by known positive interactions. By resampling validation, our identified motif pairs fit known protein complex structures very well while traditional statistical method is not. We notice a phenomenon that conservation is not a guarantee of functional sites. Moreover, the motif pairs are validated at protein interaction level. In contrast using all features in the dominating Bayes model, only those effective features are included in our classifier. Our method achieves higher specificity and sensitivity in protein-protein interaction prediction.

In the real world, the whole protein interaction network is more complex since protein may have different behavior with others depending on the many conditions, e.g., protein location, expression time, temperature. In the future, We expect to expand our work with more types of data such as the phylogenetic information, expression data and so on.

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## Appendix: Methods for Comparison

In the Appendix, we described two methods for comparison. The first is Naive Bayes Model, to be a benchmark for protein-protein interaction prediction accuracy. The second is  $\chi^2$  statistical feature selection, which is widely used based on the philosophy of that statistical significance leads to biological significance.

### 4.1 Naive Bayes Model

Naive Bayes model is based on so-called Bayesian theorem and the independent assumption of features. Given the same training data described in the text. The posterior probability of a new sample  $w$  in class  $z$  is

$$P(z|w) \propto p(w|z)p(z) = p(z) \prod_{i=1}^M w_i P(w_i|z), \quad (1)$$

where  $P(w_i|z)$  can be easily estimated by simply counting the feature in training data and  $p(z)$  is the prior probability estimated by proportion of class  $z$  in training data.

$w$  is classified as positive sample if and only if  $P(1|w)/P(0|w) > c$ , where  $c$  is a given constant threshold.

### 4.2 $\chi^2$ Feature Selection

For each feature  $F$  we calculate the statistic with Yates' correction of the  $2 \times 2$  contingency table test as follows:

|                                  | Positive sample | Negative sample |
|----------------------------------|-----------------|-----------------|
| #(F occurrence)                  | a               | c               |
| #(All other feature occurrences) | b               | d               |

$$K = \frac{N(|ad - bc| - N/2)^2}{(a + b)(c + d)(a + c)(b + d)} \sim \chi^2 \quad (2)$$

where  $N$  is the sum of  $a$ ,  $b$ ,  $c$ , and  $d$ ;  $a$  and  $b$  are the occurrences of a given feature and other features than the given feature (non-feature) in the foreground set, respectively;  $c$  and  $d$  are the same in the background set.  $K$  approximately follows  $\chi^2$  distribution.

Larger  $K$  indicates more significant systematic association between the feature occurrence and the sample label.

The most significant positive occurrence features are selected as statistical significant features.

# Web Service for Predicting Interacting Proteins and Application to Human and HIV-1 Proteins

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**Abstract.** Finding all the proteins that potentially interact with a query protein is useful when studying a biological mechanism, but it is much more difficult than finding interactions between a set of given proteins. This is because it involves intensive computation to search the relevant data in databases, and different databases have different accession numbers and names for the same protein. Recently a few servers have been developed for finding interactions between user-specified proteins, but none of these can find all the potentially interacting proteins for a given protein, including the former version of our prediction server, HPID version 1.0. This paper describes a new online prediction system, HPID 2.0 (<http://www.hpid.org>), for finding partners interacting with a query protein as well as for finding interactions between query proteins. We applied the new system to predicting the interactions between the entire human proteins, and to identifying human proteins interacting with HIV-1 proteins (<http://hiv1.hpid.org>). We believe that this is the first online server for predicting proteins interacting with a given protein, and that it will be a useful resource for studying protein-protein interactions.

## 1 Introduction

Studying a biological mechanism or function often requires a small-scale network of protein-protein interactions related to the mechanism or function rather than a genome-wide network of protein-protein interactions. However, small-scale subnetworks of the protein-protein interactions of interest are not readily available from databases. This is partly because computing all possible subnetworks involves prohibitive computation of searching data in relevant databases, and partly because different databases have different accession numbers and names for a same protein.

We have previously developed a database called the Human Protein Interaction Database (HPID; <http://www.hpid.org>) for predicting potential interactions between proteins submitted by users, as well as for providing human protein interaction information pre-computed from existing structural and experimental data [1]. However, the previous version of HPID, HPID version 1.0, is not capable of finding potentially interacting partners for a given protein. Finding all the proteins potentially interacting with a protein of interest is useful when studying a biological mechanism,

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but much more difficult than finding interactions between given proteins. Recently a few servers have been developed for finding interactions between a set of given proteins [2, 3], but none of these can search relevant databases and find potentially interacting proteins with a protein given by a user.

In an attempt to improve the capability of the online prediction system as well as the reliability of the predicted interactions, we developed a new online prediction system (HPID 2.0; <http://www.hpid.org>) using several types of information: protein domain, protein function, and sub-cellular localization. We used the new online prediction system to predict human proteins potentially interacting with a human immunodeficiency virus type 1 (HIV-1) protein. The results were built into a web-based system (<http://hiv1.hpid.org>) for analyzing and visualizing the large-scale interactions between HIV-1 and human proteins and the comparative analysis of the interactions. HPID 2.0 is the first online system for predicting proteins interacting with a given protein and will be a useful resource for studying protein-protein interactions.

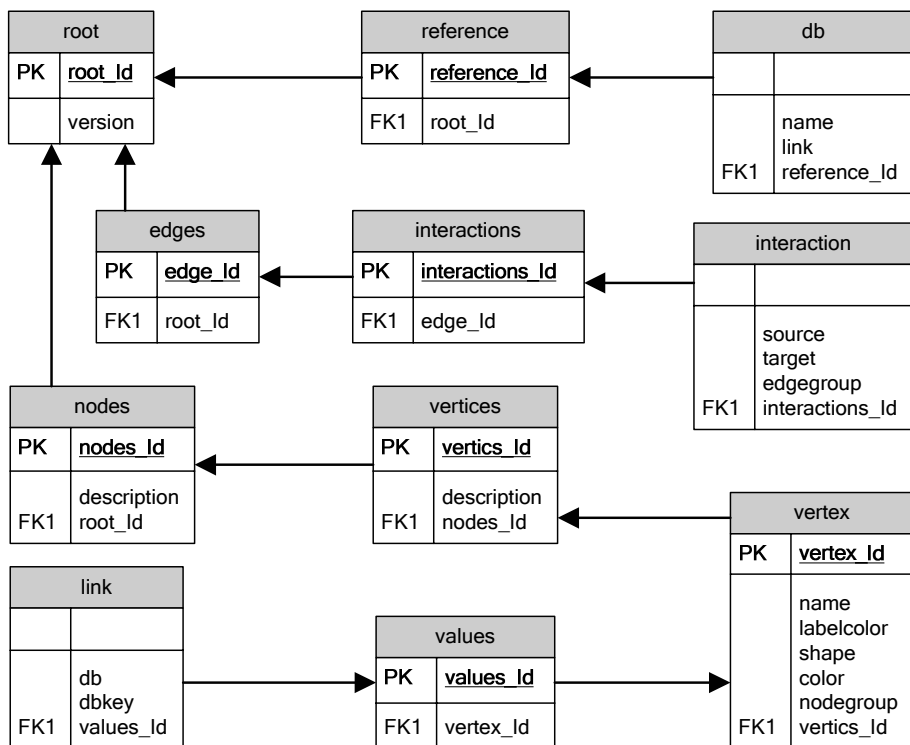
## 2 Methods of Predicting Interacting Proteins

To predict interacting partners of a protein of interest, the user should first find the superfamilies of the protein using any of the Superfamily (<http://supfam.mrc-lmb.cam.ac.uk/SUPERFAMILY>), InterPro (<http://www.ebi.ac.uk/InterProScan>) or Pfam (<http://www.sanger.ac.uk>) databases. The HPID online prediction system then takes one or more superfamilies of the protein and its protein name as input. The reason for taking the superfamilies as input instead of the amino acid sequence is partly because the assignment of superfamilies by these databases is reliable and partly because some proteins have no superfamily or assigning them a superfamily takes too long. The HPID online prediction system cannot predict interacting partners for a protein with no superfamily.

Protein interactions at the superfamily level were predicted from the Protein Structural Interactome MAP (PSIMAP) [4]. PSIMAP was constructed by extracting all the structural domain-domain interactions from PDB. It contains 37,387 interacting domain pairs that have five or more contacts within 5Å and these domain pairs were grouped into 2,171 protein family-family pairs using the SCOP family definition [4]. Unlike HPID 1.0, HPID 2.0 is not dependent on protein IDs to find interacting proteins. Interacting partners for a query protein are found by homology search of protein sequences in relevant databases, which currently include Ensembl (<http://www.ensembl.org>), BIND (<http://bind.ca>), DIP (<http://dip.doe-mbi.ucla.edu>), HPRD (<http://www.hprd.org>), and NCBI (<http://www.ncbi.nlm.nih.gov>).

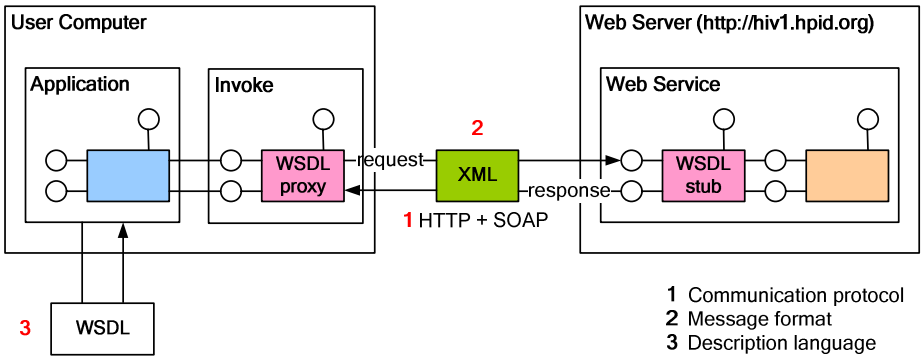
We used this method to find potential interaction partners with a human protein or human immunodeficiency virus type 1 (HIV-1) protein. Currently the search for potential interaction partners is limited to human proteins, but should be extendable to other organisms.

We developed a web service using Microsoft C# language and .NET framework. We used XML (eXtensible Markup Language) schema and the Simple Object Access



**Fig. 1.** Structure of XML schema. The ‘root’ element of the XML schema is an identification of a protein-protein interaction network. The ‘reference’ element has the addresses of the databases that have information about the proteins in the network. The user can access the information through the addresses. The ‘nodes’ element represents the node type such as protein, protein structure, protein function, and gene. Different node types can be displayed in different shapes and colors. The ‘link’ and ‘db’ elements make the user access protein information from many databases. The ‘edges’ element displays protein-protein interactions.

Protocol (SOAP) version 1.1 of W3C [5] for a data structure and a communication protocol. XML Schemas express shared vocabularies and allow machines to carry out rules made by people [6]. Fig. 1 shows the high-level structure of our XML schema (for the full XML schema see <http://hiv1.hpid.org/GraphDataSet.xsd>). SOAP is a lightweight protocol for exchange of information in a decentralized, distributed environment [7]. We used the Web Service Description Language (WSDL) for XML Remote Procedure Call (XML-RPC). WSDL is an XML format for describing network services as a set of endpoints operating on messages containing either document-oriented or procedure-oriented information [8]. Fig. 2 shows how to access the interactions between HIV-1 and human proteins from a local computer of a user. An application in the user computer can be either any web browser, WebInterViewer [9, 10], or any application program developed by the user.



**Fig. 2.** The web service of the HIV1 database (http:// hiv1.hpidd.org). When the user requests to explore protein interactions, a web browser or the standalone version of WebInterViewer is executed in the user computer. When the user clicks a hyperlink of an interesting HIV-1 gene, a request of a web service is sent to the web server. There are two methods of responding to the request. One is for the application of the user computer to get XML data directly, and the other is to instantiate the WSDL proxy object in the user computer and then to let the instance get XML data. WebInterViewer uses the first method. For the interacting proteins with the HIV-1 gene specified by the user, WebInterViewer gets results in the XML schema, as described in Fig. 1. Finally, the interacting proteins are visualized by WebInterViewer. The other method is for an application program that is to analyze protein interactions.

The user can generate a network of publishable quality from the analysis results using WebInterViewer. If the user wants to embed the Active-X control of WebInterViewer in the user's web server, he or she can include the following code in the web page at <http://hiv1.hpidd.org/usage.htm>.

```
<script language="javascript">
function View(xml) // xml: URL or Web Service
{
 document.IVax1.Options("VL,NS2");
 document.IVax1.ConnectPIEx2("HIV-1", xml);
}
</script>
tes
t1
<OBJECT id="IVax1"
codeBase="http://interviewer.inha.ac.kr/download/IVF_DiF_Ax.cab#
version=1,1,6,3"
classid="clsid:D8D13FEA-2AD6-42AC-B3D5-17AFC6C55907"
name="IVax1"></OBJECT>
```

If the user wants to run the standard alone version of WebInterViewer, he or she can use the following code.

```
<a
href="javascript:document.wivDownloader.runIV();javascript:docum
ent.wivDownloader.ConnectPIEx2('HIV-1',
'http://hiv1.hpidd.org/data/hiv1.xml')">test2
```

```
<OBJECT
codeBase="http://interviewer.inha.ac.kr/Download/IVF_DiF_Down.ca
b#version=1,2,1,4" height="0" width="0" classid="clsid:4BB61BDA-
DADE-4F94-ADB6-7EA1E8962613"
name="wivDownloader" VIEWASTEXT ID="wivDownloader"></OBJECT>
```

### 3 Results and Discussion

We built a web-based server for predicting interacting proteins and for visualizing protein interaction networks (Fig. 3). The web services provided by the server and their methods and parameters are summarized in Tables 1 and 2, respectively. The basic process of the web service is exchanging SOAP messages described in XML. When the server of web services receives the SOAP request with the parameters, the server returns the SOAP message in response to the method. Different application programs developed by various languages can use the web services, whose results can be a request message for another web service. Example XML files for the responses to the HTTP GET request can be found at the following URL addresses.

1. <http://hiv1.hpid.org/WebServices/WebInterViewer.asmx/GetInteractions?nodeID=capsid&gene=gag>
2. <http://onlineprediction.hpid.org/WebService/psimap.asmx/DoPredict?Protein=test&Superfamily=a.1.1>
3. <http://hiv1.hpid.org/WebServices/pubmed.asmx/GetPubMed?uids=10074203>

**Table 1.** Web services provided by our system

| Web Services           | Web Service Description Language (WSDL)                                                                                                 |
|------------------------|-----------------------------------------------------------------------------------------------------------------------------------------|
| WebInterViewer         | <a href="http://HIV1.HPID.org/WebServices/WebInterViewer.asmx?WSDL">http://HIV1.HPID.org/WebServices/WebInterViewer.asmx?WSDL</a>       |
| HPID Online prediction | <a href="http://Onlineprediction.hpid.org/WebService/psimap.asmx?WSDL">http://Onlineprediction.hpid.org/WebService/psimap.asmx?WSDL</a> |
| NCBI PubMed service    | <a href="http://HIV1.HPID.org/WebServices/PubMed.asmx?WSDL">http://HIV1.HPID.org/WebServices/PubMed.asmx?WSDL</a>                       |

**Table 2.** Methods and parameters of the web services

| Web Services           | Methods         | Parameters                                                    |
|------------------------|-----------------|---------------------------------------------------------------|
| WebInterViewer         | GetInteractions | nodeID: HIV-1 protein name<br>gene: HIV-1 gene name           |
| HPID Online prediction | DoPredict       | Protein: user's protein name<br>Superfamily: SCOP superfamily |
| NCBI PubMed service    | GetPubMed       | uids: PubMed ID                                               |

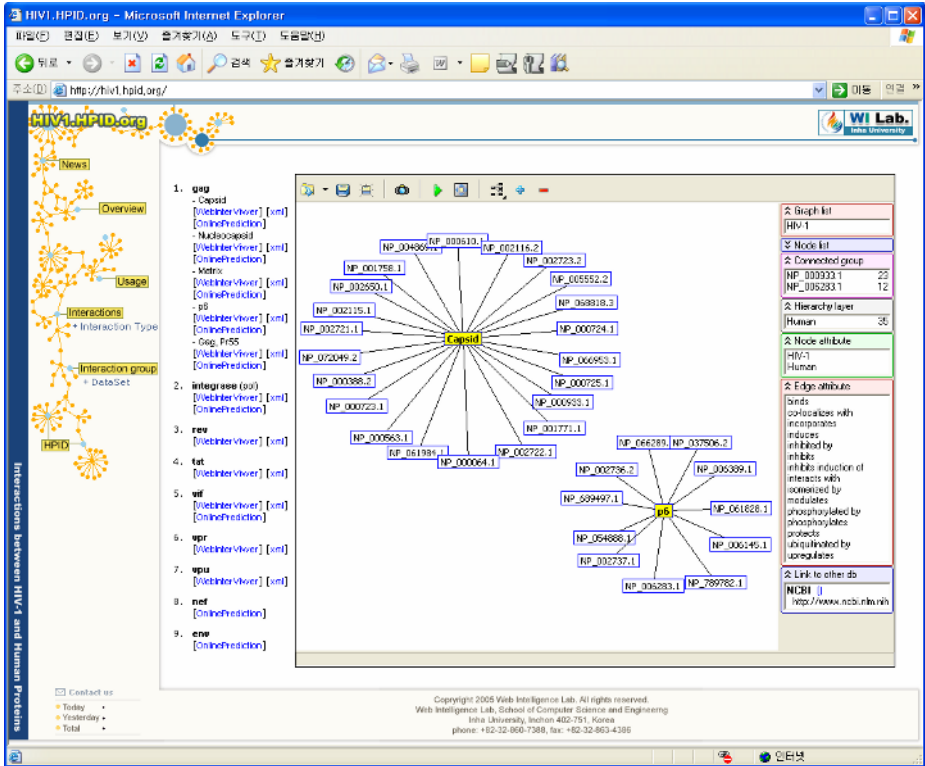
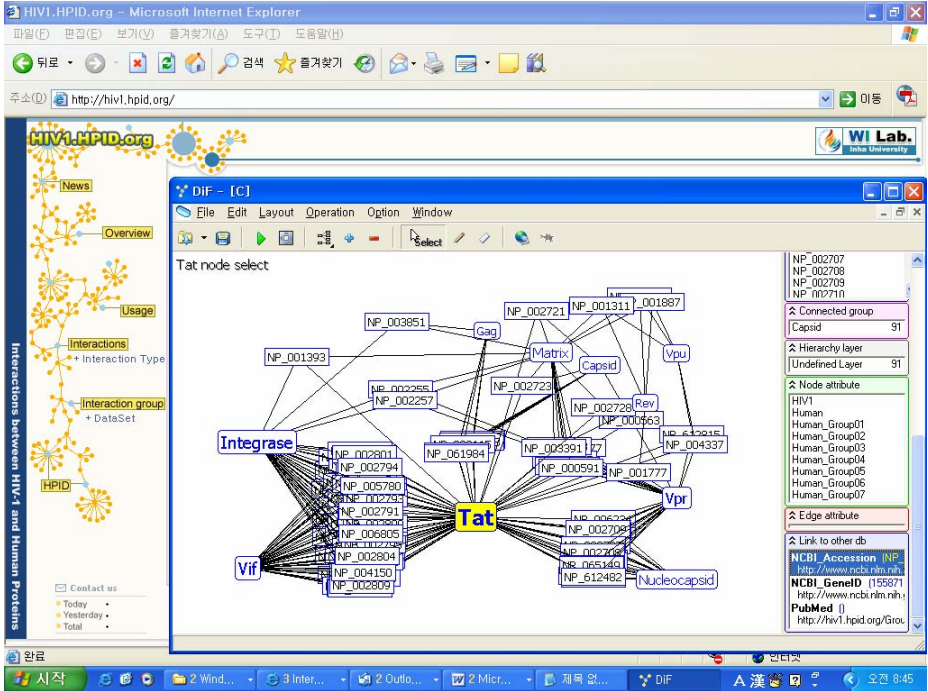


Fig. 3. The user interface of the HIV-1 database. The ‘OnlinePrediction’ button each HIV-1 protein lets the user predict potential human proteins interacting with the HIV-1 protein. When the user clicks the ‘WebInterViewer’ button below an HIV-1 protein, all human proteins interacting with it are listed. Several interactions networks can be compared and analyzed in the same window.

Our HIV1 database (<http://hiv1.hpid.org>) can be used for analyzing and visualizing the large-scale interactions between HIV-1 and human proteins and for the comparative analysis of the interactions. Relevant articles to any human or HIV-1 protein in the interaction networks, which are archived in PubMed (<http://www.pubmed.gov>), are also linked from the NCBI\_Accession in the 'Link to other db' menu of our system (Fig. 4). Detailed explanation is available in the usage section of the web page.

The rest of this section gives an example of predicting human proteins potentially interacting with the HIV-1 capsid protein. The online prediction server finds 208 human proteins from Ensembl and 147 human proteins from NCBI as the potential interaction partners with the HIV-1 capsid protein. As a supporting basis of the prediction, the prediction report shown in Fig. 5A lists two superfamilies, a.28.3 and a.73.1, assigned to the HIV-1 capsid protein. The superfamily a.28.3 has two interacting superfamilies, a.73.1 and b.1.1, and the superfamily a.73.1 has five interacting superfamilies, a.28.3, a.61.1, a.73.1, b.1.1, and b.62.1. If the user clicks on one of these interacting superfamilies, he or she can see the interacting human

proteins in the superfamily together with their reliability scores. Fig. 5B shows the network of human proteins interacting with HIV-1 *capsid* protein, visualized by WebInterViewer. It is a star-shaped network, centered on the HIV-1 *capsid* protein (yellow node in the network). The interaction network can be analyzed interactively using WebInterViewer and saved in the XML format for later analysis.



**Fig. 4.** Example of accessing relevant articles to a protein in the interaction network. When the user clicks a protein (yellow node) in the network and double clicks the NCBI\_Accession of the protein in the 'Link to other db' menu (lower right pane), all relevant articles are displayed.

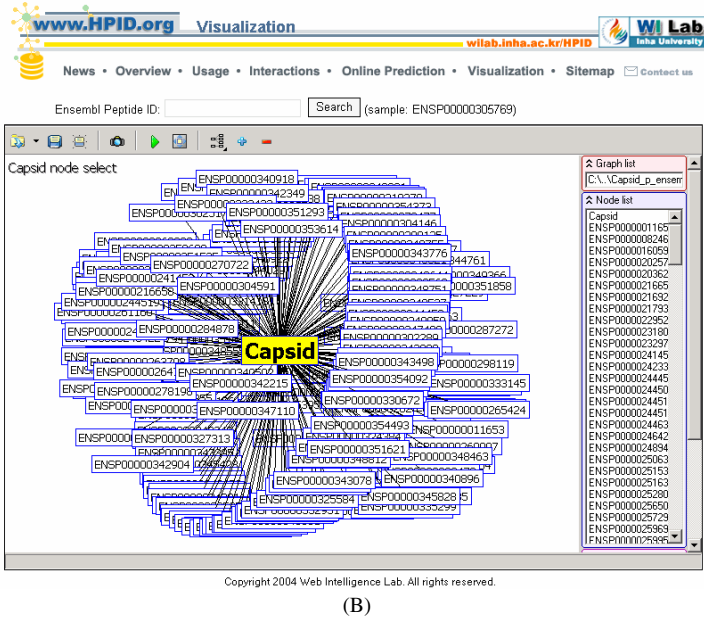
**Report**

**Protein 1: NP\_579880**

|                                 |                                                                     |
|---------------------------------|---------------------------------------------------------------------|
| Superfamily 1: a.28.3           |                                                                     |
| Superfamily's partner 1: a.73.1 | <a href="#">Click here to see protein(s) with a.73.1 structure.</a> |
| Superfamily's partner 2: b.1.1  | <a href="#">Click here to see protein(s) with b.1.1 structure.</a>  |
| Superfamily 2: a.73.1           |                                                                     |
| Superfamily's partner 1: a.28.3 | <a href="#">Click here to see protein(s) with a.28.3 structure.</a> |
| Superfamily's partner 2: a.61.1 | <a href="#">Click here to see protein(s) with a.61.1 structure.</a> |
| Superfamily's partner 3: a.73.1 | <a href="#">Click here to see protein(s) with a.73.1 structure.</a> |
| Superfamily's partner 4: b.1.1  | <a href="#">Click here to see protein(s) with b.1.1 structure.</a>  |
| Superfamily's partner 5: b.62.1 | <a href="#">Click here to see protein(s) with b.62.1 structure.</a> |

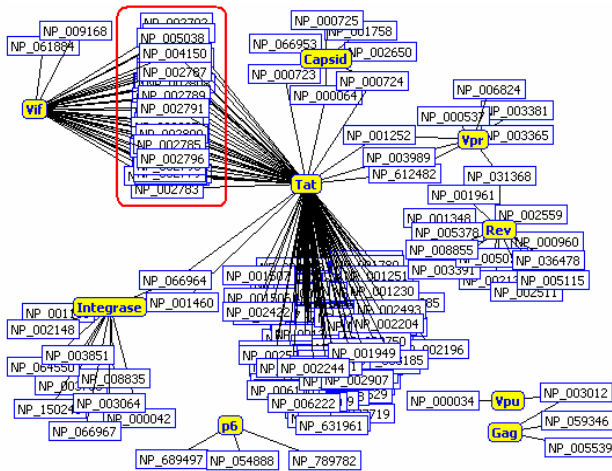
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(A)



(B)

**Fig. 5.** (A) The prediction report for the HIV-1 *capsid* protein (NCBI accession number: NP\_579880). (B) A network of 208 human proteins potentially interacting with the HIV-1 *capsid* protein, visualized by WebInterViewer.



**Fig. 6.** Interaction network of HIV-1 and human proteins, consisting of interactions of “interact with” type only. The network shows 98 interactions between 11 HIV-1 proteins and 49 human proteins. The human proteins shared by the *vif* and *tat* genes (enclosed in a red box in the network) are proteasome (prosome, macropain) subunits of a highly ordered ring-shaped 20S core structure.

We also used the HIV-1 database for the comparative analysis of the experimental data on the interactions between HIV-1 and human proteins. The experimental data was extracted from NCBI at <http://www.ncbi.nlm.nih.gov/RefSeq/HIVInteractions>. The whole interaction network contains 1,768 interactions of 65 different types with 810 human proteins. The comparative analysis identified several interesting interaction patterns from the topological analysis of the interaction networks. For example, the network shown in Fig. 6 shows an interaction network of HIV-1 and human proteins, consisting of interactions of “interact with” type only. The network has 98 interactions between 11 HIV-1 proteins and 49 human proteins. The human proteins interacting with both the *vif* and *tat* genes (enclosed in a red box in the network) have only the *vif* and *tat* genes as their interacting HIV-1 partners. The human proteins are proteasome (prosome, macropain) subunits of a highly ordered ring-shaped 20S core structure.

## 4 Conclusion

Small-scale interaction networks relevant to a protein of interest are not readily available from databases partly because computing all possible subnetworks involves prohibitive computation of searching data in the databases and because different databases have different accession numbers and names for a same protein. We constructed an online prediction system called HPID 2.0 (<http://www.hpid.org>) for searching for interaction partners of a protein given by a user. The online prediction system was also used to predict human proteins potentially interacting with HIV-1 proteins. The prediction results and experimental data were built into a web-based system (<http://hiv1.hpid.org>) for analyzing and visualizing the large-scale interactions between HIV-1 and human proteins and the comparative analysis of the interactions. We believe that this is the first online system for the comparative analysis of the interactions networks of HIV-1 and human proteins and that it is a valuable tool for scientists in the field of protein-protein interactions and HIV/AIDS research.

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# An Immunity-Based Dynamic Multilayer Intrusion Detection System

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**Abstract.** A real computer network produces new network traffic continuously in real time, thus the normal behaviors of network traffic are different in different time, but the self set of current network detection systems based on immunity are static. If the network environments change, the false negative rates and false positive rates will increase rapidly. So the traditional method can not adapt to changing network environments. In order to get over the limitation of the traditional means, an immunity-based dynamic intrusion detection system is proposed in this paper. In the proposed model, a dynamic renewal process of self set is described in detail. In addition, we establish a new set to improve the detection precision and shorten the training phase by adding the characters of the current known attacks to memory cell set. The experimental results show that the new model not only reduces the false negative rates and false positive rates effectively but also has the feature to adapt to continuous changing network environments.

## 1 Introduction

The growing numbers of machines connect to Internet and the ever increasing dependency of our world on network-based computer systems has raised the network security concerns to a crucial stake. Meanwhile, the internet revolution has been accompanied with its share of crimes and malicious activities. The continuous increase in computer crimes suggests that the traditional security systems are no longer effective to protect today's computer infrastructure [1]. Intrusion detection systems (IDSs) have been developed for that matter and are widely deployed.

An IDS is an automated system for the detection of computer system intrusions using audit trails provided by operating systems or network monitoring tools. The goal of an IDS is not only helps the administrators to detect intrusions and limit damages, but also helps to identify the source of attacks, which sometimes acts as a deterrent especially in case of insider attacks [2]. Intrusion detection functions include:

- Monitoring and analyzing both user and system activities
- Analyzing system configurations and vulnerabilities
- Assessing system and file integrity
- Ability to recognize patterns typical of attacks
- Analysis of abnormal activity patterns
- Tracking user policy violations

IDSs mainly employ two detection techniques: anomaly detection and misuse detection. The anomaly detection approach establishes the profiles of normal activities of users, systems or system resources, network traffic and services using the audit trails generated by a host operating system or a network-scanning program [3]. The misuse detection approach defines suspicious misuse signatures based on known system vulnerabilities and security policy [4]. The IDSs based on anomaly detection detect intrusion by identifying significant deviation from the normal behavior patterns of profiles, and the IDSs based on misuse detection probe whether these misuse signatures present or not in the auditing trails. The advantage of misuse detection approach is its low rate of false errors, since signatures are specific to suspicious activities. However, misuse detection approach fails to detect any attack for which they were not provided with signature, so new breeds of attacks, can go undetected in this way [5]. The strength of the anomaly detection approach is that a prior knowledge of the security flaws of the target system is not required. Thus it is able to detect not only known intrusions but also unknown intrusions, but the false negative error of this approach is very high. Because each technique has different strengths and drawbacks, the intrusion detection system should employ both anomaly detection system and misuse detection system in parallel. These two components should be reciprocal in an IDS. But currently, most of IDSs only carry out misuse detection.

Human immune systems have been successful at protecting the human body against a vast variety of foreign pathogens or organisms. One most interesting feature of the human immune system is the discriminative power to detect harmful pathogens without attacking human body self cells. The human immune system distinguishes previously known and unknown pathogens from human body self cells via its own evolutionary mechanism, which is similar to evolution of organisms in nature. The human immune system has a multi-layered architecture. It consists of passive layers such as the skin, mucus membranes, pH, temperature and generalised inflammatory responses, and adaptive layers including both the humoral (B cell) and cellular (T cell) mechanisms [4] [5] [6]. The self recognition of immune system (IS), along with the distributed, self-organized and lightweight nature of the mechanisms by which it achieves this protection, has in recent years made it the focus of increased interest within the computer science and intrusion detection communities. A number of artificial immune systems (AIS's) have been built for intrusion detection. In 1997, Forrest proposed the application of computer immune systems to computer security for the first time. In 1999, Kim and Bentley have identified the features of human immune system that can contribute to the development of effective network-based IDS. In 2000, Hofmeyer and Forrest develop an AIS for network intrusion detection, called LYSIS [6]. Different work inspired by LYSIS has recently been reported in [7]. But there are two problems in most of these works. The first problem is that most systems only adopt to anomaly detection and the FP error rates of these systems are very high. Another problem is that these systems carry out static detection, and the self and detector libraries become very large and can not adapt to dynamic changing network environment [7].

In order to overcome the limitations, an immune-based multilayer model for the dynamic intrusion detection was proposed in this paper. A dynamic renewal process of

self et is described in detail. In addition, we establish a new set to improve the detection precision and shorten the training phase by adding signature detection layer.

The remainder of the paper is organized as follows. In Section 2, we establish an immune-based multilayer model for the dynamic intrusion detection. Then in Section3, the simulations and experimental results are provided. Finally, Sections 4 gives the summary and conclusions.

## 2 Proposed Model

The IS makes use of both misuse detection and anomaly detection. It has mechanisms for detecting deviations from a set of normal patterns, and it has way of storing and recalling specific patterns associated with previous pathogenic attacks. The traditional immune IDSs only adopt anomaly detection and ignore misuse detection, so the false negative error and false positive error all are very high of these systems. In addition, the traditional systems carry out static detection, and the self and detector libraries become very large and can not adapt to dynamic changing network environment

The aim of the framework presented in this section is to develop a dynamic multilayered detection system that can be used to create a population of individuals which are able to identify a variety of known and unknown anomalous behavior to overcome the limitations of the traditional systems.

### 2.1 Model Overview

The immune-based dynamic multilayer IDS model consists of signature detection layer and adaptive detection layer. When the system starts .the antigens (IP packets captured from the monitored network) are fed into system. If one antigen is recognized as malicious behavior by either detection layer, alarming messages and some messages about this malicious behavior will be send to network administrators to help them take corresponding measures. There is a subtle difference between the signature detection layer and adaptive detection layer in running mechanism. In adaptive detection layer, if one antigen is recognized as malicious behavior by the elements of memory detector set, it is send alarming messages soon like the signature detection layer, else if an attack is recognized by the elements of the mature detector set , it just increase the value of the count filed of the corresponding mature detectors. When a mature detector's count field is over predefined threshold, model will send a signal to network administrator. If administrators give an affirmative signal which we call it co-simulation signal in fix period, the mature detector will be become memory detector and the character field will be added into the gene library to update the gene library. Otherwise, system will consider this mature detector as an invalid detector and will delete it from mature detector set. During the detection course, if the monitored network adds or uninstall some network services, the corresponding signature of these services will also be added or deleted from the self library and all the memory detectors must be computed the affinity to the elements of the self library. If the affinity of any memory detectors is over threshold, this memory detector will be removed.

The overall architecture of our proposed model is presented in Fig.1.

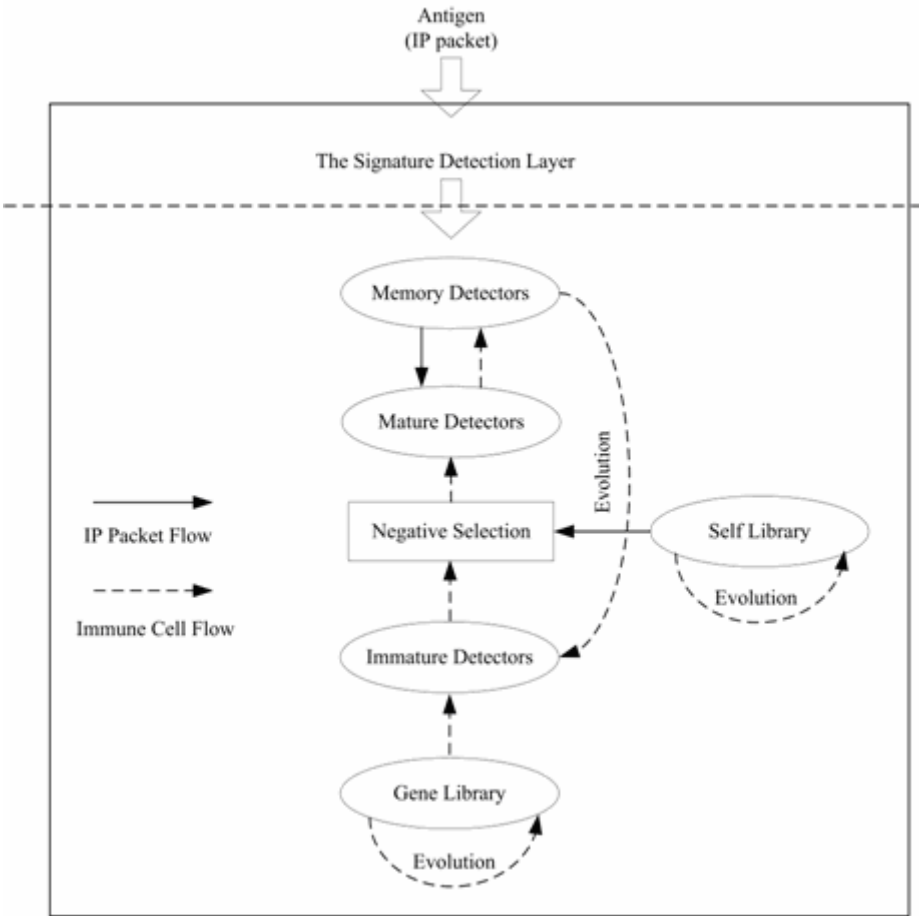


Fig. 1. Architecture of Immunity-Based Dynamic Multilayer Intrusion Detection Model

## 2.2 Signature Defense Layer

**Definition 1 Antigen Self and Nonself :** Antigens ( $Ag, Ag \subset D, D = \{0,1\}^l$ ) in our approach are fixed-length ( $l=56$ ) binary strings extracted from the Internet Protocol (IP) packets transferred in the network. An antigen consists of the source and destination IP addresses, port number, protocol type, IP flags, IP overall packet length, TCP/UDP/ICMP fields, etc. Self is defined as normal sanctioned network service transactions and harmless background clutter, while Nonself represent IP packets from a computer network attack, and  $Self \cup Nonself = Ag$ .

In the course of foetus forming, the immunoglobulin G can enter into the body of foetus by placenta or colostrum to construct the passive immune ability and this passive immune ability can make foetus get the homologous immune ability to his matrix's. Similar to innate immune system of IS, signature defense layer adopts to misuse detection.

Similar to innate immune system of IS, signature defense layer adopts to misuse detection. There is only existed one type detector---memory cell I in this layer. The memory cell I is represented as a set of binary string feature masks which are highly specific to known type malicious behavior. The antigens firstly compare to the cells of memory cell I. If an antigen match to any cells of memory cell I, alarming messages and assistant messages will be send to network administrators. Or else the antigens will be fed to adaptive detection layer.

The network administrators can add new known attack’s signatures, arranged follow the format of memory cell (described in section 2.3) to the memory cell I set to update memory cell I.

The aim we introduce signature defense layer is to decrease the false negative error and false positive error and detect familiar attacks. Experimental results show we can not only decrease the false errors but also increase system efficiency by introducing signature defense layer

### 2.3 Adaptive Defense Layer

As opposed to the innate immune system which is nonspecific in its defence against harmful pathogens, the adaptive immune system initiates a response specific to the pathogen that has entered the body. The adaptive immune system also provides memory capabilities to the immune system [9].We can make use of adaptive detection layer to detect novel and complex unknown intrusions.

**Definition 2 Mature Detector and Memory Detector :** mature detector, which is not match self antigen, start monitoring new antigens. Each mature detector attempts to bind to new antigen when a mature detector matches any new antigen and it does not immediately regard the detected antigen as nonself. Memory detector is activated mature detector, in contrast to mature detectors, memory detectors immediately regard the detected antigen as nonself when they match any single antigen and they have longer life span than that of mature detectors.

There are two mainly phases in the adaptive detection layer. The first is training phase. This involves the generation of self and detector sets. Before the system start to work, we must study the monitored network behaviors and extract the characters from these behaviors to form self set. Unlike the traditional model [10-11], the self elements changes dynamically. This is because the network behaviors are changes continuously. Some network activities, which were regarded as normal behavior before, are forbidden after the bugs are fixed. Furthermore, the network may provide more services or uninstall some services. So, the elements also need to change to keep up with the changing of the network behavior. Equation (1) depicts the dynamic evolution of self, where  $Self_{new}$  is the set of newly defined self elements at time  $t$ , and  $Self_{outdated}$  is the set of outdated self elements representing current abnormal behaviors.

$$Self(t) = \begin{cases} initial\ Self\ set & t = 0 \\ Self(t-1) \cup Self_{new} - Self_{outdated} & t \geq 1 \end{cases} \quad (1)$$

Equation (1) depicts the dynamic evolution of self, where  $Self_{new}$  is the set of newly defined self elements at time  $t$ , and  $Self_{outdated}$  is the set of outdated self elements representing current abnormal behaviors.

Immature detector is created with a randomly generated receptor string that has the same number of fields as the self string, and remains immature for a certain period of time. During this maturation period, the detector is compared to every element of self set, and if the detector matches any elements, it "dies" and is replaced by a detector with a new, randomly generated receptor string. This is analogous to negative selection of thymocytes in the thymus. If the detector survives, the maturation period without matching anything, it becomes mature, and future matches may indicate that a potentially dangerous network connection pattern was detected. However, if a mature detector stays in a mature detector population for a long period, it is highly likely that the match count of a mature detector will eventually meet the activation threshold and it becomes a memory detector. In contrast to mature detectors, memory detectors activate immediately when they match any single antigen, that is to say that the activation threshold of memory detectors is one generation. This is because memory detectors have matched true non-self antigens in the past, and thus any antigen detected by these detectors is considered as a definite non-self antigen without extra checking [12].

The match rule considered is based on hamming distance and is termed the hamming match. Two string  $a$  and  $b$  match under the hamming match rule if they have same bits in at least  $r$  positions.

$$D(a,b) = \sum_{i=1}^L \delta_i \begin{cases} \delta_i = 1, & a_i \neq b_i \\ \delta_i = 0, & a_i = b_i \end{cases} \quad (2)$$

Equation (2) depicts how to measure the hamming distance, where  $a$ ,  $b$  are two matching strings, and  $i$  is the cursor which indicate the matching position.

$$F(ab,ag,r) = \begin{cases} 1, & D(ab,ag) \geq r \\ 0, & D(ab,ag) < r \end{cases} \quad (3)$$

Equation (3) gives the hamming matching function.

When self changes, mature detectors or memory detectors should be compared to every element of  $self_{new}$ . If a detector matches any elements of  $self_{new}$ , it will be removed immediately.

The detectors in the detectors set have finite lifetimes and they are continually changing. This mechanism ensures that an attack can not repeatedly exploit the same gaps in the coverage and it also prevents the scaling problem [8]. In contrast to mature detectors, memory detectors have much extend life spans and have lower thresholds of activation.

The second phase is detection phase. In this course, memory detectors monitor antigen first when antigens are presented to the adaptive detection layer from signature detection layer. Because memory detectors remember nonself antigen patterns that are proven to be intrusions, it is expected that memory detectors detect real intrusions from

presented antigen. Then, the antigen set is presented to mature detectors after being filtered by memory detectors. Although memory detectors can detect some intrusions, there are still existed some further intrusions that have never occurred before. Mature detectors were expected to detect these new intrusions. When a mature detector binds antigen, system sends a requirement signal to system administrator to ask for co-simulation signal. In fixed period, if system receives the affirmative co-stimulation signal, it will send alarm signal to user, other system only increases the match counts of the mature detector. If the accumulated mature detector match counts meet the activation threshold and they receives the affirmative co-stimulation signal from system administrator, this mature detector is active and become a memory detector. Meanwhile, system will clone and mutate this detector.

$$Num = \xi(1 - conc). \quad (4)$$

Equation (4) indicates that the clone number when a mature detector become a memory detector. Where  $\xi$  is a constant, and  $conc$  denotes the concentration of the new memory detector. The reason that we adopt to this measure is to control clone number is that we want to the generated detectors can cover more wide shape space in order to reduce the false negative error.

### 3 Experiment

The experiment has been carried out in the Laboratory of Computer Network and Information Security at Sichuan University. A total of 40 computers in a network are under surveillance. According to the model we propose in this paper, an antigen is defined as a 56 bits length binary string composed of the source/destination IP address, port number, protocol type, IP flags, IP overall packet length, TCP/UDP/ICMP fields, and etc. And we can use true positive rate (TP) and false positive rate (FP) to evaluate the performance of the model.

**Define 6 TP and FP :** TP refers to the situation where the classification predicts an intrusion correctly. FP refers to the situation where a normal record is (falsely) identified as an intrusion [15] [16].

$$TP = \frac{\text{The number of attacks which are judged correctly by system}}{\text{The total number of the real attacks}} \quad (5)$$

$$FP = \frac{\text{The number of attacks which are not judged by system}}{\text{The total number of the real attacks}}. \quad (6)$$

There are several important parameters in the model such as tolerisation period, life span of mature detectors, and the size of initial self-set and etc. In order to evaluate every parameter's impact on model's performance, we have carried out many group experiments. The parameters that are used in the experiments are summarized in

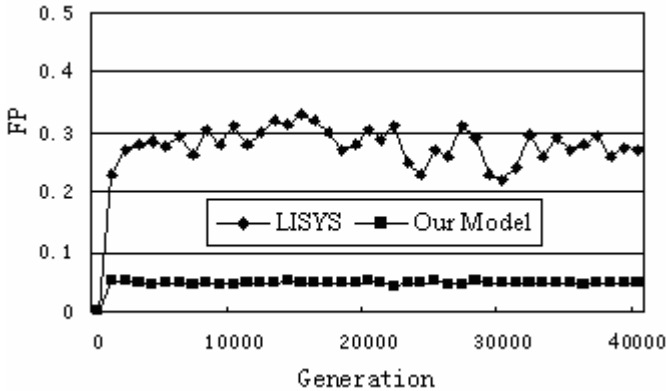


**Table 1.** Parameters used for experiments

| Parameters                                                        | Values |
|-------------------------------------------------------------------|--------|
| Tolerisation Period                                               | 50     |
| Life span of Mature Detectors                                     | 40     |
| The Size of Initial Self-Set                                      | 40     |
| The Number of New Generated Immature Cells                        | 400    |
| The Number of Immature Cells Generated in the Process of Mutation | 100    |
| Generation                                                        | 10000  |
| Activation Threshold of Mature Detectors                          | 5      |

table 1, and these values of the parameters can get relative satisfied results (FP=0.048, TP=0.962) in our experiments, which have been verified by hundreds of tests in our laboratory.

In order to verify the adaptability, and test the efficiency of our model, experiments were undertaken with regards to the LISYS [9].



**Fig. 2.** FP rates for LISYS and our model

As the Fig.2 shows that the FP rates of our model is much lower than that of LISYS and the FP rates are not fluctuant with changing of the time. So we can safely conclude that the dynamic model is more adaptable to real network environment than LISYS.

From the following Fig.3, we can see that the TP rates of LISYS are much lower than that of our model. There are two main reasons for that. One is that we add signature detection layer to the model and system can detect known intrusion rapidly and reliable. The second is that the elements of self set and detector set can vary with the changing of the network environment. So the TP rates of our model are higher than that of LISYS.

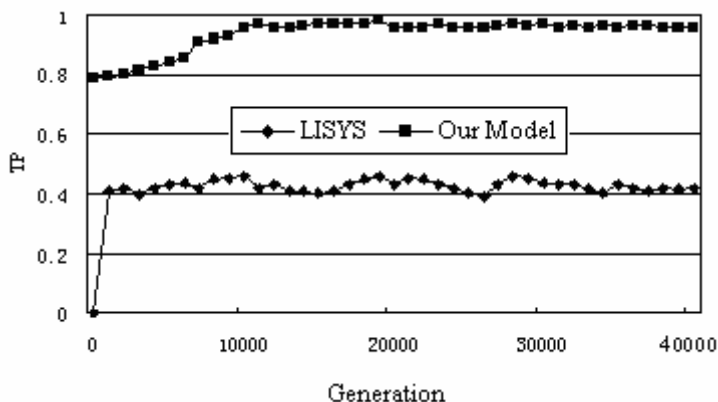


Fig. 3. TP rates for LISYS and our model

## 4 Conclusion

Inspired by the biological immune system, an immunity-based dynamic multilayer intrusion detection model was proposed in this paper. In this model, we employ misuse detection and anomaly detection in parallel, and these two detection component are reciprocal in the system. Meanwhile, in order to adapt to dynamic changing network environment, the elements of the self set and detector set can vary according to the changes of the network environment. The practical experimental results prove that this model can efficiently reduce both the false-positive error rates and false-negative error rates, and enhance the ability of self-adaptation and diversity for the network detection systems.

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# Immunity and Mobile Agent Based Grid Intrusion Detection

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**Abstract.** This paper analyzes the unique characteristics of a grid environment and the deficiencies of current grid intrusion detection systems, and proposes a novel immunity and mobile agent based grid intrusion detection (*IMGID*) model. Then, the concepts and formal definitions of *self*, *nonself*, *antibody*, *antigen* and *agent* in the grid security domain are given. Furthermore, the mathematical models of *self*, *mature MoA* (mature monitoring agent) and *dynamic memory MoA* (memory monitoring agent) *survival* are established. Our theoretical analysis and experimental results show that the model is a good solution to grid intrusion detection.

## 1 Introduction

Grid Computing shows a nice future, but also presents tough security challenges. A grid environment has many distinctive characteristics that are different from those of common network environments:

- The user population and the resource pool are large and dynamic.
- A computation (or processes created by a computation) may acquire, start processes on, and release resources dynamically during its execution.
- Resources and users may be located in different countries [1].

So the mechanisms and policies for securing the grid are more complicated.

There has been abundant research on intrusion detection for common network environments, but current research on grid intrusion detection is still in its infancy, and a few references can be used [2] [3]. M. F. Tolba, M. S. Abdel-Wahab proposed a grid intrusion detection architecture (GIDA) [4] in 2005. In the architecture, the anomaly detection is implemented using LVQ neural network. Increasing the number of IDSs (intrusion detection servers) will reduce the training time of LVQ, but increasing the number of grid users will increase the training time. Obviously, if we increase IDSs to reduce the training time, the cost will be higher and the system will not be self-adaptive to the grid environment where resources and users increase dynamically and may be large. So the detection performance of GIDA is not good.

Artificial immune system has the features of dynamicity, self-adaptation and diversity [5] [6] [7] [8] [9] [10] [11], and mobile agent has many same appealing properties as that of artificial immune system [12] [13] [14]. Thus, we apply mobile agent

technology as support for intrusion detection, and propose a novel immunity and mobile agent based grid intrusion detection (*IMGID*) model. The model that has the features of artificial immune system just meets the constraints derived from the characteristics of the grid environment and addresses the above mentioned performance problem.

In *IMGID*, the concepts and formal definitions of *self*, *nonself*, *antibody*, *antigen* and *agent* (that simulates the lymphocyte and is used as a detector to recognize non-self antigens, i.e. intrusions,) in the grid security domain are given. We define three kinds of agents: monitoring agents (*MoA*), communicator agents (*CoA*) and beating off agents (*BoA*). *MoAs* simulate B-lymphocytes in the immune system and patrol grid nodes. They are responsible for monitoring parameters simultaneously at four levels (user level, system level, process level, and packet level) and detecting intrusion. As B-lymphocytes consist of mature and memory lymphocytes, *MoAs* are divided into mature and memory *MoAs* that simulate, respectively, mature and memory cells. *CoAs* serve as communicators and are responsible for message transmission among agents. They simulate lymphokines secreted from T cells to stimulate B cells to clone themselves or eliminate cloned cells. *BoAs* simulate T killer cells that deal with intrusive activities. Once *MoAs* detect intrusions, they will stimulate *CoAs* and present the features of intrusions to *BoAs*. *CoAs* will activate *BoAs*. *BoAs* will move to the suspected place to counterattack intrusions. The counterattack strategies consist of disconnecting a node, discarding dubitable packets, killing a process, and so on. *MoAs* can clone themselves if an intrusion is detected. Some cloned *MoAs* are left here to detect more intrusions, and others are moved to other grid nodes to detect the similar intrusions. Then, the mathematical models of *self*, *mature MoA* and *dynamic memory MoA survival* are established.

In the present immunity-based intrusion detection systems [15], the memory lymphocytes have an unlimited lifecycle except they match the newly added selfs. Obviously, all the mature lymphocytes will become memory ones and the system will not have the feature of dynamicity and diversity in the end.

However, *IMGID* introduces a new idea to overcome this problem: the least recently used memory *MoAs* will degrade into mature *MoAs*, if the number of memory *MoAs* reaches or exceeds a given maximum.

## 2 The Proposed Grid Intrusion Detection Model (*IMGID*)

*IMGID* has two sub-models (see Fig. 1). The first is the model of the generation of new *MoAs*. The second is the intrusion detection model.

In the first model, we define antigens (*Ag*) to be the features of grid services and accesses, and given by:

$$Ag \in D. \quad (1)$$

$$D = \{d \mid d = \langle \text{ueser\_level}, \text{system\_level}, \text{process\_level}, \text{packet\_level} \rangle\}. \quad (2)$$

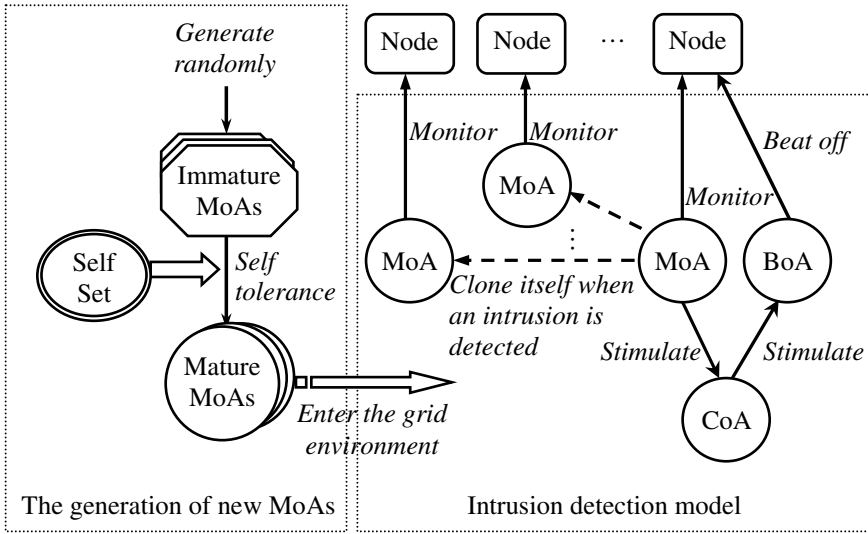


Fig. 1. The proposed grid intrusion detection model

The evolution of MoAs in grid environment is shown in Fig. 2.

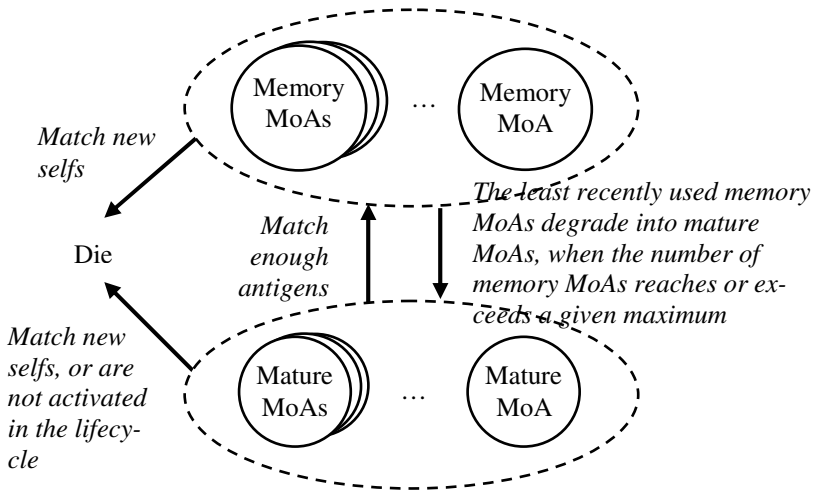


Fig. 2. The evolution of MoAs in grid environment

*user\_level*, *system\_level*, *process\_level* and *packet\_level* are, respectively, the parameter monitored by monitoring agents at user level, system level, process level, and packet level. We define *Self* to be the set of normal grid services and accesses. Similarly, *Nonsel*f is also a set of abnormal services and accesses. *Ag* contains two subsets, *Self* and *Nonsel*f, where  $Self \subset Ag$  and  $Nonsel \subset Ag$  such that

$$Self \cup Nonself = Ag, \quad Self \cap Nonself = \Phi. \quad (3)$$

In the intrusion detection model, all the agents form a set (*Agent*). *Agent* contains three elements, *MoA*, *CoA* and *BoA*. Monitoring agents, communicator agents and beating off agents form, respectively, the set *MoA*, *CoA* and *BoA*. Thus, we have:

$$Agent = \{MoA, CoA, BoA\}. \quad (4)$$

$$MoA = \{ \langle d, age, count \rangle \mid d \in D, age \in N, count \in N \}. \quad (5)$$

*d* is the monitoring agent that is used to detect an intrusion, *age* is the agent age, *count* (affinity) is the intrusion number detected by agent *d*, and  $\mathbb{N}$  is the set of natural numbers. *d*, *age* and *count* are also called, respectively, field *d*, *age* and *count* of an agent. For the convenience using the fields of a agent *x*, a subscript operator “.” is used to extract a specified field of *x*, where

$$x.fieldname = \text{the value of field } fieldname \text{ of } x. \quad (6)$$

MoAs consist of Mature MoAs and Memory MoAs (see Fig. 2). A mature MoA is a MoA that is tolerant to self but is not activated by antigens. A memory MoA evolves from a mature one that matches enough antigens in its lifecycle. Mature MoAs form a set ( $MA_{MoA}$ ). Mature MoAs detect novel intrusions that have not previously been identified. Memory MoAs form a set ( $ME_{MoA}$ ). Memory MoAs greatly enhance detection of previously seen intrusions. Therefore, we have:

$$MoA = MA_{MoA} \cup ME_{MoA}. \quad (7)$$

$$MA_{MoA} \cap ME_{MoA} = \Phi. \quad (8)$$

$$MA_{MoA} = \{x \mid x \in MoA, \forall y \in Self \ (\langle x.d, y \rangle \notin Match \wedge x.count < \beta)\}. \quad (9)$$

$$ME_{MoA} = \{x \mid x \in MoA, \forall y \in Self \ (\langle x.d, y \rangle \notin Match \wedge x.count \geq \beta)\}. \quad (10)$$

*Match* is a match relation in *D* defined by

$$Match = \{ \langle x, y \rangle \mid (x, y \in D), f_{match}(x, y) = 1 \}. \quad (11)$$

$f_{match}(x, y)$  is based on the affinity between *x* and *y*: if the affinity greater than a specified threshold, then 1 is returned, otherwise, 0 is returned. In *IMGID*, the affinity function can be *r-contiguous-bits matching rule*, *Hamming distance*, *Landscape-Affinity Matching*, etc [16].

## 2.1 The Definition of Self

In a dynamic grid environment, as time goes on, some grid services and accesses, which were normal in the past, are forbidden now. Equation (12) depicts the evolution of self, where  $Self(t)$  evolves from  $Self(t-1)$ , the mutated self antigens ( $Self_{variation}$ ) at time *t* are eliminated, and the newly defined self antigens ( $Self_{new}$ ) at time *t* are added.

$$Self(t) = \begin{cases} \{x \mid x \text{ is the initial self antigen}\}, & t = 0 \\ Self(t-1) - Self_{variation}(t) \cup Self_{new}(t), & t \geq 1 \end{cases} \quad (12)$$

$$Self_{variation}(t) = \{x \mid x \text{ is the self antigen mutated at time } t\}. \quad (13)$$

$$Self_{new}(t) = \{y \mid y \text{ is the self antigen added at time } t\}. \quad (14)$$

The model of self assures that the number of selfs is small and remains steady.

## 2.2 Mature MoAs Model

$$MA_{MoA}(t) = \begin{cases} \Phi, & t = 0 \\ MA_{retain}(t) \cup MA_{new}(t) \cup MA_{cycle}(t) - MA_{activation}(t), & t \geq 1 \end{cases} \quad (15)$$

$$MA_{retain}(t) = MA'_{MoA}(t) - A(t) \cup A'(t). \quad (16)$$

$$MA'_{MoA}(t) = \{y \mid y \in MoA, x \in MA_{MoA}(t-1), x.age < \lambda, \forall s \in Self_{new}(t) < x.d.s \notin Match, \\ y.d = x.d, y.age = x.age + 1, y.count = x.count\}. \quad (17)$$

$$A(t) = \{x \mid x \in MA'_{MoA}(t), \exists y \in Ag(t-1) < x.d, y \in Match\}. \quad (18)$$

$$A'(t) = \{y \mid y \in MoA, x \in A(t), y.d = x.d, y.age = x.age, \\ y.count = x.count + 1\} \quad (19)$$

$$MA_{cycle}(t) = \{y \mid y \in MoA, y.d = x.d, y.age = T, y.count = \beta - 1, x \in ME_{degradation}(t), T < \lambda\}. \quad (20)$$

$$MA_{activation}(t) = \{x \mid x \in A'(t), x.count \geq \beta\}. \quad (21)$$

$$MA_{new}(t) = \{y \mid y \in MoA, y.d = x.d, y.count = 0, y.age = 0, \\ x \in (I_{new}(t) - \{z \mid z \in I_{new}(t), \exists s \in Self(t) < z, s \in Match\})\}. \quad (22)$$

$$I_{new}(t) = \begin{cases} \Phi, & |MA_{MoA}(t-1)| \geq \Gamma \\ \{y_1, y_2, \dots, y_{\Gamma - |MA_{MoA}(t-1)|}\}, y_i \in D, 1 \leq i \leq \Gamma - |MA_{MoA}(t-1)|, & \text{otherwise} \end{cases} \quad (23)$$

$MA_{retain}(t)$  simulates the process that the mature cells evolve into the next generation ones, where the cells do not tolerate to those newly added self elements or have not match enough antigens ( $\beta > 0$ ) in lifecycle  $\lambda$ , will be eliminated.  $MA_{new}(t)$  depicts the generation of new mature MoAs.  $\Gamma (> 0)$  is the max number of mature MoAs in *IMGID*.  $MA_{activation}(t)$  is the set of mature MoAs which match enough antigens and will be activated and evolved into memory MoAs at time t.  $MA_{cycle}(t)$  is the set of the least recently used memory MoAs which degrade from memory MoAs into mature



MoAs and be given a new age  $T (>0)$  and count  $\beta-1$  ( $\beta \geq 1$ ). Once a mature MoA with count  $\beta-1$  matches an antigen in lifecycle  $\lambda$ , the count will be set to  $\beta$  and the mature MoA will be activated again. The method assures degraded memory MoAs priority in evolvment. Because memory MoAs have better detection capability than mature MoAs, the method enhances detection efficiency.

### 2.3 Dynamic Memory MoAs Survival Model

$$ME_{MoA}(t) = \begin{cases} \Phi, & t = 0 \\ ME_{retain}(t) \cup ME_{new}(t) - ME_{degradation}(t), & t \geq 1 \end{cases} \quad (24)$$

$$ME_{retain}(t) = ME'_{MoA}(t) - E(t) \cup E'(t). \quad (25)$$

$$ME'_{MoA}(t) = \{y \mid y \in MoA, x \in ME_{MoA}(t-1), \forall s \in Self_{new}(t) < x.d.s > \notin Match, y.d = x.d, y.age = x.age + 1, y.count = x.count\}. \quad (26)$$

$$E(t) = \{x \mid x \in ME'_{MoA}(t), \exists y \in Ag(t-1) < x.d, y > \in Match\}. \quad (27)$$

$$E'(t) = \{y \mid y \in MoA, x \in E(t), y.d = x.d, y.age = 0, y.count = x.count + 1\}. \quad (28)$$

$$ME_{new}(t) = \{x \mid x \in ME_{MoA}, y \in MA_{activation}(t), x.d = y.d, x.age = 0, x.count = y.count\}. \quad (29)$$

$$ME_{degradation}(t) = \begin{cases} \{x \mid x \in ME_{retain}(t), x.age > \gamma\}, & |ME_{MoA}(t-1)| \geq \kappa \\ \Phi, & otherwise \end{cases} \quad (30)$$

Equation (24) depicts the dynamic evolvment of memory MoAs, where the memory MoAs that match the newly added selfs will die and are matched by an antigen will be activated immediately.  $ME_{retain}(t)$  simulates the process that the memory MoAs evolve into the next generation ones.  $ME_{new}(t)$  is the set of new memory MoAs evolved from mature ones.  $ME_{degradation}(t)$  is the set of memory MoAs that are not activated by antigens lately and degrade from memory MoAs into mature MoAs when the number of memory MoAs reaches or exceeds a given maximum  $\kappa$ .  $\gamma (>0, \text{natural number})$  is the lifecycle of memory MoAs.

## 3 Simulations and Experiment Results

The experiments were carried out in the Laboratory of Computer Network and Information Security at Sichuan University. We developed a grid simulation toolkit based on GridSim [17] to satisfy our needs. The simulation environment simulates users

with different behaviors, resources and agents. A total of 40 computers in a grid were under surveillance. 10 immature MoAs was given.

To prove the steady performance and high efficiency of *IMGID*, we developed the first set of experiments to show the effect of self's number on training time in *IMGID*. The initial number of selfs was 40. The training time increased due to the increasing of selfs number. The number of selfs was small and the increase rate of selfs was low. So the training time for mature MoAs was not long and the increase rate of the training time was low. The experiment results are shown in Fig.3. The short training time illustrates the high efficiency and the low increase rate of the training time illustrates the steady performance in *IMGID*.

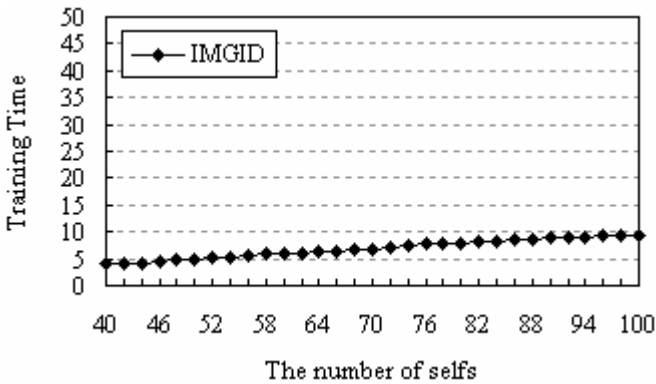


Fig. 3. Effect of the number of selfs on the training time in *IMGID*

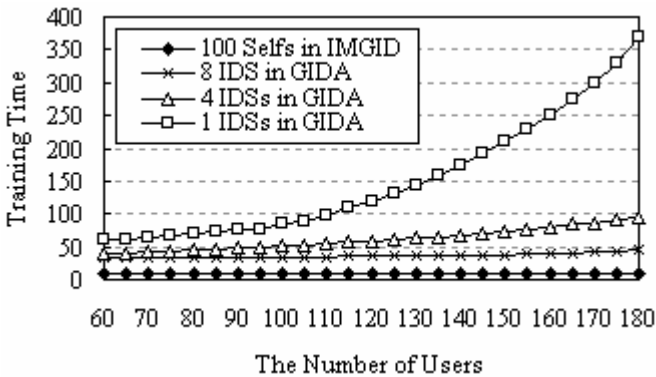


Fig. 4. Effect of the number of IDSs and users on the training time in *IMGID* and GIDA

To prove the self-adaptive capacity and steady performance of *IMGID*, we developed the second set of experiments to compare *IMGID* with LVQ. In GIDA, the number of IDSs was set to 1, 4, 8, respectively. The training time for detectors in GIDA increased due to the increasing of users or reducing of IDSs. Specially, the

training time increased rapidly when only one IDS was used. In *IMGID*, the number of tolerated selfs was 100. We increased grid users and made experiments on the training time of *IMGID* when the number of selfs kept 100. The training time depended on the number of selfs and was hardly affected by dynamically varying IDSs and users. The results in Fig.4 illuminate that the number of IDSs and users has a great effect on the training time in GIDA, while no effect on that in *IMGID*.

Comparison between the curve trend of the training time in *IMGID* (Fig.3) and those three in GIDA (Fig.4) shows the increase rate of the training time in *IMGID* was lower than that in GIDA.

Therefore, the experiment results show that *IMGID* has high efficiency and steady performance to adapt the dynamically varying grid environment.

## 4 Conclusions

The proposed immunity and mobile agent based grid intrusion detection (*IMGID*) model is an active grid security technique.

In *IMGID*, the concepts of *self*, *nonsel*, *antigen*, *antibody* and *agent* have been abstracted and extended. Besides, *IMGID* introduces a new idea of *dynamic memory MoAs survival*, which assures dynamicity and diversity in immunity-based IDS. Furthermore, the mathematical models of *self*, *mature MoA* and *dynamic memory MoA survival* are presented.

The theoretical analysis and the experiment results show that the proposed method is an effective solution to intrusion detection for grid security.

## 5 Future Researches

The effects of several import parameters on system performance are very important in the models of mature MoA and dynamic memory MoA survival. The set of appropriate parameters could enhance detection efficiency and assure steady performance. These parameters include the new age  $T$  and count  $\beta-1$  of degraded memory cells in the models of mature MoA,  $\kappa$  and  $\gamma$  in the models of dynamic memory MoA survival.

The *match algorithm* and the mathematical models of *CoA* and *BoA* need to be abstracted and extended.

## Acknowledgment

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# Immune-Based Peer-to-Peer Model for Anti-spam

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**Abstract.** Spam (or junk email) has been a major problem on the Internet. A lot of solutions have been proposed to deal with it. However, with the evolvement of spammers' techniques and the diversification of email content, the traditional anti-spam approaches alone are no longer efficient. In this paper, a new anti-spam Peer-to-Peer (P2P) model based on immunity was presented. *Self, Non-self, Antibody, Antigen* and immune cells in email system were defined. The model architecture, the process of Antigen presenting, clone selection and mutation, immune tolerance, immune response, life cycle of immune cells and some other immune principles were described respectively. The analyses of theory and experiment results demonstrate that this model enjoys better adaptability and provides a new attractive solution to cope with junk emails in P2P environment.

## 1 Introduction

Nowadays, the overrun of spam brings people a lot of troubles. In order to deal with spam, a lot of approaches have been proposed: such as Blacklisting and Whitelisting method, rule-based method [1], statistics-based method [2][3][4], and secure authentication-based method [5]. All these approaches have achieved some effects.

However, there are still some limitations to these approaches. As the source address of an email can be forged, the Blacklisting and Whitelisting method is not so effective; As rule-based method is static and statistics-based method needs a lot of training examples, they are often got through by spammers using various tricks, for example text obfuscation, random space or word insertion, HTML layout, and text embedded in images; Though the secure authentication-based method enjoys high security, the easiness of usage is affected. On the other hand, with the continuous growth of Internet, the type and content of emails are becoming more and more diverse. And users' interests are changing continuously too. In addition, there are great differences between Chinese and English [6]. Finally, filters based on these methods work independently, so they are lack of knowledge about new forms of spam.

With the development of distributed system, some anti-spam approaches based on Peer-to-Peer (P2P) network have been proposed [7][8][9] to collaboratively share knowledge about spam. But some of the limitations mentioned above still exist and most of these approaches are designed for structured network environment. Considering the Biological Immune System (BIS) has the characteristics of high distribution

and self-adaptation [10], immunity is introduced in this paper to build an anti-spam model in P2P environment. The analysis of theory and experimental results demonstrate that it enjoys better adaptability and provides a new attractive solution to cope with junk emails in P2P environment.

## 2 Anti-spam P2P Model Architecture

Due to the collaborative computation advantage of P2P technology, it is a good choice to propose an anti-spam solution in P2P environment, based on the following considerations: (1) Users who joined the same peer group share approximately the same interests. Therefore, the spam information can be shared among them. (2) In central control system, as mail server is the bottleneck, it is not desirable to implement complicated filtering strategies on mail server, or the quality of service will be affected. (3) It is a most dynamic environment that all the peer nodes and junk emails keep changing all the time, so a model that is adaptive to changes is needed.

The architecture of the proposed model is shown in figure 1.

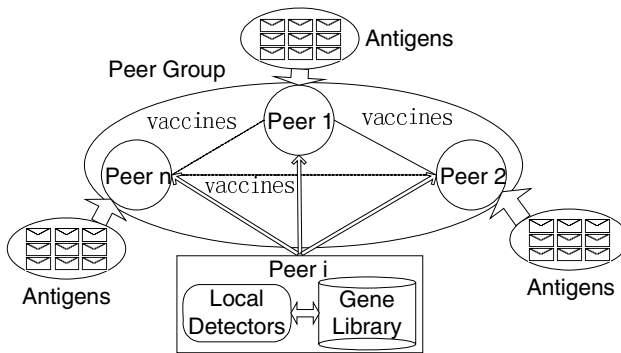


Fig. 1. Architecture of the proposed anti-spam P2P model

Once a user joins the peer group, the peer will keep communication with several nearest peers in the peer group and exchange information about spam with each other. Every time a peer receives an email (*Antigen*), its local detectors that are used to simulate immune cells in the model will be activated (immune response) to execute filtering function. While some other immune mechanisms (e.g. clone selection and mutation, life cycle of immune cells) occur too.

As each peer only faces part of the Antigen space, it is necessary to share the spam information in the peer group. This is done by dynamically handing around spam vaccines, which can be implemented by mobile agent or some other approaches. Through this mechanism, the global spam information can be collected with the collaborative work of all the peers in the peer group.

### 3 Immune Principles

For convenience, the following notations are established:

- $N$ : the set of natural numbers;
- $Set\_String$ : the set of string;
- $Set\_C$ : the set of immune cells;
- $Set\_MC$ : the set of memory cells;
- $Set\_IC$ : the set of immature cells;
- $Th\_Deg$ : the threshold of degeneration for memory cells;
- $Th\_aff\_Rec$ : the threshold of affinity for recognition;
- $Th\_aff\_Mutate$ : the threshold of affinity for mutation;
- $Th\_Spam$ : the threshold of score for spam;
- $Num\_init\_Mcount$ : the initial matching number of memory cells;
- $Num\_init\_Icount$ : the initial matching number of immature cells;
- $Num\_const\_Clone$ : clone constant;
- $Num\_const\_Mutate$ : mutation constant;
- $m$ : the number of Antigen fields;
- $n$ : the number of vector fields;
- $⋅$ : the operation of citing a field from a vector.

#### 3.1 Antigen Presenting

Let Antigens be the emails received by users. Let  $E$  be the set of string contained in Antigens and  $E \subset Set\_String$ .

In order to simulate the Antigen presenting of BIS, the features of an email are extracted to get the features of an Antigen: *Antigenic determinant* [10]. First of all, the procedure of preprocess [11] is executed to reduce the influence of noise (e.g. removing HTML tags and tokens in the stop-list) after an email is decoded. And some of the common features found in most junk emails are extracted. If it is Chinese, the process of words segmentation is done subsequently [6]. Then keywords and the associate weights are extracted and the email is processed into the form of Antibody. Actually, it is a data mining process [11] and content-based filtering strategy can be brought into effect.

$$Ag = \{ \langle F_1, \dots, F_m \rangle \mid F_i \in E, i \in [1, m], m \in N \} \quad (1)$$

Equation (1) defines the set of string that are extracted from the header and body of an email, standing for the transaction features of an email.  $F_i$  is the  $i^{th}$  transaction feature vector, i.e. the  $i^{th}$  gene segment of  $Ag$ , which is described by (2).

$$F_i = \langle Str_1, \dots, Str_n \rangle, Str_i \in Set\_String, i \in [1, n], n \in N \quad (2)$$

$L$  is the set of Lymphocytes as defined by (3), where  $d$  is the Antigenic Determinant and  $count$  is the matching number of  $d$ . Actually,  $L$  is the detectors (*Antibodies*) used in the model to determine whether an email is spam or not.

$$L = \{ \langle d, count \rangle \mid d \in Ag, count \in N \} \quad (3)$$

*Self* is defined to mean the set of legitimate emails and *Nonself* represents the set of junk emails. Equation (4) expresses the relationship between *self* and *Nonself*.

$$Self \cup Nonself = Ag \wedge Self \cap Nonself = \emptyset, Self \subset Ag \wedge Nonself \subset Ag \tag{4}$$

The set of memory cells *Set\_MC* denotes cells that don't match *Self* and whose count value is high above the activation threshold of memory cells. And *Set\_IC* is the set of immature cells. Obviously, there is the following relationship as (5).

$$Set\_C = Set\_MC \cup Set\_IC \wedge Set\_MC \cap Set\_IC = \emptyset \tag{5}$$

### 3.2 Affinity Measure

$$f_{match}(c, v) = \begin{cases} 1 & \text{if } f_{affinity}(c, v) \geq Th\_aff\_Rec \\ 0 & \text{otherwise} \end{cases}, c \in L, v \in Ag \tag{6}$$

Equation (6) defines the matching relationship in *E*, where  $f_{affinity}(c, v)$  is used to compute affinity between an Antigen and a detector and 1 represents Antigen *v* is matched by a specific detector *c*.

The function of computing affinity between an Antigen and a detector is described as follows, representing the matching degree between feature sets.

```
function faffinity(c, v)
begin
 faffinity(c, v) := 0;
 for i := 1 to m do
 begin
 cs := the shorter vector in c.d.Fi and v.Fi;
 cl := the longer vector in c.d.Fi and v.Fi;
 num := the number of string in cs present in cl;
 len := the number of string in cs;
 faffinity(c, v) := faffinity(c, v) + (num / len) * wi;
 end;
end.
```

In the above pseudocode,  $w_i$  is the weight that is corresponded to the transaction feature  $F_i$  of an Antigen.

### 3.3 Clone Selection and Mutation

$$Set\_C_{clone\_mutate} = \bigcup_{j=1}^{\lceil Nim\_const\_Clone * f_{affinity}(c, v) \rceil} f_{clone}(c) \bigcup_{i=1}^{\lceil Nim\_const\_Mutate * (1 - f_{affinity}(c, v)) * Len \rceil} f_{mutate}(f_{clone}(c)), c \in Set\_C \tag{7}$$

Equation (7) describes clone selection and mutation, where  $Len = \max(\text{Length}(c.d, v))$ ,  $c \in Set\_C$ ,  $v \in Ag$ , which means the longer length of vector between *c.d* and *v*. *c* belongs to the immune cells set where every detector matches current Antigen *v* and it is affirmed by user, i.e. the set of candidate immune cells to be cloned and mutated. Function  $f_{clone}(c)$  is the clone process for detector *c*. And function  $f_{mutate}(c')$  denotes the mutation operation for the cloned cell *c'*. From (7), it is shown that the



relationship between clone number and affinity is direct ratio while the relationship between mutation degree and affinity is inverse ratio. At the same time, in order to avoid producing too random or too similar Antibodies, the mutation range is limited during this operation (i.e. immune tolerance, referring to section 3.4). Through the process of clone selection and mutation, the diversity of detector is assured. And it is possible to detect the new mutated junk emails.

Equation (7) also shows the dynamic evolvement of the immune model. The procedure of clone selection and mutation is detailed by the following pseudocode.

```

procedure clone_selection_mutation(Ag: v, float: aff)
begin
 Set_Candidate := Φ ;
 //get the candidate set of cells to be cloned
 for each(c \in Set_C) do
 begin
 if ($f_{affinity}(c,v) > aff$) then
 Set_Candidate := Set_Candidate \cup {c};
 end;
 for each(c \in Set_Candidate) do
 begin
 //clone operation
 c'.d := c.d;
 c'.count := Num_init_Icount;
 aff := $f_{affinity}(c',v)$;
 num_clones := round(Num_const_Clone * aff);
 Len := max(Length(c'.d,v));
 num_mutate := round(Num_const_Mutate *
 (1 - aff) * Len);
 for i := 0 to num_clones do
 begin
 b := c';
 //mutation operation
 for j := 0 to num_mutate do
 begin
 pos_mutate := get the position of random
 mutation for b;
 replace the string at pos_mutate of b with
 the string from appropriate gene library
 end;
 //immune tolerance
 if ($f_{tolerance}(b) = 1$) then
 Set_IC := Set_IC \cup {b}
 end;
 end;
 end;
end.

```

### 3.4 Immune Tolerance

In BIS, new immature cells are produced in the Bone Model [10]. Before a new produced immature cell joins immune circle, it must pass through the process of immune

tolerance, avoiding *Auto-immune Reaction*. Equation (8) defines the procedure of immune tolerance, where 0 means tolerance failure and 1 means success.

$$f_{tolerance}(b) = \begin{cases} 1, & \text{if } \forall c \in Set\_C, f_{affinity}(c,b) \in (Th\_aff\_Rec, Th\_aff\_Mutate) \\ 0, & \text{otherwise} \end{cases}, b \in Ag \tag{8}$$

The immune tolerance is realized by *Negative Selection Algorithm* [10], which simulates the process of immature cells' maturation. If a new produced detector is too similar to one of Antibodies (the existing detectors) or too random, it means tolerance failure and will be deleted.

### 3.5 Immune Response

$$f_{classify}(c, v) = \begin{cases} 1, & \text{if } \exists (f_{score}(c, v)) \geq Th\_Spam \\ 0, & \text{otherwise} \end{cases}, c \in Set\_C, v \in Ag \tag{9}$$

$$f_{score}(c, v) = f_{score\_innate}(c, v) + f_{score\_adaptive}(c, v), c \in Set\_C, v \in Ag \tag{10}$$

$$f_{score\_x}(c, v) = f_{affinity}(c, v) \times 100, x = innate \vee adaptive, c \in Set\_C, v \in Ag \tag{11}$$

Equation (9) defines the classification function, which determines whether an email is classified as spam or not. For convenience, a scoring function is defined by (10), which consists of innate immune response and adaptive immune response. Equation (11) shows the scoring function of the two parts. The affinity of innate immune response and adaptive immune response can be calculated according to the pseudocode in section 3.2.

The immune response consists of three layers. Layer 1: innate immune response. Layer 2: the immune response of memory cells. Layer 3: the immune response of immature cells. Obviously, with the increase of search scale, the response speed of the above three layers decreases in turn. The procedure is detailed by the following pseudocode.

```

procedure immune_response(Ag: v)
begin
 aff := 0;
 flag_spam := FALSE;
 //innate immune response
 f_score := score from innate immune response;
 if (f_score >= Th_Spam) then
 begin
 move the email to spam box;
 flag_spam := TRUE;
 end
 else //adaptive immune response
 //the second and the first immune response in turn
 for (each(c ∈ (Set_MC ∪ Set_IC))) do
 begin
 if ((f_affinity(c,v) >= Th_aff_Rec) and
 ((f_score + f_score_adaptive(c,v)) >= Th_Spam)) then

```

```

begin
 move the email to spam box;
 flag_spam := TRUE;
 aff := $f_{affinity}(c,v)$;
 break;
end
end;
// costimulation from end users
if ($f_{costimulation}(v) = 1$)
begin
 add Antigenic determinant of v to the
 appropriate Antibody gene library;
 if (aff > 0) then
 begin
 clone_selection_mutation(v, aff);
 //evolvment of immune cells
 Set_Match := all the detectors that matched v;
 for each($c \in \text{Set_Match}$) do
 begin
 if ($c \in \text{Set_MC}$) then
 c.count++;
 if ($c \in \text{Set_IC}$) then
 begin
 c.count := Num_init_Mcount;
 Set_MC := Set_MC \cup {c};
 Set_IC := Set_IC - {c};
 end
 end;
 end;
end;
//False Positive
if (flag_spam = TRUE and $f_{costimulation}(v) = 0$)
begin
 Set_DC := all the detectors that matched v;
 for (each($c \in \text{Set_DC}$)) do
 begin
 Delete Antigenic determinant of detector c from
 the appropriate Antibody gene library;
 Set_C := Set_C - {c}
 end
end
end.

```

Because whether an email is spam or not is determined by end users eventually, it is inevitable to classify a legitimate email as a spam (*False Positive*) or classify a junk email as a legitimate one (*False Negative*). So the final step of immune response is user's costimulation, as described by (12). According to user's feedback, an Antigen's Antigenic determinant is added into or deleted from the appropriate Antibody gene library. While the operation of clone selection and mutation is executed.

$$f_{costimulation}(v) = \begin{cases} 1, & \text{outside signal treats } v \text{ as } NonSelf \\ 0, & \text{otherwise} \end{cases}, v \in Ag \quad (12)$$

In P2P environment, once a new spam is detected in one peer, the new produced detector will be delivered to its nearest peers in the same peer group, simulating the process of vaccination in BIS [10]. Therefore, other peers in the group can detect the new junk email rapidly without further learning. Through the mechanism of vaccine distribution, the information about spam can be shared in the peer group and the efficiency of spam filtering can be improved.

Considering security and privacy factors in P2P network, it is necessary to encrypt the vaccine with *Secure Hash Algorithm* [9]. At the same time, an enhanced authentication mechanism is needed in the model too.

### 3.6 Life Cycle of Immune Cells

In the course of immune tolerance, if a new produced cell interacts with an element of immune cell set (*Auto-immune Reaction*) or is too random, it will be deleted. Otherwise it will be saved in *Set\_IC* and join immune circle. During immune circle, once a memory cell matches an Antigen correctly, its matching number will be increased by one and its life cycle will be lengthened. Once an immature cell matches an Antigen (the first immune response) correctly, it will be evolved to be a memory cell. A memory cell has a much longer life cycle and can response rapidly to an Antigen which has been recognized before (the second immune response).

In order to simulate the senescence of immune cells, all the immune cells' count value is decreased regularly. If a memory cell's count value is less than the threshold *Th\_Deg*, it will be degenerated to be an immature cell. And if an immature cell hasn't matched any junk emails and its count value is decreased to zero, it will die naturally. Meanwhile, any detectors that don't pass through user's costimulation will be deleted too. This mechanism assures the diversity of immune cells, the continuous search ability towards Antigen space and the survival of the best immune cells.

The evolvement of immune cells has been described by the pseudocode in section 3.5 and the degeneration of immune cells is shown in the following.

```

procedure degeneration
begin
 for each (c ∈ Set_C) do
 c.count--;
 //degeneration of memory cell
 if (c ∈ Set_MC and c.count < Th_Deg) then
 begin
 Set_MC = Set_MC - {c};
 c.count = Num_init_Icount;
 Set_IC = Set_IC ∪ {c};
 end;
 //death of immature cell
 if (c ∈ Set_IC and c.count = 0) then
 begin
 Set_IC = Set_IC - {c};

```

```

 Delete Antigenic determinant of detector c from
 the appropriate Antibody gene library;
 end;
end.

```

## 4 Results

### 4.1 Experimental Setup

For lack of common Chinese email corpus, the experimental data was collected by authors and authors' friends. Emails were extracted to be Lymphocytes (detectors), which were consisted of six gene segments, e.g. IP addresses, mail addresses, subject, hyperlinks, etc. Some of the main parameters in the experiments are shown in table 1.

In order to simulate the real environment, the average frequency of receiving emails was 10 emails per day, including 3 junk emails averagely. And the emails in the test set were arranged in the receiving time. The final results were calculated by taking the mean of these data. And six peers consisted of the peer group in order to simulate the distribution of vaccine in P2P environment. Recall, precision, and accuracy [12] were taken to evaluate performances of the model.

**Table 1.** Experimental parameters

| Parameter               | Value | Range |
|-------------------------|-------|-------|
| <i>Num_init_Mcount</i>  | 20    | >0    |
| <i>Num_init_Icount</i>  | 10    | >0    |
| <i>Th_Deg</i>           | 15    | >0    |
| <i>Num_const_Clone</i>  | 7     | >0    |
| <i>Num_const_Mutate</i> | 0.8   | 0-1   |
| <i>Th_Spam</i>          | 50    | >0    |
| <i>Th_aff_Rec</i>       | 0.2   | 0-1   |
| <i>Th_aff_Mutate</i>    | 0.5   | 0-1   |

For convenience, the proposed model in the paper is named "ASID" (Anti-spam system based on immunity and data mining). ASID is a self-learning and self-adaptability system, it can learn knowledge about spam from the continually received emails. And this accords with the realistic situation, because there is no or less emails that can reflect his or her personality to train when he or she begins to use email system. So there is no any training process for ASID in the following experiments.

In our comparison experiment between ASID and rule-based method, we found that rule-based method could achieve good performances only when the features of spam were very common, because it was lack of learning ability. So ASID achieved better performances than rule-based method. And Bayesian method, one of the most popular used anti-spam methods, was taken to compare with the proposed approach. The security level in the two approaches was set at the same level: middle.

## 4.2 Experiment 1: Comparison Between ASID and Bayesian Method

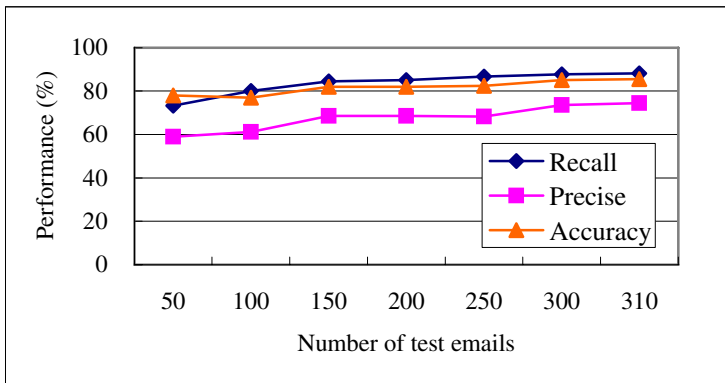
This experiment was performed with 750 emails where 519 were manually classified as legitimate and the rest 231 were assumed of spam. While 140 junk emails and 300 legitimate emails were chosen to be the training set for Bayesian method. And 66,480 non-spam words and 58,885 spam words were collected respectively after the training. Detectors were then tested against a collection of 219 legitimate emails and 91 junk emails. Table 2 shows the experimental results.

**Table 2.** The comparison results between ASID and Bayesian method

| Performance | ASID   | Bayesian method |
|-------------|--------|-----------------|
| Recall      | 88.17% | 77.42%          |
| Precision   | 74.41% | 82.15%          |
| Accuracy    | 85.48% | 88.06%          |

From table 2, we can find that the performances on precision and accuracy of Bayesian method are superior to those of ASID. It is reasonable because Bayesian filter learns lots of knowledge about junk and legitimate emails from training set. While ASID is lack of such pre-knowledge and the number of test emails in the experiment is not big enough. However, considering they are achieved without any training, it is inspiring to get the results whose differences are not so big.

With the increase of Antigen space, the knowledge learned from receiving emails is increased too. So the performances of ASID are improved gradually. This tendency can be found from figure 2. It can be anticipated that ASID will achieve better performances than Bayesian method with more test emails. And our later experiment verified this anticipation. When the test emails were increased to 450 (77 new junk emails and 63 new legitimate emails were added into the above test set), the performances of ASID on recall, precision and accuracy were 84.79%, 77.57% and 84.22%



**Fig. 2.** Performances of ASID

respectively, while the data of Bayesian method were 69.04%, 81.07% and 81.56%. Because more new junk emails were contained in the new added test emails, there was a little decrease on recall and accuracy of ASID compared with those in table 2.

During the experiment, we found that if the scale of training set used for Bayesian method was small, the performances were very bad. We also found those junk emails whose features were not contained in the scope of statistics escaped the filtering of Bayesian method. Conversely, such junk emails could be learned in the first immune response and be recognized quickly in the second immune response using ASID.

From the above experiments, we found another feature of ASID was that the number of detectors produced during immune circle was not so big. The reason is that innate immune response is introduced to deal with normal junk emails using traditional methods (e.g. list-based method and rule-based method). And adaptive immune response is used to cope with junk emails with various tricks.

### 4.3 Experiment 2: Distribution of Spam Vaccine in P2P Environment

In the simulated P2P environment, we firstly separated the test emails into 6 portions and use ASID to filter junk emails in the six peers respectively. Then we exchanged the test emails with each other and found that the exchanged emails could be classified correctly in other peers. And the idea of vaccine distribution is validated.

## 5 Conclusion

This paper presents a new model to fight against junk emails (especially Chinese junk emails) in P2P environment. Many filtering strategies are integrated in this model. And the implementations of immune principles are described in detail. The experimental results show that better self-adaptability is achieved. Using fewer detectors, it achieves similar or better performances to some other anti-spam methods. Therefore, it provides a new attractive solution to anti-spam problem.

Further research will be focused on an improved affinity function, ways to simplify detector and integrate other feature extraction methods, e.g. visual features [13].

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# NASC: A Novel Approach for Spam Classification

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**Abstract.** The technology of spam filters has recently received considerable attention as a powerful approach to Internet security management. The traditional spam filters almost adopted static measure, and filters need be updated and maintained frequently, so they can not adapt to dynamic spam. In order to get over the limitation of the traditional means, an immunity-based spam classification was proposed in this paper. A brief review about traditional technology of spam filter is given first, particularly, the Bayes probability model. Then the NASC is described in detail by introducing self, non-self, detector and detect algorithm. Finally, a simulation experiment was performed, and the important parameters of the model were analyzed. The experimental result shows that the new model increases the recall of filter greatly in condition that precision also increasing, and demonstrate that the model has the features of self-learning and self-adaptation.

## 1 Introduction

The effective development and full utilization of Internet have propelled the social and economic development, and have changed the means of people's work, life and communications. Following the enlarging of Internet scale and business, the amount of netizen is increasing rapidly. Among the services of Internet, the e-mail service is the mostly welcomed one with the most users. However, a few users domestic and abroad send enormous Unsolicited Commercial email (or UCE or "spam") that not only occupy network resources, but also affect normal communications, which makes the spam e-mail the serious international problem [1], [2], [3], [4].

By the late 1990s, spam had become a major problem for Internet Service Providers (ISPs) and businesses. ISPs and enterprises were forced to take steps to stop spam from overwhelming their email servers and flooding computer networks.

True anti-spam technologies, referred to below as second and third generation technologies [5], are a relatively new development that followed the advent of spam in the mid 1990s. Anti-spam technologies are entirely new and are sharply differentiated from basic MTA controls. In particular, Bayesian algorithms and more recent advances in text analysis are a radical departure from pre-existing mechanisms characterized or repurposed as anti-spam tools [5].

Although the anti-spam technologies have get rapid development, but most of these technologies adopt to static methods and they can not adapt to the change of spam.

Spam changes over time as new products become available or popular, but it also changes because the problem is co-evolutionary spammers adapt to filters, and filters adapt to spam.

The immune system model lends itself reasonably well to creation of adaptive system [5] and artificial immune systems (AIS) have been used for a diverse set of things including spam detection. AIS produced contains a unique set of detectors, making it harder for spam senders to create messages that will go through many such systems. It can detect not only repeat messages, but also materials that have not already been seen by the system. AIS has many of the advantages, and in addition it can use fairly complex heuristics as detectors, that should lead to more accurate matching.

The aim of this paper is to establish an immune-based model which called NASC for dynamic spam detection. The experimental results show it is a good solution for spam detection.

The rest of this paper is organized as follows. In Section 2, we review the technologies that have used to combat spam. In Section 3, a novel approach for spam classification was proposed and described in detail. Section 4 the simulations and experimental results are provided. The conclusions are given in Section 5.

## 2 Anti-spam Technologies

There are many solutions that can be used to combat the various types of email-based spam. Filtering messages, blocking message senders, ensuring senders are authentic, and Challenge/Response Systems are all methods used to combat spam. In this section, we briefly review the technologies that have used to combat spam.

### 2.1 Message Filtering

In general, implementing message filtering is straightforward and does not require any modifications to existing email protocols. A good filter design will minimize the number of false positives (filtering of a message that is not spam) and maximize the efficiency of the filter. Filters simply prevent spam from entering inboxes, but do not stop the generation of spam.

Message filtering often rely on humans to create detectors based on the spam they've received. Humans can create good heuristic detectors, but with spam senders intelligently adapting to anti-spam solutions, it is hard to keep up. A dedicated spam sender can use the frequently publicly available information about such heuristics and their weightings to evade detection [1], [3], [5].

### 2.2 Black List Sender Email Addresses

This is a simple spam blocking technique that is often used. Users create a black list of from addresses that should be prevented from entering the network and reaching the user's inbox. There are a few disadvantages with using this technique. Because spammers can create many false from email addresses, it is difficult to maintain a black list that is always updated with the correct emails to block. Also, some spammers do not even use a from address so a black list would not be able to catch these cases. Even a rule to block emails without a from address would not be sufficient because some legitimate emails,

such as newsletters to which a user may subscribe, may also not include a from address. Black list sender email addresses is effective in temporarily blocking a small amount of spam but ineffective as an overall anti-spam solution. As an alternative to black lists, some users set up an e-mail white list consisting of acceptable e-mail addresses or domains. Users only accept e-mail from users that are listed on their white list, while all other e-mail is blocked. However, it does not solve the problems associated when people who legitimately want to send you e-mail have not previously corresponded with you via e-mail, have multiple e-mail addresses, or have a new e-mail address.

### 2.3 Challenge/Response Systems

Challenge/response systems are used to counter spammers who use automated mailing programs to generate millions of spam emails per day. These systems are designed to slow down spammers by putting roadblocks up for the incoming spam.

Challenge/response systems work under the assumption that spammers using fake sender email addresses would never receive the challenge, and spammers using real email addresses would not be able to reply to all of the challenges. But Challenge/response systems also have a number of limitations [1], [2], [3], [4].

## 3 Immunity-Based Spam Classification Model

The aim of this paper is to establish an immune-based model which called NASC for dynamic spam detection. The model is composed of three parts: mail character presenting module (MCPM), training module and filtering module. MCPM use vector space Model (VSM) and present the received mail in discrete words. Training module generates various immature detectors from gene library. However, some of these new immature detectors are false detectors and they will be removed by the negative selection process [5], which matches them to the training mails. If the match strength between an immature detector and one of the training mails is over the pre-defined threshold, this new immature detector is consider as a false detector. Filtering module matches the received mails to the mature and detectors. If the match strength between a received mail and one of detectors, the mail will be consider as the spam.

### 3.1 Mail Character Presenting Module (MCPM)

Computer is not in possession of human being's intelligence and it only can recognize 0 and 1. So, the mails must be converted the form which computer can catch on at first, if we want to implement the spam filtering function by using computer. According to the Bayes-hypothesis, we can represent the document by means of keywords and index terms. The vector space model (VSM) has been widely used in the traditional information retrieval (IR) field [4], [6]. Most search engines also use similarity measures based on this model to rank Web documents. Documents are mapped into term vector space. A document is conceptually represented by a vector of keywords extracted from the document, with associated weights representing the importance of the keywords in the document and within the whole document. The form of the vector is listed below:

$$V = (t_1, w_1, t_2, w_2 \dots t_n, w_n) \quad (1)$$

Where,  $t_i$  represent keyword and  $w_i$  is the associated weights representing the importance of the keywords in the document.

MCPM contains two subsets: Chinese dividing module and keywords retrieving module. The task of Chinese dividing module is to separate the document into words and phrase. The algorithm used in dividing model proposed in this paper is maximum matching method [6], [7].

Once the Chinese dividing module has finished its job, the keywords retrieving model is to pick up suited keywords according to the weight of keywords and form the term vector space. The weight of a term in a document vector can be determined in many ways. A common approach uses the so called *tf x idf* method [6], in which the weight of a term is determined by two factors: how often the term  $j$  occurs in the document  $i$  (the term frequency  $tf_{i,j}$ ) and how often it occurs in the whole document collection (the document frequency  $df_j$ ). Precisely, the weight of a term  $j$  in document  $i$  is  $w_{i,j} = tf_{i,j} \times idf_j = tf_{i,j} \times \log N \div df_j$ , where  $N$  is the number of documents in the document collection and *idf* stands for the inverse document frequency. This method assigns high weights to terms that appear frequently in a small number of documents in the document set.

### 3.2 Training Module

**Define 1 Gene:** the keywords which are include in the uninteresting e-mail.

According to the document’s structure, the gene library is divided into two subsets: mail list gene library and content gene library. Mail list gene library consists of suspicious email addresses or domains which are issued by the authoritative institution. User can update the library not only by the internet but also by adding the unacceptable email addresses by himself. Content gene library consists of keywords which are picked up from spasm. The initial genes of content gene library used in this paper are all from China anti-spam alliance. We can also update content gene library by making use of filtering module after the system works.

**Define 2 Immature Detector:** the term vector which is organized in pre-defined structure <sender mail address, subject, keyword1,keyword2...keywordn> and every elements of the term vector are all from gene library.

**Define 3 Affinity:** the match strength between two documents, when documents are mapped into term vector spaces, common similarity measure, known as the cosine measure, determines the angle between the document vectors and the query vector when they are represented in a n-dimensional Euclidean space, where n is the vocabulary size. Precisely, the similarity between a document  $D1$  and a query  $D2$  is defined as

$$Sim(D_1, D_2) = \frac{\sum_{k=1}^n w_{1k} \times w_{2k}}{\sqrt{\left( \sum_{k=1}^n w_{1k}^2 \right) \left( \sum_{k=1}^n w_{2k}^2 \right)}} \tag{2}$$

Where  $w_{2j}$  is the weight of term  $j$  in the query, and is defined in a similar way as  $w_{ij}$ . The denominator in this equation, called the normalization factor, discards the effect of document lengths on document scores.

If the match strength between an immature detector and one of the training mails is below the pre-defined threshold, the detector is considered as a mature detector. The matching function  $f\_aff$  is defined below:

$$f\_aff(D_1, D_2) = \begin{cases} 1, & \text{iff } (sim(D_1, D_2)) \geq \delta \\ 0, & \text{other} \end{cases} \quad (3)$$

Where  $\delta$  is the pre-defined threshold.

**Define 4 Mature Detector:** the detectors whose affinity between nonself is over the pre-defined threshold. The structure of detector is list below:

$$MC = \langle \text{term vectors, count, age} \rangle. \quad (4)$$

Where count represents the detected spam number, and age is the survival period and the initial value of age is 0.

During the training stage, the goal is to populate the gene libraries, produce an initial set of immature cells from training examples. The training module generates immature detectors by choosing random sections from gene library. Negative selection [5] is used to pre-censor the generated immature detectors against training example. This guarantees that false-positive errors [5] do not occur against a self as any detector matching self is removed before fielding. An overview of this algorithm is described by the Pseudocode list below

```

program Train (var l, m:integer)
 begin
 repeat
 generate l immature detectors
 foreach(detectors ∈ the set of generated immature
 detectors)
 compute the affinity between detector and self
 if the affinity of a detector is over threshold
 remove the detector
 else
 add the detector to the set of mature detectors
 end foreach
 until the number of the mature detectors is over m
 end.

```

### 3.3 Filtering Module

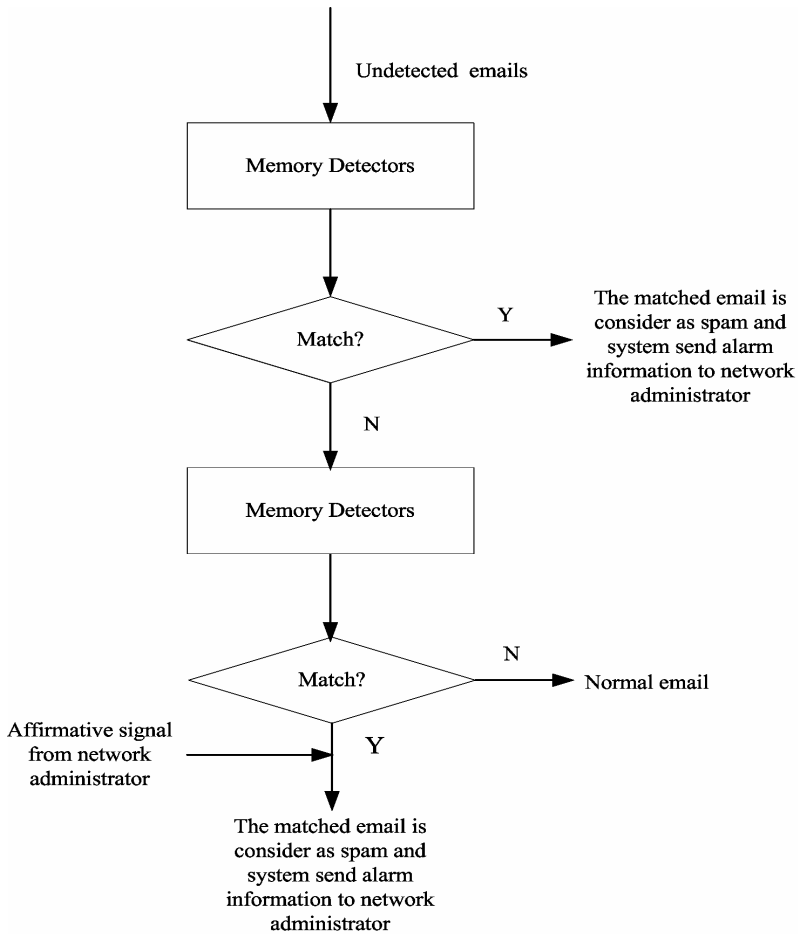
**Define 5 Memory Detector:** the detector which is considered as reliable detector. A mature can become a memory detector if the matching threshold is over active threshold. The structure of memory detector is list below:

$$MMC = \langle \text{term vectors, time, count} \rangle \quad (5)$$

Where count represent the detected spam number, and time indicate the time when the detector detect the spam and this parameter is used in the memory detector update procedure.

**Define 6 Co-stimulation:** the signal which comes from administrator to system. This signal is used in the following two situations:

1. When mature detectors detect a suspicious mail, system need this signal to judge the suspicious mail whether is junk.
2. When the count field of one mature detector is over active threshold, system will need the co-stimulation signal. If an affirmative co-stimulation signal writes back to system from network administrator in fixed period, this mature detector will become memory detector. Otherwise, it will be recognized as invalid detector and deleted from mature detector set.



**Fig. 1.** The system working flow of filtering model

As the Fig.1 shows, the undetected e-mails are compared with memory detectors firstly. If one e-mail match any elements of memory detector set, this e-mail is classified as spam and send alarming information to user. In NASC, E-mail classified as junk is not deleted but removed to a temporary store. Mature Detectors must have become stimulated to classify an e-mail as junk, and therefore it is assumed the first stimulatory signal has already occurred. Feedback from administrator is then interpreted to provide a co-stimulation signal. If an e-mail is simply deleted from this store we assume the algorithm has performed a correct classification as the user really was not interested in that e-mail and so a co-stimulation signal has occurred. The cell is rewarded by being allowed to reproduce. If, on the other hand, the user does not delete the e-mail the algorithm has performed a misclassification, signal two does not occur and mature detector or memory detector is removed appropriately.

To both counteract the increase in population size brought about by reproduction and keep the algorithm dynamic, all detectors in the model are all given an expiry date. Expiry allows the system to remove old detectors that have never matched any messages so that they do not waste processing time of the system. In addition, this expiry is what allows the system to forget detectors that are no longer in active use. Once old detectors have been removed, new detectors can be generated to replace them, starting the cycle again.

## 4 Simulations and Experimental Results

### 4.1 The Evaluation Method of the Model

The essence of spam classification is a special text classification. So the evaluation standard of spam classification is same to text classification's, we can use recall ratio and precision ratio to evaluate the performance of the model [6], [7].

### 4.2 Experimental Environment and Procedure

The experiment has been carried out in the Laboratory of Computer Network and Information Security at Sichuan University. The whole experiment is divided into two phase: training phase and application phase. The different between the training phase and application phase is that training phase does not use filtering module. At the beginning of the system working, the set of detectors is empty. Experiments were performed with 2000 e-mails of which 750 were manually classified as spam, the remaining 1250 were assumed of normal email. We partition these 2000 emails into 10 equal parts and choose one part randomly as a training example, then the remain parts are used for test and we can get 9 group recall and precision ratios. The average value of these 9 group values is considered as the model's recall and precision ratio.

### 4.3 Experimental Result and Result Analysis

There are several important parameters in the model such as initial detectors scale  $M$ , active threshold  $\delta$ , matching threshold  $\beta$ , mature detector life cycle  $\lambda$  and the vector's

dimension  $k$ . In order to evaluate every parameter’s impact on model’s performance, we have carried out 9 group experiments. The experimental result and result analysis are described below:

**Table 1.** The effect on the experimental Result by modifying the parameter

| $M$ | $\delta$ | $\beta$ | $A$ | $k$ | recall (%) | precision (%) |
|-----|----------|---------|-----|-----|------------|---------------|
| 50  | 10       | 0.5     | 120 | 10  | 77.65      | 84.8          |
| 100 | 10       | 0.5     | 120 | 10  | 79.46      | 85.9          |
| 150 | 10       | 0.5     | 120 | 10  | 78.54      | 85.7          |
| 100 | 5        | 0.5     | 120 | 10  | 83.98      | 85.11         |
| 100 | 10       | 0.5     | 120 | 10  | 79.46      | 85.9          |
| 100 | 15       | 0.5     | 120 | 10  | 56.96      | 87.2          |
| 100 | 10       | 0.3     | 120 | 10  | 84.62      | 82.3          |
| 100 | 10       | 0.5     | 120 | 10  | 78.54      | 85.7          |
| 100 | 10       | 0.8     | 120 | 10  | 63.47      | 86.1          |
| 100 | 10       | 0.5     | 60  | 10  | 74.63      | 84.8          |
| 100 | 10       | 0.5     | 120 | 10  | 79.46      | 85.7          |
| 100 | 10       | 0.5     | 360 | 10  | 82.39      | 85.3          |
| 100 | 10       | 0.5     | 120 | 5   | 78.14      | 85.11         |
| 100 | 10       | 0.5     | 120 | 15  | 75.86      | 86.6          |
| 100 | 10       | 0.5     | 120 | 20  | 60.68      | 87.9          |

The effect of initial detectors scale  $M$ : As the table 1 shown, with the increasing of  $M$ , the recall and precision rises rapidly at beginning, but the recall and precision all hold the line when system has worked for a time whatever the change of the value of  $M$ . This is because  $M$  controls the scale of the detectors. There are more detectors if  $M$  increases, so the recall and precision also increase. But after the system running for some time, the recall and precision change little because the match algorithm adopt to imprecise match and the detectors of low  $M$  model also can recognize familiar spam. So the initial detectors scale is not decisive factor to the model’s performance. But the value of  $M$  should not be too low.

The effect of active threshold  $\delta$ : According to table 1, the recall is in positive proportion to  $\delta$ . There are more memory detectors if  $\delta$  is low and model can detect more spasm. Otherwise, cause of the mature detectors has expiry date, many mature detectors has been invalid before it become memory detectors and model can not afford to enough detectors to detect spasm, So the recall is decline. We can also get a conclusion from table 1 that  $\delta$  has little affection on the precision.

The effect of life cycle  $\lambda$ : The life time of mature detectors is more long, the number of the mature detectors is more big and the number of the memory detectors also more big. So the recall increase with the increasing  $\lambda$ . As the table 1 shown,  $\lambda$  has no impaction on precision.



The effect of match threshold  $\beta$ : As table 1 shown, the  $\beta$  is more high, the recall is more high and the precision is more low. This is because system can correctly detect really spam in strict match condition, but due to the strict match condition, some of spam can not be detected by model and the precision decreases.

The effect of the vector's dimension  $k$ : According to table 1, with the increasing of  $k$ , the recall can increase gradually and it will reach max when  $k=15$ , then it will decrease gradually. This is because the dimension is low and vector space can not stand for document, but if dimension is high, it will introduce classification noises.

Experiment was repeated 10 times when turning the parameters. A satisfied result (recall=75.84% ,precision=85.7%) is obtain with  $M = 100$ ,  $\delta = 10$ ,  $\beta = 0.5$ ,  $\lambda=120$ ,  $k=15$ . In the same condition, the recall and precision of Bayes method [9], [10] are 67.76% and 83.98%. This is immune method can adapt to dynamic spam and has the features of self-learning and self-adaptation.

## 5 Conclusion

The previous models or methods almost adopted static measure, and filters need be updated and maintained frequently, so they can not adapt to dynamic spam and lack of self-adaptation.

In this paper, an immune-based dynamic model called NASC for spam detection has been built. The experiment shows that this model can efficiently raise both the recall ratio and precision ratio, and enhance the ability of self-adaptation and diversity for the spam.

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# Prediction Algorithms in Large Scale VOD Network Collaborations

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**Abstract.** VOD (Video on Demand) is one of significant services for next generation networks. VOD networks mean local networks to provide VOD services to communities in a scale about 500 to 1000 users simultaneously. Many VOD networks could cooperate through external networks link internet. The cooperation requires not only huge local bandwidth but great backbone bandwidth. This paper presents prediction algorithms to reduce the cost in external communications which is very important for VOD operators. Basic algorithms can reduce overall costs about 30% and well trained ANN can provide extra 10% performance.

## 1 Introduction

VOD systems have been implemented in market for nearly ten years. In early years, it started from KTV discs based system, which was operated by a PC to provide single video clip through local Ethernet networks. Video clips were compressed in RM or MPEG1 standards with a CIF resolution, the quality was very close to VCD. The services could be delivered to tens of customers if there were enough PCs available. The second generation VOD services were implemented in hotels for customers to enjoy personal TV programs. Some of them were provided in 2M TS stream with MPEG2 standards similar to DVD quality. Single service cost 2Mbps bandwidth and it was difficult to provide the service out of the hotel. Now, VOD systems enter the third generation, which targets provide VOD services to everyone through local networks. And the rapid popularizing is expected when IPTV and HDTV enter families. From now on, VOD not only is an engineering term, but raises some academic interests. How to provide good service with current infrastructure is very important to promote VOD services in market.

It is very clear that for each local area, and local networks, to provide VOD, a server or a server group is required and it transfer video clips from storage to customers. There are lots works done on the single VOD networks[1][2][3][4][5].

Most of them concentrated on the efficiency of local server group or local bandwidth and tried to reduce the latency for a single requirement. Now VOD system can be implemented in community scale and it is not difficult and not expensive to run a VOD system to serve 1,000 users simultaneously. Recent works concern more on mobile devices and large scale VOD problems [6][7][8][9].

Single VOD networks, especially ones serve local communities can not be equipped with all video clips available to deliver and customers always want more to watch and most of video clips not available in where they get the services. In these cases, VOD networks can seek to cooperate to provide more programs and because there are many video clips transferred through internet, it costs great internet bandwidth and even backbone bandwidth. Bandwidth consuming is core problem for VOD operators to consider, and if there is no good methods to reduce the costs, operators can hardly tend to cooperative mode. Another problem is to build a complete new video warehouse; served clips should be in good format like MP4 or H.264, where input video should be in different format as DVD, VCD, or even VHS. For huge transcending works, it is better to distribute works on many local VOD systems and share all clips through internet.

For collaborations, there are two kinds of basic sharing strategies. The first is all sharing are not cached and each customer can require video clips from external accessing. Obviously, it costs bandwidth a lot and it avoids any problems invoked by copying from one networks to another. The second methods assume two or more networks belong to the same group and there is nothing wrong to cache programs from one. For any single requirement, it makes a copy of required video clip and transfers it to customers locally. This method avoids some unnecessary transferring but gets another kind of unnecessary transferring when the user just wants to skim those clips. In most cases, it is difficult to say which method is better.

This paper presents a few prediction algorithms for VOD networks to cooperate and it also presents predicting methods based on the working mode. With prediction, systems could know if the transferring is necessary or in which cases it is necessary. The prediction also could show the probabilities for each transferred copy to be used in short future, which is very important for server groups to optimize the performance of whole system. Following sections will presents cooperative architecture of VOD, predicting approaches, and cooperative training to improve prediction result. At the end of this paper, some simulation results will be presented to indicate the performance of prediction.

## 2 Cooperative VOD Networks Architecture

For a single VOD networks, it works in following way:

The video clips are stored in a SAN or similar device. A server or server group get clips from storage and transferred to terminal devices. In the testbed for this paper, the video clips follow H.264 and enhanced AAC+ standard, packed into TS stream format, which can be implemented in general broadcasting devices. For video stream with a resolution of 640 by 360 at 30 FPS, it can provide a DVD quality video with 512Kbps bandwidth. In this case, the overall performance is much better than most of VOD systems.

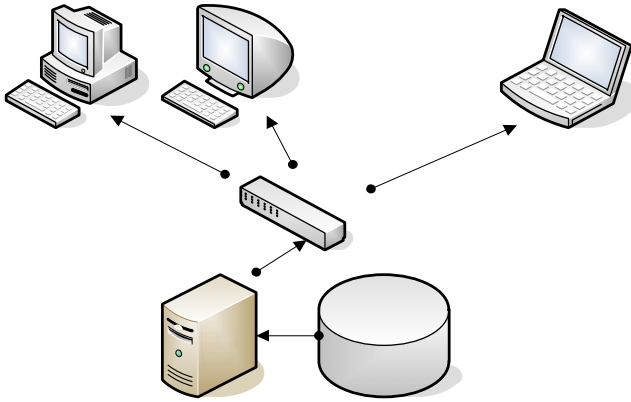


Fig. 1. VOD networks

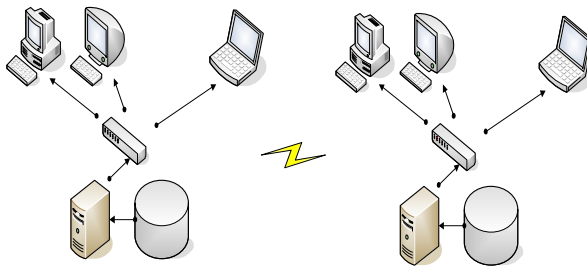


Fig. 2. Cooperative VOD networks

Commonly, two VOD networks are connected through internet, and for special reason, they can be connected through a dedicated cable. For the first case, the internet bandwidth is also shared by other purposes and costs considerable expensive. This is why to optimize cooperative methods for VOD networks.

The testbed for this paper can serve about 500 VOD request simultaneously. The main obstacle to serve more customers is the effective local bandwidth and server groups output capability. Assuming there are about 2,000 users in a communities use this kind of VOD services, 3% programs are not available in local VOD networks, each programs lasts about half an hour, getting all clips from external system needs about 54G bits each day. For some new and hot programs, the costs can be great. The person in Charge of those services can manage it in this way: for some clips they think hot and popular, get them from external and serve them locally, and this solution leads to the prediction methods described in following section.

In most cases, two VOD networks work in four modes as following:

- Mirror mode, one networks works as another one's mirror, when there are any new clips available in main networks, mirror can pull it to local storage;
- Peer to peer mode, two networks work independently, they will exchange clips only when users require, when transcoding works are distributed in VOD

networks, this mode can be basic mode;

- Two networks are managed by a system, which manage all clips like distributed storage; this mode involves different sharing strategies.

In this paper, first two kinds of modes are discussed and prediction algorithms are implemented in systems to reduce external bandwidth consuming.

### 3 Prediction Algorithms for VOD Networks

It is not difficult for human to decide which clip is hot or not, but it is not easy for computer system to know about it. A clip is required by a user, maybe in different conditions:

- User want to watch it from beginning to end
- User want to know about the story of it, he will skip most of details
- User want to know if he had watched or not
- User want to know if there is any player he likes
- User want to continue watching from last time position
- User make a mistake to click on it
- .....

Generally, different conditions show different signal to system, and system could analyze what the original intention of the user.

If each user's intention is clear, system could get an overall trends for users to a video clips. Operators can provide preview clips and detailed information for each clip to help users to find what to watch and how to watch. It is very important for systems to know well about users' intentions.

For each video program, there are also many conditions different from each other:

- New video program never being required
- New video program required many times
- Old video program required many time recently
- Old video program required many time, but last requirement was made a year ago
- Old video program seldom being required, but until now there still some requirements made for it
- .....

Generally, system could make a rank list for each video program to be evaluated, if the rank higher than a threshold, it could be a hot program and of course, for any external requirement, it is better to get the full video and put it in local storage.

The statistics of video requirements and user access log can help external visitor know about the programs and ranked list can help it decide what to do next. For prediction methods is to find what will happen next, especially for video program without a clear future. And all the predictions are based on statistics and rules produced by the system.

In a VOD network, for a user's single requirement, assume  $A$  represents all operations for this requirement, each  $A_i$  represents a single operation and its timestamp like watching from position a to position b. Then a user operation model  $U(A)$  can be implemented to decide the type of this requirement.

For a video program,  $R$  represents all requirements since it put into the storage.  $R_i$  represents a single requirement for this video program. Then a video program usage model  $V(R, U(R_1), \dots, U(R_n))$  can be implemented to decide the type of this video program.

When  $U(A)$  and  $V(R, U(R_1), \dots, U(R_n))$  are available, a prediction can be made through  $P(V(R, U(R_0), \dots, U(R_n), U_p))$ , where  $U_p$  means current requirement type.

The main problem for the prediction is model is not easy to build, for different user group, user models is much different from each other. A young people model can not be used on old people. Another problem is how to estimate time factor in the models. Time factors will vary from different. Two basic factors can not be ignored: one is strategy of operator, and another one is internet tariff standard, both of them can affect models above greatly. If tariff is higher enough, the cooperative transferring can be ignored. If the system can provide detailed introduction, the users can decide if to require the program before send requirement. Any way, it is possible to estimate user behavior and program accessing pattern, which lead to a prediction to show how much probabilities this program can be required by other users in a short time.

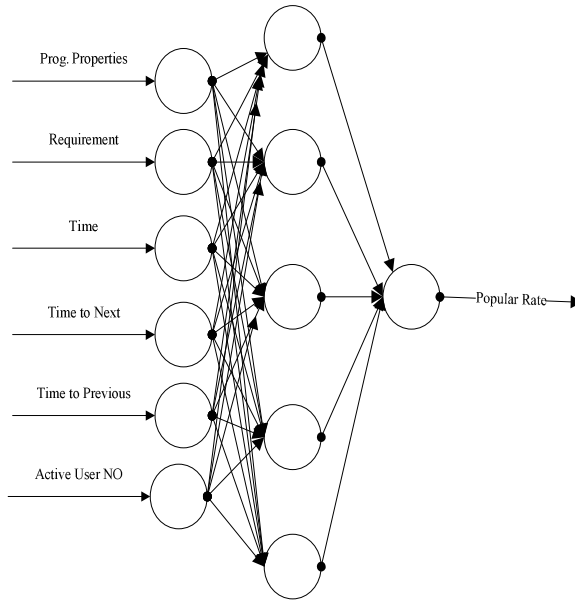
For stochastic estimation, it is not easy to tell how close from a model to reality, but the estimation should be limited with a border, not to introduce too many errors to later prediction.

An ANN was implemented to estimate video program model as figure 3. The input is video program properties and a single requirement, with parameters as time, operation, duration, time to previous requirement and time to next requirement. The ANN is trained with real data from system and could output a popular rate.

For a few cooperative VOD networks, it is not difficult to evaluate a program's popular rate in each network. Overall result can be used to calculate the related probabilities.

There are three prediction models for program popular rate compared in the test-bed. The first one is simple fuzzy logic model. Preset the rules and formulas to calculate the probabilities. For example, rules can be in this way:

- If the same type of program is hot, this program with a middle above popular rate, the probability is high
- If the program is new and the type is popular and the topic is OK, the probability is middle
- If the program is old, and recent usage is not bad, the probability is middle
- .....



**Fig. 3.** ANN to produce program model

The performance of this prediction depends on the rules very much. For different system, rules should be adjusted to adapt new system, boring and low efficient.

The second prediction method is by Monte-Carlo methods and Bayesian methods. The main problem is the observed result is not probabilities what the prediction produced. In this case, another parameter was used to evaluate usage of supposed to be transferred video programs, the time span to next requirement in local networks. The prediction algorithm needs to use requirement recodes in required networks to estimate the time span and it is very difficult to make a right estimation for new programs while there are not enough data to be used in perdition.

The third method is ANN. ANN methods can also be implemented in predicting the time span.

ANN performance bases on the number of samples. For a small network, it is difficult to get a converged ANN for general usage.

It is recommended to combine different methods at same time to achieve better performance.

User behaviors should be also predicted based on the user profiles and user operation. The basic ideas are the same with program popular rate predictions. And the affective issues are more than popular rate predictions. For instance, the time of a requirement affects not only the number of simultaneous requirements, but also accessing patterns of users. And a user's accessing operations are in his own pattern should be analyzed individually.



Two VOD networks cooperate is not enough to provide highly cooperative environment. For more than three networks, sharing their model and prediction ANN will be also very efficient to improve the overall performance.

### 4 Experimental Results and Explanation

It is still difficult for our testbed to simulate a real VOD system provides 500 programs simultaneously. So a simulation program developed to evaluate the performance of prediction algorithms.

The simulation was set in following way:

- Video clips are compressed with H.264 and Enhance AAC+, resolution 640 by 360, 30 fps, stereo audio, packed in TS stream, 512Kbps  
Storage is an 30T raid5 SAN, connected with Fiber Channel Card to VOD server
- VOD server is about 32 CPU and 64GB RAM, maximal capability to serve 1,000 users simultaneously
- Local connection is 1000M Ethernet to desktop
- Users are classified into six group, by age and sex
- Video program are classified into ten type, some subtypes are stressed like cartoons and hot movies

Figure 4 compare external bandwidth usage for three strategies. Here, prediction strategy is combination of fuzzy logic and ANN.

The data in Figure 4 stresses more hot programs to share and the share rate is about 3%.

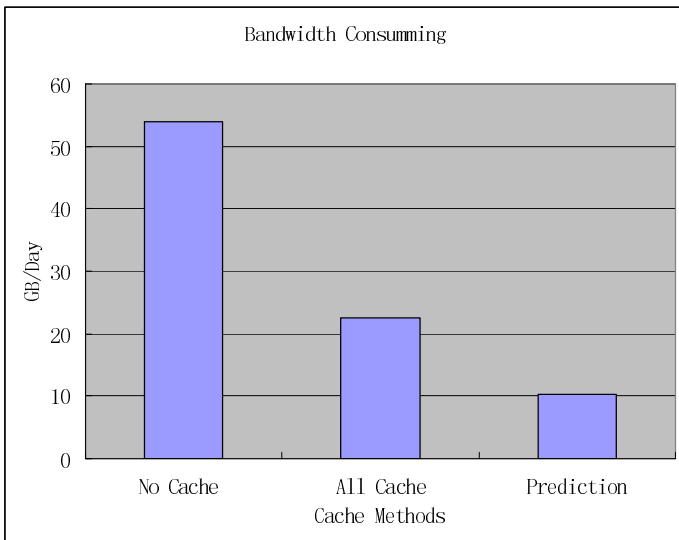
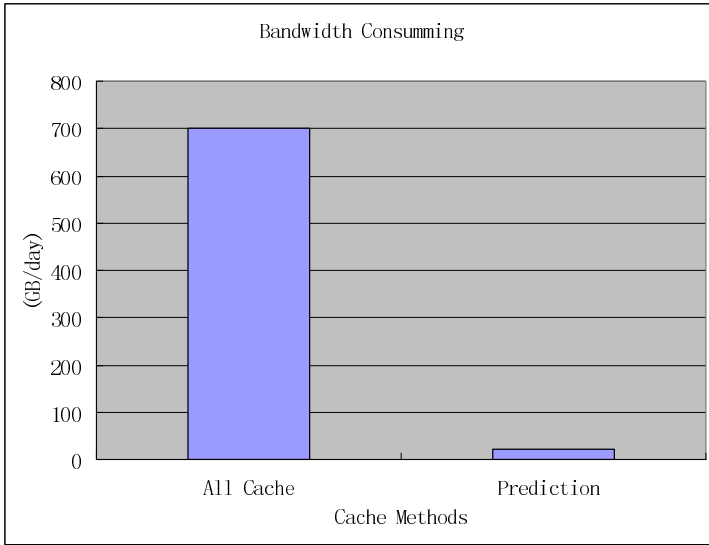
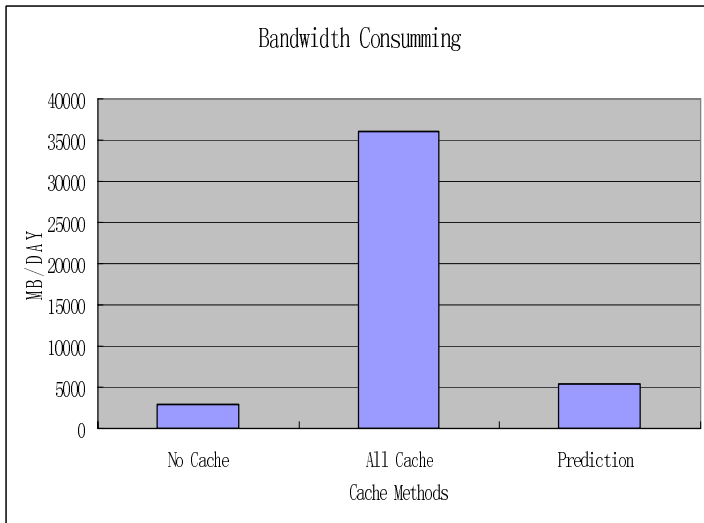


Fig. 4. External bandwidth consuming



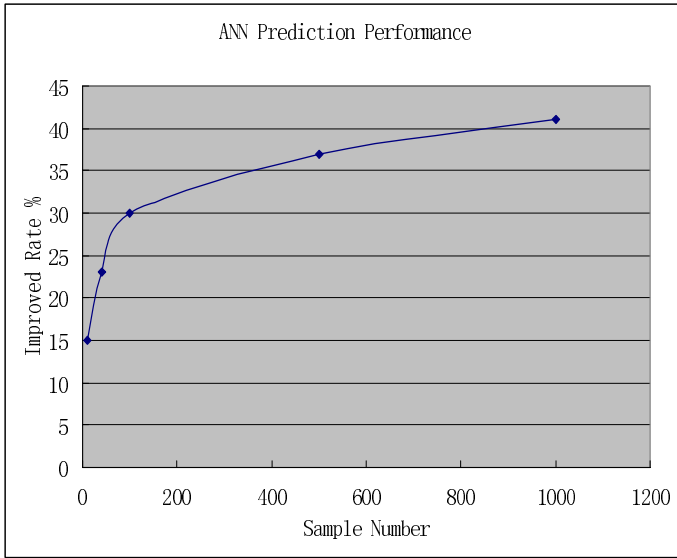
**Fig. 5.** External bandwidth consuming for mirror mode



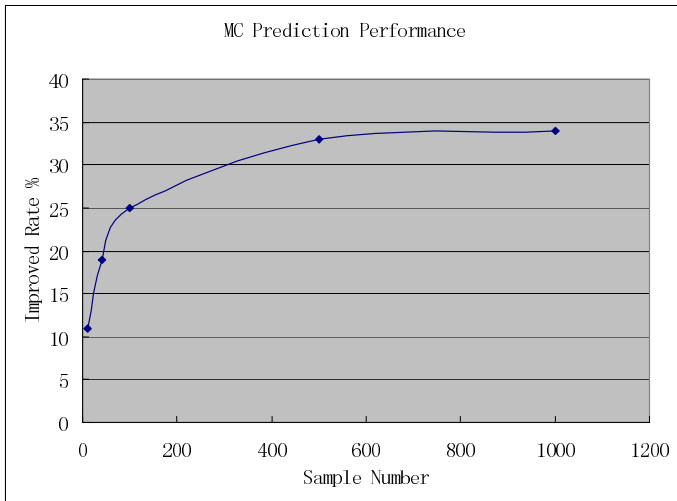
**Fig. 6.** Flowing bytes of external networks

Figure 5 shows in mirror mode, the performance of the prediction methods.

In a short time the prediction methods allow only very popular programs to be transferred, in the experiment, it ranged from 3% to 5%. There may be some in future, about 10% to 15% to be transferred. For a huge program warehouse, most of them are ignored by most of users.



**Fig. 7.** Trained ANN prediction performance



**Fig. 8.** Monte-Carlo prediction performance

For some requirements just to watch no more than 10 minutes. Figure 7 shows the external bandwidth consuming in a simulation process.

The performance is very bad when the system caches all things to play. In this case, prediction can reduce the transferring costs by user model.

It is not difficult to find, prediction methods can help VOD networks to reduce costs invoked in cooperative works. The question is what the extent and where is the limitation.

Figure 7 shows the performance curve for ANN prediction trained to achieve better performance. It was improved with extra fuzzy based rules and it can be improved with more training samples and more rules.

ANN can be trained to close the reality, but it can't get too close. It affected the performance of prediction algorithms. Before a good model to describe prediction and user behaviors in VOD area, ANN could be used for a good balance system performance.

Figure 8 shows Monte-Carlo prediction performance. Fixed PDFs were implemented in these experiments. Because the PDFs is preset and can't describe system very well, the performance is a bit poor compared to ANN results.

## 5 Conclusion and Future Work

Some starting works in prediction algorithm for VOD networks to cooperative presented in this paper. A testbed to VOD service and VOD networks to cooperate is build. During the development of VOD system, we found it very important to do some preparation for future cooperative works. Multi VOD networks and even other kinds of video providers can work together to serve better and save resources.

For VOD networks cooperation, cooperative learning and remote learning will be our future work to do. We also hope to push these research works to other area.

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# A Computational Korean Lexical Access Model Using Artificial Neural Network\*

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**Abstract.** In this paper, we propose a computational Korean lexical access model based on connectionist approach. The model is designed to simulate the behaviors observed in human lexical decision task. The proposed model adopts a simple recurrent neural network architecture which takes a Korean string of 2-syllable length as an input and makes an output as a semantic vector representing semantic of the input. As experimental results, the model shows similar behaviors of human lexical decision task such as frequency effect, lexical status effect, word similarity effect, semantic priming effect, and visual degradation effect.

## 1 Introduction

Researches on the process of mental lexicon access and the representation of mental lexicon are very important to find out the internal mechanism of lexical processing in human brain. In order to measure the processes that are involved in mental lexical access, we need a task that guarantees that a lexical entry is accessed. A naming task, stroop task, and lexical decision task(henceforth **LDT**) are frequently used in the study of lexical access. Among them, LDT is a most frequently adopted methods. The LDT has been proven to be a fruitful method for exploring the nature of the mental lexicon. In LDT, subjects are asked to discriminate words from nonwords by pressing YES or NO button if the stimulus is a word or a nonword.

There are several basic findings that are consistently obtained using the visual LDT and these findings are observed independently on languages. The major

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findings are frequency effect, lexical status effect, word similarity effect, semantic priming effect, and visual degradation effect. Many researchers agree with that a persuasive lexical access model must be able to explain the major effects.

Many different lexical access models have been proposed to explain internal mechanism involved in mental lexical process in human brain. The proposed models are such as the search model[2], the logogen model[6], the interactive-activation model[5] and the verification model[1]. These models successfully account for most findings but for exceptional effects. However, as all of the models are theoretical models, it is very hard to perform computational experiments and simulations without human subjects.

Computational experiments and simulations are very helpful to elaborate or to make the model complete by handling experimental environment. In addition, computational model may suggest fruitful areas for experimentalists to investigate. Also, partial lesions of neurological areas and pathways can be modeled in a straightforward if connectionist modeling is used. The intensional lesion study using the connectionist computational model is never possible with human subjects.

In spite of the advantages of computational model in the study of cognitive neuro psychology, researches on developing computational mental lexicon model have been rarely tried[3], [7]. Furthermore, all the previous works have been focused on the models of English and researches on developing computational Korean mental lexicon have been never performed except for the symbolic computational model of [4].

Lim and Nam propose a computational model for Korean mental lexicon which simulate length effect and frequency effect using FB-trie[4]. FB-trie is a modified trie data structure to enable more frequent words are accessed faster by visiting minimal elements and nodes. Lim and Nam aimed to model language ability or proficiency with the size of training corpus. Correlations of frequency of Trie1 and Trie2 are very small while those of FB-trie1 and FB-trie2 are relatively large and very similar to those of human recognition. The reason of high correlations of length of Trie1 and Trie2 is due to an inherent characteristic of the trie indexing structure requiring more time for retrieving a longer string. The experiment results were very promising in that correlations of frequency and length with human reaction times are higher with the larger training corpus than with the smaller. But, the proposed model tried to simulate only length effect and frequency effect. It did not show the extendability to simulate other language phenomena.

In this paper, we propose a computational Korean lexical access model which can simulate major language phenomena in LDT by using connectionist approach. The organization of this paper is as follows: We briefly introduce the major language phenomena which our model must be able to explain to be a persuasive lexical access model. We will describe input/output pairs which is used to train Korean lexical access model, the network architecture, training procedure. Then, we will show some experimental results whether the proposed model can account for the basic findings aimed to mimic. Finally, we will present some conclusion and future works.

## 2 Major Language Phenomena in LDT

There are several basic findings that are consistently obtained using the visual lexical decision task[8]. Among them, the major findings are frequency effect, lexical status effect, word similarity effect, semantic priming effect, and visual degradation effect. These effects must be explained by any model which purports to be an account of lexical access.

**Frequency effect.** The time taken to make a lexical decision response to a highly frequently word is less than that to a word of low frequency. For example, subjects will recognize the common word HOUSE more quickly than the rarer word ROUSE.

**Lexical status effect.** The time taken required to classify a letter string as a nonword is longer than a word. For example, it takes longer for the subjects to categorize the word BLINK into word than the word FLINK into nonword.

**Word similarity effect.** When a letter string which is sufficiently similar to a word, it is hard to classify as a nonword

**Semantic priming effect.** When a word is preceded by a semantically related word, it becomes easier to classify as a word. For example a nonword like TRIAN, which is a word with two letters transposed, is associated with longer response times and a higher error rate than a nonword like TRUAN which is not generated from a word in this way.

**visual degradation effect.** When a letter string is visually degraded, it becomes more difficult to classify as a word or nonword

## 3 Overview of the Model

The proposed model adopts a simple recurrent neural network architecture which takes a Korean string of 2-syllable length as an input and makes an output as a semantic vector representing semantic of the input. The model consists of three layers: input layer, hidden layer, and output layer. The input layer consists of input units which represents orthography and context units which represent the history of the early activations of hidden units. When the network makes the output, it is regarded that the network make a lexical decision over the input data. But, as the time to spend in making an output in the network is always identical for every input data, response time to an input is calculated indirectly by using the error rate of the output.

Developing the model involves making four sets of design decisions that apply to the development of connectionist model. The following four sections describe the characteristics of the model, which are the main sections of this paper.

**Input/Output Design.** What input/out pairs is the network trained on to deal with Korean?

**The Network Architecture.** What type of units is used, how are the units organized into groups, and in what manner are the groups connected?



| First Consonants(19) |                      |
|----------------------|----------------------|
| ㄱ                    | 10000000000000000000 |
| ㅋ                    | 01000000000000000000 |
| ㆁ                    | 00100000000000000000 |
| :                    | :                    |
| ㅈ                    | 00000000000000000010 |
| ㅊ                    | 00000000000000000001 |

| Middle Vowels(21) |                        |
|-------------------|------------------------|
| ㅏ                 | 1000000000000000000000 |
| ㅑ                 | 0100000000000000000000 |
| ㅓ                 | 0010000000000000000000 |
| :                 | :                      |
| ㅕ                 | 0000000000000000000010 |
| ㅗ                 | 0000000000000000000001 |

| Last Consonants(27) |                            |
|---------------------|----------------------------|
| ㄴ                   | 10000000000000000000000000 |
| ㄷ                   | 01000000000000000000000000 |
| ㄹ                   | 00100000000000000000000000 |
| :                   | :                          |
| ㅌ                   | 00000000000000000000000010 |
| ㅍ                   | 00000000000000000000000001 |

Fig. 1. Representation of Orthography

**The Training Procedure.** How are examples presented to the network, what procedure is used to adjust the weights to accomplish the task, and what is the criterion for halting training?

**Evaluation of the Model.** How is performance of the network evaluated- specifically, how is time of lexical decision task measured in the network? What are the experimental results?

### 4 Input/Output Design

Some representation methods of English orthography have been proposed such as in [5], [3], and [7]. But, as Korean is very different from English, such representation methods can not be used in representation of Korean orthography. We propose a method for representing Korean orthography for connectionist models. A typical form of a Korean syllable is CVC(first Consonant-middle Vowel-last Consonant) or CV(first Consonant-middle Vowel). The number of the first consonant and the last consonant are 19 and 27 respectively. The number of vowel is 21. We may represent a Korean syllable with 15 bits: 5 bits are used to represent each consonant and vowel. But, with this scheme, two different syllables can be represented with the very similar bit stream. This may be problematic in visual LDT experiment. Thus, we propose a orthogonal representation in which different consonants or vowels are represented with different bit streams.

The proposed orthography, a Korean syllable is represented as a 67-bit vector; 19 bits are used to represent first consonant, 21 bits for middle vowel, and 21 bits for last consonant. Every possible Korean syllable can be represented with this representation scheme. Figure 1 shows some example of vector representation of Korean syllables.

We represent the semantics of the input words in terms of 210 pseudo semantic features. The assignment of semantic features to words has the property that words in the same category tend to be more similar than words in different categories. The number of the semantic categories is seven and thirty words are assigned to each category.

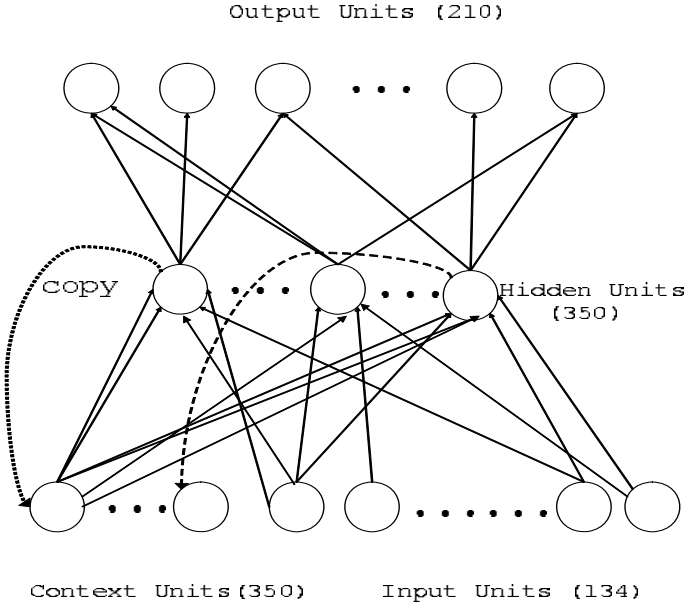


Fig. 2. The Network Architecture

## 5 The Network Architecture

Figure 2 depicts the network architecture of the proposed model. The network is a simple recurrent network which contains connections from the hidden units to a set of context units. The network consists of three layers: input layer, hidden layer, and output layer. The input layer includes 134 input units (grapheme units), and 350 context units. The 134 grapheme units and context units are fully connected to a group of 350 hidden units. The hidden units are also fully connected to 210 output units and context units.

Each unit except context unit has a real-valued activity level ranging between 0 and 1, computed by a smooth nonlinear function of the summed input received from other units. The activities of the context units are 0s or direct copies of the hidden unit activities on the previous time step whether the experimental task is priming task or not. If the task is not priming task, all of context units are set to 0s. If the task is priming task such as semantic priming task, the units are set by copying from hidden units.

## 6 Training and Evaluation of the Model

The network was initialized to have small random weights, so that at the beginning of training the pattern of semantic activity produced by the word was quite different from its correct semantics. A modified version of backpropagation algorithm was used to compute the way the each weight in the network should change so as to reduce this difference. The error of output unit was calculated by sum of cross entropy of each output unit. Response time in lexical decision time was measured in terms of semantic stress measure which was used in [7]. More formally, the semantic stress  $S_j$  of  $unit_j$  is a measure of the information content (entropy) of its activation  $a_j$ , corresponding to the degree to which it differs from the "neutral" output of 0.5. The higher value of semantic stresses means that the network makes more correct semantic output pattern. If the network makes higher average value of semantic stresses of all output nodes in a fixed time, the network is taken to respond more quickly on the input data.

## 7 Experimental Results

Figure 3-figure 7 show our experimental results. In the figures, x-axis and y-axis represent the number of training iterations and value of the semantic stress respectively. These figures show differences of semantic stress between two sets

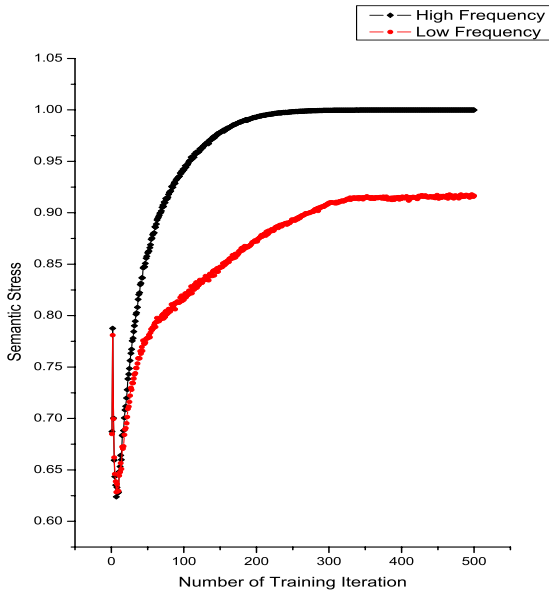
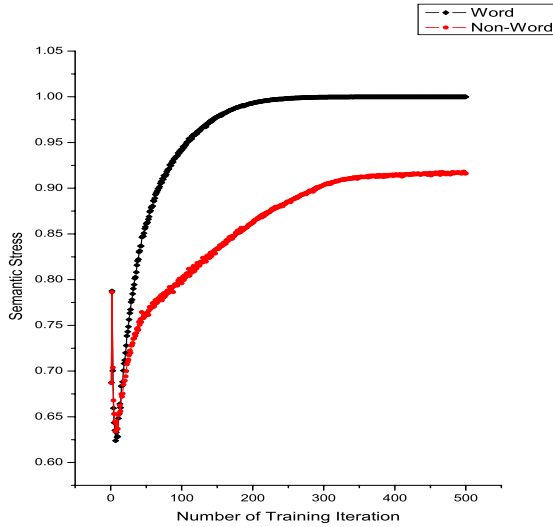
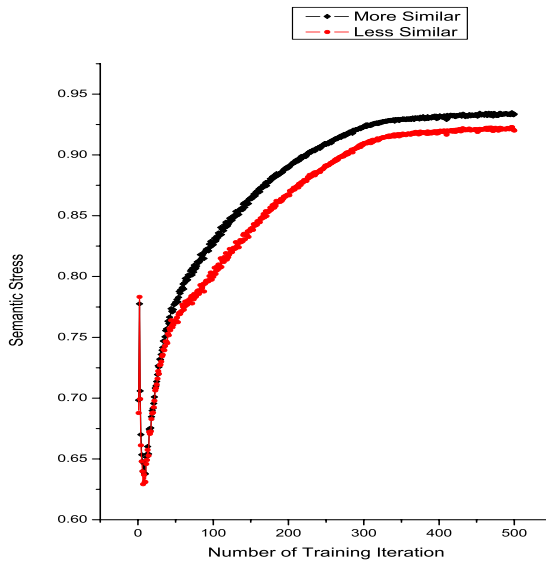


Fig. 3. Frequency Effect



**Fig. 4.** Lexical Status Effect



**Fig. 5.** Word Similarity Effect

of each material. In every experiment, the difference of the average semantic stress was not shown while it is very definite after about 100 training iterations. Although it seems that the difference of the average semantic stress is not obvious as shown in figure 5, every aimed language phenomena including similarity effect

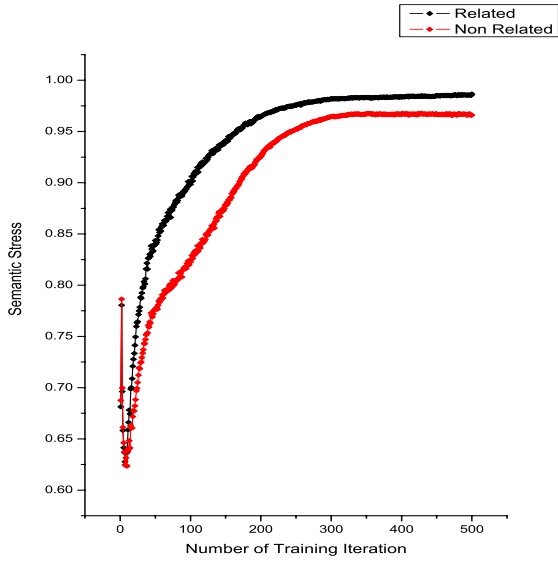


Fig. 6. Semantic Priming Effect

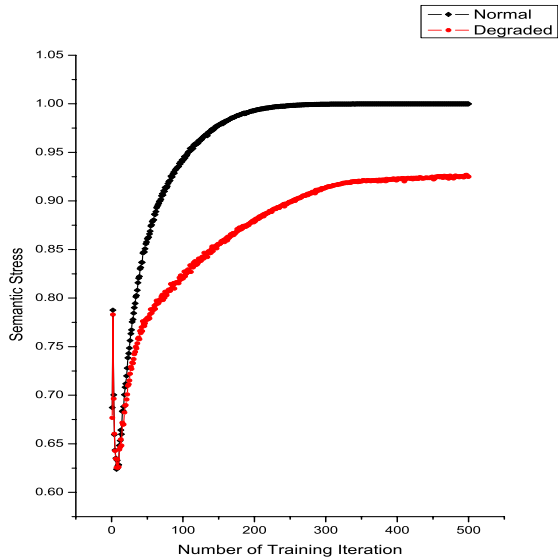


Fig. 7. Visual Degradation Effect

can be simulated statistically significantly after about 100 training iterations. The simulations reveal that the model is reasonably successful in replicating the human performance in LDT.

## 8 Conclusion

This paper proposes a computational model which can simulate Korean LDT. The model is designed to simulate the behaviors observed in human lexical decision task. The proposed model adopts a simple recurrent neural network architecture which takes a Korean string of 2-syllable length as an input and makes an output as a semantic vector representing semantic of the input. As experimental results, we acquired quite encouraging results; the model successfully simulate basic findings observed in human lexical decision task. To our knowledge, the proposed model is only Korean computational model that attempts to simulate human performance in LDT. However, the model is incomplete in that it still has room to be improved to simulate many other symptoms of language disorders such as aphasia and dyslexia. In the future, we will try to perform lesion study to reproduce characteristics of dyslexia by deleting links or modifying weights of links of the propose model.

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# An Artificial Retina Chip Using Switch-Selective Resistive Network for Intelligent Sensor Systems

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**Abstract.** We designed and fabricated a bio-inspired CMOS vision chip for edge detection using a switch-selective resistive network. A CMOS buffer circuit, which is embodied in the structure of a common drain amplifier, is commonly used for both raw and smoothed images by using additional switches. By using the switch-selective resistive network, the total number of MOSFETs in the unit pixel and fixed-pattern noise (FPN) was reduced. In addition, by applying the saturating resistive network, the chip outputs a uniform edge signal under various lighting conditions. From the experimental results of a fabricated one-dimensional array with 20 pixels, we could confirm the operation of the vision chip.

## 1 Introduction

Vision systems, which have image sensors and subsequent processing units for particular purposes, do not use raw images from image sensors such as charge-coupled devices (CCD) and CMOS image sensors (CIS) [1-2]. Indeed, they use filtered images to improve performance and reduce error rate. In particular, Laplacian filtering, by which the edge part of an image is emphasized, have been used in many image processing field such as pattern recognition, and the enhancement of noisy images (e.g. medical images, silhouettes, infrared red images) [3-5]. In order to get edge information, computer vision systems, which consist of CCD and digital computers, have been conventionally used [1-2]. The systems, however, are limited in terms of size, power consumption, and speed regarding real applications, because they consist of two separate modules, which do not interact. Recently, bio-inspired vision chips have been proposed to overcome these problems [6-12]. The vision chips, which mimic the functions of image capturing and processing in the human retina, offer several advantages including compact size, high speed, low power dissipation, and dense system integration.

Two challenges of bio-inspired vision chips include low resolution and noise problems [7-12]. Comparing with conventional CISs, the unit pixel of a bio-inspired vision chip requires additional analog/digital circuits (such as an in-pixel noise reduction circuit, an analog buffer, and some other functional circuits), therefore the size is about several hundred times larger than that of conventional CIS. Noise also occurs from additional circuits, due to the mismatches of the MOSFETs; the process variation; and the temporal fluctuation of power, control signals and biases. In particular,

the vision chips for edge detection require a resistive network, which functions as Gaussian filtering in digital image processing and specialized circuits for the acquisition of both raw and smoothed images. These additional circuits can cause additional area consumption, power dissipation and noise. Therefore, the design of the structure, as well as circuits, is very important for the optimization of their operation. Previously, two structures of bio-inspired vision chips have been proposed [7-8, 10-12]. One type is a voltage division type. The other uses two analog buffers to achieve raw and smoothed images. Otherwise, these structures have their own disadvantages in power and area consumption, signal aliasing and additional noise. To overcome these problems, a new structure, a so-called switch-selective resistive network, is proposed.

In addition, a saturating resistive network is applied to the vision chip to get uniform edge information under various lighting conditions, so-called light adaptation [11-12]. It can help enhance the quality of a final edge image.

The vision chip, which is based on these ideas, has been designed and fabricated with a 20 pixel array using 0.35  $\mu\text{m}$  2-poly 4-metal standard CMOS technology. The operation of the vision chip was tested via experiments.

## 2 Theory

### 2.1 The Principle of Edge Detection

It is well known that the photoreceptors, horizontal cells, and bipolar cells of the retina are concerned with edge detection [13]. Photoreceptors transform the input light into electrical signals and yield voltage in proportion to the input light intensity. Horizontal cells perform spatial smoothing under the influence of the neighboring photoreceptor output. Bipolar cells respond to differences between the photoreceptors and horizontal cells i.e. a signal is yielded which corresponds to the edges of an input pattern. All operations for edge detection are done in a parallel manner. Therefore, we can obtain the edge information of an input image in real-time.

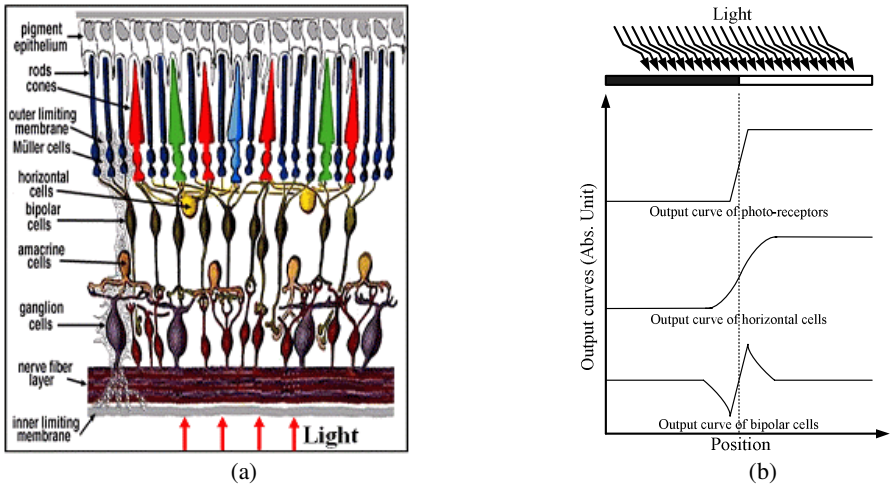
In Figure 1, the structure of a biological retina and the principle of edge detection in a retina are shown. The x-axis represents the position of each cell and the y-axis represents the normalized output curves of photoreceptors, horizontal cells, and bipolar cells, respectively. If a bright light is projected only on the right-hand side of the photoreceptor array, the output of the photoreceptor is a high-level signal. On the other hand, when a dim light is projected on the left-hand side of the photoreceptor array, the output of the photoreceptor is a low-level signal. Horizontal cells receive signal of the photoreceptors and spatially smooth them. Edge signals, the differences between the outputs of the photoreceptor and the horizontal cell, are yielded through bipolar cells.

### 2.2 The Modeling of a Retinal Structure in Electrical Devices

Photoreceptors, horizontal cells, and bipolar cells in the retina are three key elements that embody vision chip for edge detection [7-13]. First, a raw image is necessary to extract edge information. CCDs are used to sense incident image in high quality. They require a special process for fabrication; thus, it is impossible to embed other circuits for image processing. The problem of on-chip integration can be solved by using CIS



technology. The function of horizontal cell can be embodied by using a resistive network, which has been proposed by Mead’s research group in which all photo-sensors in unit pixels are connected horizontally and vertically through resistive circuits [5]. The current flow, from the higher-potential area to the lower-potential area, contributes to image smoothing. Image smoothing is done in a spatially parallel manner, therefore, the mechanism is proper for real-time applications. The function of bipolar cells can be embodied by using differential circuits. In addition, addressing circuits and noise suppression circuits are necessary for practical design.



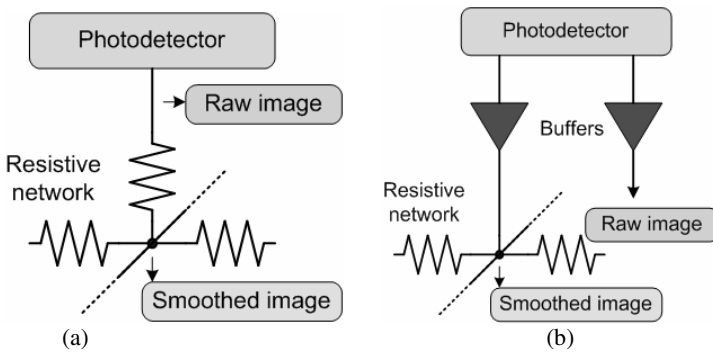
**Fig. 1.** Edge detection mechanism: (a) Structure of a biological retina; (b) Principle of edge detection

### 3 Circuit Design

#### 3.1 Previous Structures of a Resistive Network

Figure 2 shows previously proposed structures of a resistive network. Actually, the commercial linear resistor requires a large area in order to materialize it in CMOS technology. The resistors in the figure are special circuits, so-called resistive circuits, which control current the flow. Fig. 2 (a) shows a voltage division type [7-8]. This type requires a vertical resistive circuit and several horizontal resistive circuits for a unit pixel. The number of horizontal resistive circuits depends upon the designer’s choice. If a designer wants to create a hexagonal resistive network, the number of horizontal resistive circuits should be 6. Vertical and horizontal resistive circuits are different in obtaining optimum output. By using this type of resistive network, raw and smoothed images can be obtained at the upside and downside nodes of a photodetector, respectively. This resistive network has several weak points. It consumes a great amount of power. Bias circuits become the main source of power dissipation because of the continuously flowing current which keeps the operating point of

analog circuits. To operate resistive circuits under optimum conditions, vertical and horizontal resistive circuits individually require a different bias circuit. It means that this type of resistive network requires at least two bias circuits (when all horizontal resistive circuits commonly use a bias circuit) in order to operate each unit pixel. For an entire chip, the total number of bias circuits increases linearly according to the resolution. The complex biases make it difficult to control the chip under optimum condition. The final edge information of a vision chip delicately depends on the characteristics of a resistive network. This control difficulty is another weak point. The third weak point is the distortion of a raw image. The node for a raw image is also connected to a neighboring unit pixel via resistive circuits, therefore, the node cannot keep the original information, the output of a photodetector.



**Fig. 2.** Previous structures of a resistive network: (a) Using voltage division (b) Using two parallel buffers

Figure 2 (b) shows a resistive network using two parallel buffers [10-12]. This type has some advantages, such as a distortion-free raw image and convenience in optimizing the resistive network because of its simple structure; nevertheless, it also has many problems such as large power dissipation, large area consumption, and additional noise. First, the circuit requires additional power dissipation in order to operate the two additional buffers. The total power dissipation from the buffers increases in proportion to the resolution. These buffers also require area consumption as well as power dissipation. This is the second weak point. The third weak point is that the mismatch between these two separated buffer causes fixed pattern noise (FPN). The third weak point is a critical problem regarding realization.

### 3.2 Proposed Structure and Embodiment

To overcome these problems, a novel structure is required. Figure 3 shows a block diagram of the proposed circuit. Switches were embedded in the unit pixel in order to connect neighboring unit pixels via a resistive circuit; i.e. the node at the downside of a photodetector outputs a raw image when the switch is open. The output node, otherwise, outputs a smoothed image when the switch is closed. The first advantage of this structure is low power dissipation, because the switches do not require any

additional current. Raw and smoothed images are achieved at the same node; thus there is no FPN from the structure. This is the second advantage. The third advantage is that the resistive network requires less area. The proposed circuit requires additional switches; it does not require a vertical resistive circuit or buffers comparing with previous types. Switches only require very small area for fabrication in CMOS technology. The fourth advantage is that there is no aliasing problem between the raw and smoothed images, because the resistive network is physically disconnected when the switches are open. The other advantage is that the characteristic of resistive network is easily controlled, due to their simple structure. By using this advantage, we could apply a saturating resistive network to the vision chip in order to enhance the final edge image. Structural disadvantages include additional switching noise and additional control complexity, but they are not critical problems.

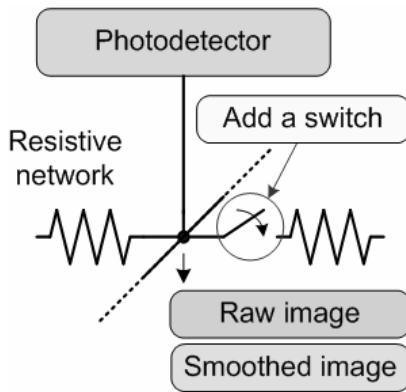


Fig. 3. A block diagram of a switch-selective resistive network

Figure 4 shows a unit pixel’s circuit schematic of the proposed vision chip. The circuit contains a active pixel sensor(APS) for image capturing, two simplified correlated-double sampling (SCDS) circuits for reducing FPN and yielding the difference between raw and smoothed image data, and a saturating resistive element (SRE) which consists of four MOSFETs (MDM, ML1, ML2, and MNB). ‘RE’ in the Figure 4 means resistive element.

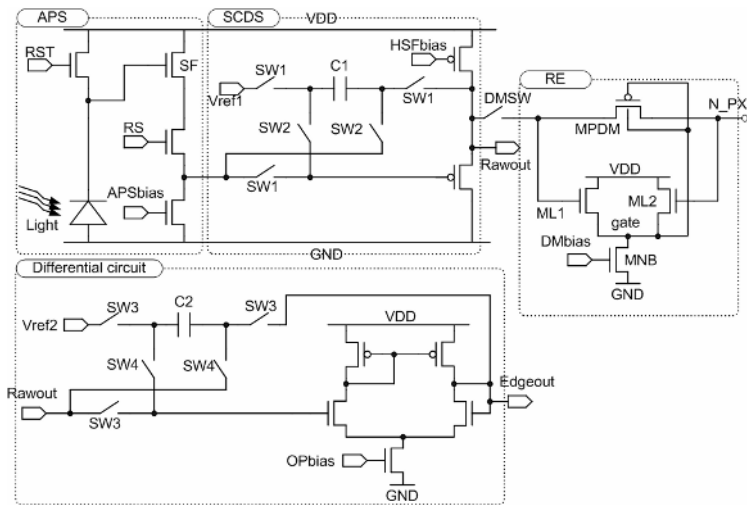
Tree-transistor APS and SCDS were used for image capturing and noise reduction, respectively. APS is an imager, where by every pixel includes at least one active transistor. Transistors in the APS may operate as both an amplifier and a buffer in order to isolate the photogenerated charge from the large capacitance of the common output line. The photodiode capacitance is charged to a reset voltage by turning on the RST. During the integration time, electrons are accumulated in the photodiode capacitance according to the light intensity. After the integration time, the light signal is sampled when the SW1 is turned on. The sampled signal has FPN due to the process variation for fabrication. In order to reduce the FPN, a correlated-double sampling (CDS) circuit is required.

For the vision chip, the area consumption of the noise reduction circuit should be considered, as well as the performance of noise reduction. By this reason, a SCDS,

which was proposed by Kavadias, was applied to our vision chip [14]. A dominant cause of area consumption of the CDS is its capacitors for analog memory. From this point of view, SCDS is very effective method for noise reduction. The key advantage of SCDS is that the circuit requires one capacitor. Therefore, we can easily minimize the area consumption. Compared with SCDS, conventional CDSs use two capacitors in order to memorize both image and reference signals. Detailed operation of SCDS can be found in the reference [8, 14].

We applied a switch-selective resistive network. The structure used a common drain amplifier for both raw and smoothed images. Each image could be selected by using the switch, DMSW. FPN was reduced, because the output node for the raw and smoothed images is the same. Area consumption was also reduced.

To yield the difference between the raw and smoothed images, a modified SCDS was used. By using the modified SCDS, we could achieve the difference in unit gain without extra noise. When SW3 is in a high state, the noise-reduced raw image is sampled in C2. After sampling the raw image, the DMSW is turned on, then the smoothing operation starts. For a sufficient smoothing operation, about 100  $\mu\text{sec}$  is required. After the smoothing operation, the smoothed image is sampled by turning on SW4.



**Fig. 4.** A circuit schematic of the proposed unit pixel

In order to achieve the enhanced edge image, a so-called light adaptation, a saturating resistive network was applied to the vision chip [11-12]. SRE limits current flow to a constant level when the pixel-to-pixel potential difference is above the threshold voltage. Otherwise, when it is below the threshold voltage, there is little current flow through the resistive element. This is the operating principle of the light adaptation in the edge detection circuit. The circuit sends uniform signal under various light conditions. Therefore, improved edge image could be achieved.

Figure 5 shows the timing diagram that controls the proposed circuit.

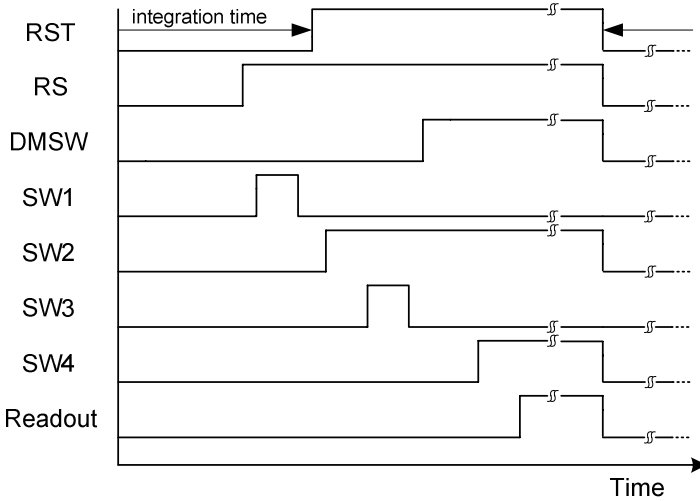


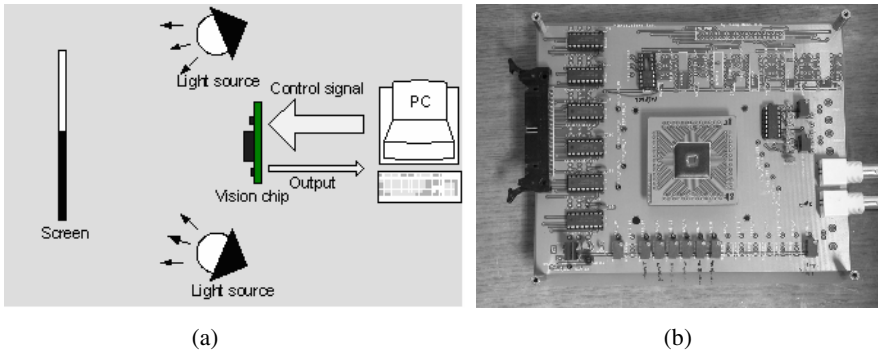
Fig. 5. Timing diagram

## 4 Experimental Results and Discussion

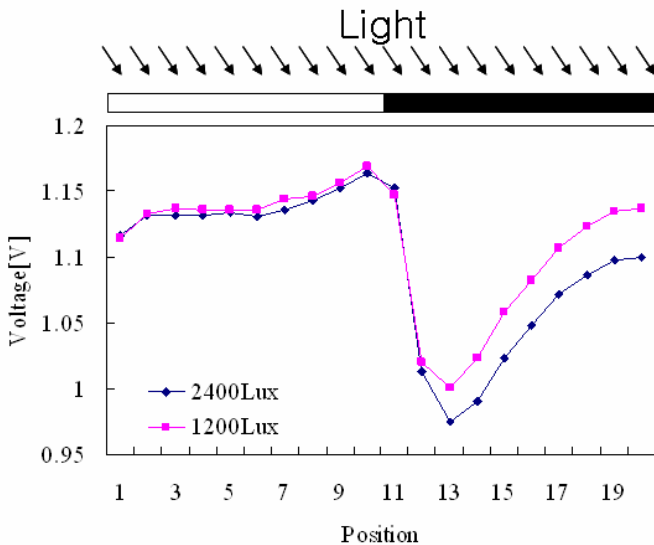
The chip was materialized by using  $0.35\ \mu\text{m}$  2-poly 4-metal standard CMOS process. We fabricated a 20-pixel array in order to investigate the characteristic of the circuit. A data acquisition card (DAQ) and LabVIEW of the National Instrument Company was used to generate control signals and achieve output signals. A lens with a focal length of 16 mm was mounted in a C-mount format, for projecting an input image onto the chip surface. Figure 6 shows the measurement setup and the fabricated vision chip on a test PCB. The test PCB contains a interconnection component for digital I/O, several digital signal buffers for shifting voltage-level (DAQ outputs 5 V signal through digital I/Os, but the operating power of the vision chip is 3.3 V), several variable resistors for biasing, an analog signal buffer and several interconnection components for transferring output signals.

Figure 7 shows the edge output of the chip. We investigated the light adaptation capability by using two different light conditions of 1200 Lux and 2400 Lux. These light conditions are quite different, because the photo-current in the APS exponentially increases by an increase in the light intensity. From the results of the two light conditions, we confirmed the light adaptation of the vision chip.

Our chip spent several hundred msec for charge integration under the illumination condition of 2000 Lux. It is a rather long time, as compared with the conventional CCD camera. The reason of the problem was that the CMOS process for fabrication is not optimum for image sensors; i.e. the photo-efficiency was relatively poor because of the layers for insulation. Although the photodetector did not perform well, we could confirm the operation of the proposed circuit.



**Fig. 6.** Measurement: (a) Measurement setup; (b) Fabricated vision chip on a test PCB



**Fig. 7.** Experimental results

## 5 Conclusion

We designed and fabricated a bio-inspired vision chip for edge detection. By using a switch-selective resistive network, several advantages, such as low power dissipation, low area consumption, less noise, and convenience of control, were achieved. A SCDS to reduce FPN and a saturating resistive network to improve the quality of a final edge image were applied to the vision chip. The fabricated chip, with a 20 pixel array, was working well although the process for fabrication was not optimum for image sensors. Light adaptation of the vision chip was also investigated. From the results, we can expect that the edge image of an incident image can be effectively

extracted by applying the proposed structure to the edge-detection vision chip. By employing the proposed vision chip in the pattern recognition applications, real time and robust computations, with a compact hardware, could be achieved.

## Acknowledgement

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# An Efficient Feedback Canceler for Hearing Aids Based on Approximated Affine Projection<sup>\*</sup>

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**Abstract.** In the feedback cancelation systems in hearing aids, signal cancelation and coloration artifacts can occur for a narrow-band input. In this paper, we propose a new adaptive feedback cancelation algorithm that can achieve fast convergence by approximating the affine projection (AP) algorithm and prevent signal cancelation by controlling the step-size. A Gram-Schmidt prediction error filter (GS-PEF) is used for a stable approximation of the AP algorithm, and the step-size is varied using the prediction factor of the input signal. Simulations results are presented to verify efficiency of the proposed algorithm.

## 1 Introduction

Howling, caused by acoustic feedback, is a persistent and annoying problem for hearing aid users. It also limits the maximum usable gain of hearing aids and, in turn, degrades overall performance. To alleviate this well-known problem, many adaptive feedback cancelation systems have been developed, in which the entire effect of the feedback is eliminated by estimating the acoustic feedback path.

In the adaptive feedback cancelation system, fast adaptation to the variations of feedback path and input spectrum is required. However, fast adaptation often generates ringing and coloration artifacts. Thus, when the feedback environment is time-varying, the desired adaptation behavior is a compromise between fast adaptation required to track changes in the feedback path and slow adaptation required to improve the sound quality of the system.

Another problem associated with the hearing aids is the correlation between the input and output signals, which leads to a bias in the estimate of the feedback path, unless adequate delay is provided [1]. For a broadband input, such delays enable an adaptive system to converge to an accurate estimate of the feedback path. But for a narrowband input, even with a delay, the feedback cancelation system tends to minimize the error signal by canceling the input instead of modeling the feedback path. Adaptation with a sinusoidal input, in general,

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causes system instability and ringing or coloration of the output signal [2]. One approach to maintaining system stability is to constrain adaptations [3]. However, the constrained adaptation will not distinguish between deviation caused by error in the noise model and deviation caused by a change in the external feedback path.

In this paper, we propose an efficient adaptive feedback cancellation system for hearing aids. The proposed system employs a new adaptive algorithm that approximates the affine projection (AP) algorithm with much less computational cost.

Due to its simplicity and efficiency, the LMS adaptive filter has been widely used for the feedback cancellation in hearing aids [1-3]. The convergence performance of the LMS algorithm, however, is often deteriorated by colored input signals. To overcome this problem, the affine projection (AP) algorithm [4] that updates the weight vector based on a number of recent input vectors can be used. The AP algorithm allows a higher convergence speed than the LMS algorithm, especially for the colored input signal. But it is computationally complex. Many fast versions of the AP algorithm have been suggested to provide significant simplifications [5], but they require a process of matrix inversion, which is not only computationally expensive but also a source of numerical instability.

The proposed algorithm approximates the AP algorithm by orthogonalizing the input vectors using a Gram-Schmidt prediction error filter (GS-PEF) [6]. To attain a stable approximation, the proposed algorithm applies a weighted error vector to the GS-PEF for the weight vector update. In addition, the proposed algorithm uses a new step-size control scheme that can prevent the signal cancellation and coloration artifacts caused by adaptation with narrowband inputs. The proposed algorithm performs the AP approximation and step-size control in a unified filter structure with a minimum structural complexity.

## 2 Approximation of the Affine Projection (AP) Algorithm

### 2.1 AP Algorithm with Orthogonalized Input Vectors

The AP algorithm updates the weight vector based on  $K$  most recent input vectors [4]. Similar to the well-known normalized LMS (NLMS) algorithm, a step-size is used to control the rate of convergence and the steady-state excess mean-square error. Let  $\mathbf{w}(n)$  be an  $(N \times 1)$  estimate of an unknown weight vector, the affine projection algorithm with a projection order  $M$  is summarized as

$$\mathbf{w}(n) = \mathbf{w}(n-1) + \mu \Delta(\mathbf{n}), \quad (1)$$

$$\Delta(\mathbf{n}) = \mathbf{X}(n) (\mathbf{X}^T(n) \mathbf{X}(n))^{-1} \mathbf{e}(n), \quad (2)$$

$$\mathbf{e}(n) = \mathbf{d}(n) - \mathbf{X}^T(n) \mathbf{w}(n-1), \quad (3)$$

where  $\mathbf{X}(n) = [\mathbf{x}(n) \mathbf{x}(n-1) \cdots \mathbf{x}(n-M+1)]$  denotes an  $(N \times M)$  input data matrix,  $\mathbf{e}(n)$  and  $\mathbf{d}(n)$  represent  $(M \times 1)$  primary input and error output vectors, respectively.  $\mu$  is the step-size.

Consider a Gram-Schmidt (GS) orthogonalization of the reference input vectors  $\mathbf{x}(n-i), 0 \leq i \leq M-1$ . The output vectors of GS orthogonalization, denoted by  $\mathbf{u}_i(n), 0 \leq i \leq M-1$ , can be written in a compact matrix form [6]:

$$\mathbf{U}(n) = \mathbf{X}(n)\mathbf{L} \tag{4}$$

where  $\mathbf{U}(n) = [\mathbf{u}_{M-1}(n)\mathbf{u}_{M-2}(n)\cdots\mathbf{u}_0(n)]$  and  $\mathbf{L}$  is an  $(M \times M)$  unit lower-triangular matrix. Transformation matrix  $\mathbf{L}$  in Eq. (4) is obtained by solving  $M$  linear prediction problems of orders of 0 through  $M-1$ , which are described as

$$\min_{\mathbf{a}_{M-i-1}} \|\mathbf{x}(n-i) - \bar{\mathbf{X}}(n-i-1)\mathbf{a}_{M-i-1}\|_2, \quad i = 0, 1, \dots, M-1, \tag{5}$$

where  $\mathbf{a}_i$  is a  $(M-i-1) \times 1$  weight vector. Bar marks that the related matrix contains only their  $M-i-1$  rightmost vectors of  $\mathbf{X}(n-i-1)$ , and  $\|\cdot\|_2$  denotes  $l_2$  norm. The output vectors of the GS orthogonalization are given as the residue of the prediction error filter:

$$\mathbf{u}_{M-i-1}(n) = \mathbf{x}(n-i) - \bar{\mathbf{X}}(n-i-1)\mathbf{a}_{M-i-1}, \quad i = 0, 1, \dots, M-1. \tag{6}$$

Let  $\mathbf{D}$  denote the correlation matrix of the output vectors  $\mathbf{u}_i(n)$ . We can write  $\mathbf{D}$  as

$$\begin{aligned} \mathbf{D} &= \mathbf{U}^T(n)\mathbf{U}(n) \\ &= \mathbf{L}^T(\mathbf{X}^T(n)\mathbf{X}(n))\mathbf{L} \\ &= \text{diag}\{\|\mathbf{u}_{M-1}(n)\|_2, \|\mathbf{u}_{M-2}(n)\|_2, \dots, \|\mathbf{u}_0(n)\|_2\}. \end{aligned} \tag{7}$$

Due to a one-to-one correspondence between  $\mathbf{x}(n-i)$  and  $\mathbf{u}_i(n)$ , we have

$$\mathbf{X}(n) = \mathbf{U}(n)\mathbf{L}^{-1}. \tag{8}$$

Thus, we can rewrite Eq. (2) as the following:

$$\Delta(n) = \mathbf{U}(n)\mathbf{D}^{-1}\epsilon(n) = \sum_{i=0}^{M-1} \frac{\epsilon_i(n)}{\|\mathbf{u}_i(n)\|_2} \mathbf{u}_i(n) \tag{9}$$

where  $\epsilon(n) = [\epsilon_{M-1}(n), \epsilon_{M-2}(n), \dots, \epsilon_0(n)]^T$  denotes an  $(M \times 1)$  transformed error vector given by  $\epsilon(n) = \mathbf{L}\mathbf{e}(n)$ .

On the other hand, it is straightforward to show that the error vector can be written as [9]

$$\mathbf{e}(n) = \begin{bmatrix} e(n) \\ (1-\mu)\bar{\mathbf{e}}(n-1) \end{bmatrix}, \tag{10}$$

where  $\bar{\mathbf{e}}(n-1)$  is a vector consisting of the uppermost  $M-1$  elements of  $\mathbf{e}(n-1)$ . Thus, for  $\mu = 1$ , the error vector is simplified to  $\mathbf{e}^T(n) = [e(n) \ \bar{\mathbf{0}}_{M-1}^T]$ , where  $\bar{\mathbf{0}}_{M-1}$  is an  $(M-1) \times 1$  zero vector. In this case,  $\mathbf{L}\mathbf{e}(n) = e(n)$ , and we have

$$\Delta(n) = \frac{e(n)}{\|\mathbf{u}_{M-1}(n)\|_2} \mathbf{u}_{M-1}(n). \tag{11}$$

Eq. (11) indicates that the process of matrix inversion can be implemented by solving the problem:  $\min_{\mathbf{a}_{M-1}} \|\mathbf{x}(n) - \bar{\mathbf{X}}(n-1)\mathbf{a}_{M-1}\|_2$ . Thus, with a linear predictive pre-processor, the AP update is simplified to an NLMS-like equation. Similar approximation of the AP algorithm was presented in [8].

### 2.2 Approximation of the AP Algorithm Using Gram-Schmidt Predictors

As shown in Eqs. (10) and (11), significant approximation is possible for the case that  $\mu = 1$ . However,  $\mu$  in practical cases is arbitrary, since it governs the convergence speed and the excessive mean-square error in the steady-state. For arbitrary  $\mu$ , we generally need to solve  $M$  systems of  $M$  equations.

In this paper, a new adaptive algorithm approximating the AP algorithm with much less computational cost is proposed and applied to the problem of feedback cancelation in hearing aids. The proposed algorithm is based on a Gram-Schmidt prediction error filter (GS-PEF) [6] that iteratively performs Gram-Schmidt orthogonalization.

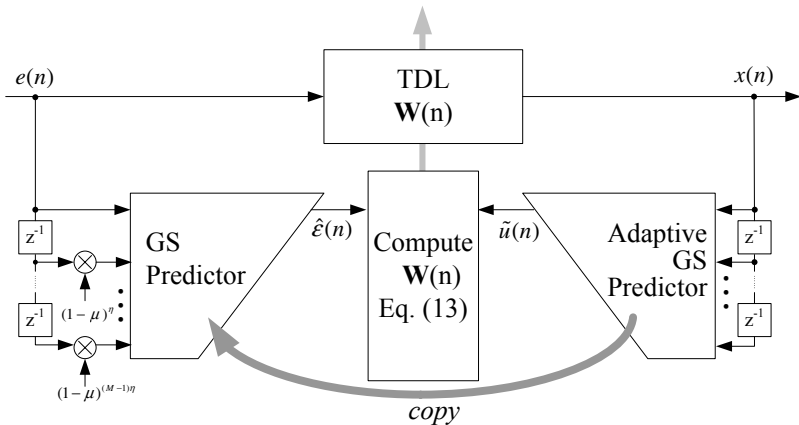
Given  $\hat{\mathbf{h}}_{M-1}(n)$ , the equivalent weight vector of an  $M$ th-order GS-PEF, the proposed algorithm is summarized as

$$\hat{\mathbf{w}}(n) = \hat{\mathbf{w}}(n-1) + \mu \frac{\hat{\varepsilon}_{M-1}(n)}{\|\tilde{\mathbf{u}}(n)\|_2 + \delta} \tilde{\mathbf{u}}(n), \tag{12}$$

$$\tilde{\mathbf{u}}(n) = \begin{bmatrix} \hat{u}_{M-1}(n) \\ \tilde{\mathbf{u}}(n-1) \end{bmatrix}, \quad \hat{u}_{M-1}(n) = \hat{\mathbf{h}}_{M-1}(n)\mathbf{x}(n), \tag{13}$$

$$\hat{\varepsilon}_{M-1}(n) = \hat{\mathbf{h}}_{M-1}(n)\mathbf{e}_a(n), \quad \mathbf{e}_a(n) = \begin{bmatrix} e(n) \\ (1-\mu)^\eta \bar{\mathbf{e}}_a(n-1) \end{bmatrix}, \tag{14}$$

where  $\hat{u}_{M-1}(n)$  is the prediction error of the  $M$ th-order GS-PEF using  $\mathbf{x}(n)$  as an input vector, and  $\hat{\varepsilon}_{M-1}(n)$  is a prediction residue of the weighted error vector obtained using the same GS-PEF. Again, bars in the equations mark that the related vectors with dimension  $i$  contain only their  $(i-1)$  uppermost elements. The input vector  $\tilde{\mathbf{u}}(n)$  for the weight update is obtained by appending  $\hat{u}_{M-1}(n)$

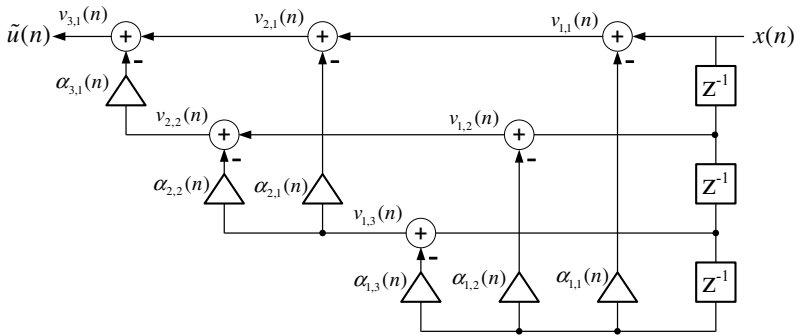


**Fig. 1.** Schematic diagram of the proposed algorithm approximating the AP algorithm using Gram-Schmidt predictors

to the beginning of the previous input vector  $\tilde{\mathbf{u}}(n - 1)$ , which will reduce the computational complexity required to obtain the input vector.

If  $\mu \neq 1$  and  $\eta = 1$ ,  $\mathbf{e}_a(n)$  is identical to  $\mathbf{e}(n)$  in Eq. (10) and the algorithm approximates Eq. (9) using only an  $(M - 1)$ th order linear prediction filter implemented through the GS-PEF. As  $\eta$  increases, less weight on  $\tilde{\mathbf{e}}_a(n - 1)$  is used. Thus,  $\eta$  is a factor of compromising between the cases that  $\mu = 1$  and  $\mu \neq 1$  in the approximation of the AP algorithm by using an  $(M - 1)$ th order prediction filter. Fig. 1 shows a schematic diagram of the proposed algorithm approximating the AP algorithm using Gram-Schmidt prediction error filters.

Coefficients of the GS-PEF can be adaptively adjusted, and any adaptive algorithm can work for the proposed algorithm. However, as a low-complexity system is required, the normalized LMS algorithm is suitable to this application. Fig. 2 shows a schematic diagram of the GS-PEF for the projection order  $(M)$  of 4.



**Fig. 2.** The NLMS Gram-Schmidt predictor for M=4

The NLMS updates for the GS-PEF can be summarized as the following pseudo code [6]:

$$\begin{aligned}
 &v_{0,i} = x(n - i + 1), 1 \leq i \leq M \\
 &\text{for } l = 1 : M \\
 &\quad \chi_l(n) = (1 - \hat{\beta})\chi_l(n - 1) + \hat{\beta} |v_{l-1,M-l+1}(n)|^2 \\
 &\quad \text{for } m = 1 : M - l \\
 &\quad\quad v_{l,m}(n) = v_{l-1,m}(n) - \alpha_{l,m}(n)v_{l-1,M-l+1}(n) \\
 &\quad\quad \alpha_{l,m}(n + 1) = \alpha_{l,m}(n) + \frac{\hat{\beta}}{\chi_l(n)}v_{l-1,M-l+1}(n)v_{l,m}(n) \\
 &\quad \text{end of } m \\
 &\quad \text{end of } l \\
 &\tilde{u}(n) = v_{M-1,1}(n)
 \end{aligned} \tag{15}$$

where  $0 < \hat{\beta} < 1$  is a convergence parameter controlling time span of the adaptation.

The proposed algorithm is similar to the approximated AP algorithm proposed in [7]. However, the algorithm in [7] updates the weight vector based on the assumption that  $\mu = 1$ , i.e., the error sample  $e(n)$  is used instead of the residue of the weighted error vector as in Eqs. (12)~(14). Thus, when  $\mu$  is close to 1, the algorithm in [7] works quite well. But, in practice, the weight update is performed with an arbitrary  $\mu$ . Moreover,  $\mu$  should be small to control the steady-state performance of the adaptive filter. When small  $\mu$  is used, the algorithm suffers from the convergence problem, and even becomes unstable.

### 3 Step-Size Variation

For the variation of the step-size, we define the prediction factor defined as a prediction error power normalized by the input power:  $\rho = \frac{\|\mathbf{u}_{M-1}(n)\|_2}{\|\mathbf{x}(n)\|_2}$ . In case that the order of the predictor is at least of the order of the input AR process  $x(n)$ , the prediction error will be statistically white. Then, the minimum prediction error power becomes  $J_{min} = \|\mathbf{u}_{M-1}(n)\|_2$ . Furthermore, since  $\mathbf{X}^T(n-1)\mathbf{u}_{M-1}(n) = \mathbf{0}_{M \times 1}$ ,  $J_{min}$  can be written as  $J_{min} = \|\mathbf{x}(n)\|_2 - \|\mathbf{X}(n-1)\hat{\mathbf{a}}_{M-1}(n)\|_2$ . Thus,  $\rho = J_{min}/\|\mathbf{x}(n)\|_2 = 1 - \|\mathbf{X}(n-1)\hat{\mathbf{a}}_{M-1}(n)\|_2/\|\mathbf{x}(n)\|_2$ . Note that the ratio  $\rho$  can never be negative and the ratio  $\|\mathbf{X}(n-1)\hat{\mathbf{a}}_{M-1}(n)\|_2/\|\mathbf{x}(n)\|_2$  is always positive, we therefore have  $0 \leq \rho \leq 1$ . Thus, the prediction factor always lies between zero and one.

Given an instantaneous estimate of the prediction factor, denoted by  $\hat{\rho}(n)$ , the step-size of the proposed algorithm is determined as

$$\beta(n) = \lambda\beta(n-1) + (1-\lambda) \min\{T_{\max}, \hat{\rho}(n)\} \tag{16}$$

$$\kappa(n) = \begin{cases} s_{\text{tone}}\beta(n), & \beta(n) < T_{\text{tone}} \\ \beta(n), & \text{otherwise} \end{cases} \tag{17}$$

$$\hat{\mu}(n) = \kappa(n)\mu_{\max} \tag{18}$$

where  $\mu_{\max}$  controls the maximum magnitude of the step-size. The instantaneous estimate of prediction factor is computed using the GS-PEF as  $\hat{\rho}(n) = \|\tilde{\mathbf{u}}(n)\|_2/\|\mathbf{x}(n)\|_2$ . In the algorithm,  $\hat{\rho}(n)$  is limited by  $T_{\max}$  to disregard over-estimated ones, and it is averaged using a simple-pole IIR filter to have  $\beta(n)$ .  $\beta(n)$  will be close to unity for wideband inputs, and it will become small for narrowband inputs. Therefore, the algorithm will use large step-sizes for wideband sections and small step-sizes for narrowband sections of the input, which will provide a more accurate estimate of the feedback path than using a fixed step-size. When tone signals such as DTMF or tone-like signals are added to the input, the prediction factor will decrease abruptly. The step-size then decreases too and adaptation will be inhibited. Thus, the system can avoid adaptation using tone-like inputs. To further inhibit adaptation for tone-like inputs,  $\beta(n)$  is compared with a threshold  $T_{\text{tone}}$ . When the input is judged as a tone-like signal, a small constant  $s_{\text{tone}}$  less than 1 is multiplied to the smoothed prediction factor.

Fig. 3 shows a complete block diagram of the proposed adaptive feedback canceler, which uses the GS-PEF to approximate the AP algorithm using Eqs.

(12)~(14) and (15)~(17). The reference input signal  $x(n)$  is fed to the adaptive GS-PEF and the residual is obtained. The coefficients of the GS-PEF are copied into another GS-PEF connected to the error signal, by which the residue of the weighted error vector is obtained. If the feedback path is rapidly changing, the

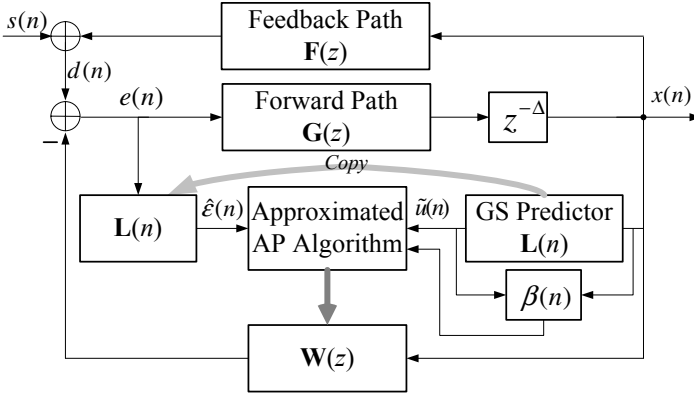


Fig. 3. Block diagram of the proposed adaptive feedback canceler

hearing aid output will also rapidly increase due to a mismatch between the current estimate and the new feedback path. The mismatch will emphasize the error at frequencies with small gain margin relative to other frequencies [2]. Consequently, the output spectrum will vary dramatically. The spectral variation, in turn, influences the prediction factor of the prediction filter. During the period of adaptation to the spectral variation, the GS-PEF will produce large prediction errors, which results in a big step-size. Thus, the feedback cancelation filter can quickly adapt to the new feedback path.

In a howling situation the feedback canceler must use a large step-size, but the prediction factor will rapidly decrease because howling is normally associated with strong tone signals at the output. However, since the power of howling tones is abnormally high, those tones can be easily discriminated from tones embedded in the input by monitoring the output power.

### 4 Computer Simulations

For the simulations, 20dB hearing aid gain was assumed, and an 80-sample decorrelation delay was inserted in the forward path together with a probe noise of 40dB SNR. The feedback path was modeled using a 128-tap FIR filter at the sampling rate of 16kHz, and a 32-tap adaptive filter was used for the feedback cancelation.

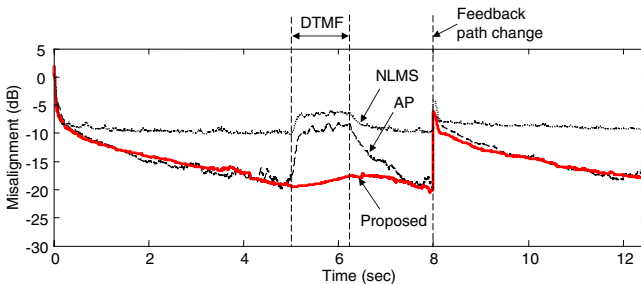
Firstly, the proposed algorithm was tested using a speech-shaped noise which was generated by passing the white noise through a 16<sup>th</sup>-order AR filter modeling

the speech spectrum. For simulations we added a 1.2-second long DTMF tone corresponding to the digit '3' to the input at the time index 5sec, and the change of feedback path was simulated at the time index 8sec, at which the impulse response of the feedback path was modulated using a 10Hz sine with an amplitude 4. We also used a 3rd-order GS-PEF to approximate the AP algorithm of order 4. Parameter values used for the simulation were that  $\mu_{\max} = 0.01$ ,  $\lambda = 0.001$ ,  $T_{\min} = 0.25$ ,  $T_{\text{tone}} = 0.05$ , and  $s_{\text{tone}} = 0.25$ , where  $T_{\min}$  and  $T_{\text{tone}}$  were empirically determined to obtain the best performance. Step-sizes for the AP and NLMS were 0.002 and 0.02, respectively.

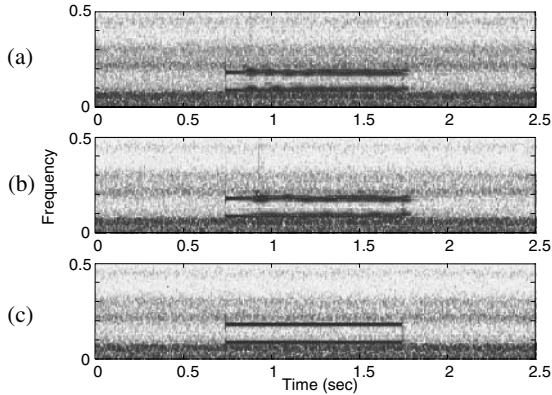
Misalignments are shown in Fig. 4, which shows that the proposed algorithm achieved close approximation to the AP algorithm in terms of convergence speed and steady-state misalignment. It always provided lower misalignments and faster convergence speed than the NLMS algorithm. Also, the new algorithm was not obviously affected by the temporary DTMF tone in the input. The NLMS and AP algorithms, on the other hand, quickly reacted to the input DTMF tone, which resulted in high misalignments and ringing sound during the presence of DTMF tone. Fig. 5 shows the output spectrograms extracted for the DTMF period. It can be seen that, unlike the NLMS and AP algorithms that canceled the input pure tone to minimize the modeling error, the proposed algorithm provides stable outputs.

Another simulation was performed using a true speech signal. 30dB SNR was assumed, and 1.2-second long DTMF tones corresponding to '3', '5', and '7' were added at the time indices of 4, 9 14 seconds, respectively. The feedback path was changed at 7 and 13 seconds, respectively, similarly to the previous case. Other parameters were the same as the previous simulation.

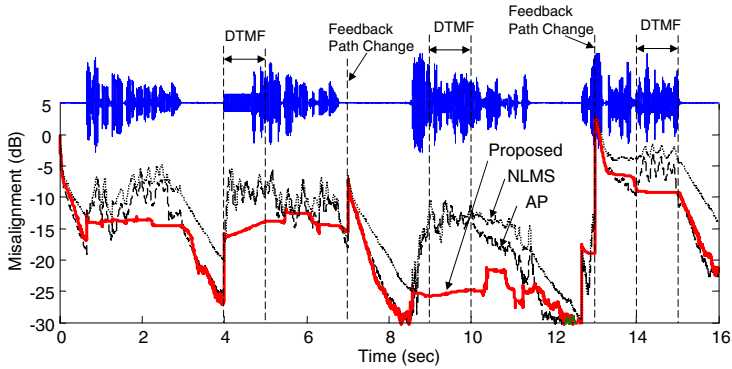
Misalignments are shown together with the input speech in Fig. 6. The results show that convergence rate of the proposed algorithm is comparable to the AP algorithm, but provides more stable outputs. The overall sound quality provided by the proposed algorithm was clean and stable. No ringing and coloration artifacts were heard except for a short click occurred in a transient period of adaptation to the new feedback path. But the NLMS and AP



**Fig. 4.** Misalignments of feedback canceler for a speech-shaped noise: NLMS algorithm (dotted line), AP (dashed line), and proposed (solid line) algorithms



**Fig. 5.** Spectrograms of the hearing-aid output signals for the case in Fig. 4: (a) NLMS, (b) AP, and (c) proposed algorithms



**Fig. 6.** Input speech and misalignments of feedback cancelers for a speech input: NLMS algorithm (dotted line), AP (dashed line), and proposed (solid line) algorithms

algorithms produced annoying artifacts during the periods of pure tones and some narrowband sections of the input speech.

## 5 Conclusions

A new adaptive algorithm for feedback cancellation in hearing aids has been presented. The proposed algorithm could achieve an approximation of AP algorithm with less computational cost, and by varying the step-size according to the spectral variation of the input, it could prevent system instability and coloration artifacts due to the narrowband inputs. Simulation results showed that the proposed algorithm was also capable of detecting and tracking the changes in the feedback path.



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# Robust Real-Time Face Detection Using Hybrid Neural Networks\*

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**Abstract.** In this paper, a multi-stage face detection method using hybrid neural networks is presented. The method consists of three stages: preprocessing, feature extraction and pattern classification. We introduce an adaptive filtering technique which is based on a skin-color analysis using fuzzy min-max(FMM) neural networks. A modified convolutional neural network(CNN) is used to extract translation invariant feature maps for face detection. We present an extended version of fuzzy min-max (FMM) neural network which can be used not only for feature analysis but also for pattern classification. Two kinds of relevance factors between features and pattern classes are defined to analyze the saliency of features. These measures can be utilized to select more relevant features for the skin-color filtering process as well as the face detection process.

## 1 Introduction

Convolutional neural networks (CNN) have been successfully applied to object recognition [1, 2]. The CNN model is a bio-inspired hierarchical multi-layered neural network that achieves some degree of shift and deformation invariance using three ideas: local receptive fields, shared weights, and spatial subsampling. Growing interest in computer vision has motivated a recent surge in research on problems such as face recognition, pose estimation, face tracking and gesture recognition. However, most methods assume human faces in their input images have been detected and localized [3, 4, 5]. Fuzzy min-max (FMM) neural network is a hyperbox-based pattern classification model [6, 7]. In this paper, we present an extended version of the WFMM model for face detection. Since the weight factor of the network can be adjusted by training process, the system can prevent undesirable performance degradation which may be caused by some environmental factors such as illumination

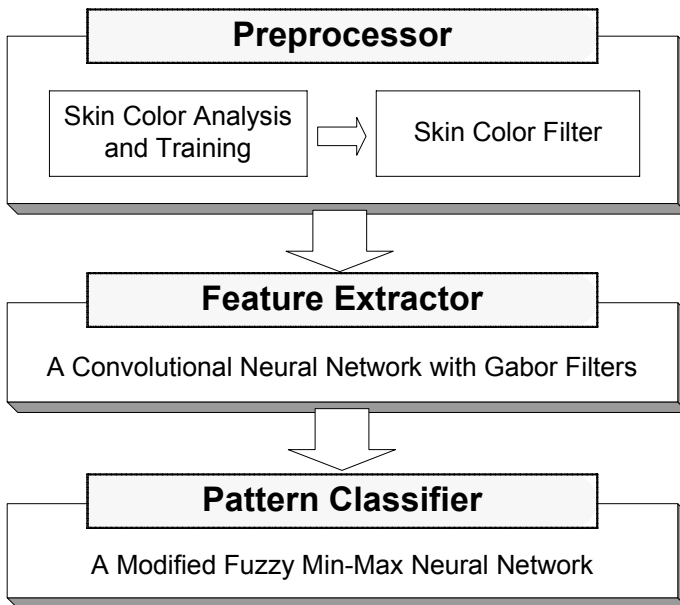
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changes in face detection system. We introduce a multi-stage face detection method using a hybrid neural network which combines a convolutional neural network and a fuzzy min-max neural network. The proposed method consists of three sub-processes: preprocessor, feature extractor and pattern classifier. We introduce an adaptive filtering technique which is based on a skin-color analysis using the proposed model. A modified convolutional neural network is used to extract translation invariant feature maps for face detection. We define two kinds of relevance factors between features and pattern classes. Through the feature analysis technique, we can select the most relevant features for the skin-color filter as well as the pattern classifier. Moreover, the training process makes it possible to adaptively adjust the feature ranges of the skin-color filter.

## 2 Multi-stage Face Detection

As shown in Fig. 1, the underlying face detection system consists of three modules: preprocessor, feature extractor and pattern classifier.



**Fig. 1.** The underlying face detection system

The feature extractor is implemented using a convolutional neural network in which a Gabor transform layer is added at the first layer. Through the skin color analysis and the training process, the system can generate an adaptive skin model and a relevant feature set for the given illumination condition. The feature extractor generates numerous features from the input image. The number of features affects the computation time and performance of the system. Therefore we propose a feature

analysis technique to reduce the amount of features for the pattern classifier. More details of the method are described in Section 3 and Section 4.

### 3 Skin Color Filtering Using WFMM Neural Networks

In general, a skin color filtering problem is considered as a pixel classification problem. We have employed an extended version of FMM neural network for the adaptive skin color filter. In this paper we present a weighted fuzzy min-max(WFMM) neural network and its application to feature analysis technique. Through the learning capability of the model, the skin color filter can dynamically adjust the feature set and the feature ranges for the variance of environmental conditions such as illumination changes. Fig. 2 shows the structure of the WFMM model.

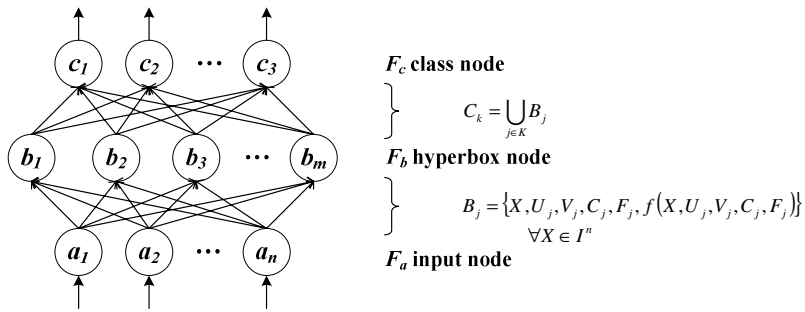


Fig. 2. The structure of the WFMM model

The membership function of a hyperbox is defined as Equation (1).

$$B_j = \{X, U_j, V_j, C_j, F_j, f(X, U_j, V_j, C_j, F_j)\} \quad \forall X \in I^n \tag{1}$$

In the equation,  $U_j$  and  $V_j$  mean the vectors of the minimum and maximum values of hyperbox  $j$ , respectively.  $C_j$  is a set of the mean points for the feature values and  $F_j$  means the a set of frequency of feature occurrences within a hyperbox. As shown in Equation (2) and (3), the model employs a new activation function which has the factors of feature value distribution and the weight value for each feature in a hyperbox.

$$b_j(A_n) = \frac{1}{\sum_{i=1}^n w_{ji}} \bullet \sum_{i=1}^n w_{ji} [\max(0, 1 - \max(0, \gamma_{jiv} \min(1, a_{ni} - v_{ji}))) + \max(0, 1 - \max(0, \gamma_{jiv} \min(1, u_{ji} - a_{ni}))) - 1.0] \tag{2}$$

$$\begin{cases} \gamma_{jiU} = \frac{\gamma}{R_U} & R_U = \max(s, u_{ji}^{new} - u_{ji}^{old}) \\ \gamma_{jiV} = \frac{\gamma}{R_V} & R_V = \max(s, v_{ji}^{old} - v_{ji}^{new}) \end{cases} \tag{3}$$

In the equation,  $w_{ij}$  is the connection weight which means the relevance factor between  $i$ -th feature and  $j$ -th hyperbox. The learning process of the model consists of three sub-processes: hyperbox creation, expansion, and contraction processes.

If the expansion criterion shown in Equation (4) has been met for hyperbox  $B_j$ ,  $f_{ji}$ ,  $u_{ji}$ ,  $v_{ji}$  and  $c_{ij}$  are adjusted using Equation (5) and (6).

$$n\theta \geq \sum_{i=1}^n (\max(v_{ji}, x_{hi}) - \min(u_{ji}, x_{hi})) \tag{4}$$

$$\begin{cases} f_{ji}^{new} &= f_{ji}^{old} + 1 \\ u_{ji}^{new} &= \min(u_{ji}^{old}, x_{ki}) \\ v_{ji}^{new} &= \min(v_{ji}^{old}, x_{ki}) \end{cases} \tag{5}$$

$$c_{ji}^{new} = (c_{ji} * f_{ji}^{old} + x_{hi}) / f_{ji}^{new} \tag{6}$$

As shown in the equations, the frequency value is increased by 1 at every expansion and the min and max point expansion operations are similar to the fuzzy intersection and fuzzy union operations [6]. The mean point value,  $c_{ji}$ , is updated by Equation (6). During the learning process the weight values are determined by Equation (7) and (8).

$$w_{ji} = \frac{\alpha f_{ji}}{R} \tag{7}$$

$$R = \max(s, v_{ji} - u_{ji}) \tag{8}$$

As shown in the equations, the weight value is increased in proportion to the frequency of the feature. In the equations,  $s$  is a positive constant to prevent the weight from having too high value when the feature range is too small. The value of  $f_{ji}$  is adjusted through the learning process. The contraction process is considered as an optional part of our model. The contraction process is to eliminate the possible overlappings between hyperboxes that represent different classes. We can expect that the weights concept of the model replace the role of overlapping handling because the weights reflect the relevance of feature values and hyperbox as different values. We define a new contraction method including the weight updating scheme. To determine whether or not the expansion has created any overlapping, a dimension by dimension

comparison between hyperboxes is performed. If one of the following four cases is satisfied, then overlapping exists between the two hyperboxes.

For each of these cases, contraction process is performed. If  $\delta^{old} - \delta^{new} > 0$ , then  $\Delta = i$ ,  $\delta^{old} = \delta^{new}$ , signifying that there was an overlap for  $\Delta$ th dimension. Otherwise, the testing is terminated and the minimum overlap index variable is set to indicate that the next contraction step is not necessary, i.e.  $\Delta = -1$ . If  $\Delta > 0$ , then the  $\Delta$ th dimension of the two hyperboxes are adjusted. Only one of the  $n$  dimensions is adjusted in each of the hyperboxes to keep the hyperbox size as large as possible and minimally impact the shape of the hyperboxes being formed.

$$\begin{aligned}
 \text{case1} : & u_{ji} < u_{ki} < v_{ji} < v_{ki} \\
 & \delta^{new} = \min(v_{ji} - u_{ki}, \delta^{old}) \\
 \text{case2} : & u_{ki} < u_{ji} < v_{ki} < v_{ji} \\
 & \delta^{new} = \min(v_{ki} - u_{ji}, \delta^{old}) \\
 \text{case3} : & u_{ji} < u_{ki} < v_{ki} < v_{ji} \\
 & \delta^{new} = \min(\min(v_{ki} - u_{ji}, v_{ji} - u_{ki}), \delta^{old}) \\
 \text{case4} : & u_{ki} < u_{ji} < v_{ji} < v_{ki} \\
 & \delta^{new} = \min(\min(v_{ji} - u_{ki}, v_{ki} - u_{ji}), \delta^{old})
 \end{aligned}$$

We have defined new adjustment schemes from the new definition of hyperbox for the four cases. The frequency factor is increased in proportion to the relative size of the feature range, and the mean point value is adjusted by considering the expanded feature range.

### 4 Feature Analysis Technique Based on WFMM Model

This section describes a feature analysis technique for the skin-color filter and the classifier. We define two kinds of relevance factors using the proposed FMM model as follows:

$$\begin{aligned}
 RF1(x_j, C_k) & : \text{the relevance factor between a feature value } x_j \text{ and a class } C_k \\
 RF2(X_i, C_k) & : \text{the relevance factor between a feature type } X_i \text{ and a class } C_k
 \end{aligned}$$

The first measure *RF1* is defined as Equation (9). In the equation, constant  $N_B$  and  $N_k$  are the total number of hyperboxes and the number of hyperboxes that belong to class  $k$ , respectively. Therefore if the  $RF1(x_i, k)$  has a positive value, it means an excitatory relationship between the feature  $X_i$  and the class  $k$ . But a negative value of  $RF1(x_i, k)$  means an inhibitory relationship between them. A list of interesting features for a given class can be extracted using the *RF1* for each feature.

$$RF1(x_i, C_k) = \left( \frac{1}{N_k} \sum_{B_j \in C_k} S(x_i, (u_{ji}, v_{ji})) \cdot w_{ij} \right) - \frac{1}{(N_B - N_k)} \sum_{B_j \notin C_k} S(x_i, (u_{ji}, v_{ji})) \cdot w_{ij} / \sum_{B_j \in C_k} w_{ij} \tag{9}$$

In Equation (9), the feature value  $x_i$  can be defined as a fuzzy interval which consists of min and max values on the  $i$ -th dimension out of the  $n$ -dimension feature space. For an arbitrary feature  $X_i$ , let  $x_i^L$  and  $x_i^U$  be the min and max value, respectively, then the similarity measure  $S$  between two fuzzy intervals can be defined as Equation (10).

$$S(x_i, (u_i, v_i)) = S((x_i^L, x_i^U), (u_i, v_i)) = \frac{Overlap((x_i^L, x_i^U), (u_i, v_i))}{Max(x_i^U - x_i^L, v_i - u_i)} \tag{10}$$

In Equation (10), if two fuzzy intervals are all point data, then the denominator part of the equation,  $Max(x_i^U - x_i^L, v_i - u_i)$  becomes zero. Therefore we define the similarity measure in this case as Equation (11). As shown in the equation, the similarity value is 1.0 when two intervals have an identical point, and 0 when they indicate two different points.

$$S((x_i^L, x_i^U), (u_i, v_i)) = \begin{cases} 1 & \text{if } (x_i^L = x_i^U = u_i = v_i) \\ 0 & \text{Otherwise} \end{cases} \tag{11}$$

But if  $Max(x_i^U - x_i^L, v_i - u_i)$  is greater than zero, the value is determined as described in Equation (16).

$$Overlap((x_i^L, x_i^U), (u_i, v_i)) = \begin{cases} x_i^U - u_i & \text{if } (x_i^L \leq u_i \leq x_i^U \leq v_i) \\ v_i - u_i & \text{if } (x_i^L \leq u_i \leq v_i \leq x_i^U) \\ x_i^U - x_i^L & \text{if } (u_i \leq x_i^L \leq x_i^U \leq v_i) \\ v_i - x_i^L & \text{if } (u_i \leq x_i^L \leq v_i \leq x_i^U) \\ 0 & \text{Otherwise} \end{cases} \tag{12}$$

The second measure  $RF2$  can be defined in terms of  $RF1$  as shown in Equation (13). In the equation,  $L_i$  is the number of feature values which belong to  $i$ -th feature.

$$RF2(X_i, C_k) = \frac{1}{L_i} \sum_{x_j \in X_i} RF1(x_j, C_k) \quad (13)$$

The  $RF2$  shown in Equation (13) represents the degree of importance of a feature in classifying a given class. Therefore it can be utilized to select a more relevance feature set for the skin color filter.

## 5 Feature Extraction and Face Classification

The most advantageous feature of convolutional neural network is invariant detection capability for distorted patterns in images [1, 2]. As shown in Fig. 3, the underlying system employs a convolutional neural network in which a Gabor transform layer is added at the first layer. The first layer of the network extracts local feature maps from the input image by using Gabor transform filters. The other layers of the feature extractor include two types of sub-layers called *convolution layer* and *sub-sampling layer*. Each layer of the network extracts successively larger features in a hierarchical set of layers. Finally a feature set is generated for the input of the pattern classifier. The pattern classifier has been implemented using the proposed WFMM neural network. For the feature extractor, a set of  $(38 \times 42)$  candidate areas has been selected as input data. The Gabor filter layer generates eight  $(28 \times 32)$  feature maps. Each unit in each feature map is connected to a  $(11 \times 11)$  neighborhood into the input retina. In the sub-sampling layer, the feature map has half the number of rows and columns of the input data. Therefore the layer has eight feature maps of size  $(14 \times 16)$ .

The convolutional layer generates 44 feature maps. Each unit is connected to  $(3 \times 3)$  neighborhood at identical locations in a subset of the feature maps of the Gabor transform layer. In the feature extraction layer, 44 kinds of feature values are generated. These data become the input data of the pattern classifier. The number of input features can be reduced through the feature analysis technique described in the previous section.

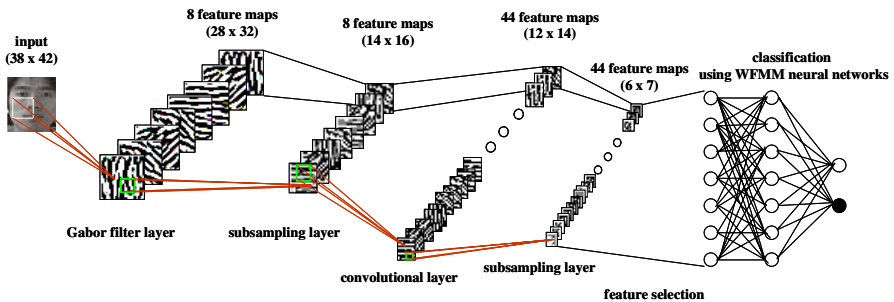


Fig. 3. Face detector using hybrid neural networks



## 6 Experimental Results

Two types of experiments have been conducted for a set of real images. For the training of skin-color filter, the system considers eleven color features: *Red, Green, Blue, Intensity, Cb, Cr, magenta, Cyan, Yellow, Hue, and Saturation*. Fig. 4 shows two input images captured under different illumination conditions and the face detection results.

Table 1 shows the skin-color analysis result and the feature range data derived from the training process. As shown in the table, different kinds of features can be adaptively selected for a given condition, and the feature ranges of skin-color can be also adjusted by the training process.

The table shows four features which have the highest value of the relevance factor *RFI*. As shown in the table, a number of hyperboxes for face and non-face patterns have been generated and the relevance factors are also adjusted through the training process. Therefore the system can select more effective features adaptively for the given environment.

We have selected face patterns from the real images and non-face patterns from the background images. 50 face patterns and 50 non-face patterns have been used for training process. 100 face patterns and 100 non-face patterns have been used for the test stage. Table 2 and Fig. 5 show the change of detection rate and false alarm rate by varying the number of training patterns, respectively. The result shows that the detection rate increases as more training patterns are used, and the false alarm rate decreases as more non-face counter examples are used for training.



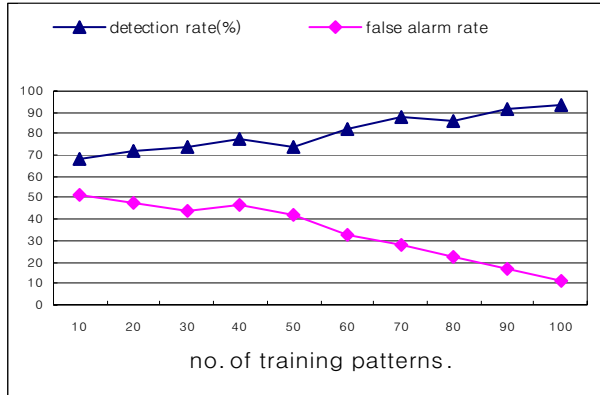
**Fig. 4.** Two training data captured under different illumination conditions

**Table 1.** Feature analysis results for the two images

| <i>image - 1</i>  |               |            | <i>image - 2</i>  |               |            |
|-------------------|---------------|------------|-------------------|---------------|------------|
| features          | feature range | <i>RFI</i> | features          | feature range | <i>RFI</i> |
| <i>Saturation</i> | 0.072 ~ 0.322 | 6.734      | <i>Cb</i>         | 0.538 ~ 0.742 | 9.274      |
| <i>Yellow</i>     | 0.388 ~ 0.594 | 6.423      | <i>Blue</i>       | 0.445 ~ 0.626 | 9.261      |
| <i>Cb</i>         | 0.562 ~ 0.729 | 5.881      | <i>Saturation</i> | 0.074 ~ 0.283 | 8.716      |
| <i>Cr</i>         | 0.114 ~ 0.355 | 5.217      | <i>Cr</i>         | 0.123 ~ 0.368 | 7.662      |

**Table 2.** Detection rate and false alarm rate as varying the number of training patterns

| number of training patterns |                   | performance    |                  |
|-----------------------------|-------------------|----------------|------------------|
| face patterns               | non-face patterns | detection rate | false alarm rate |
| 10                          | 10                | 72             | 48               |
| 20                          | 20                | 78             | 47               |
| 30                          | 30                | 82             | 33               |
| 40                          | 40                | 86             | 22               |
| 50                          | 50                | 93             | 11               |

**Fig. 5.** Detection rate and false alarm rate as varying the number of training patterns

## 7 Conclusion

The weighted FMM neural network is capable of utilizing the feature distribution and frequency in learning process as well as in classification process. Since the weight factor effectively reflects the relationship between feature range and its distribution, the system can prevent undesirable performance degradation which may be caused by noisy patterns. Through the training process, the skin-color filter is adapted for the

illumination condition under which the given images are captured. Two types of feature relevance measures have been defined for the feature selection technique. The first measure *RFI* makes it possible to eliminate the hyperbox contraction process since the measure represents different relevance values within overlapped hyperbox feature ranges. The learning algorithm of the weighted FMM neural network has been presented. The receptive field structure of CNN model provides invariant feature extraction capability and the use of shared weight also reduces the number of parameters in the system.

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# The Novel Feature Selection Method Based on Emotion Recognition System\*

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**Abstract.** This paper presents an original feature selection method for Emotion Recognition which includes many original elements. Feature selection has some merit regarding pattern recognition performance. Thus, we developed a method called an ‘Interactive Feature Selection’ and the results (selected features) of the IFS were applied to an emotion recognition system (ERS), which was also implemented in this research. Our innovative feature selection method was based on a Reinforcement Learning Algorithm and since it required responses from human users, it was denoted an ‘Interactive Feature Selection’. By performing an IFS, we were able to obtain three top features and apply them to the ERS. Comparing those results from a random selection and Sequential Forward Selection(SFS) and Genetic Algorithm Feature Selection(GAFS), we verified that the top three features were better than the randomly selected feature set.

**Keywords:** Reinforcement Learning, Feature selection, Emotion Recognition, SFS, GAFS.

## 1 Introduction

Emotion recognition research has been typically attempted using four kinds of medium. They are speech, image, physiological signal, and gesture. In addition, our IEEE survey papers published from 1990 to 2005 show that papers using the speech medium have been published more often than others have. The reason for this result is probably due to feature set extraction from speech and image being easier than physiological signal or gesture and the possibility of classification is higher. In particular, EEG, ECG, and SC sensors are used to obtain a physiological signal but the signal from those sensors may be obstructed by electrical signals from fluorescent lamps or electric home appliances. This problem is the one obstacle in emotion recognition using a physiological signal. For an image, this means facial expression recognition and the main problem in this case is usually lighting conditions, which often change, or personal accessories like glasses which affect recognition performance. A problem of gesture recognition is similar to that of image recognition and the bigger problem is that it

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may not include much information regarding emotion. Apart from above the problems which these three media present, speech signal can send much more information regarding emotion. For example, talking over the telephone, one can recognize emotions and this shows the validity of speech signal for emotion recognition. Even a cheap microphone can be used sufficiently as a sensor for collecting speech signals and noise will not affect the extraction of the feature set unless it is too loud to be classified as a coming from the source of the signal. These reasons are why most researchers have focused on speech signal and why we have selected this medium for our paper. The commonly used feature set for emotion recognition from speech consists of pitch, energy, formant, and speech rate. Some researchers select all four of the feature sets, others select only one, and the features are generally extracted statistically from the four feature sets. In [1], 87 features were extracted from pitch, energy, and formant and they were classified into five emotions. In [2], 17 features were extracted from pitch, energy, speech rate and so on with sex also being classified. In addition, In [3], 11, 40, and 13 features were extracted. The fact that feature set selection is not fixed suggests that features may or may not be relevant to emotion recognition. This problem will plague researchers in this field until exceptional results are obtained. For this case, there is a GA based selection method, Floating search method and so on which can somewhat reduce difficulties for researchers [4]. Especially, the Sequential Forward Selection and Sequential Backward Selection methods of a Floating search method have been frequently used. In [2], a Forward Selection(FS) method was used and in [1], the 10 best features were selected out of 87 features by using a Sequential Floating Forward Selection algorithm(The extended version of SFS). In [5], a Sequential Forward Selection algorithm was also used and the best feature subset was selected out of 39 candidate feature sets and In [6], a good feature set was found using genetic programming for the music genre classification related problem. These feature selection methods provided a good solution for "The curse of dimensionality" and contributed to the performance of pattern recognitions. In addition, feature selection methods included supervised and unsupervised cases. Generally, a supervised case is employed more often than an unsupervised case. This is due to unsupervised feature selection methods having a high probability of incorrect results for corresponding patterns regarding perceived speech[7]. Although, there are many cases that cannot obtain an explicit supervised value, the unsupervised method has advantages. We propose a method using reinforcement learning taking advantage of both the supervised and unsupervised method, which can alleviate the shortcomings of both methods. Researches of the reinforcement learning have been proceeded using many methods, i. e. Dynamic programming, Monte Carlo method, TD method, Q learning etc. proposed by Sutton and Barto. Since there is such a variety of methods and the main elements such as "state", "action" and "reward" may be freely defined and implemented by a developer, this method is thought to be a very important one for machine learning techniques[9]. In this study, rather than using a specific reinforcement learning method, we propose a method which selects feature sets by calculating rewards received when an action

is performed in a state. In particular, this method does not only calculate the frequency of emotion transit but also the sum of the rewards for the evaluation of a feature selection. Therefore, this method has the advantage that the more frequently it contacts a user, the better its performance becomes. The outline of the paper is as follows, In Section II, it explains the emotion recognition method and Section III explains the proposed algorithm. The Section IV shows a simulation and result of using the proposed algorithm. Section V conclude and shows future works.

## 2 Emotion Recognition Method

This paper addresses emotion recognition by extracting features of speech. The emotion recognition with speech is largely divided into cases using acoustic information and language or discourse information. The former is a method that uses some feature sets such as pitch, formant, speech rate, timbre, etc. and the latter uses the meaning of a word. That is, whether the word is positive or negative to whether it represents a happy or sad state. The process of emotion recognition consists of collecting emotional speech, the acoustic analysis, implementing DB, feature set extraction and such features are trained and classified with emotions using a pattern classification method.

### 2.1 Database and Preparation

Emotional speeches were collected from 10 male graduate students. Their ages ranged from 24 to 31 years old and they were asked to say with 10 short sentences emotionally. The choice of the 10 sentences(scripts) was decided upon from the result of another survey or experiment. In the first stage, 30 sentences had been prepared and all the 30 sentences were asked to say by the subjects. After the recording, the speeches were listened to by other people and they were asked the question “What emotion do you feel when listening to the given

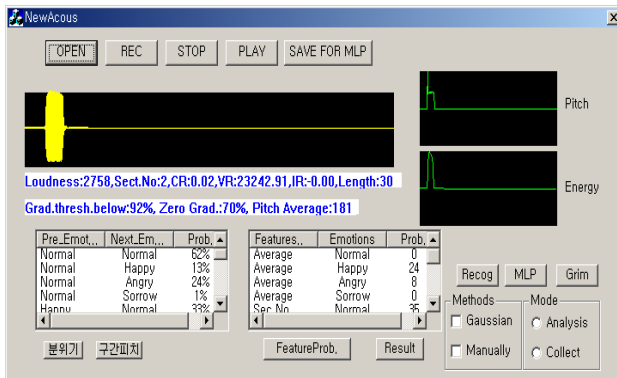


Fig. 1. Emotion recognition system

**Table 1.** Parameters of ANN

| Parameter        | Values                |
|------------------|-----------------------|
| Input Units      | 3~5                   |
| Hidden Units     | 11                    |
| Output Units     | 2                     |
| Learning Rate    | 0.003                 |
| Tolerance        | 0.25                  |
| Sigmoid function | $\frac{1}{1+e^{-3x}}$ |

recording?”. The emotions conveyed in the 10 sentences that were read and the answers given by the subjects in this experiment were in agreement 90% of the time. In addition, the length of the prepared sentences was limited from 6 to 10 syllables. The recording format was 11Khz, 16bit, mono and the subjects were asked to keep a distance of 10 cm between themselves and the microphone. Since the distance of the microphone affected loudness or intensity, maintaining the required distance was very important. Recorded files were preprocessed and stored in DB(MS-ACCESS). In the preprocessing stage, there were several processes to signals such as FFT (extracting spectrum), Pitch extraction (by an autocorrelation method), IR(Increasing Rate) of pitch, CR(Crossing Rate), VR(Variance), and statistical values etc[10]. Fig. 1 shows emotion recognition system we implemented, which has the function of recording, preprocessing as uttered above and pattern recognition.

## 2.2 Pattern Classification Method

We used an artificial neural network for pattern classification, which commonly performs well and is robust to a signal with noise. It has been the most popular method to use in the pattern recognition field. This method commonly uses a Back Propagation Algorithm for tuning network parameters. In this study, we fixed the setting to ANN as follows, The number of Input Units and Hidden Units and Output Units and Learning rate and Tolerance and Sigmoid function are 3~5 and 11 and 2 and 0.003 and 0.25 and  $\frac{1}{1+e^{-3x}}$ , respectively.

## 3 The Interactive Feature Selection Algorithm

Typically, researchers in the emotion recognition use various feature sets. Some researchers looked into the relation between acoustic analysis and emotion and used the feature sets based on that relation. However, because this method is subjective, it may easily lead to local minima. For this reason, recent studies consider a feature selection method for finding small superior features (4~10) out of as many as 30 to 90 features. Most researchers do not use all features because they cannot confirm whether they are valid or not and noises with every features may deteriorate. Therefore, feature selection methods are popular in the

pattern classification field[7]. According to John et al.[8], there are two main approaches to FS: filtering and wrapping. In the former, a feature subset is selected independently of the learning method that will use it. In the latter, a feature subset is selected using an evaluation method based on the same learning algorithm that will consider this subset of features. Although wrapper approaches have been shown to perform better, they can be rather time-consuming and it is sometimes infeasible to use them[7]. For this reason, the proposed algorithm tries to combine the characteristics of both the wrapper and filtering.

### 3.1 Reinforcement Learning Algorithm

Reinforcement learning consists of an agent and environment and is a learning method that leads the agent to perform a target action for a user. The process of learning is as follows, given an environment, an agent firstly performs an action and the agent receives a reward for the action from the environment. At that time, each time step is denoted as  $t$ , an environment state which the agent may include is denoted as  $s_t \in S$  ( $S$  is a set of possible environments) and an action is denoted as  $a_t \in A(s_t)$  ( $A(s_t)$  is a set of possible actions in a state). A reward for an action is denoted as  $r_t$  and when an episode has been completed, the  $r_t$  is expressed as the following equation.

$$R_t = \sum_{k=0}^T \gamma^k r_{t+k+1} \quad (1)$$

$\gamma$  is a discount coefficient in the above equation and does not make the sum of rewards an infinity in the case of being defined as  $t = \infty$ . In addition, if the discount coefficient is zero, it means that only the current reward value is admitted. That is, we can give the weight to a future value differently according to the discount coefficient. Finally, reinforcement learning is a method that determines a policy to maximize the eq. 1.

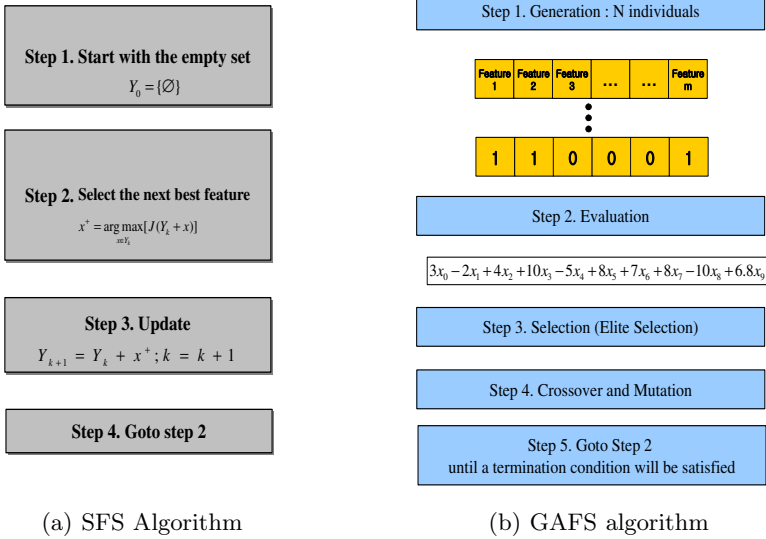
### 3.2 Sequential Forward Selection(SFS) Algorithm

Sequential Forward Selection is the simplest greedy search algorithm. In this paper, we will briefly explain this algorithm. The fig2(a) shows the algorithm. Starting from the empty set, sequentially add the feature  $x^+$  that results in the highest objective function  $J(Y_k + x^+)$  when combined with the feature  $Y_k$  that has already been selected.

### 3.3 Genetic Algorithm Feature Selection Algorithm (GAFS)

The Genetic Algorithm is popular method for finding an optimized solution. This algorithm has also good performance to the problems like nonlinear problems, which are hard to be solved by using the classic optimization techniques. The problem we are treating is also a nonlinear problem and thus, we think this problem may be solved by Genetic Algorithm. So, we tried to search good feature set using the Simple Genetic Algorithm. The fig.2(b) is the algorithm of the GAFS.



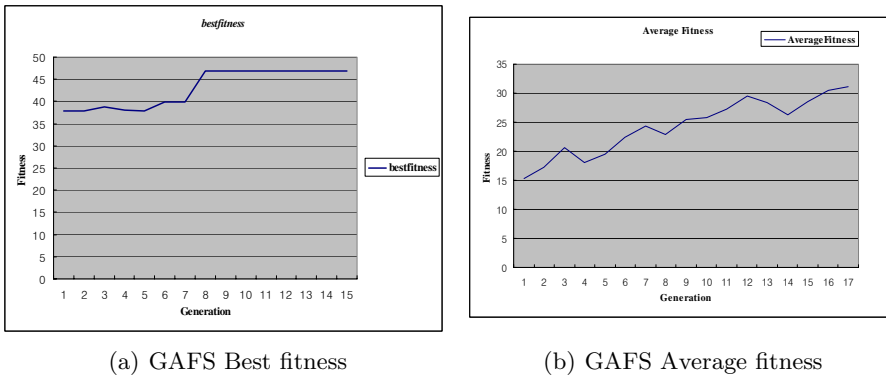


**Fig. 2.** SFS and GAFS algorithm

The fig. 3(a), 3(b) is the performance graph of Genetic algorithm feature selection. Because this method is included in the part of wrapping, an evaluation function is needed. So, the function which is used for evaluation is as follows,

$$3x_0 - 2x_1 + 4x_2 + 10x_3 - 5x_4 + 8x_5 + 7x_6 + 8x_7 - 10x_8 + 6.8x_9 \quad (2)$$

In the fig. 3(a), we can see the best fitness converged on the about 8 generations and the fig. 3(b) shows the average fitness is being increased. This simulation verifies that the GAFS is working well.



**Fig. 3.** Performance graph of GAFS ( Crossover rate: 0.5, Mutation rate: 0.02, Chromosome length: 10, Population No.: 100)

### 3.4 Interactive Feature Selection Algorithm (IFS)

The Interactive Feature Selection algorithm we are proposing is an algorithm based on reinforcement learning. Specially, popular algorithms such as SFS, SBS and so on, are deductive algorithms but our proposed algorithm is inductive. Also, these feature selection algorithms are based on the rationale of correlation and information-theoretic measures. Correlation is based on the rationale that good feature subsets contain features highly correlated with a class, yet are uncorrelated with each other. The IFS is also based on the correlation concept. Moreover, the feature selection algorithms consist of a search strategy and an evaluation by objective function but the conventional methods are incompetent in the search strategy part. Therefore, an IFS focuses on both the search strategy and evaluation by objective function. Fig 4(a) shows an IFS process. We assume that an emotion recognition system that includes this algorithm will be applied to a home robot or appliance. If such a situation is considered, users may be comfortable inputting emotional speech and a user’s emotional state at that time(as a supervisor value). Due to this characteristic, this algorithm is a user adaptive system that can efficiently solve a problem and the more a user is in contact with this system, the better it will perform. The fig 4(b) shows an example of the IFS algorithm and is based on the Fig 4(a). First, this algorithm starts with a full feature set and when a new feature set and an emotion identifier is inputted, it assigns a +1 or -1 to the “return sign”(if an old emotion ID equals a new emotion ID then +1, Otherwise -1). Thereafter, the product of “return sign” and the difference of each feature is stored in an array “Pointstorage”. This iteration is repeated for one

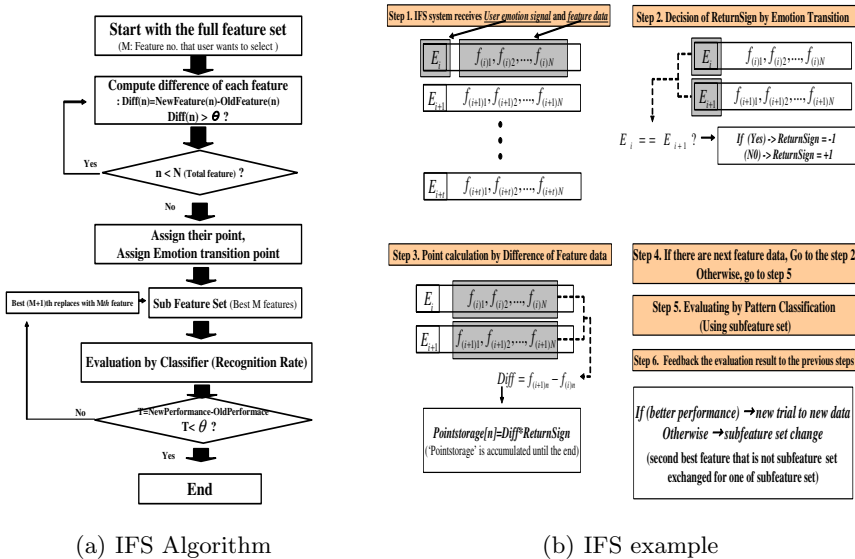


Fig. 4. IFS algorithm and an example

episode(user can arbitrarily define an episode). After the episode, the feature set that was selected first is applied to an objective function(Pattern Classification System) and the evaluation result is stored. If the next evaluation result is worse than the previous, the worst feature of the selected feature set will be replaced with the best feature among those that were not selected(step 6 in Fig 4(b)).

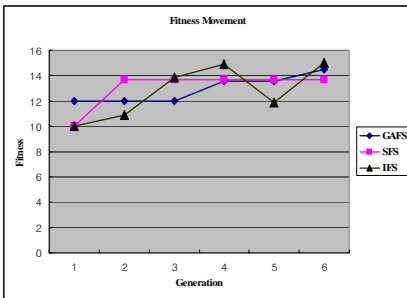
## 4 Experimental Results

### 4.1 Simulation and Results

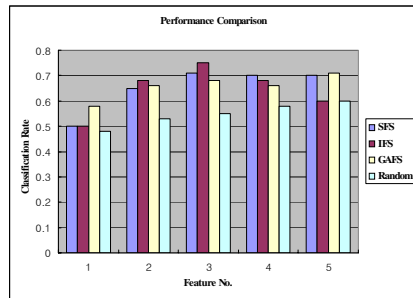
We applied 11 original features to the IFS simulator;Pitch features( max, min, mean, median, crossing rate, increasing rate), Loudness ;Intensity(max, min, mean),Sect.No and Speech rate. This program was made only for an IFS and the results from this program were applied to the Emotion Recognition System using ANN. That is, the feature set applied to ERS was the features previously outputted by IFS and then the emotion recognition experiment was performed. Classification was attempted using four methods. Results are shown in the fig 5(a) and 5(b). The fig 5(a) shows the fitness movement on every generation.

From the Fig 5(a),we can see that the IFS system searched for better SFS results and improved gradually. In the algorithm,because the searching work was performed again when the new evaluation result was worse than the previous one, there was some range in the steady state(The range of 3~5 and 6~8 in the Time axis). In addition, from Fig 5(b), this graph compares four methods(IFS, SFS, GAFS and random selection) with the changed feature no. As expected, random selection performed poorly but IFS and SFS and GAFS similarly performed better. In the IFS and SFS and GAFS case, the results show a subtle distinction but the IFS with features 1,2 and 3 was better. However, with features 4 and 5, SFS showed better results.

Fig 6 shows the selected feature set from IFS system.



(a) Fitness movement for 3 methods



(b) Emotion Classification Rate Comparison

Fig. 5. Experiment Result

| Feature No. | Features                                  |
|-------------|-------------------------------------------|
| 1           | Pitch Mean                                |
| 2           | Pitch Mean,Speech rate                    |
| 3           | Pitch Mean,Speech rate,Loudness           |
| 4           | Pitch Mean,Speech rate,Loudness, Sect.No. |

**Fig. 6.** Selected Feature Sets

## 5 Conclusions

This paper presents a solution to feature selection when there is an emotion recognition problem. The solution called an IFS performed as well as an SFS and GAFS. In particular, it is reinforcement based learning and supplements the role of search strategy in the feature selection process. Using the IFS simulator, we found some of the best features and used them in the emotion recognition experiment and results were compared to those of SFS and GAFS and Random selection. Performance was slightly better than SFS and GAFS. However, IFS has some disadvantages. If the amount of training data is too small, selection results may be not better than SFS. SFS does not require much training data. It is also sufficient that training data be only one set. If an objective function is clear, SFS will be adequate. However, in the case of emotion recognition, SFS may not perform as well as it had. In this case, the correlation-based method like the IFS will be better.

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# Unsupervised Feature Extraction for the Representation and Recognition of Lip Motion Video

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**Abstract.** The lip-reading recognition is reported with lip-motion features extracted from multiple video frames by three unsupervised learning algorithms, i.e., Principle Component Analysis (PCA), Independent Component Analysis (ICA), and Non-negative Matrix Factorization (NMF). Since the human perception of facial motion goes through two different pathways, i.e., the lateral fusiform gyrus for the invariant aspects and the superior temporal sulcus for the changeable aspects of faces, we extracted the dynamic video features from multiple consecutive frames for the latter. The multiple-frame features require less number of coefficients for the same frame length than the single-frame static features. The ICA-based features are most sparse, while the corresponding coefficients for the video representation are the least sparse. PCA-based features have the opposite characteristics, while the characteristics of the NMF-based features are in the middle. Also the ICA-based features result in much better recognition performance than the others.

## 1 Introduction

Recently the extraction of basis features from motion video has attracted a lot attention. Especially extracted features from lip motion may be utilized to recognize noisy speeches in cooperation with lip-reading [1] as well as to graphically synthesize the lip motion for Text-To-Speech applications [2].

Different decomposition techniques are applied for extracting basis elements of video images. Principle Component Analysis (PCA) had been widely used for feature extraction from images [3], while Non-negative Matrix Factorization (NMF) [4] and Independent Component Analysis (ICA) [5] have been applied recently. The PCA-basis features are non-local, and ICA results in localized basis features [6]. The NMF comes with non-negative constraints, and usually results in regional features, i.e., between the global and local features. The non-negativity of NMF and the sparsity of ICA are motivated from the biological neural systems.

In previous studies the features are extracted from single-frame images and the sequential nature of the motion video is not utilized. However, it is commonly

understood that the human perception of facial motion goes through two different pathways, i.e., the lateral fusiform gyrus for the invariant aspects of faces and the superior temporal sulcus for the changeable aspects of faces such as lip movement. [7] Therefore, the features of lip motion may be different from the features for the face recognition, and require more representation from consecutive multiple frames.

In this paper, we applied the 3 decomposition techniques, i.e., PCA, NMF, and ICA, to multi-frame lip videos. The effects of the time frames and statistical characteristics are investigated for both the extracted features and corresponding representation coefficients. The extracted features are also utilized for the recognition of lip motion, and the multi-frame features demonstrate better recognition performance than the single-frame features.

## 2 Feature Extraction Algorithms

Let  $\mathbf{s} = [s_1 \dots s_N]^T$  be the unknown basis image (features), and  $\mathbf{x} = [x_1 \dots x_N]^T$  be the observed image which are considered as the linear mixture of basis images. Here,  $N$  is the number of pixels in the images, and  $\mathbf{s}$  and  $\mathbf{x}$  are 1-dimensional re-shaped versions of 2-dimensional images by concatenating all columns. The mixing model can be written as the combination of  $\mathbf{s}$  and unknown mixing matrix  $\mathbf{A}$ , i.e.,

$$\mathbf{x} = \mathbf{A}\mathbf{s} \text{ or } \mathbf{X} = \mathbf{A}\mathbf{S} \quad (1)$$

where  $\mathbf{X} = [\mathbf{x}_1 \dots \mathbf{x}_M]$  and  $\mathbf{S} = [\mathbf{s}_1 \dots \mathbf{s}_M]$  are matrices consisting of all the observed and basis images as the columns, respectively, and  $M$  is the number of images. The feature extraction algorithms find the unknown basis images (features)  $\mathbf{S}$  and the mixing matrix  $\mathbf{A}$  from the observed images  $\mathbf{X}$  only. This is an underdetermined problem, and additional constraints are usually required. The popular choices are orthogonal basis images for PCA, linear independence for ICA, and non-negativity of NMF.

Principle Component Analysis (PCA) is probably the most commonly used technique for image processing tasks. PCA computes a set of orthogonal subspace basis vectors for an image database, and project the images into the compressed subspace. PCA generates compressed data with minimum mean-squared reproduction error, and is an unsupervised learning that produces global feature vectors. [3]

Non-negative Matrix Factorization (NMF) is a recently developed method for finding the representation of the data based on non-negative characteristics of biological neural signals. The non-negativity constraint of NMF only allows the addition of representation, and produces a part-based representation of the data which encodes much of the data using few active components [4].

ICA decomposes data image into linear combination of statistically independent mixtures. While PCA is based on the second-order statistics of the images, ICA decorrelates the high-order moments of the input in addition to the second-order moments. The ICA-based features are locally supported and usually very sparse [5].

### 3 Lip Motion Database

The lip motion videos employed for this research are the video part of the Tulips database [8], which consists of both video and audio data. The data set contains 96 digitized videos of 12 individuals (9 males and 3 females) saying the first four digits in English (“one”, “two”, “three” and “four”) twice. The images are made for every 1/30 second, and the number of image frames for each video clip is between 6 and 16. The original dataset consists of 934 images, with 65 x 87 pixels each with 8-bit gray levels. Ten corners of the lips are marked by human hands for each of the images.

The images were first corrected for the rotation based on the manually-specified critical points (corners) on the lip boundary. Then, the lip images are segmented and normalized in fixed size, i.e., 32 x 18 pixels. To reduce the computational complexity, each image was vertically cut into the left-half and the right-half, and considered as two different images. The dataset now consists of 1868 images of which each one is re-sampled into 16 x 18 (288 in total) pixels. All the feature extractions were done on these half-images. However, in all the subsequent lip figures, the full images were restored with left-to-right symmetry for easy visual understanding.

The iterative ICA algorithm requires extensive computation for the large number of images. For the efficient computation of the ICA-based features it is commonly adopted to get the essence of the original images using the PCA. In this paper the dominant 60 principal components, which approximate the frame-difference images with about 95% accuracy, are used for the extraction of ICA-based features.

### 4 Results

The  $n$ -frame database was obtained by considering the  $n$  consecutive frame images as an element of the database. Therefore, the  $n$ -frame images consist of  $288n$  pixels, while the number of the elements in the database becomes smaller. The PCA, NMF, and ICA algorithms are applied to these databases with the  $n$  from 1 to 4. The case of  $n=1$  actually corresponds to the case of single-frame method.

In Table 1 the numbers of principle components are shown for given representation accuracy with PCA. Also, the compression ratio, i.e.,  $C = (\text{Number of PCAs}) / (\text{Number of Pixels})$ , is shown. The number of principal components for a given accuracy does not change much on the number of frames. Therefore, the more frames are used, the more efficient features are extracted.

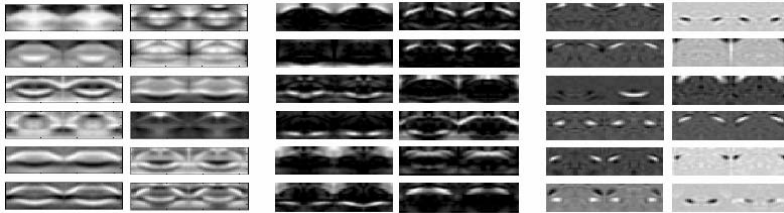
**Table 1.** Numbers of principle components and compression ratios for given representation accuracy

| Accuracy | Numbers of Principle Components |          |          |          | Compression Ratio |          |          |          |
|----------|---------------------------------|----------|----------|----------|-------------------|----------|----------|----------|
|          | Single Frame                    | 2 Frames | 3 Frames | 4 Frames | Single Frame      | 2 Frames | 3 Frames | 4 Frames |
| 90%      | 11                              | 12       | 14       | 15       | 0.038             | 0.021    | 0.016    | 0.013    |
| 95%      | 19                              | 23       | 27       | 30       | 0.066             | 0.040    | 0.031    | 0.026    |
| 99%      | 56                              | 78       | 95       | 109      | 0.194             | 0.135    | 0.110    | 0.095    |



In Fig. 1 the extracted lip motion features are shown for the cases of  $n=1, 2,$  and  $3$  for comparison. Only top twelve features, sorted by the variance of the corresponding coefficients and their accumulated values are shown for simplicity. The delta (difference in imaging condition) has been plotted on the second row of each basis components for the 2-frame and 3-frame cases. The increased delta value denotes the features are dynamic, and the multiple-frame approaches may be advantageous over the popular single-frame approach.

The efficiency of data representation may be related to the sparseness of the features and corresponding coefficient values. With only a few non-zero values, the sparse representation results in efficient data coding, transmission, and storage. A qualitative measure of the sparseness is kurtosis, related to the 4<sup>th</sup> order moments. Positive kurtosis denotes super-Gaussian distributions, and the higher value of kurtosis means only a few is enough to represent the data with less error. In Table 2, the kurtosis values are summarized. Unlike the PCA-based and ICA-based features/coefficients, the NMF-based features/coefficients do not have zero mean and the kurtosis is calculated after adding negative data for symmetry.



**Fig. 1.** Extracted lip motion features by PCA (*left figures*), NMF (*center figures*), and ICA (*right figures*) algorithms. Only features from 2-frames are shown for simplicity.

**Table 2.** Kurtosis values of extracted features and corresponding coefficients

| Feature Extraction Method | Features     |          |          |          | Coefficients |          |          |          |
|---------------------------|--------------|----------|----------|----------|--------------|----------|----------|----------|
|                           | Single Frame | 2 Frames | 3 Frames | 4 Frames | Single Frame | 2 Frames | 3 Frames | 4 Frames |
| PCA                       | 0.31         | 0.30     | 0.33     | 0.29     | 15.1         | 15.0     | 14.8     | 14.7     |
| NMF                       | 11.5         | 11.6     | 9.4      | 9.9      | 3.2          | 2.9      | 4.0      | 3.7      |
| ICA                       | 31.9         | 22.1     | 23.7     | 22.2     | 0.72         | 0.66     | 0.80     | 0.63     |

Using different number of frames to find the basis components, we found that the kurtosis values and the sparseness do not change much among the same decomposition method. The ICA algorithm has the greatest kurtosis for feature values. The PCA has the lowest value, and NMF is located between ICA and PCA. On the other hand, kurtosis values of coefficients are the other way around. Higher kurtosis value means there are more data concentrated near the zero. Since the efficiency of the data representation depends not only on the coefficient matrix but also the features matrix, it is difficult to predict the best technique based on the value of its kurtosis.

We also had conducted lip-motion recognition experiments based on the extracted features. Although Hidden Markov Model (HMM) is the popular choice for continuous speech recognition tasks, Dynamic Time Warping (DTW) is utilized here. The DTW shows similar performance for isolated-word recognition tasks [9], and also is more biologically-plausible with elastic neural networks. [10] To obtain better accuracy on the recognition rates with limited dataset, the  $N$ -fold hold-out methods with  $n=4, 6,$  and  $12$  divisions are incorporated. Actually 22 experiments are conducted for each algorithm and consecutive frame number, and the average recognition rates are summarized in Table 3. Also, to remove the effects of small number of frames for each word with 30 msec intervals, each video clip is interpolated to obtain simulated video clip with 15 msec frame intervals. Therefore, the  $(2N-1)$ -frame video clips are generated from the  $N$ -frame video clips, where  $N$  is between 6 and 16 in the Tulips1 database.

**Table 3.** Recognition rates (%) of lip motion video with different features and frame length

|     | Single<br>Frame | 2<br>Frames | 3<br>Frames | 4<br>Frames |
|-----|-----------------|-------------|-------------|-------------|
| PCA | 57.8            | 53.8        | 51.2        | 57.6        |
| NMF | 57.3            | 57.5        | 63.4        | 58.9        |
| ICA | 69.6            | 66.5        | 65.8        | 64.8        |

As shown in Table 3, the ICA-based features result in better performance than the PCA and NMF-based features. It shows the advantage of sparse local representation of the ICA-based features. On the other hand, provided enough numbers of features were used for the recognition, the multi-frame features do not improve the performance. It may come from the fact that the recognition performance is closely related to the representation accuracy, not to the number of frames in the features.

## 5 Discussion

Comparison of the feature extraction methods based on PCA, NMF, and ICA is not straight-forward. The efficiency of the data representation depends not only on the coefficient matrix but also the feature matrix, and their relative significance is dependent upon the applications.

While ICA results in much sparse features, PCA results in much sparse representation coefficients. The characteristics of the NMF-based features are between those of the PCA and ICA-based features. For telecommunication applications the sparseness of the coefficients is very important, and the PCA-based features may be more advantageous. For the recognition of lip motion it is shown that the ICA-based features are superior.

Also the number of frames affects on the sparseness. Since only a small number of features are needed for the videos of the same frame length, the multiple-frame features have higher compression ratio and becomes more advantageous in efficiency.

The lip motion synthesis may be done by adding and subtracting these multi-frame features. Combining these images will create a video clip of lip motion. Also, the lip-motion features and phonetic speech features will be combined for the audio-visual speech recognition. Provided the lip-motion features were associated to the phonetic features, it will also be applied to the lip motion synthesis in close correlation to the human speeches.

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# A Novel Method for Expanding Current Annotations in Gene Ontology

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**Abstract.** Since the gap between the amount of protein sequence data and the reliable function annotations in public databases is growing, characterizing protein functions becomes a major task in the post genomic era. Some current ways to predict functions of a protein are based on the relationships between the protein and other proteins in databases. As a large fraction of annotated proteins are not fully characterized, annotating novel proteins is limited. Therefore, it is of high demand to develop efficient computation methods to push the current broad function annotations of the partially known proteins toward more detailed and specific knowledge. In this study, we explore the capability of a rule-based method for expanding the current annotations per some function categorization system such as Gene Ontology. Applications of the proposed method to predict human and yeast protein functions demonstrate its efficiency in expanding the knowledge space of the partially known proteins.

## 1 Introduction

Since the gap between the amount of sequence data and the reliable function annotation in public databases is growing, it becomes an immediate task to predict and to characterize the function facets for increasingly identified proteins. Some current methods to predict function(s) of a protein are based on the sequence homologies between the protein and other proteins in protein databases. Roughly 20%-40% of proteins can not be characterized in this way, which is also prone to making errors when the sequence identity is below 40% [10]. In recent years, several more involved computation methods are developed for inferring protein functions with help of other information sources, including analysis of phylogenetic profiling based on the hypothesis that proteins with a similar function(s) are more likely to be in the same evolutionarily conserved protein family or cluster across organisms [13]; analysis of

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gene fusion events [6, 11]; analysis of gene expression data, by assuming the presence of a link between transcription similarity and function sharing [17]; and analysis of networks of protein-protein interactions which focus on neighboring nodes' functions in the network [10]. All these methods first identify the non-function relationships between a studied protein and known proteins, and followed by deriving (predicting) the function(s) of the protein based on the function knowledge of its associated proteins. Although many successes are achieved by using these methods, a large number of annotations remain incomplete and to be further characterized, perhaps via newly developed computation algorithms.

Most of current function prediction methods are limited in expanding the existing annotations because they were designed for predicting function(s) for new proteins, and thus lack the necessary mechanisms to integrate the partial knowledge depicted by the broader descriptions. As such, we propose a novel method for expanding function annotations, in which the correlations between different functions instead between proteins are studied. We explore Gene Ontology, a standardization of protein function descriptions using controlled vocabularies, to seek for the correlation patterns between various functions [1]. Based on the correlation profiles, we determine whether yet uncharacterized functions that a protein might have, or more specific function(s) could be annotated to the protein. There is a recent study [15] that attempts to use the partial function knowledge in Gene Ontology(GO) of genes and their expression profiles for further characterizing their functions (i.e., annotating to deeper GO terms). However, the researchers only analyzed the parent-child relationship and identified 14 learnable function terms among the significantly expressed genes.

Protein sequence data are one of the most abundant and reliable sources for inferring protein functions. Besides the homology search, the default method in many sequence databases such as SWISS-PROT, the protein sequence signature data achieved in InterPro [12], Prosite [7], PRINTS [2] and Pfam [3] provide alternative information and ways for inferring protein functions. The function of a protein might be obtained if it shares some signatures with the proteins of known functions. Nevertheless, this procedure can become complex when there is a many-to-many relationship in which one signature is conserved for many proteins or one sequence has a number of signatures. Obviously, a data mining tool that is able to efficiently learn and integrate high-dimension characteristics of an object is desired for gathering, analyzing and evaluating the information from the diverse sources. Decision tree algorithm stands out to be one of the best learners and is integrated into the Spearmint system [8] for characterizing proteins according to multiple signature matches. Our proposed approach with a decision tree as the learner adopts the categorization system inherent in the GO hierarchy. It differs from other function prediction methods in several aspects. First, it aims at expanding current annotations, and hence the proteins of partial knowledge become the targets to predict. Second, it is based on the correlation between the functions of proteins, i.e. the function attribute of proteins other than the attributes (e.g. transcriptions) used in the previous studies. Third, because of the nature, it fully utilizes the partial function knowledge that proteins already have. Hence, it is expected to have more power and prediction accuracy than an *ab initio* prediction algorithm that does not use the prior information. Base on the correlation

patterns between GO function classes, and the derived classifiers, we have analyzed human and yeast proteomes, and demonstrated that high true positive ratios for most predictions can be achieved. Meantime, we obtain the results for the relationships between learnability and GO function levels.

## 2 Methods

None of the biological functions acts in isolate. Instead many functions often work in a concerted way to perform a common task. On the other hand, a single protein may play an important role in different cellular processes and biochemical cascades. Such multiple function attributes of a protein can be used to identify several related functions because they share a common element (the protein). Based on the activity of the protein, it is also possible to deduce which pairs of functions are more likely co-activated or co-repressed under the protein state.

### 2.1 Correlations Between Different Functions in Gene Ontology

GO is used in this study to explore the correlations between functions. It provides a comprehensive source of structured knowledge of gene product function in terms of “molecular function”, “biological process” and “cellular function”. The function categorizations are represented with nodes (or called terms, classes) in a directed acyclic graph in which one node may have more than one parent node. Protein function knowledge annotated to the deepest GO nodes gives the most specific function description(s).

We often have rather abstract (broad) function knowledge for some proteins, which are annotated to one of few nodes at high levels of GO hierarchy [9]. Prior to further wet-lab function studies, expanding the current annotation is necessary. According to the GO structure, we define two types of correlations between different GO terms. As shown in Fig. 1a, two types of correlations are defined: inherited (e.g. parent-child) and non-inherited (e.g. between siblings) correlation.  $GO_i$  has two functionally more specific child nodes ( $GO_{i_1}$  and  $GO_{i_2}$ ). Its relation with  $GO_j$  is non-inherited although they may be involved in regulating a same or similar biological process. A novel protein with function  $GO_i$  will be judged whether it has the function  $GO_j$  or the functions describing the child nodes ( $GO_{i_1}$  or  $GO_{i_2}$ ) by a protein signature matching.

### 2.2 Data-Driven Discovery of Rules for Protein Function Classification Using Sequence Signatures

For the data mining process, given a dataset or training dataset of protein sequences with known functions, the goal is to establish the correlation between each pairs of GO function nodes by inducing a classifier(s) of high discriminating power for distinguishing this correlation from others using protein signature profiling. Then, the function for a novel protein sequence can be assigned if it fits a partition established by the classifier (or alternative classifiers). The schematic framework for the proposed algorithm is illustrated in Fig. 1b.

Fig. 1a

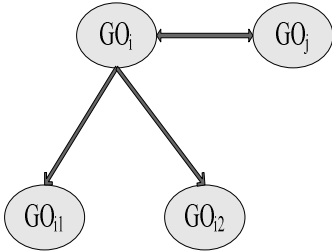


Fig. 1b

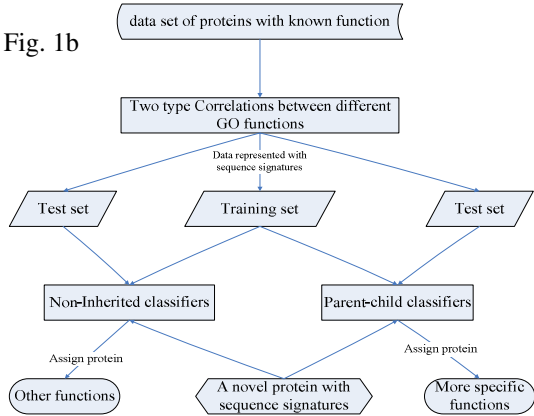
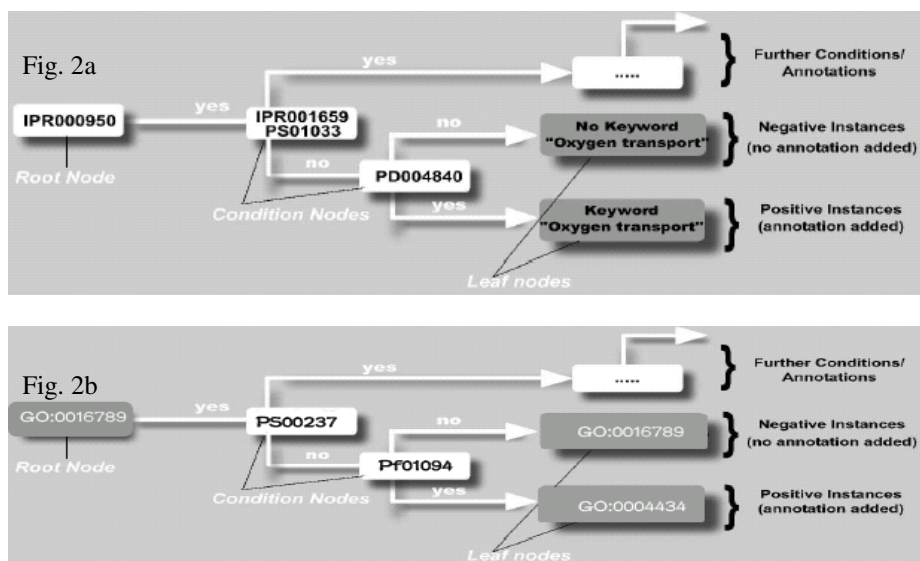


Fig. 1. (a): Two types of GO term correlations. (b): Algorithmic flow chart for expanding function knowledge.

### Data Representation and Decision Tree Algorithm

Most data mining algorithms aim to characterize instances with a reduced subset of a finite set of attributes. In this study, protein sequences (in addition to its function attributes) are described by a vocabulary of sequence signatures from the databases integrated by InterPro such as Prosite, PRINTS or Pfam. The data formulations are very similar to Spearmint system. Suppose that a set of proteins contain a total of  $N$  signatures (any protein may lack some of the signatures). A protein is thus encoded by an  $N$ -bit binary profile where the  $i$ -th bit is 1 if the corresponding signature is present in the protein, and zero otherwise. Note that each binary profile is also associated with a label that identifies the function of the protein.

We use the CART decision tree algorithm for building signatures-based classifiers. To illustrate the procedure, an example is given in Fig. 2, compared with Spearmint system. The employed decision tree algorithm classifies the proteins of the training dataset into positive and negative domains based on a reduced subset of protein signatures. The resulting tree consists of a root node, internal nodes and leaf nodes. The internal nodes, obtained from learning all the sequences documented in some secondary databases like Pfam or Prosite, capture significant signature features for partitioning protein samples, whereas the root node depicts the most broad annotation that all the trained proteins share, and leaf nodes give the sample partitions that the tree achieves. The proposed decision tree algorithm differs from Spearmint system in two aspects. First, we use the GO terms as function annotation (Fig. 2b) while Spearmint uses SWISS-PROT keywords (Fig. 2a), which can be seen from the leaf nodes. Second, we use existing function knowledge to divide classification space to induce a set of similar proteins, while Spearmint selects the proteins belonging to a same InterPro domain as training samples to learn a classifier. By predicting a novel protein from the root node (its current annotation) to a leaf node (its newly assigned function), we expand the function knowledge of the protein.



**Fig. 2.** (a): Decision tree that classifies proteins belonging to IPR000950. The Spearmint prediction is: “Add the Keyword “Oxygen transport”, if the protein belongs to IPR000950 (InterPro), but neither to IPR001659 nor to PS01033 (PROSITE) and if it has a hit to PD004840 (ProDom)”. (b): Decision tree that classifies proteins belonging to GO:0016789. The prediction rule is “Add the another annotation GO:0004434, if the protein has the annotation GO:0016789 and not belong to PS00237 (PROSITE), but has a hit to Pf01094 (Pfam)”.

### Local Classifiers for Two Types of GO Term Correlations

*Decision tree learning for non-inherited relationship:* we define the correlation between two GO terms (e.g.  $g_i$  and  $g_j$  in Fig. 1a) as non-inherited relationship if there is at least one protein whose annotation covers the annotations of two child proteins. First, we set  $g_i$  as the reference for defining the classification space and all the proteins annotated to it are used for the training dataset. An  $M$  matrix of protein signature attributes is constructed, where each row is an  $N$ -bit binary vector for a protein and each column corresponds to a signature. The matrix is then associated with a label vector whose elements are defined as  $g_{ij}$  if the corresponding protein (to a row in the protein signature matrix) has both annotations of  $g_i$  and  $g_j$  or  $\bar{g}_{ij}$  if the corresponding protein has  $g_i$  but not  $g_j$  annotation. Proteins labeled with  $g_{ij}$  are positive instances, and the remaining are negatives. Once a decision tree classifier is built by learning a training dataset, it is used to annotate a novel protein from  $g_i$  to  $g_j$ . Then,  $g_j$  is taken as the reference and a classification space is defined as above, followed by constructing the protein signature profiles and the label vector, building the classifier and making decision for a novel protein in a similar way.

*Decision tree learning for parent-child relationship:* Suppose that GO terms  $g_i$ ,  $g_{i_2}$ ,  $\dots$ ,  $g_{i_n}$  are child nodes of  $g_i$  and  $n \geq 2$ . Classifiers trained for this type of relationship are able to acquire a more specific annotation(s) described by one or



more child terms. Obviously, only proteins that have been annotated to child nodes are useful for learning the classifier. Here, we take the parent node  $g_i$  as the reference for defining the classification space that includes all the proteins annotated. For a given child node  $g_{i_h}$  ( $1 \leq h \leq n$ ), a protein is labeled with  $g_{i_h}$  (positive instance) if it is annotated to the node and otherwise  $\bar{g}_{i_h}$  (negative instance). Then, a decision tree is learnt for pushing the annotation of a novel protein from  $g_i$  to  $g_{i_h}$ . Note that there may be  $n$  classifiers to be learned for  $n$  child nodes. Generally, a specific classification space and an attribute matrix are constructed for each learnable correlation. A correlation is learnable only when both positive and negative instances are more than  $\lambda$ , a criterion used for selecting learnable correlations.

### 3 Results

The numeric experiment is to explore the potential of the proposed method for expanding the existing annotations. By dividing a dataset into training and test dataset, we are able to obtain an unbiased estimate of accuracy that a classifier can achieve. For this purpose, we adopt a 5-fold cross-validation in which the positive instances and negative instances are divided randomly into  $n$  parts of roughly equal size, respectively. A random combination of a positive part and one negative part constitutes a test dataset, and the remaining data are used as the training dataset. One cycle of an  $n$ -fold cross-validation produces  $n \times n$  pairs of training and test datasets, and also results in  $n \times n$  classifiers. We use precision ( $=TP/(TP+FP)$ ), where  $TP$  and  $FP$  are true and false positives, respectively), and recall ( $=TP/(TP+FN)$ ), where  $FN$  are false negatives), as the measure for classification performance since we are most concerned on how a classifier is right in its positive predictions.

#### 3.1 Performance from Human Proteome

In order to get the most accurate and comprehensive function annotation data, we use all the 9071 manually edited human proteins in GOA (Gene Ontology Annotation). GOA is a project sponsored by the European Bioinformatics Institute that aims to provide accurate assignments of gene products to the Gene Ontology (GO) database. In the first stage of this project, GO assignments have been applied to a dataset covering human proteome by using both electronic mapping and manual curation [4]. The download data are of direct annotations which are associated to the most specific nodes in GO. In GO, a gene annotated to a node is also annotated to its ancestor nodes of the same branch from the child node to root node. This upward propagation results in “general annotations”, based on which the correlations between GO terms (nodes) are analyzed.

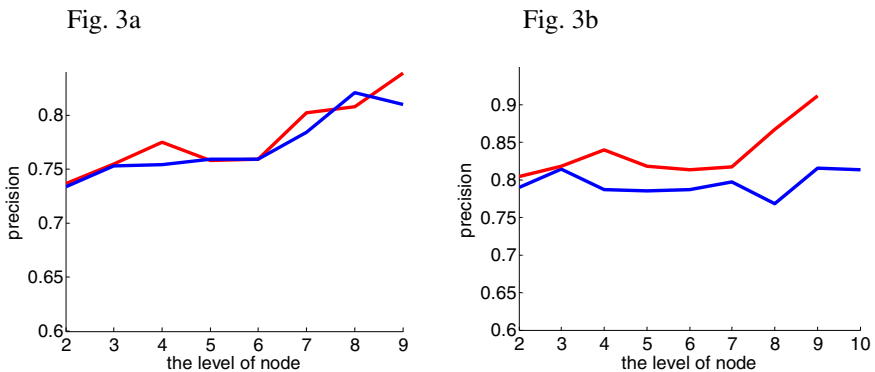
*Non-inherited relationship:* there are totally 71628 non-inherited relationships containing at least 10 proteins. For a numeric demonstration, we focus on the “Molecular Function” (MF) branch. The number of relationships is 2208, including 239 GO nodes if the criterion of 10 proteins (i.e.  $\lambda > 10$ ) is applied. Fig. 3a illustrates the relationship between classification performance and level of classification space (i.e. defined by  $g_i$ ), after removal of low-performance classifiers with precision  $< 50\%$ . As

a result, half of the remaining classifiers have a precision  $>75\%$ . In the range from level 2 to 9, precision rises slowly. The reason for the variation is that the more homogeneous the proteins are, the easier it is for the classifiers to learn the pattern. In Fig. 3b, the red line shows the non-inherited relationship classification sensitivity and the level of classification space, similar with precision, more homogeneous the proteins are, the more proteins are correctly predicted by the classifiers.

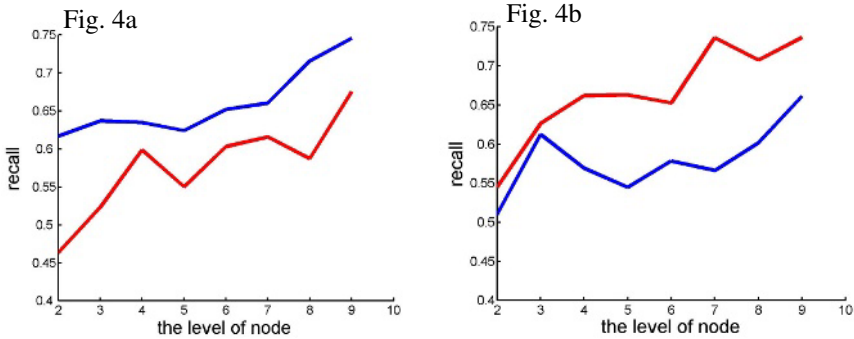
*Parent-child relationship:* we identify 316 learnable parent nodes with a total of 842 child nodes by using  $\lambda > 10$ . As illustrated in Fig. 3a, half of the classifiers have precision  $>81\%$ . Similar to the non-inherited relationship, precision rises slowly with the level of parent nodes increasing. Compared to the previous study [15], a much larger of function classes are analyzed, and the proposed algorithm reaches a deeper level (up to the 10th GO hierarchy versus the 7th in the previous study). We also estimate the precisions for the three dimensions of GO: molecular function: 87%; biological process: 72%; and cellular component: 77%, respectively. It appears that protein signatures are more informative for revealing “molecular function” than other two dimensions, which might also be the reason of only dimension of “molecular function” being investigated previously [14]. The blue line in Fig. 4a shows that the sensitivity of classifiers learned from parent-child relationship performs better than non-inherited relationship.

### 3.2 Performance from Yeast Proteome

Protein signatures diverged gradually between different organisms during the evolutionary trajectories, and hence can be good molecular features for reversely constructing a phylogeny [16]. The protein signature profiles for human are much more complex than yeast that may have better performance for function knowledge expansion. The function annotation data for yeast are derived from SGD [5]. Fig. 3b gives the performances of the classifiers trained on the yeast data. For non-inherited relationship, precision increases with the nodes of deeper levels being used, which is the same as observed in human data, but precision is higher, with half of the classifiers



**Fig. 3.** (a) The relationship between classification performance and the level of nodes for human proteins. (b) The relationship between performance and the level of nodes for yeast proteins. Red – non-inherited relationship; Blue – parent-child relationship.



**Fig. 4.** (a) The relationship between classification sensitivity and the level of nodes for human proteins. (b) The relationship between classification sensitivity and the level of nodes for yeast proteins. Red -- non-inherited relationship; Blue -- parent-child relationship.

having a value > 83%. However, for parent-child relationship, the trend is not so clear, possibly due to the fact that the classifiers might have achieved the nearly optimal performance so that further improvement is not obvious. Another limiting factor for the function classes of deeper levels is smaller sample sizes. Half of the parent-child classifiers have a precision > 76%. The classifiers' sensitivity performance is illustrated in Fig. 4b.

We only find one work related to function expanding [15]. In that work, they used gene expression data to further predict gene function in Gene Ontology and used neural network to train classifiers. They implemented the method on the small serum dataset consisting of 517 differentially expressed genes, and only 14 learnable parent nodes were selected. Compared to their work, we use sequence signature instead of gene expression data, and the samples are 9071 compared to their 517 genes. By this way, more learnable parent nodes (316 parent nodes) are selected. The average precision of 14 classifiers is 87.1%, 12 of which are also learnable in our work. Precision of the 13

**Table 1.** The learnable parent nodes and their performance based on either gene expression (Precision 1) or sequence signatures (Precision 2)

| Parent node                              | Precision 1 | Precision 2 |
|------------------------------------------|-------------|-------------|
| GO:0030003, cation homeostasis           | 0.95        | 0.88        |
| GO:0000279, M phase                      | 0.96        | 0.77        |
| GO:0046907, intracellular transport      | 0.75        | 0.70        |
| GO:0009653, morphogenesis                | 0.73        | 0.51        |
| GO:0042592, homeostasis                  | 0.93        | 0.90        |
| GO:0009058, biosynthesis                 | 0.73        | 0.80        |
| GO:0008202, steroid metabolism           | 0.95        | 0.80        |
| GO:0006350, transcription                | 0.99        | 0.90        |
| GO:0006351, transcription, DNA-dependent | 0.85        | 0.41        |
| GO:0006464, protein modification         | 0.77        | 0.78        |
| GO:0007600, sensory perception           | 0.95        | 0.79        |
| GO:0009607, response to biotic stimulus  | 0.90        | 0.76        |

classifiers are illustrated in Table 1. Compared to the precision for the three branches: molecular function: 87%; biological process: 72%; cellular component: 77%, their result is little better than ours. We think that the reason that their result is better is the smaller dataset. Since they had to use the differentially expressed genes, their dataset is only about 1/40 of ours in size. Consequently, the classifiers are easier to learn and the result is better. In comparison, we use much more learnable parent nodes. More importantly, our proposed algorithms can also consider non-inherited relationships. Naturally, we can further predict gene function both vertically and horizontally.

## 4 Discussion

Fragmentary knowledge for a large number of proteins as documented in public databases calls for studies for computationally expanding the current annotations. Though most *ab initio* function prediction approaches can accrue the number of current annotations by predicting the functions for totally unknown proteins, it is even more important to develop an efficient method(s) to expand the existing function annotations because as demonstrated in several studies including the present study, integrating the partially knowledge of a protein into a function prediction model is one of the most economical and promising ways to acquire the most accurate and specific function knowledge for a large number of proteins. This study describes such an efficient computation algorithm based on GO. We first define two types of correlations between function terms in GO hierarchy. Then, we identify the most important protein signatures for any pair of protein that follows either type of correlations in order to build a classifier for predicting a partially known protein. Next, a protein function expansion is realized by the prediction(s) of the classifier for the protein. This study suggests that protein signatures are informative and can be better features than gene transcriptions for function recognition. Protein signature data have advantages over gene expression data because they can be accurately characterized. In addition, use of sequence signatures rather than full-length sequences reduces the false-positive rate induced by multi-domains of proteins. Spear-mint system uses 800 Swiss-Prot keywords to predict protein function automatically and achieves very small error rates for predictions. The next effort of Spear-mint system is to further compile the annotations in GO, although analysis of more than 20 thousands function classes in GO can be formidable if without an efficient computational algorithm(s). Our results from analysis of protein signatures might provide some insights for large-scale function further annotations.

## Acknowledgements

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# Identifying the Modular Structures in Protein Interaction Networks

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**Abstract.** Identifying the modular structures in Protein Interaction Networks (PINs) is crucial to the understanding of the organization and function of biological systems. We propose a new module definition taking into account the degree of a subgraph instead of a vertice, and design a corresponding agglomerative algorithm, which is implemented into a computational tool called ModuleSpider, to recognize modules within a network. The application of ModuleSpider to the yeast core protein interaction network identifies 97 simple modules which are biologically meaningful according to the GO annotation of proteins in the modules. In addition, the results of comparison analysis demonstrate that ModuleSpider modules show stronger biological relevance. Further, the ModuleSpider is able to construct the interaction web of modules, which provides insights to the high level relationships of different functional modules. ModuleSpider is freely available upon request to the authors.

## 1 Introduction

Accumulating evidence suggests that biological systems are composed of individual, interacting modules [1,2,3,4]. Recently, high-throughput techniques, such as yeast two-hybrid screens [5] and affinity purification using mass spectrometry [6], accelerated the discovery of the complete Protein Interaction Networks (PINs) in several organisms. The complete dataset of interactions, for the first time, enables us to investigate the uncharted territories of the modular structures in PINs, leading to a deeper understanding of the organization, function and evolution of cellular systems.

Much effort has been put in the identification of biological relevant modules. According to the description of the connectivity of proteins, the available approaches can generally be dichotomized into two categories. One kind of approaches considers the PIN as a weighted graph by quantifying the connection between proteins. For example, Pereira-Leal et al. weighted a protein interaction based on the number of experiments supporting the interaction [7]. Arnau et al. weighted the distance between two proteins by the length of the shortest path between them [8]. However, in the traditional clustering methods to find functional modules within PINs, their strategies usually generate many identical distances and lead to a *tie in proximity* [9] problem. Meanwhile, Asthana et al. treated protein interactions probabilistically to predict

protein complex membership [10], which, unfortunately, ignores the dependence of types of evidence used.

The other kind of broadly adopted approaches employs binary representation of protein interactions without accounting for the quality or quantity of evidence that supports each interaction. Under this assumption, many researches focused on identifying cliques, where every pair of nodes tends to interact with each other, in the network [11,12,13,14,15]. However, the complete subgraph rarely appears in reality; thus the clique-finding methods inevitably neglect the peripheral edges, and the subgraphs which are not fully connected but truly biologically relevant. Another approach to identify modules based on the binary topology is to iteratively divide the network into smaller and smaller subnetworks, and recognize modules during the division. Girvan and Newman [16] proposed the concept of edge betweenness, which is defined as the number of shortest paths between all pairs of vertices that run through the edge. Edges between modules tend to have more shortest-paths running through them than do edges inside modules, and thus have higher betweenness values. The deletion of edges with high betweenness can separate the network, while keeping the module structure intact. Based on this principle, Girvan and Newman proposed a divisive algorithm (G-N algorithm) to construct a tree to find module structures in an unweighted network. As the original G-N algorithm does not include a clear definition of module, it cannot formally tell which parts of the tree are modules. Radicchi et al. [17] combined the G-N division process with two new module definitions and proposed a new self-contained algorithm to identify modules from a network. However, the module definitions they proposed may not be suitable for finding modules in biological networks because of several limitations within them.

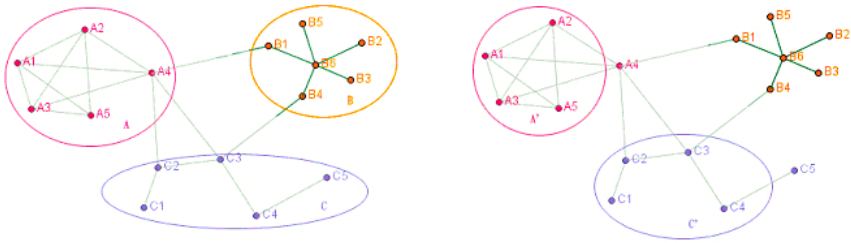
In this paper, we extend the concept of degree from vertices to subgraphs and propose a new quantitative definition of a module in a network. By combining this new module definition with the edges generated by the G-N algorithm, we propose a new agglomerative algorithm to identify modules in a network. A computational tool, called ModuleSpider, is developed based on this approach. ModuleSpider was applied to the yeast core protein interaction network from the Database of Interacting Proteins (DIP) [18]. Most modules identified are rich in significant co-occurrence of proteins of related biological functions, and exhibit lower P-values than the modules defined by Radicchi et al. We also compare the modules obtained by ModuleSpider with the quasi-cliques identified by the approach proposed by Bu et al. Further, ModuleSpider maintains the relationships between adjacent modules resulting in a network of modules. This higher-level interaction network between modules allows a system-level understanding of the relationship between modules representing different biological processes and functions.

## 2 Method

### 2.1 Definition of the Module

Many possible module definitions have been proposed [17,19,20]. Generally, a module in a network is a subnetwork that has more internal edges than external edges. A module definition must be able to capture the essence of this intuition. Radicchi et al.

extended the degree definitions to the vertices in an undirected graph and proposed two module definitions: strong modules and weak modules. Given an undirected graph, they defined the indegree of a vertex in a module as the number of edges connecting it to other vertices in the same module and the outdegree of a vertex as the number of edges connecting it to the vertices outside the module. For a strong module, each vertex has higher indegree than outdegree; and for a weak module, the sum of indegree is greater than the sum of outdegree of all vertices in the module. However, these definitions do not appear to follow the general understanding of a module precisely. Firstly, the determination of a strong module can be strongly influenced by the degree of a single vertex, which would neglect highly-connected peripheral nodes with high possibility of being members of the module. Secondly, in the weak module definition, the edges inside a subgraph have been counted twice, which will result in considering a subgraph, in which nodes are loosely grouping together, as a weak module (see Fig. 1). Thirdly, Radicchi et al. only test their module definitions on social networks, which are different from the biological networks. For example, the biological networks show strong disassortativity while most social networks do not [21]. Thus, the definitions of strong and weak modules may not be suitable for identifying biologically meaningful modules in biological networks.



**Fig. 1.** Examples of the limitations of strong and weak module definitions. In the left panel, all three subgraphs are not strong modules because each subgraph has at least one vertex (A4, B4, C3) that does not have more indegree than outdegree. Only one strong module, Module A' at the right panel can be identified by removing the highly-connected node from the Module A. In the weak module definition, even if a subgraph (C' at the right panel) has more external edges than internal edges (4 versus 3), it may still be considered to be a module.

To overcome these limitations, we extend the concept of degree from the individual vertex to the subgraph in order to characterize the connectivity of a subgraph in a graph (a graph is identical to a network in this paper):

**Definition of degrees of a subgraph.** Given a graph  $G$ , let  $E$  denote the edge set and  $E_{ij}$  denote the edge connecting node  $i$  and node  $j$  ( $E_{ij}$  and  $E_{ji}$  are identical in an undirected graph and only counted once in the formulas below), then, for a subgraph  $V \subset G$ , the indegree of  $V$  is defined as:

$$K^{in}(V) = \sum E_{ij}, \quad (1)$$



where both node  $i$  and node  $j \in V (i \neq j)$ . The outdegree of  $V$  is defined as:

$$K^{out}(V) = \sum E_{pq} . \quad (2)$$

where node  $p \in V$  and node  $q \notin V$ , or node  $q \in V$  and node  $p \notin V$ .

**Definition of a module.** Given a graph  $G$ , a subgraph  $V \subset G$  is a module if

$$K^{in}(V) > \alpha K^{out}(V) . \quad (3)$$

where  $\alpha$  is the module strictness tuning coefficient. To further distinguish different levels of modules in the network, we define the complex module and the simple module as follows.

**Definition of complex and simple modules.** A module is a complex module if it can be separated into at least two modules by removing edges inside it using the G-N algorithm. Otherwise, it is a simple module.

This module definition directly captures the general understanding of the module concept and it is very flexible. Similar to the approach of Radicchi et al, this definition is based on the relationship between internal and external links, rather than relying on internal links only [11]. Also, this module definition can be tuned to a stricter one by increasing the coefficient  $\alpha$ , otherwise to a looser one by decreasing  $\alpha$ . Interestingly, when  $\alpha=0.5$ , definition (3) is equal to the weak module definition proposed by Radicchi et al. Furthermore, this definition, based on the connectivity of subgraphs, makes it easy to define the adjacent relationship between modules.

**Definition of adjacent modules.** Given two modules  $U, V \subset G$ ,  $U$  and  $V$  are adjacent if  $U \cap V = \emptyset$  and there are edges directly connecting vertices in  $U$  and  $V$ .

According to the adjacent module definition above, we can easily deduce that: Given two modules  $U, V \subset G$ , If  $U$  and  $V$  are adjacent, the subgraph  $w=U \cup V$  is also a module. This deduction suggests that merging two adjacent modules will generate a complex module. Also, the definition of the complex module and the simple module implies that the separation of a simple module into two subgraphs using the G-N algorithm can at most generate one module.

## 2.2 Algorithm

We propose a new agglomerative algorithm to identify the simple modules of smallest size within a PIN, and implemented it into a computational tool, ModuleSpider.

Similar to conventional agglomerative algorithms, our agglomerative algorithm initially puts each vertex into a singleton subgraph. Then, the subgraphs are gradually merged to find the simple modules in the network. There are two important properties of our algorithm - the occurrence of merging and the order of merging.

As mentioned above, the order of deletion based on the betweenness in the G-N algorithm reflects the relative relationship between edges inside modules and edges between modules in the network. The later the edge is deleted, the more likely it is an edge inside a module. In ModuleSpider, the edge deletion order generated by the G-N algorithm is reversed and used as the merging order in the agglomerative algorithm. By

gradually adding edges to the subgraphs in the reverse order deleted edges, ModuleSpider assembles the singleton subgraphs into simple modules. As a key goal of this approach is to identify simple modules of smallest size, only the merge between two non-modules is allowed. And, once a simple module is identified, it will not be merged with other subgraphs. This merging scheme generates compact simple modules and prevents merging with loosely connected subgraphs. The agglomerative algorithm is summarized as follows:

1. The G-N algorithm [16] is run on the network until no edges remain, and the order of edge deletion is obtained.
2. An edge list is created in the reverse order of edge deletion in Step (1).
3. Initialize each vertex as a singleton subgraph with no edges.
4. Pop-up an edge from the top of the edge list.
5. If the edge connects vertices in the same subgraph, add it to the subgraph.
6. If the edge connects vertices in two different subgraphs:
  - 1) If the two subgraphs are both non-modules, Merge them, retain the edge, and:
    - a. If the merged subgraph is a ModuleSpider simple module, set it as a simple module.
    - b. Otherwise, go to Step (7).
  - 2) Otherwise, discard the edge and go to Step (7).
7. Repeat steps (4) – (7) until no edges are left in the edge list.

The computational complexity of the ModuleSpider algorithm is  $M^2N + M \approx O(M^2N)$ , where  $M$  is the number of edges and  $N$  is the number of vertices.

## 3 Results

### 3.1 Dataset

The dataset used in this study is the yeast core protein interaction network downloaded from the DIP database [18] (version ScereCR20060116). This interaction dataset is generated by filtering the large high-throughput protein interaction data using two different computational methods, the Expression Profile Reliability Index and the Paralogous Verification Method, to improve reliability of the interaction data [22]. After removing all self-connecting links, the final core protein interaction network includes 2554 yeast proteins and 5728 interactions.

### 3.2 Simple Modules Identified in the Yeast Core Protein Interaction Network

Using the strictness tuning coefficient  $\alpha = 1.0$ , ModuleSpider has found 192 compact simple modules, whose sizes range from 2 to 467 proteins, in the yeast core protein interaction network. All 192 simple modules together include 2158 of the 2554 proteins in the network. 97 modules (totally 1933 proteins) whose sizes are larger than 3 proteins are identified.

**Table 1.** Top 15 ModuleSpider modules with lowest P-value GO terms

| Module No. | GO term                                        | Cluster freq. <sup>a</sup> | Genome freq. <sup>b</sup> | P-value <sup>c</sup> |
|------------|------------------------------------------------|----------------------------|---------------------------|----------------------|
| 294        | Nucleocytoplasmic transport                    | 30/43                      | 112/7291                  | 1.17E-44             |
| 318        | Golgi vesicle transport                        | 28/32                      | 144/7291                  | 6.28E-44             |
| 339        | Actin cytoskeleton organization and biogenesis | 31/53                      | 105/7291                  | 2.76E-43             |
| 340        | Some biogenesis and assembly                   | 37/52                      | 249/7291                  | 1.47E-42             |
| 281        | Proteolysis                                    | 25/28                      | 164 /7291                 | 1.94E-38             |
| 337        | rRNA processing                                | 28/38                      | 170/7291                  | 7.41E-38             |
| 342        | Cellular morphogenesis                         | 40/117                     | 160/7291                  | 2.85E-36             |
| 236        | Hydrogen ion homeostasis                       | 12/12                      | 23/7291                   | 9.71E-31             |
| 243        | mRNA metabolism                                | 17/18                      | 188/7291                  | 1.72E-26             |
| 122        | mRNA 3'-end processing                         | 10/10                      | 21/7291                   | 3.92E-26             |
| 244        | Regulation of cell growth                      | 9/11                       | 11/7291                   | 2.22E-24             |
| 110        | Cyclin catabolism                              | 8/8                        | 12/7291                   | 5.38E-23             |
| 304        | Meiosis I                                      | 11/13                      | 58/7291                   | 6.20E-22             |
| 123        | ATP biosynthesis                               | 8/8                        | 20/7291                   | 3.20E-21             |
| 269        | Peroxisome organization and biogenesis         | 9/11                       | 38/7291                   | 1.54E-19             |

<sup>a</sup> The number of proteins in the module annotated with the GO term out of the module size. <sup>b</sup> The number of proteins in the module annotated with the GO term out of the total number of proteins in the yeast genome. <sup>c</sup> The probability that the co-occurrence of proteins with this GO term had occurred in a cluster of this size by chance.

To substantiate whether the modules found by ModuleSpider are biologically meaningful, we first obtain the GO annotation for each protein in the network downloaded from the *Saccharomyces Genome Database* (SGD) [23]. Manual inspection of the annotations shows that most modules are rich in proteins of similar functions. For example, all 12 proteins of module 236 belong to the hydrogen ion homeostasis; all 10 proteins in module 122 are related to mRNA 3'-end processing; all 8 proteins of module 123 (ATP1, ATP2, ATP4, ATP5, ATP6, ATP7, ATP17 and ATP18) are subunits of the mitochondrial ATP synthase complex, which is crucial for ATP synthesis; 9 out of 11 proteins in module 244 are involved in the regulation of cell growth, and when using the SGD GO Term Finder to designate these proteins to a common biological process (BP) category, it is indicated that only 11 out of 7291 proteins in the whole SGD repository belong to this category. These findings suggest that proteins identified within a ModuleSpider module are closely related in similar biological pathways and functions.

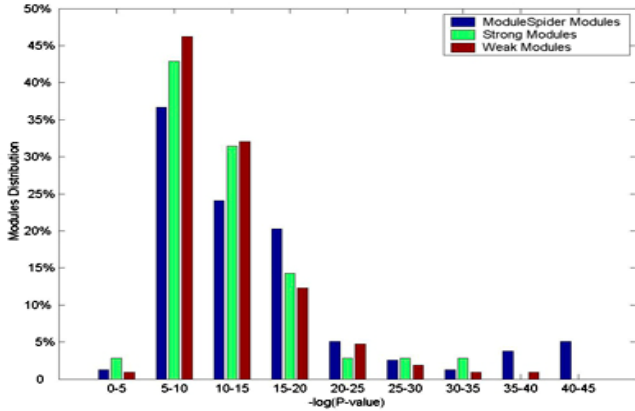
To further evaluate the biological relevance of ModuleSpider modules, we estimate the statistical significance of GO BP term co-occurrence using the SGD GO Term Finder. The results show that most modules (95%) demonstrate significant GO terms

enrichment beyond what would be expected by chance. If the P-value cutoff  $1.82E-5$  is used based on the Bonferroni correction, and if the modules with too large size ( $> 300$  proteins) are removed, there are 79 ModuleSpider modules left. The average lowest P-value of GO terms for all 79 modules is  $3.18E-7$ , ranging from  $1.01E-5$  to  $5.93E-44$ . We list a part of compact simple modules with lowest P-value GO terms in Table 1.

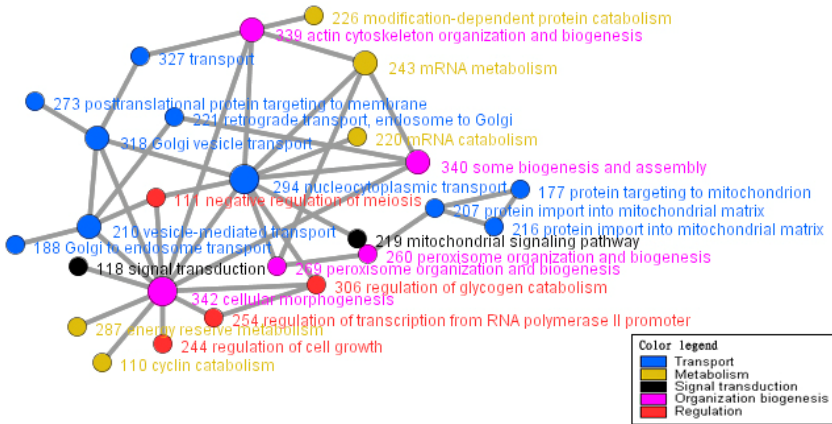
### 3.3 Comparison with Other Module Definitions

To test the effectiveness of our module definition, we apply the same agglomerative algorithm, from the same dataset as ModuleSpider to detect strong and weak modules defined by Radicchi et al. There are 41 strong modules obtained from the yeast core protein interaction network with their sizes ranging from 3 to 300 proteins. All 41 strong modules include only 236 of the 2554 core proteins. At the same time, 135 weak modules are identified with their sizes ranging from 3 to 300 proteins. There are total 1597 proteins in these weak modules. Similarly, we use the SGD GO Term Finder to quantify the statistical significance of the GO BP term co-occurrence in the strong and weak modules obtained. There are 35 strong modules that show significant GO terms co-occurrence (P-value  $< 1.82E-5$ ). However, the average lowest P-value of GO terms of the 35 strong modules is  $6.65E-7$ , which is higher than that of the 79 simple modules identified by ModuleSpider ( $3.18E-7$ ). For weak modules, 106 out of 135 weak modules show significant GO terms co-occurrence. The average lowest P-value of GO terms for these weak modules is  $5.29E-7$ , still less significant than that of the 79 ModuleSpider simple modules. Fig. 2 shows the distribution of lowest P-value GO terms for modules obtained by different module definitions. There are fewer high P-value modules and more low P-value modules in simple module groups obtained by ModuleSpider than in other two module groups. For example, there are 7 (9.0%) ModuleSpider simple modules with P-value lower than  $1.00E-35$ , but there is only 1 (0.9%) weak module and no strong module with such low P-values.

We also make a comparison between the modules obtained by ModuleSpider and the quasi-cliques obtained by the spectral analysis approach proposed by Bu et al [15]. We still use the GO Term Finder to quantify the statistical significance of the GO BP term co-occurrence of two kinds of modules, respectively. 44 of the 48 quasi-cliques show significant lowest GO BP term P-values, and the average P-value is  $4.19E-8$ , which is lower than that of the 79 ModuleSpider modules. However, the major limitation of Bu's approach is that the requirement of the quasi-clique is too strict; such stringency makes it hard to detect subgraphs whose nodes are not densely connected with each other but are truly biologically meaningful, such as the Arp2/3 complex in yeast [24]. A careful observation of the 48 quasi-cliques also validates the conclusion drawn above. In these 48 quasi-cliques, there is no quasi-clique consisting of less than 10 proteins, which, obviously contradicts our awareness of the formations of functional complexes in reality. Further, if we only consider the ModuleSpider modules whose sizes are no less than 10 proteins, the average P-value of the 25 ModuleSpider modules obtained is  $1.64E-8$ , which is more significant than that of the corresponding 48 quasi-cliques ( $4.19E-8$ ). Finally, to find all modules in a protein interaction network, the ModuleSpider algorithm is more efficient than Bu's spectral analysis approach, which has been proved to be NP-Complete.



**Fig. 2.** Distribution of different types of modules according to their lowest P-value of designated GO terms. Modules whose sizes are less than 3 or larger than 300 are not counted.

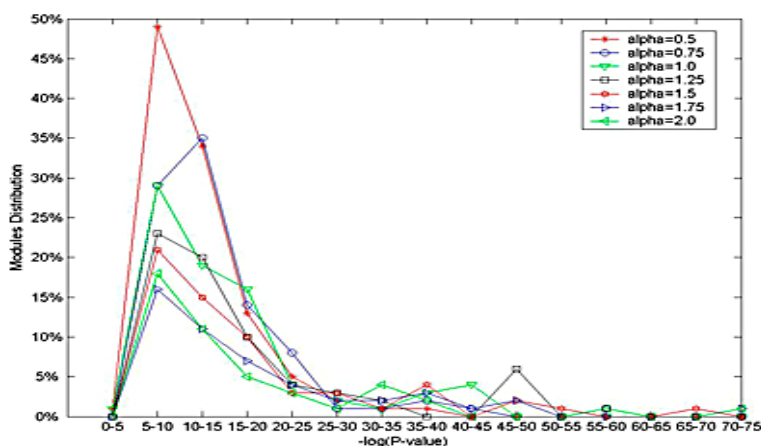


**Fig. 3.** A subsection of the interconnected module network. Each node denotes a module and each edge denotes a connection between two modules. Modules representing similar biological processes are shown by the same color.

### 3.4 Interaction Between Modules

In order to gain insights into how the ModuleSpider modules relate to each other within the cellular system, we assemble an interconnection network of the 97 simple modules identified by ModuleSpider from the yeast core protein interaction network. The network of modules is constructed as follows: for each adjacent module pair, the edge that is deleted last by the G-N algorithm is selected from all the edges that connect two modules to represent the link between them. The network of modules obtained is highly connected, which suggests that the cell is a complex web of highly interconnected functional modules. Fig. 3 is a subsection of this module network. In Fig. 3, the edges reflect the relationships between modules; the size of the nodes reflects the hub status

of modules - the bigger the node is, the more edges connecting the module to other modules. Although these relative relationships are based on the structural information in the network, many of them are biologically meaningful. In Fig. 3, highly connected modules are usually connecting to closely related modules and to other highly connected modules (hubs). For instance, Module 294 (nucleocytoplasmic transport) serves as a hub for related modules including Module 243 (mRNA metabolism), Module 219 (mitochondrial signaling pathway) and Module 269 (peroxisome organization and biogenesis). At the same time, this module also connects with other hubs such as Module 342 (cellular morphogenesis), Module 340 (some biogenesis and assembly) and Module 318 (Golgi vesicle transport). The network of modules provides a panoramic viewpoint of the relationship between different biological processes and functions represented in each module.



**Fig. 4.** Distribution of ModuleSpider modules according to the lowest P-value of designated GO terms, using 7  $\alpha$  values. Modules whose sizes are less than 3 or larger than 300 are not counted.

## 4 Discussion

The results of the ModuleSpider modules are obtained when the coefficient  $\alpha = 1.0$ . In order to analyze how different  $\alpha$  values affect the identification results, we test the GO BP term co-occurrence of the ModuleSpider modules using the same agglomerative algorithm with different  $\alpha$  values (from 0.5 to 2.0, with a step of 0.25). Fig. 4 shows the Distribution of ModuleSpider modules using 7  $\alpha$  values; Table 2 presents some statistics of the modules identified under different  $\alpha$  values. Statistics in Table 2 indicates that when  $\alpha = 1.25$ , modules identified by ModuleSpider exhibit lowest average P-value of GO term co-occurrence; and Fig. 4 also shows a peak of module accumulation within the  $[1.0E-45, 1.0E-50]$  bin compared with that of other 6  $\alpha$  values. Thus, it is suggested that more simple modules with high biological significance can be recognized by ModuleSpider when  $\alpha = 1.25$ .

**Table 2.** Statistics of ModuleSpider modules identified using 7 different  $\alpha$  values

| $\alpha$ | Significant Modules | Ave P-value | P-value < 1.0E-20 |
|----------|---------------------|-------------|-------------------|
| 0.5      | 106                 | 5.29E-07    | 8.5% (9)          |
| 0.75     | 92                  | 3.89E-07    | 15.2% (14)        |
| 1.0      | 79                  | 3.18E-07    | 17.7% (14)        |
| 1.25     | 69                  | 2.54E-07    | 23.2% (16)        |
| 1.5      | 61                  | 4.18E-07    | 24.6% (15)        |
| 1.75     | 49                  | 2.58E-07    | 30.6 (15)         |
| 2.0      | 46                  | 2.77E-07    | 26.1% (12)        |

## 5 Conclusion

In this paper, we extend the degree concept from the vertex to the subgraph and propose a new definition of module within a network based on the degree definition of the subgraph. A new agglomerative algorithm is designed to assemble simple modules from protein interaction networks, using the relative order of edges generated by the G-N algorithm as the merging order. The new approach has been implemented in the ModuleSpider program.

Application of ModuleSpider to the DIP yeast core protein interaction network identifies modules significantly rich in proteins of similar functions. These results imply that modules identified based on network structural information are biologically meaningful. Comparison with the strong and weak module definitions of Radicchi et al. shows that the ModuleSpider modules obtained are more biologically significant. ModuleSpider also casts superiorities upon the approach proposed by Bu et al.

Furthermore, the ModuleSpider can construct the network of modules conveniently. Manual evaluation of the module connections suggests that the interactions between modules are of biological significance.

In conclusion, the ModuleSpider algorithm and computational tool provides an excellent approach to decipher the modular structures of biological networks, which will deepen our understanding of the organization, function, and evolution of cellular systems.

## Acknowledgement

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# An Analysis of Gene Expression Relationships Between Periodically Expressed Genes in the HeLa Cells

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**Abstract.** The availability of increasingly accumulated time-series expression profiles has provided the data structures to study the temporal relationship between genes. The aims of the study were to explore the modes of relationship between the genes periodically expressed in human HeLa cell cycle, and to reversely engineer the dynamic networks of gene transcription. We also studied the phase-specific properties of the genetic relationships by decomposing the whole network into the sub-networks according to the cell cycling phases. The results demonstrated that the gene-gene relationships within a same phase or between different phases followed different modes.

## 1 Introduction

A cell cycle is often composed of four stages: G1, S, G2 and M phase. In normal tissues, cell division *in vivo* is precisely regulated by a cascade of events that determine when a cell is going to divide. Therefore, a proper regulation of the cell division cycling is essential for the growth and development of all organisms. Understanding these underlying regulation mechanisms is of great importance for studying many disease mechanisms where abnormal cellular behaviors are involved, most notably some cancers. There are many known and yet unknown molecular determinants that control the cell cycle or lead to the transition of normal cells into cancerous cells when mutated. These interferences can occur in any of the cell cycle phases: G1, G2, S and M or boundaries. It is one of the focuses in current cell biology and human genetics to understand the dynamic behaviors of these molecular interplays that regulate the cell cycle in both normal and cancer cells.

DNA microarray technology [1] has enabled researchers to simultaneously monitor the expression levels of thousands of genes. In the experiments of time-series gene

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expression, a comprehensive transcriptional profile of a gene can be obtained to capture its temporal trends and characteristics, by measuring its activities at different time points in a cell cycle. Up to now, the genome-wide transcriptional program during the cell cycle has been investigated in a wide range of the organisms. Some previous studies (e.g. [2]) focused on elucidating the gene relationships based on global correlation pattern over the whole time-course, and identifying the clusters of genes whose expression levels simultaneously rise and/or fall. Obviously, the global clustering algorithm is unable to distinguish the detailed dynamic facets of a gene relationship in the cell cycling. Therefore, in this study, a local clustering algorithm [3] is proposed to characterize four modes of temporal relationships: correlated, time-shifted, inverted and inverted time-shifted. We applied this method to analyze a HeLa cell cycle dataset, and revealed the relationships between the periodically expressed genes in the HeLa cells.

## 2 Materials and Methods

### 2.1 Gene-Expression Datasets

In this study, we used the expression dataset of HeLa cells [4] which were synchronized by three different methods, collected from five independent microarray experiments. The 1134 clones (representing 874 genes) that showed the most significant periodic variations during the cell cycle became our studied targets. Here, we only analyzed two datasets which were synchronized by double thymidine block methods (Thy2 and Thy 3).

### 2.2 Data Preprocessing

The expression data were normalized using a “Z score” method [5], so that for each gene the average expression ratio was 0 and the standard deviation was 1.

### 2.3 Local Clustering

The normalized expression level at time point  $i$  (or  $j$ ,  $i, j = 1, 2, \dots, n$ ) for gene  $x$  (or  $y$ ) was denoted as  $x_i$  (or  $y_j$ ). A “score matrix” was used for measuring the similarities between the expressions for genes  $x$  and  $y$ , and was defined as:

$$M(x_i, y_j) = x_i y_j. \tag{1}$$

Two summary matrices  $E_{i,j}$  and  $D_{i,j}$  were computed, with the initial conditions:  $E_{0,j} = 0$ ,  $E_{i,0} = 0$ ,  $D_{0,j} = 0$ , and  $D_{i,0} = 0$ .

$$E_{i,j} = \max(E_{i-1,j-1} + M_{i,j}, 0). \tag{2}$$

$$D_{i,j} = \max(D_{i-1,j-1} - M_{i,j}, 0). \quad (3)$$

An overall maximal *Score* value was found by comparing the two maxima for matrices  $E_{i,j}$  and  $D_{i,j}$ , representing the match *Score* for the two genes. If the maximum is off-diagonal in its corresponding matrix, the two genes have a time-shifted relationship. A maximal value from matrix  $D_{i,j}$  indicates the two genes have an inverted relationship, and otherwise paralleled (i.e. the maximal *Score* is from  $E_{i,j}$ ).

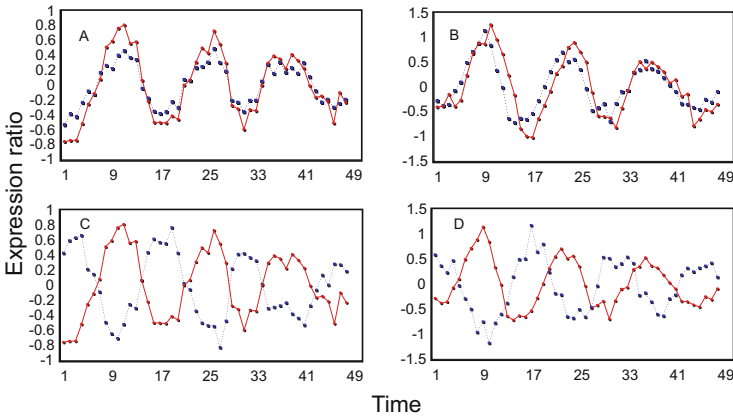
## 2.4 Statistical Significance Determined by Permutation Tests

A permutation statistic was used to determine the significance of an observed relation. One hundred sets of random expression profiles were generated by shuffling the normalized expression levels at different time points (e.g. interchanging their column (time point) locations). The P-value is the probability that the observed match *Score* is larger than any *Score* derived from the random profiles. The smaller P-value relates to the more significant *Score*. We set the critical value that corresponds to the 0.1% level of significance (P-value = 0.001). A statistically significant relationship was claimed if the match *Score* was greater than the critical value.

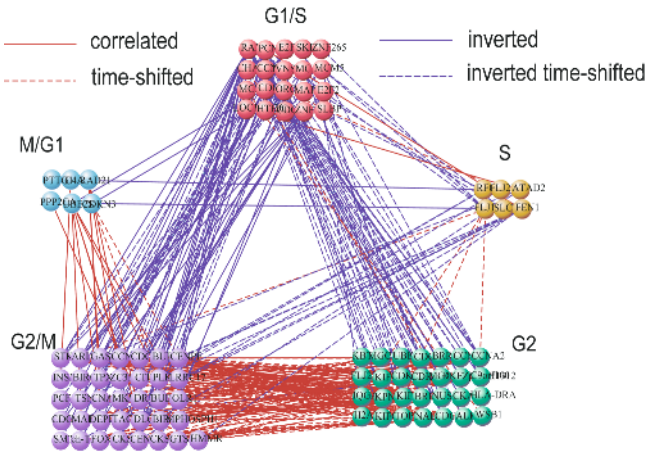
## 3 Results

### 3.1 Four Modes of Relationships

A total of 740 significant relationships were identified. Figure 1 shows the basic temporal characteristics of four relative modes (from analysis of the Thy3 dataset).



**Fig. 1.** Four expression relationships were found by a local clustering algorithm. (a) Simultaneous (correlated) relationship. (b) Time-shifted relationship. (c) Inverted relationship. (d) Inverted time-shifted relationship.



**Fig. 2.** Between-phase network. All expression relationships between different phases are shown. Each point represents a gene. Color is used to indicate the phase of the gene. Red solid and red dotted links indicate correlated and time-shifted relationships, respectively. Blue solid and blue dotted links indicate inverted and inverted time-shifted relationships, respectively.

### 3.2 Construction of the Relation Networks

To provide a picture view of the expression relationships, we built a network by globally clustering the HeLa cell cycle datasets. Then, we decomposed the whole network into two kinds of subnetworks: within-phase networks and between-phase networks.

#### Between-phase Networks

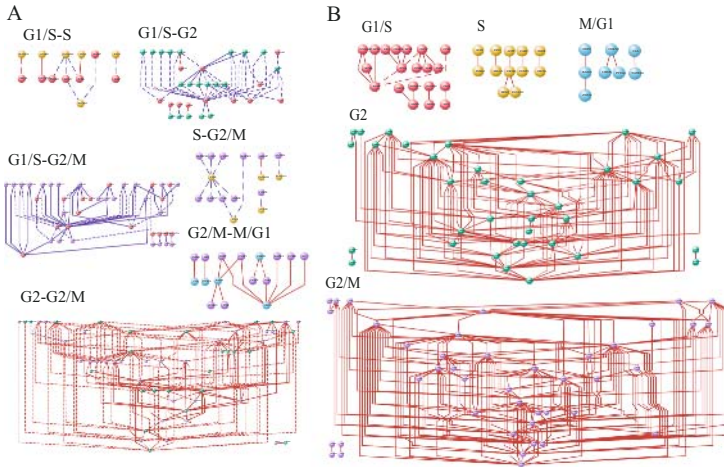
Figure 2 shows the between-phase network. Obviously, there is a triangle in this network, suggesting that the between-phase networking often occurred between the genes in the phase pairs of G1/S-G2, G2-G2/M and G2/M-M/G1. Figure 3A shows the more detailed between-phase sub-networks derived by direct peeling off the whole network. In G1/S-G2 sub-network most relationships are inverted time-shifted and in G1/S-G2/M most relationships are also inverted time-shifted. However, in G2-G2/M most relationships are time-shifted.

#### Within-phase Networks

We further constructed the within-phase networks (Fig 3B). To our surprise, we did not find any blue edge (i.e. inverted or inverted time shifted modes) in these sub-networks. Only positive relationships (i.e. correlated or time shifted modes) were observed in these within-phase networks.

## 4 Discussion

In each between-phase sub-network, some kind of relationships was predominant. For example, the majority relationships in G1/S-G2 and G1/S-G2/M sub-networks were inverted time-shifted. In G2-G2/M sub-network, the time-shifted relationship was the



**Fig. 3.** Between-phase sub-networks and within-phase networks. A) Between-phase sub-networks constructed by peeling off the whole network shown in Figure 2. B) Within-phase sub-networks per phase.

leading mode. In the within-phase networks, the majority were of the correlated relationships. Although the reasons for these patterns are largely unknown, they may reflect the inherent characteristics of the gene-gene interplays for the cell cycling. Integrating the functional knowledge of the genes (e.g. using Gene Ontology) may help elucidate the detailed molecular mechanisms for the cell cycling.

The further studies might be to probe deeply the unknown space of the built networks, for example, to find the hub genes. These important genes should play an important role(s) for phase transitions. We found that gene RAMP played a hub role in G1/S, G1/S-G2 and G1/S-G2/M sub-networks. RAMP is the gene that encodes RA-regulated nuclear matrix-associated protein. The protein, a serine/threonine-rich protein, is associated with the nuclear matrix protein, and is translocated from the nucleus to the cytoplasm during mitosis and cytokinesis. It has a significant role in the proliferation of the human embryonic carcinoma cells[6]. The transcriptional activity of gene RAMP is highly correlated with the cell proliferation rate of NT2 (human embryonic carcinoma cell line) cells. It has been demonstrated that overexpression of RAMP induces a transient increase in the proliferation rate of NT2 cells. The present study also indicates that RAMP may be an important hub in the gene networks for the HeLa cell cycling, which deserves a further verification with wet-lab experiments.

## 5 Conclusion

In summary, we found four modes of gene-gene relationships among periodically expressed genes that regulate the HeLa cell cycling. We constructed different kinds of gene networks to capture the dynamic and temporal properties of genetic regulations. The results demonstrated that the gene-gene relationships within a same phase or between different phases were inclined to follow different modes.

## Acknowledgements

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# Analysis of Sib-Pair IBD Profiles Using Ensemble Decision Tree Approach: Application to Alcoholism

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**Abstract.** There is currently a great interest in using single-nucleotide polymorphisms (SNPs) in genetic linkage and association studies because of the abundance of SNPs as well as the availability of high-throughput genotyping technologies. Here, we apply a novel ensemble decision approach to extract the relevant SNPs for alcoholism using sib-pair IBD profiles of pedigrees. The results indicate that ensemble decision tree is a promising algorithm for mining genetic markers for complex genetic diseases.

## 1 Introduction

Single nucleotide polymorphisms (SNPs) can be used as genetic markers that, in combination with other technologies, will help reveal the genetic basis of complex human diseases and enable medicines to be targeted to those patients likely to benefit. Alcoholism is a complex disorder in which multiple genes may contribute to the risk. To address this complexity, the Collaborative Study on the Genetics of Alcoholism (COGA) researchers designed a large-scale family study and collected multiple alcoholism and alcoholism-related phenotypes from the participants.

Current linkage and association methods have proven to be extremely successful in identifying genetic loci responsible for the development of diseases shown to have simple Mendelian modes of inheritance. However, most inherited diseases do not follow simple Mendelian patterns. The etiologies of these diseases are considered to be complex in nature, consisting of the interactions of multiple genetic loci as well as possible environmental factors. It is important to investigate how our current methodologies perform in the realm of complex diseases. For the time being, there have been a number of approaches for extracting alcoholism relevant SNPs from the Genetic Analysis Workshop 14 (GAW14) COGA data. For example, genetic algorithm-support vector machine hybrid [1] and sliding windows [2] have been used to mine alcoholism relevant SNPs.

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In this study, we extend our ensemble decision approach [3] for mining alcoholism relevant SNPs using the genome-wide SNP data generated for GAW14. Using the dbSNP [4] and the OMIM databases, we identified the SNPs close to some genes that are associated with alcoholism.

## 2 Methods

### 2.1 Defining the Phenotypic Attribute of a Sib Pair and Features to Be Mined

We extend our ensemble decision approach to sib-pair analysis of pedigrees. First, we define the phenotypic attribute of a sib pair, the affection status of a sib pair for alcoholism. For the binary trait, there are three possible attributes, of which two attributes are chosen to be the phenotypes for learning: both sibs in a sib pair are affected; and no sibs in a sib pair are affected. The genetic features are defined to be the estimated proportions of alleles shared IBD by the sib pair at the SNP positions, provided by the GENIBD of the SAGE package [5].

### 2.2 Mining Alcoholism Relevant SNPs

In this study, we use the Genetic Analysis Workshop 14 COGA real data sets to demonstrate the behaviors and properties of the proposed method for mining alcoholism relevant SNPs. For computational convenience, we perform the same analysis procedures separately for each investigated chromosome.

In order to build up multiple pairs of training sets  $\{L_d\}$  and test sets  $\{T_d\}$ , we introduce  $n$ -fold cross validation (CV), in which the data of each class is randomly divided into  $n$  roughly equal parts. For example, there are two classes, in each class the data are randomly divided into  $n$  non-overlapping subsets of roughly equal size, denoted as  $D_i (i = 1, 2, \dots, 5)$  and  $N_i (i = 1, 2, \dots, 5)$ . A random combination of  $D_i$  and  $N_i$  constitutes a test set and the rest of the subsets are used as the training set. The  $n$ -fold CV resampling produces  $n \times n$  pairs of training sets and test sets. We repeat the cross-validation  $M$  times and obtain  $n \times n \times M$  pairs of training and test sets.

Sib-pair IBD profiles can be described as an  $n \times p$  matrix,  $\mathbf{X} = (x_{ij})$ , where  $x_{ij}$  is the IBD value for the  $i$ th sib pair at the  $j$ th SNP locus. Our proposed ensemble decision method is a supervised-learning approach based on a recursive partition tree. The procedures of tree building are as follows. First, we split the dataset into two subsets, training set and test set. Then, a binary tree is grown on training set. By a recursive partition algorithm. The search for feature SNPs starts at the root of the tree and proceeds to its leaves. At each internal node, a decision is made with regard to the choice of a feature SNP and a threshold value (cutoff) such that the class impurity is reduced to a minimum when a branch is made by an induction rule. After the optimal bifurcation is made, the samples are divided into two non-overlapping subsets (two child nodes). For each subset, the same process is conducted successively until a leaf is



reached or stopping criteria for tree growth are satisfied. Here the impurity is assessed by Gini inequality index [3]. For each grown tree, one subset of SNPs is extracted and is tested on the sister test set. This process for feature selection is repeated on each pair of training sets,  $\{L_d\}$  ( $d=1,2,\dots,m$ ) and test sets,  $\{T_d\}$  ( $d=1,2,\dots,m$ ), which consequently forms the decision forest that is composed of an ensemble of SNP feature subsets,  $G_1, \dots, G_d, \dots, G_m$ ,  $G_d = \{g_1^d, g_2^d, \dots, g_k^d\}$ , or called SNP forests.

To test whether an extracted subset of SNPs (Tree  $G_d$ ) is able to significantly distinguish the affection status of a sib pair using the sister test sample ( $T_d$ ), we propose a  $\chi^2$  statistic:

$$\chi^2 = \frac{[n_{00}n_{11} - n_{01}n_{10}]^2 n}{(n_{00} + n_{01})(n_{10} + n_{11})(n_{00} + n_{10})(n_{01} + n_{11})} \tag{1}$$

where  $n=n_{00}+n_{01}+n_{10}+n_{11}$  and  $n_{00}$ ,  $n_{01}$ ,  $n_{10}$  and  $n_{11}$  are the frequencies for true negative, false positive, false negative and true positive, respectively. A Chi-squared test was carried out on a 2x2 table to see whether the extracted subset of SNPs (Tree  $G_d$ ) is able to significantly distinguish the affection status of a sib pair using the sister test sample ( $T_d$ ). This statistic follows an asymptotic Chi-squared distribution with one degree of freedom.

Based on the constructed SNP forests, we make an ensemble decision for selecting an alcoholism relevant SNP. Whether a SNP feature is relevant to the disease depends on the magnitude of its relevance intensity (or called an ensemble vote), FV.

For a particular SNP feature  $g_k$ , define:

$$FV(g_k)=F(G_1, G_2, \dots, G_m)=\frac{\sum_d \omega_d I(g_k, G_d)}{\sum_d \omega_d}, \tag{2}$$

where  $I(g_k, G_d)$  is an indicator function:

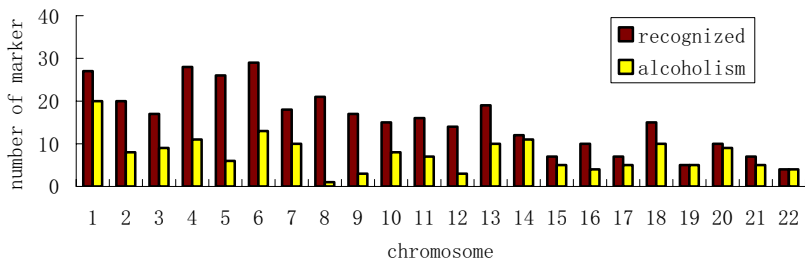
$$I(g_k, G_d)=\begin{cases} n_d^k & g_k \in G_d \\ 0 & otherwise \end{cases} \tag{3}$$

A weight,  $\omega_d$ , can be a measure for the classification performance of  $G_d$ , for example,  $\omega_d = \chi^2_d$  or set  $\omega_d=1$  for an equal weight for all the SNP feature subsets.

We resort to a permutation approach to generate the null distribution of  $FV$ , for which we randomly assign a phenotypic attribute to a sib pair. A critical value  $FV_{\beta}^0$  for a specified significance level,  $\beta$  (e.g. 0.05 in this study) is then obtained. A SNP feature is selected if its  $FV \geq FV_{\beta}^0$  (one-tailed).

### 3 Results

In this study, we perform a 5-fold cross-validation 20 times. Totally, we extract 344 significant SNPs at the 5% significance level, of which 166 are related to alcoholism (supported by the existing knowledge). The chromosomal distributions for the significant SNPs are shown in Fig.1. However, we focus our attentions on chromosomes 1, 4, and 7 (the results as shown in Table 1) because previous studies defined some regions on these chromosomes that may harbor several genes for alcoholism [6].



**Fig. 1.** The brown bar represents the SNPs we recognized with 5% significance level and the yellow bar represents the recognized SNPs related to alcoholism

In large-scale genome-wide association studies, ‘false positives’ can be a thorny problem. To see if the proposed ensemble decision approach can well control the number of ‘false positive’, we apply this method to the 100 simulated replicates for GAW14. The results from analyzing the simulated data demonstrate that we have successfully recognized all the simulation ‘answers’ or the SNPs closest to an answer, suggesting that the ensemble decision approach is robust and powerful in identifying the true loci for alcoholism. Nevertheless, the existing knowledge about the genes related to alcoholism in biomedical databases (e.g. NCBI GENE database) is very limited. Therefore, we view the results derived from this data analysis as exploratory, which might have support from the existing knowledge pool (i.e. in the manner of ‘knowledge validation’) or lacking of such a support waiting for further wet-lab experiment to verify their involvements in the pathogenic pathways to alcoholism.

**Table 1.** List of the significant SNPs on chromosomes 1, 4 and 7 (P<0.05)

| SNP Name  | Band     | Genetic Position | Alcoholism gene region |
|-----------|----------|------------------|------------------------|
| rs1171466 | 1p34.2b  | 39215299         | GRIK3(1P34-P33)        |
| rs1441523 | 1p34.3d  | 34069870         |                        |
| rs1408946 | 1p34.1e  | 42392561         |                        |
| rs1418490 | 1p36.23a | 7002001          | FRAP1 (1p36.2)         |
| rs1399437 | 1p36.13c | 18227689         |                        |
| rs1599169 | 1p36.31b | 4349628          |                        |
| rs320039  | 1p33b    | 48793370         | AKR1A1(1P33-P32)       |
| rs2896880 | 1p32.2b  | 56453092         |                        |
| rs1933392 | 1p33d    | 46803463         |                        |
| rs1079130 | 1p33b    | 49115058         |                        |
| rs728719  | 1p32.2a  | 57482150         |                        |
| rs2077402 | 1p13.2b  | 111186557        | CEPT1(1P13.3)          |
| rs1390474 | 1p31.3c  | 64748336         | ADH5P2(1P31.1)         |
| rs2388956 | 1p31.1b  | 80644475         |                        |
| rs1354061 | 1p31.3a  | 64467663         | CRYZ(1P31-P22)         |
| rs1775986 | 1p22.3b  | 86587517         |                        |
| rs3782    | 1p22.3c  | 85446633         |                        |
| rs066751  | 4q25f    | 112347992        | ADH5(4q21-25)          |
| rs1349629 | 4q21.21b | 75685262         |                        |
| rs1604153 | 4q21.22a | 78382893         |                        |
| rs951299  | 4q23a    | 99843682         | ADH6(4q23)             |
| rs720327  | 4q22.1   | 91866437         | ADH4(4q22)             |
| rs725386  | 4p15.33c | 12928421         |                        |
| rs2310396 | 4p15.1f  | 31912292         | PI4K2B(4P15.2)         |
| rs1113428 | 4p12a    | 44643625         | GABRA2(4p12)           |
| rs1349629 | 4q21.21b | 75685262         | DCK(4q13.3-q21.1)      |
| rs1604153 | 4q21.22a | 78382893         |                        |
| rs293441  | 4p13.3c  | 69495689         |                        |
| rs961489  | 4p13.2c  | 66079872         |                        |
| rs1005959 | 7q31.2a  | 112780691        | CHRM2(7q31-q35)        |
| rs1012709 | 7q32.2b  | 129770032        |                        |
| rs967919  | 7q22.1h  | 102532434        | TRRAP(7q21.2-22.1)     |
| rs717352  | 7q22.2a  | 103367208        |                        |
| rs1375670 | 7q22.1a  | 95057063         |                        |
| rs2887978 | 7q21.11e | 80899643         |                        |
| rs722471  | 7q21.3d  | 94572400         |                        |
| rs878903  | 7p15.1c  | 29559251         | NPY(7p15.1)            |

## 4 Discussion

We extend ensemble decision approach to a wide range of areas, in this paper, we apply it to mine alcoholism relevant SNPs. In summary, some potential candidate

regions on chromosomes 1, 4, and 7 linked with alcoholism susceptibility loci were found. These findings are consistent with previous reports [7]. Caution should be taken in interpretation of the SNP feature selection for alcoholism. Many causes can contribute the relevance of a SNP to alcoholism, for example, linkage disequilibrium between loci and gene-gene interactions, which require further genetic analysis to be clarified. For the time being, interactions are frequently at the center of interest in single-nucleotide polymorphism (SNP) association studies. When interacting SNPs are in the same gene or in genes that are close in sequence, such interactions may suggest which haplotypes are associated with a disease. The results show our approach delivers useful results and gives a competitive tool that facilitates the further study of global-view SNP relevance network(s) for alcoholism.

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# Association Research on Potassium Channel Subtypes and Functional Sites

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**Abstract.** Potassium channels, a group of membrane proteins and found in virtually all cells, are of crucial physiological importance for understanding cell biology and channelopathy. Studying the association of channel subtypes with their functional sites, and mining the functional sites mostly relevant to channel subtypes, can not only enhance molecular classification of potassium channels but only provide some clues for the functional targets. Here, we proposed to use functional sites profiles as features, where the functional sites are often used to characterize ion channels in biomedical research domains. We employed a novel integrated decision method to recognize the functional sites subset that is mostly relevant to the differentiation of potassium channel subtypes.

## 1 Introduction

Potassium channels, a group of special proteins in cytolemma, play critical roles in some important cellular processes such as the production of cell transmembrane current, and resting potential maintenance. The proteomic investigation of the potassium channels has been a focus in biomedical domains in recent years. All potassium channels implement their biological functions via some relevant functional sites, for example, kalium ion binding site, cuprum ion binding site etc. Inhibition of these sits can cause the loss of ion channel integrated activity leading to a list of disorders called channelopathy. Among these disorders, the channelopathy associated with the disruption of potassium channel is one of the most common types. Although biologists are able to localize the underlying functional sites for ion channels in laboratory by using X-ray crystal diffraction and nuclear magnetic resonance technique, these experiments are both too time-consuming and costly. Alternatively, with the rapidly accumulated biomedical data for ion channels, bioinformatics approaches such as various machine learning algorithm may provide the promises and were proposed to resolve the functional characterizations using the sequence

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conserved regions [1]. Typical algorithms include h-function algorithm,  $\Gamma$ -function algorithm,  $\Theta$ -function algorithm, Markov's chain model, vectorized sequence-couple model, and discriminant function algorithm. With more and more functional sites predicted and confirmed so far, how to make full use of these available data, and to establish the coherence and relevance between potassium channel subtypes and the functional sites become an immediate task in the proteomic studies of channelopathy.

Up to the present, no report for analyzing the relevance between potassium channels and their functional sites has been seen in literature. Here, we presented a bioinformatics approach to analyze and to evaluate the strength of relevance between the profiles of functional sites and ion channels. An ensemble approach based on decision trees [2] was employed to extract an optimal feature site subset(s) that was to precisely classify the studied potassium channel subtypes. In addition to identification of a functional site subset to achieve the maximal prediction accuracy, we also identified the functional sites mostly relevant to the ion channel subtype discrimination. An application of this approach to analyze the functional sites data from PDB [3] and PDBsite [4,5] is given to demonstrate its performance for mining relevant features based on the distribution of functional features over the decision forest using an ensemble voting approach.

## 2 Method

### 2.1 Constructing Functional Sites Profiles for Potassium Channels

First, we extracted channel subtypes and 3D structure information of potassium channels from 3D Protein Structure database (PDB). Then these data were annotated to the database of Protein's Functional site (PDBsite) to retrieve the corresponding information for functional sites. As a result, we constructed the functional sites profiles for potassium channels, which were linked with the phenotypic dimension of channels.

The potassium channel functional site profile can be described by an  $m \times p$  matrix,  $C = (c_{ij})$ , where  $c_{ij}$  describes the existence for the  $j$ th functional site ( $s_j$ ) on the  $i$ th sample  $C_i$ . When the subtype of an ion channel sample is known, the data for the sample consist of a vector of functional site profile,  $C_i = (c_{i1} \dots c_{ip})$  and a category label ( $y_i$ ). Suppose that the studied channel samples belong to  $K$  categories  $\omega_1, \omega_2, \dots, \omega_k$ . Define a class label,  $y_i$ , to be an integer from 1 to  $K$ . Let  $n_k$  be the number of samples in the  $k$ th category.

### 2.2 Constructing the Partition Tree

An  $n$ -fold cross-validation (CV) resampling technique was employed to build up pairs of training sets,  $\{L_d\}$  ( $d=1, 2, \dots, n$ ), and test sets,  $\{T_d\}$  ( $d=1, 2, \dots, n$ ), for learning and testing, respectively. For each resampling constructed pair,  $L_d$  and  $T_d$ , a recursive partition tree is grown on the training set  $L_d$  with the class impurity as the

criterion for tree splitting and the built tree was then tested on the holdout set  $T_d$ . Feature site selection proceeded in a manner that the best site was sought so that impurity was minimized at a node (say  $t$ ), from which a new bifurcation was attempted. Hence, the process of growing a tree parallels the process of recognizing future sites. When tree growth was stopped, a subset of feature sites,  $S_d$ , was obtained from the particular training set,  $L_d$ .

The above feature site subset building algorithm was applied to the multiple training sets and test sets, generated by the  $n$ -fold cross-validation resampling technique. Consequently, a set of feature subsets were obtained by inducing the decision trees, denoted  $\{S_1, S_2, \dots, S_n\}$ . For a feature functional site, whether it is relevant to channel subtypes depends on the magnitude of its relevance intensity (or called an ensemble vote),  $FV$ . For a particular feature site  $s_k$ , define:

$$FV(s_k) = F(S_1, S_2, \dots, S_n) = \frac{\sum_d \varpi_d I(s_k, S_d)}{\sum_d \varpi_d}, \quad (1)$$

where  $FV \in [0, 1]$ , and  $I(s_k, S_d)$  is an indicator function:

$$I(s_k, S_d) = \begin{cases} 1 & s_k \in S_d \\ 0 & \text{otherwise} \end{cases}. \quad (2)$$

A weight,  $\varpi_d$ , can be a measure for the classification performance of  $S_d$ , or for simplicity,  $\varpi_d = 1$  for an equal weight for all the feature subsets. To determine the significance of a candidate subset of functional sites, we resorted to a permutation approach [2] to simulate the null distribution of  $FV$  and to identify the significance cut-off value, denoted as  $FV^*$ .

### 3 Data

We obtained the data on 62 functional sites for 45 potassium channels, by first retrieving 66 potassium channels from the Protein's 3D Structure Database (PDB) and then annotating to the PDBsite database where knowledge about protein functional sites is stored. The extract potassium channels belong to three subtypes: voltage-gated, calcium-gated and inward rectifier potassium channel. To better characterize the functional sites, we designed three types of profiles, each being a 45-by-62 matrix with a row a channel and a column a functional site. In the first profile (or called existence profile), the functional features were coded as defined by equation (3), i.e. the binary values for existence or absence of a functional site. The feature in the second profile (or called intensity profile) was an integer that corresponds to the repeated number of the feature site that a channel has. By using this information, we

$$c_{ij} = \begin{cases} 1 & \text{if site exists} \\ 0 & \text{otherwise} \end{cases} \quad (3)$$

expected to capture the accumulated effect of a functional site. Finally, to reveal the randomness of a feature site, we construct a random profile, in which each element with a non-zero value in the first and second profiles was substituted by a random value from 1 to 10. We applied the tree-based ensemble method to the three profiles for mining the functional sites that are most likely relevant to the partition of the three subtypes for potassium channels.

## 4 Results and Discussion

### 4.1 Two Classes Problem and Significant Level

We developed successfully a novel tree-based ensemble method to resolve classification problem of two-class sample and obtained satisfactory result. For example, we applied this ensemble method to gene expressional profile datasets for mining feature genes which related to disease. Here, we extended the application of this method to multi-class sample. The strategy is changing multi-class sample to two-class sample by taking out one class as the exist-alone-class in turn, and incorporates other classes as a new one. With this strategy, a three-class sample profile was changed into three two-class sample datasets (called voltage-gated, calcium-gated and inward rectifier datasets). Applying 4-fold cross-validation (CV) resampling technique to these datasets to generate training sets and test sets. Finally, we obtained 320pairs of training and test sets in all.

### 4.2 Effect of Site's Intensity and Subtype-Specific Phenomena

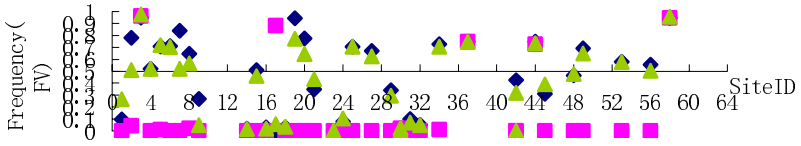
Compared the results of existence profile and intensity profile, we found that the sites identified from intensity profile had distinct difference and convergence in distribution. See Fig.1 (a) for example, there were 5 sites' frequency upon 0.7, while other sites' frequency below 0.05. It's easier for us to make estimate of subtype-related-sites. The reason of this phenomenon was that not only the existence but also the intensity of functional sites relevant to the subtype of the potassium channel.

During the compare of the sites identified from existence profile and random profile, we found that they had the similar distribution. The reason of this phenomenon was that the random intensity had no relevancy to the subtype of the channel. This phenomenon also confirmed our hypothesis that the intensity of sites had relevancy to the subtype of the channel.

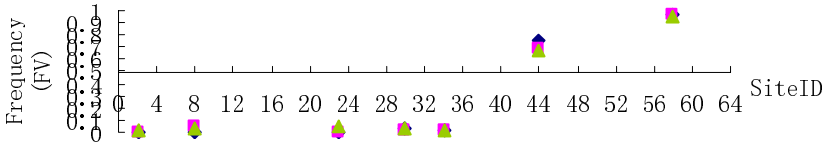
Compared the results of Voltage-gated dataset and calcium-gated dataset, see Fig.1 (b), we found the sites identified from Voltage-gated dataset had same distribution among existence profile, intensity profile and random profile. It means the relevancy of site's intensity and the subtype of the channel has Subtype-specific.



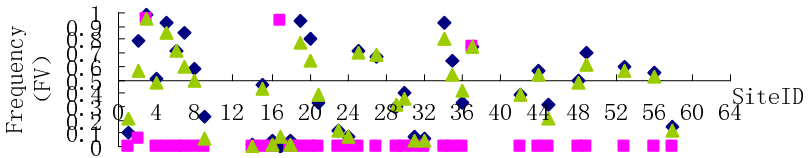
(a)



(b)



(c)



**Fig. 1.** a) The result of the voltage-gated dataset. b) The result of the calcium-gated dataset. c) The result of the inward rectifier dataset. Blue diamond, red square and green triangle means the site mining from the existence profile, the intensity profile and the random profile respectively.

Here, we choose  $FV^* = 0.5$ , the frequency of feature site more than  $FV^*$  was identified as the sites that had most relevant to the subtype of the potassium channel.

The results had been listed in table1. In table 1, the site of number 3, Copper Iron binding site, has the highest frequency in the result, which means that it has most relevant to the subtype of potassium channel. Luckily, this result had been confirmed by experiment. In 2003, F.J. Morera and D. Wolff reported that copper ion was one kind of important inhibitor of voltage-gating potassium channel; it inhibits the potassium channel by changing the gating kinetic properties of the channel [6]. In this paper, we applied a tree-based ensemble method to mine the functional site and got a set of functional site that most relevant to the subtype of potassium channel. By contrasting the result of the three profiles, we also found that not only the existence but also the intensity of the functional sites had relevant to the subtype of the potassium channel. In future, we'll try our best to research the similarity of these functional sites in structure and sequence.

**Table 1.** The functional site that most relevant to subtype of potassium channel from the intensity profile

| Dataset                  | Site ID | FV   | Notation                   | Site ID | FV    | Notation                 |                                                           |
|--------------------------|---------|------|----------------------------|---------|-------|--------------------------|-----------------------------------------------------------|
| voltage-gated dataset    | 44      | 0.73 | Metal atom in binding site | 562     | 58    | 0.947                    | Residues making water-mediated hydrogen bonds with ribose |
|                          | 37      | 0.75 | EGL Binding site           |         |       |                          |                                                           |
|                          | 17      | 0.88 | GOL binding site           | 3       |       |                          |                                                           |
| calcium-gated dataset    | 44      | 0.69 | Metal atom in binding site | 562     | 58    | 0.969                    | Residues making water-mediated hydrogen bonds with ribose |
| inward rectifier dataset | 37      | 0.75 | EGL binding site           | 3       | 0.963 | Copper Iron binding site |                                                           |
|                          | 17      | 0.94 | GOL binding site           |         |       |                          |                                                           |

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# Nonequilibrium Model for Yeast Cell Cycle

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**Abstract.** In the living cells, molecules including proteins, DNAs, RNAs and so on, with interactions between them cooperate as networks that govern various cellular functions. In this paper, a stochastic model with trigger mechanism is proposed based on what are known about the genes and proteins controlling the cell cycle of budding yeast. With respect to the biological observations, it looks more natural and understandable than deterministic dynamical model and our former stochastic model. Our model vividly describes that the protein interaction network goes through the biological pathway and forms an endless loop.

## 1 Introduction

The emergence and development of many high-throughput data-collection techniques, such as microarrays [1], protein chips or yeast two-hybrid screens [2], automated RTPCR and 2-D gel electrophoresis help us to simultaneously obtain the status of a cell's components and determine how and when these molecules interact with each other. It presents an opportunity to infer the real gene networks from experimental observation. Meanwhile it stimulates quantitative understanding of biological systems and functions from their components and interactions. Recently, a considerable amount of attention has been paid to the quantitative modeling and understanding of the budding yeast cell cycle regulation [3,4,5,6,7,8,9,10,11,12].

In particular, Li *et al.* [5] introduced a deterministic Boolean network model and investigated its dynamic and structural properties. In Li's work, the network was both dynamically and structurally stable. Seven global attractors of the dynamics were identified but only one could be interpreted as a biological stationary state, and the corresponding attracting trajectory as a biological pathway. We further advanced a stochastic model [13] based on Li's model, in which only the biological stationary state and the pathway were conserved under a wide range of noise level. We used a pseudo potential function to describe the dynamic landscape of the system and the biological pathway was considered as a valley in the landscape [14,15]. Unfortunately, those former works were all built upon equilibrium systems without concerning of extern signals such as cell size. In fact, the biological cell cycle is an endless progress accompanying with positive entropy production and thus a nonequilibrium system. In this work, we introduced a nonequilibrium stochastic model for yeast cell cycle.

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where

$$P_r(s_i(t + 1) = \sigma_i | s_1(t), \dots, s_{11}(t)) = \frac{\exp(\beta(2\sigma_i - 1) \sum_{j=1}^{11} a_{ij}s_j(t))}{\exp(\beta \sum_{j=1}^{11} a_{ij}s_j(t)) + \exp(-\beta \sum_{j=1}^{11} a_{ij}s_j(t))},$$

if  $\sum_{j=1}^{11} a_{ij}s_j(t) \neq 0, \sigma_i \in \{0, 1\}$ ;  
and

$$P_r(s_i(t + 1) = s_i(t) | s_1(t), \dots, s_{11}(t)) = \frac{1}{1 + e^{-\alpha}}, \tag{2}$$

if  $\sum_{j=1}^{11} a_{ij}s_j(t) = 0$  and  $\{s_1(t), \dots, s_{11}(t)\} \neq \{0, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0\}$ ;  
and

$$P_r(s_{cln3}(t + 1) = 0 | S(t) = \{0, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0\}) = \frac{1}{1 + e^{-\gamma}}, \tag{3}$$

We define  $a_{ij} = 1$  for a positive regulation of protein  $j$  to protein  $i$  and  $a_{ij} = -1$  for a negative regulation of protein  $j$  to protein  $i$ . If the protein  $i$  has a self-degradation loop,  $a_{ii} = -0.1$ . The positive constants  $\alpha, \beta$  and  $\gamma$  are temperature-like parameter characterizing the noise in the system [16]. Especially,  $\gamma$  plays a trigger role, so  $0 < \gamma < \alpha$  and the last equation act as an extern cell size signal.

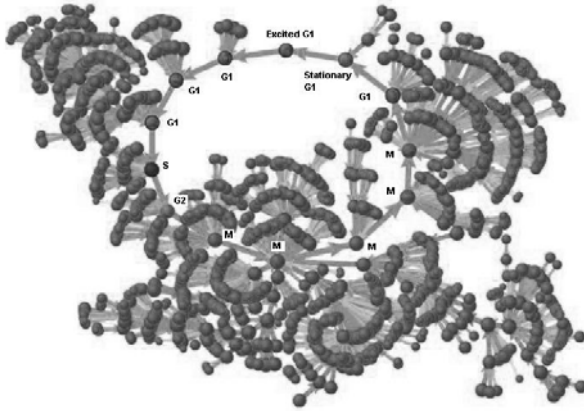
The Markov chain is ergodic since it consists of finite states and is irreducible. The steady-state probability distribution can be estimated by the simulation of stochastic processes as follows:

$$\pi_n = \frac{\#n}{\sum_{m=0}^{2047} \#m}, \tag{4}$$

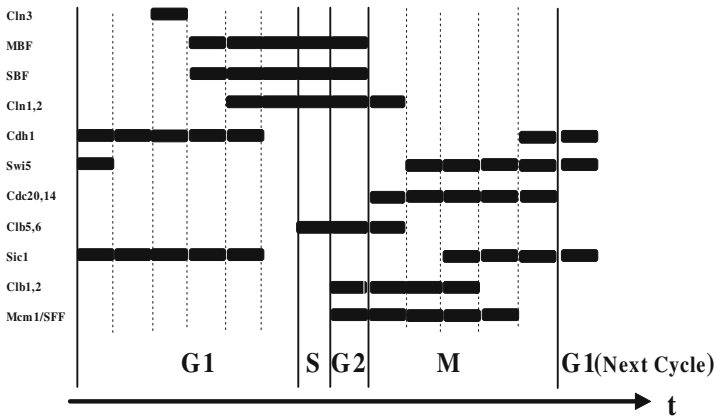
where  $\#m$  denotes the number of times the state  $m$  is being visited in the simulate iterations.

### 3 Results

For state  $m$  and  $n$ , the pure probability flux from  $m$  to  $n$  is denoted as  $\pi_m p_{mn} - \pi_n p_{nm}$ , where  $p_{mn}$  is the transition probability from  $m$  to  $n$ . Fig. 2 is an example of the probability flux among all 2048 states. There is a distinct difference between Fig. 2 and the Fig.3 in [13]. The arrow representing the probability flux from the stationary G1 state to the excited G1 state (the START of the cell-cycle) is a real part of the cycle instead of a dashed line. States of proteins on different stage of cell cycle can be seen clearly in Fig. 3, which fit the known biologically knowledge very well. The result demonstrates that the stationary G1 state is not a steady state, but a metastable state. Other states in the system are more unsteady metastable states. Qian *et al.* ([17]) proved that irreversible



**Fig. 2.** The probability flux. Each node represents one of the 2048 states. The size of a node reflects the stationary distribution probability of the state. If the stationary probability of a state is larger than a given threshold value, the size of the node is in proportion to the logarithm of the probability. Otherwise, the node is plotted with the same smallest size. The nodes on the biological pathway (the loop in the figure) are denoted with different characters: Stationary G1, Excited G1, G1, S, G2 and M. The arrows reflect the pure probability flux (only the largest flux from any node is shown). The width of an arrow is in proportion to the logarithm of the probability flux it carries. For a node, only the largest flux from it is shown. The simulations were done with  $\alpha = 3$ ,  $\beta = 3$  and  $\gamma = 1$ .



**Fig. 3.** The states of proteins on different stage of cell cycle. Black bar means activation.

Markov chain will inevitably lead to a loop. Such a system will generate positive entropy. That is also the property of alive system, such as cell cycle system. Qian *et al.* ([17]) gave the definition of entropy production rate as

$$e_p = \frac{1}{2} \sum_{i,j \in S} (\pi_i p_{ij} - \pi_j p_{ji}) \ln \frac{\pi_i p_{ij}}{\pi_j p_{ji}} \quad (5)$$

We computed the entropy production rate when  $\beta = 3$ ,  $\alpha = 3$  and  $\gamma = 1$ , and the value is about 12.2.

## 4 Conclusion

In conclusion, we introduced a nonequilibrium stochastic model for the yeast cell cycle network by considering external signals effects (such as cell size) in the model. A real alive life system must be an open system. The loop existing in real cell cycle can be seen clearly in the result of our model. Because of negative entropy production rate from external environment (absolute value of which equals the positive entropy production rate of the internal system), the system can maintain cycling.

## Acknowledgments

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# Tissue Classification Using Gene Expression Data and Artificial Neural Network Ensembles\*

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**Abstract.** An important challenge in the use of large-scale gene expression data for biological classification occurs when the number of genes far exceeds the number of samples. This situation will make the classification results are unstable. Thus, a tissue classification method using artificial neural network ensembles was proposed. In this method, a feature preselection method is presented to identify significant genes highly correlated with tissue types. Then pseudo data sets for training the component neural network of ensembles were generated by bagging. The predictions of those individual networks were combined by simple averaging method. Some data experiments have shown that this classification method yields competitive results on several publicly available datasets.

## 1 Introduction

Microarray experiment technology allows gene expression levels to be measured for the entire genome simultaneously. Such experiments collect enormous amounts of gene expression data that clearly reflects underlying biological processes. Array methodologies have led to a tremendous acceleration in the rate at which gene expression pattern information is accumulated [6], [13], [14]. In the medical field, determination of cancer type and stage is often crucial to the optimal treatment of patients [10], [12]. However, poorly differentiated cancers can be difficult to diagnose by routine histopathology and morphology. Normal cells can evolve into malignant cancer cells through a series of mutations that control the cell cycle, apoptosis, and genome integrity. Diagnostic classification of cancers from their gene-expression profiles has become a novel promising method. In this field, the major tasks of bioinformatics research are to identify gene sets that contributed to cancer classification and find optimal classification methods for diagnosis. These tasks are also called *feature selection* and *supervised classification*, two commonly addressed problems in machine learning. But the number of genes in microarray data set is very large, about 2000 to

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20000, it is impossible to search all the possible feature subsets for global optimal results. Furthermore, the sample sizes are limited that will make the classification results unstable. So microarray techniques have led to several important challenges for pattern recognition. In recent years, several mathematical approaches have been developed to tissue classification using microarray data, including *voting* scheme [10], *unsupervised clustering* [2], *support vector machine* [17], *Bayesian regression models* [19] and some hybrid approaches [8], [22]. Ben-Dor et al. [3] and Dudoit et al. [7] have compared performances of several traditional classification approaches that applied in this area. These classification methods include *k*-NN, *Classification And Regression Trees* (CART) and so on.

One of the basic characteristics of *Artificial Neural Networks* (ANNs) is that they can discover interrelationships within large sets of data. In complex biological systems, characterized by an abundance of data, ANNs allow pattern recognition, which would otherwise prove difficult. They have been chosen as a primary analysis tool in medical studies. Some research groups [12], [15], [20] reported tumor classification by multilayered backpropagation neural networks respectively. Hornik et al. showed that feedforward artificial neural networks with one hidden layer can approximate any functions in any accuracy. However, until now there is no rigorous theory indicating how to do such error-free approximation. Therefore whether an artificial neural network based application will be successful or not is almost fully determined at present by the who is the user. In general, the more experiences the user has on artificial neural networks, the more chances the application will have in gaining success. Unfortunately, in real-world applications the users are often those with little knowledge on neural computing. Therefore artificial neural networks techniques sometimes do not lead to ideal results in the microarray application [7]. In the beginning of the 1990s, Hansen and Salamon [11] showed that the generalization ability of an artificial neural networks system can be significantly improved through ensembling artificial neural networks, i.e. training several artificial neural networks and combining their predictions. Since artificial neural network ensembles work remarkably well and are easy to be used, they are regarded as a promising methodology that can profit not only experts in artificial neural network research but also engineers in real-world application. The techniques have been successfully applied to many real-world domains such as handwritten digit recognition, scientific image analysis, face recognition, OCR, seismic signals classification, breast cancer diagnosis, and in-vitro fertilization treatment [22].

In this paper, based on the recognition of the power of artificial neural network ensemble, a novel classification approach for gene expression microarray data analysis was proposed. In this approach, significant genes for classification were selected by Wilcoxon test. Then learning data sets for each member of neural network ensembles were generated by *convex pseudo-data* (CPD) methods. The predictions of those individual networks were combined by simple averaging method.

## 2 Methods

For our purpose, gene expression data on  $p$  genes for  $n$  mRNA samples may be summarized by an  $n \times p$  matrix  $X=(x_{ij})$ , where  $x_{ij}$  denotes the expression level of gene (variable)  $j$  in mRNA sample (observation)  $i$ . The expression levels might be either

absolute (e.g. oligonucleotide arrays) or relative with respect to the expression levels of a suitably defined common reference sample (e.g. cDNA microarrays). When the mRNA samples belong to known classes (e.g. follicular lymphoma), the data for each observation consist of a gene expression profile  $\mathbf{x}_i=(x_{i1},x_{i2},\dots,x_{ip})$  and a class label  $y_i$ , i.e., of predictor variables  $x_i$  and response  $y_i$ . For  $K$  classes, the class labels  $y_i$  are defined to be integers ranging from 0 to  $K-1$ .

A predictor or classifier for  $K$  tumor classes partitions the space  $X$  of gene expression profiles into  $K$  disjoint and exhaustive subsets, such that for a sample with expression profile  $\mathbf{x}_i=(x_{i1},x_{i2},\dots,x_{ip})$ , the predicted class is  $k$ , that is, one of the values between 0 to  $K-1$ . Here,  $K$  is set to 2 for we will only discuss two label classification problems. Predictors are built from past experience, i.e. from observations which are known to belong to certain classes. Such observations comprise the learning set (LS)  $\mathbf{L}=\{(\mathbf{x}_1,y_1), \dots,(\mathbf{x}_{nL},y_{nL})\}$ . Predictors may then be applied to a test set (TS),  $\mathbf{T}=\{\mathbf{x}_1, \dots,\mathbf{x}_{nT}\}$ , to predict for each observation  $\mathbf{x}_i$  in the test set its class  $\hat{y}_i$ .

### 2.1 Gene Selection

The intrinsic problem with classification from microarray data is that sample size  $n$  is much smaller than the dimensionality of the feature space, i.e. the number of genes  $p$ . Many genes are non differentially expressed across the samples and irrelevant for phenotype discrimination. Dimensionality reduction of the feature space has been performed by many authors, see for example Golub et al. [10], Ben-Dor et al. [3] and Dudoit et al. [7], among others. It drastically eases the computational burden and for many problems improves class prediction due to the reduced amount of noise. Our feature selection is based on scoring each individual gene  $g$ , with  $g \in \{1, \dots, p\}$  according to its strength for phenotype discrimination. We use a nonparametric method that is based on ranks and was presented by Park et al. [16]. It is in fact equivalent to the test statistic of Wilcoxon’s two sample test,

$$s(g) = \sum_{i \in N_0} \sum_{j \in N_1} I(x_j^{(g)} - x_i^{(g)} \leq 0) \tag{1}$$

where  $x_i^{(g)}$  is the expression value of gene  $g$  for individual  $i$  and  $N_m$  represents the set of the sample indices  $\in \{1, \dots, n\}$  having two different class labels in  $m \in \{0, 1\}$  (i.e. belonging to two different classes in this case).  $I(\cdot)$  denotes the indicate function, equaling 1 if the condition in parentheses is true and 0 otherwise. The score function can be interpreted as counting for each individual having response (class label) value zero, the number of instances with response one that have smaller expression values, and summing up these quantities. Viewing it as Wilcoxon’s test statistic, it allows ordering of the genes according to their potential significance. It captures to what extent a gene  $g$  discriminates the response categories and it is easy to notice that both values near the minimum score zero and the maximum score  $n_0n_1$  indicate a differentially expressed, informative gene. The quality measure  $q(g)= \max(s(g),n_0n_1-s(g))$ , thus gives the highest values to those genes whose expression levels have the best strength for phenotype discrimination. We then simply take the  $p^* \ll p$  genes with the highest values of  $q(g)$  as our top features and restrict the boosting classifier to work

with this subset. The number of predictor variables is a tuning parameter whose optimal value varied across different datasets. A formal choice of  $p$  is possible via cross validation on the learning data or by determining the correct null distribution by bootstrap methods and a decision on significance levels as in Park et al. [16]. Many more variable selection criteria for gene expression data have been proposed in the literature. We think that our approach based on Wilcoxon's test statistic is more suitable in the context of gene expression data than the t-statistic used in Dudoit et al. [7] or the TNoM score [3] which corresponds to counting the number of errors made by the best stump, a decision tree with two terminal nodes. The situation is similar to the trade-off between  $t$ -, Wilcoxon- and sign-test. It is known from robustness theory that the  $t$ -test is highly sensitive to outliers and (even small) deviations from the normal distribution, whereas the sign-test (TNoM score) wastes useful information about the magnitude of gene expression levels. A good compromise is the Wilcoxon test which has nearly optimal power properties over a large class of data-generating distributions. We selected  $p^*$  with highest  $q(g)$  value as our predictors' feature subset..

## 2.2 ANN Construction

In our work, the component neural network has same topology. Each member of ensemble is a multilayered feedforward with error backpropagation neural network.

$O_j^{(l)}$  denotes the output signal of the  $j$ th neuron in the  $l$ th layer and  $w_{ij}^{(l)}$  the connection weight coming from the  $i$ th neuron in the  $(l-1)$  layer to the  $j$ th neuron in the  $l$ th layer.  $b_j^{(l)}$  is the bias of the  $j$ th neuron in the  $l$ th layer.  $f(\cdot)$  is the transfer function.

Thus, the relationships between different layers can be represented by

$$O_j^{(l)} = f\left(\sum_i w_{ij}^{(l)} O_i^{(l-1)} + b_j^{(l)}\right). \quad (2)$$

In this application, the topology of each neural network in the ensemble adopted three layer structures. The number of neurons in the input layer was equal to the number of genes  $p^*$  used for diagnosis of each sample. The number of neurons in the hidden layers is 5. Despite increasing this number can reflect more complicated problems, but the accuracy of our application is not increased remarkably and it will add burden to training time. Our research is only limited to two-class classification, the output layer adopt only one node, it gave an output between 0 (not this category) and 1 (this category). Purelin function, i.e.,  $f(y) = y$  was used as the transfer function between input layer and hidden layer. Logsig function, i.e.,  $f(y) = 1/(1 + e^{-y})$  was used as the transfer function between hidden layer and output layer. For training these neural networks, batch gradient descent approach with momentum was adopted. The number of the epochs for backpropagation training algorithm equals 1000. The learning rate is 0.7 and the Momentum is set to 0.3.

## 2.3 Artificial Neural Network Ensembles

The major feature of microarray data is the numbers of samples are limited, not more than a few dozens. This situation will lead to single neural networks hard to be trained. In general, a neural network ensemble is constructed in two steps, i.e., training a number

of component neural networks and then combining the component predictions. As for training component neural networks, the most prevailing approaches are *Bagging* and *Boosting*. Bagging which based on *bootstrap sampling* was proposed by Breiman [4]. It generates several learning sets from the original training set and then trains a component neural network from each of those training sets. Boosting was proposed by Schapire [18] and improved by Freund et al. [9]. It generates a series of component neural networks whose training sets are determined by the performance of former ones. Training instances that are wrongly predicted by former networks will play more important roles in the training of later networks. There are also many other approaches for training the component neural networks. Bagging and Boosting have been found to be powerful classification techniques that can highly increase accuracy on various problems, especially in higher dimensions. Since the speeds of neural network training always converge slowly, Bagging is used more frequently.

In our work, we create perturbed learning data sets based on convex pseudo data (CPD). Each perturbed learning sets is generated by repeating the following  $n_L$  times:

Select two instances  $(x, y)$  and  $(x', y')$  at random from the learning set  $L$ .

Select at random a number  $v$  from the interval  $[0, d]$ ,  $0 \leq d \leq 1$ , and let  $u = 1 - v$ .

The new instance is  $(x'', y'')$  where  $y'' = y$  and  $x'' = ux + vx'$ .

As in Bagging, multiple altered learning set  $L_b$ , of the same size as the original learning set  $L$ , are generated and used to train the components of ensembles. Because the performance is improved in the initial turns, we only generated 5 data sets for each original learning sets by above algorithm. As for combining the predictions of component neural networks, *simple averaging* was used, that is, the outputs of each component neural networks were averaged as the final output. To gain the best performance, several values of  $d$  were tried,  $d=0.1, 0.25, 0.5, 0.75, 1$  and the values of  $d$  with the smallest test set error rate were retained. Note that when  $d$  values is 0, CPD reduced to bagging.

### 3 Results

#### 3.1 Datasets

We explored the performance of our classification techniques on two publicly available datasets:

1. *Leukemia Dataset*. This dataset [10] contains gene expression levels of  $n=72$  patients either suffering from acute lymphoblastic leukemia (ALL, 47 cases) or acute myeloid leukemia (AML, 25 cases) and was obtained from Affymetrix oligonucleotide microarrays.
2. *Colon Dataset*. In this dataset, expression levels of 40 tumor and 22 normal colon tissues for 6500 human genes are measured using Affymetrix technology. A selection of 2000 genes with highest minimal intensity across the samples has been made by Alon et al. [2], and these data are publicly available at <http://microarray.princeton.edu/oncology/>.

### 3.2 Independent Tests and Cross Validations

We first describe the results on the leukemia data set [10]. In this study, the data were already divided into a training set of 38 mRNA samples and a test set of 34 mRNA samples. The observations in the two set came from different labs and were collected at different times. The test set comprises a broader range of samples, including samples from peripheral blood as well as bone marrow, from childhood AML patients, and from laboratories that used different sample preparation protocols. When training the classifiers and for the pre-selection of genes, we first reduced the set of available genes to the top  $p^*=50, 100$  and  $200$  genes as ranked in terms of Wilcoxon score based Park et al. procedure [16]. To compare our results (ANN ensembles) we also applied the three other traditional discriminant analysis procedures single artificial neural network (ANN), 1-NN and CART. The results are given in table 1.

**Table 1.** Classification rates by the four methods for the leukemia data set with 38 training samples (27 ALL, 11 AML) and 34 test samples (20 ALL,14 AML). Given are the number of correct classification out of 38 and 34 for the training and test samples respectively. The  $d$  values are reported in parentheses.

| $P^*$ | ANN ensembles | ANNs | INNs | CARTs |
|-------|---------------|------|------|-------|
| 50    | 34 (0.05)     | 33   | 33   | 33    |
| 100   | 33 (0.05)     | 33   | 33   | 33    |
| 200   | 33 (0.5)      | 33   | 33   | 33    |

Among these results, all the 34 test samples using 50 genes and ANN ensembles were classified accurately, which is performed better than that of Golub et al. in the same number of genes. To further evaluate the performances of the classifiers, we applied the cross validation tests to the above two datasets. In these tests, we randomly selected one third of the original data sets as a test set and remaining ones as a training set. In the principle comparison, for each learning set/test set run, the top  $p^*=50, 100$  and  $200$  genes with largest Wilcoxon's scores are selected using the learning sets. Next, predictors are constructed using the learning set and test set error rates are obtained by applying the predictors to the test sets. For CPD, several values of the parameters  $d$  are examined:  $d=0.1, 0.25, 0.5, 0.75$  and  $1$ . All above procedure is repeated 150 times.

**Table 2.** Comparison of accuracy rates with four classification methods

| $P^*$            | ANN ensembles (%) | ANNs (%)   | INNs (%)   | CARTs (%)  |
|------------------|-------------------|------------|------------|------------|
| leukemia dataset |                   |            |            |            |
| 50               | 98.03±2.63 (0.05) | 97.75±3.26 | 93.88±4.67 | 94.96±4.65 |
| 100              | 97.50±2.77 (0.05) | 97.36±3.03 | 94.93±4.35 | 94.55±5.19 |
| 200              | 97.31±2.56 (0.5)  | 97.03±3.07 | 92.64±5.70 | 94.26±5.36 |
| Colon dataset    |                   |            |            |            |
| 50               | 85.90±5.62 (0.5)  | 83.11±6.13 | 80.70±6.29 | 78.53±7.63 |
| 100              | 85.87±6.59 (0.5)  | 83.27±7.00 | 78.90±6.92 | 76.70±7.66 |
| 200              | 86.22±6.49 (0.75) | 84.70±7.08 | 76.47±7.34 | 77.07±7.67 |

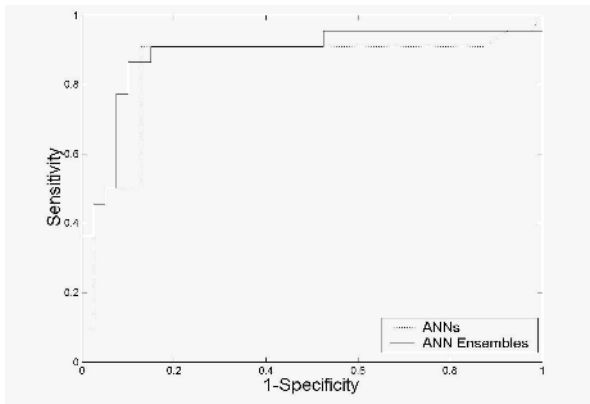
The average error rates are recorded in the table 2. The  $d$  values used in CPD are reported in parentheses. From the table above, one can see that the accuracy rates predicted by ANN ensembles are higher than that predicted by other classifiers.

### 3.3 ROC Curves

Estimates of classification accuracy give only a partial insight on the performance of a method. In our evaluation, we treated all errors as having equal penalty. In a clinical setting, one often prefers to punish misclassifications asymmetrically, since false negative error, i.e., classifying a tumorous tissue as normal can be fatal, whereas false positive errors, i.e., predicting a normal tissue as a tumor may be less serious since in this case additional tests will be carried out. Receiver Operator Characteristics (ROC) curves illustrate how accurate classifiers are under asymmetric losses, by plotting the tradeoff between false positives and false negatives. Each point on the two dimensional ROC curve corresponds to a particular probability  $\beta \in [0,1]$  that was used as a threshold for positive (tumorous) classification. The  $(x,y)$  coordinates of each point are then the fractions of negative and positive samples that are classified as positive with this particular threshold  $\beta$ . In general, ROC curves are between these two extremes, with a larger area under the ROC curve (AUROC) indicating a better performance. In the ideal case, the ROC curve goes through  $(0,1)$ , the upper left corner of the plot, that is, AUROC equals to 1. We selected top 50 genes for tests in this data set. The AUROC of neural network ensemble and single neural network are 0.890 and 0.851 respectively. It demonstrated that the sensitivity of neural network ensembles is better than that of single neural networks.

## 4 Conclusion

The artificial neural network ensemble is a recently developed technology, which has the ability of significantly improving the performance of a system where a single artificial neural network is used. In this paper, we proposed a tissue classification



**Fig. 1.** ROC curves for neural network ensembles and neural networks applied on colon data set

method using DNA microarray data, which utilize artificial neural network ensemble to identify different cancer subtypes. The experiments demonstrated that this method will improve the performances of classification. Its accuracy of classification is better than single neural networks, INNs and CARTs. The results showed the feasibility of cancer classification based on neural network ensembles and microarray data. In this paper, we only consider the model for two class type discriminant. Extension to more than two categories using neural network ensembles needs further research. Some previous reports, e.g. [1] presented some hints to resolve this problem.

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