

# Coherence Studies of Photons Emitted from a Single Terrylene Molecule Using Michelson and Young's Interferometers

Seung-Jin Yoon, Cong Tai Trinh, and Kwang-Geol Lee\*

*Department of Physics, Hanyang University, Seoul 133-791, Korea*

(Received October 26, 2015 : revised November 9, 2015 : accepted November 11, 2015)

Coherence length (time) is a key parameter in many classical and quantum optical applications. Two interferometers – Michelson and Young's double-slit – are used to characterize the temporal coherence of single photons emitted from single terrylene molecules. For quantitative analysis, a dispersion-related distortion in the interference pattern of a Michelson interferometer is carefully corrected by a simple dispersion compensation. Additionally, it has been demonstrated that Young's interferometer can be used in temporal coherence studies at the single photon level with high accuracy. The pros and cons of the two systems are discussed. The measured coherence lengths in the two systems are consistent with one another under the self-interference interpretations.

*Keywords* : Coherence length, Single photon source, Interferometry

*OCIS codes* : (030.1640) Coherence; (120.3180) Interferometry; (270.5290) Photon statistics

## I. INTRODUCTION

An on-demand single photon source is an essential ingredient for the successful realization of many quantum optical applications like quantum cryptography, computing, imaging, and metrology [1-3]. Photons from solid state single emitters, such as single molecules, quantum dots, and diamond color centers, are considered to be promising candidates as high-quality 'on-demand' single photon sources because of their good photo-stability and high controllability [1-4]. Different properties of single photons are required for different applications. For an example, quantum information processing requires photons to be indistinguishable with long quantum coherence times [5]. In contrast, optical coherence tomography (OCT) requires shorter coherence lengths in order to obtain better imaging depth resolution. OCT has been developed based on classical broad-band sources [6, 7], and quantum OCT has also been demonstrated [8]. The coherence of light sources plays a key role in many optical applications (e.g., the examples mentioned above); therefore, it is important to correctly characterize the coherence properties of a light source.

Several different methodologies have been used in coherence studies that have investigated many different types of light sources (including single photon sources) [9-12]. To date,

the Michelson interferometer (MI) has been most widely used in temporal coherence studies because the temporal coherence length can be obtained directly from the decay constant of its interference oscillation amplitude. We also use MI as a test bench of the temporal coherence length measurement of single photons and compare these results with those obtained from Young's double interferometer (YDI). In our measurements, MI showed an inherent dispersion broadening, which caused a distortion in the interference pattern. Therefore, we applied a simple dispersion compensation in order to systematically remove this problem.

Since the triumphant success of Thomas Young more than 200 years ago, YDI has been applied to the proof of principle demonstrations of interference [13, 14], and to spatial coherence studies [15]. However, researchers have been reluctant to use YDI in temporal coherence studies because the fast-decaying diffraction signal conceals the interference features at long delays. For a broad-band source, however, its coherence length can be short enough to be characterized by YDI. In addition, there is no distortion in the interference signal which might appear in MI as mentioned earlier. In this study, we show that the temporal coherence length of single photons from single molecules at room temperature can be measured with high accuracy using YDI. The measured coherence lengths in the two systems are consistent with

\*Corresponding author: [kglee@hanyang.ac.kr](mailto:kglee@hanyang.ac.kr)

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one another under the self-interference interpretations. [13].

## II. DISPERSION CALIBRATION IN A MICHELSON INTERFEROMETER (MI)

A basic diagram of MI is shown in Fig. 1(a). Here, the source beam is divided by a 50/50 beam splitter (BS) into two paths – the reference path and the signal path. The optical path length difference  $\Delta$  between the two beam paths is controlled by a piezo-tube (PZT). If the reference and the signal beams travel the same length inside of the dispersive media, the interference pattern is given to be symmetric to the zero delay  $\Delta = 0$ . However if the two beams travel different distances inside a cube-type BS (as happens in our case) and the material (BK7) of the BS is dispersive as shown in Fig. 1(b), the interference pattern appears to be asymmetric (Fig. 1(c)). To compensate for this dispersive broadening, two glass slides are inserted with different tilting angles, as depicted in Fig. 1(a). A broadband halogen lamp is used in this proof of principle demonstration. The refractive index of the glass slide (soda lime) is different from that of BS (BK7) but is shifted almost constantly within the considered wavelength range. At  $\theta = 47$  degrees, the symmetric shape can be recovered,

and the original roundtrip travelling length difference between the two beams inside the BS is calculated to be  $240 \mu\text{m}$ . Note that the reduced visibility at zero delay in (d) compared to (c) is due to the unbalanced field intensity caused by different reflection losses at the glass slide surface for the two paths.

## III. COHERENCE OF A SINGLE PHOTON SOURCE MEASURED BY MI

In the next step, we use this dispersion calibrated MI to investigate the coherence characteristics of photons from single terrylene molecules. Figure 2(a) shows the experimental schematics. A thin *para*-terphenyl crystal layer with embedded single terrylene molecules is generated on a cover glass via spin-coating. A *p*-polarized 532 nm cw-mode laser is coupled through a high numerical aperture oil-objective (NA = 1.4) in a total internal reflection geometry to efficiently excite molecules, which are aligned almost vertically to the sample surface [16]. Fluorescence from the molecules collected by the same objective is passed through a spatial mask to remove the background, and then sent to the spectrometer, the Hanbury-Brown & Twiss (HBT) interferometer (used to measure the second-order correlation function  $g^{(2)}(\tau)$ ),

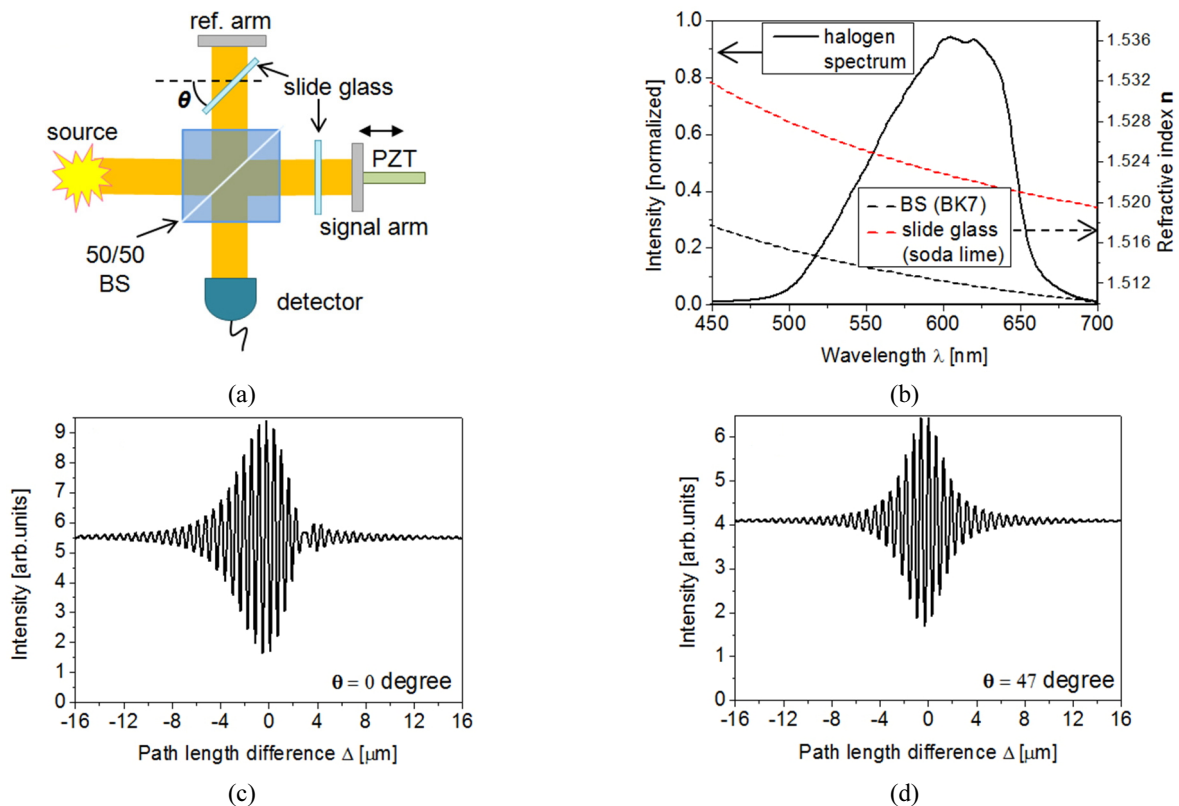


FIG. 1. (a) Dispersion compensation in MI. Two glass slides with different tilting angles are inserted to compensate for the dispersion broadening caused by the BS. (b) Spectrum of the source halogen lamp (black solid) and refractive indices of the BS (black dashed) and the glass slide (red dashed). (c) Measured interference pattern with a tilting angle  $\theta=0$  degrees. (d) Symmetric shape is recovered at  $\theta=47$  degrees.

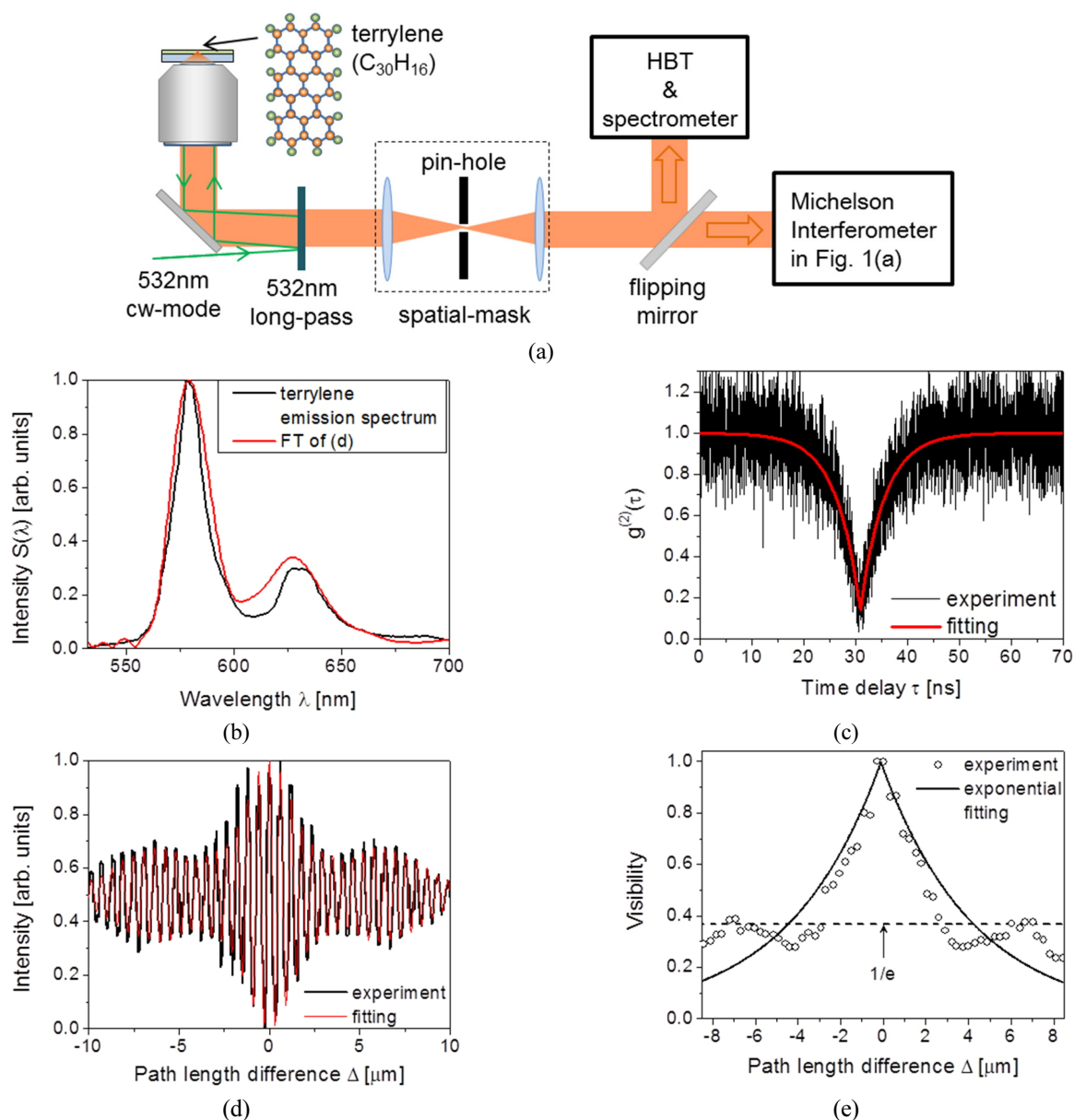


FIG. 2. (a) Experimental schematics. Photons from a single terrylene molecule are sent to MI (shown in Fig. 1(a)), the Hanbury-Brown & Twiss (HBT) interferometer, and the spectrometer. A spatial mask is used to cut the backgrounds out of the signal. (b) The black line is the terrylene emission spectrum measured by the spectrometer, and the red line is the inverse Fourier transform of the interference pattern in (d). (c) Second-order correlation function  $g^{(2)}(\tau)$  measured by the HBT interferometer. An exponential fitting is shown in red. (d) Measured interference pattern (black), and the fitting based on the self-interference (red). (e) Visibility derived from the interference pattern (open circles), and an exponential fitting (black solid).

and MI. The black line in Fig. 2(b) shows the emission spectrum of a terrylene molecule. All of the measurements are performed at room temperature; therefore, the spectrum is phonon-broadened, and two vibronic level peaks are clearly visible. To check that detected photons are emitted from a single molecule, the second-order correlation function  $g^{(2)}(\tau)$  is measured by the HBT interferometer. As shown in Fig. 2(c), the measured value of  $g^{(2)}(\tau=0)=0.14$  clearly demonstrates the single photon nature of our source [1]. This non-zero dip is attributed to the small background

level and its portion is about 7% in this case [17]. The contribution of the backgrounds can be systematically removed both in second-order correlation measurements [17] and in first-order correlation measurements. The black line in Fig. 2(d) is the interference pattern obtained by the dispersion-calibrated MI. The overall shape is almost symmetric, which is expected. Additionally, the beating shapes caused by the two vibronic spectral peaks are clearly seen.

The total interference pattern of single photons is given as the sum of the self-interference. Therefore, the fitting

function can be written simply as follows

$$I(\Delta) = \int_{\lambda} d\lambda S(\lambda) \left[ \langle I_1 \rangle + \langle I_2 \rangle + 2\sqrt{\langle I_1 \rangle \langle I_2 \rangle} \cos\left(\frac{2\pi}{\lambda} \cdot \Delta\right) \right],$$

where  $\langle I_1 \rangle$  and  $\langle I_2 \rangle$  are the mean photon number averaged for a suitably long time in the reference and signal paths, respectively. In addition,  $S(\lambda)$  is the intensity spectrum shown in Fig. 2(b). The fitting curve (red in Fig. 2(d)) matches very well with the experiment. Because the total interference pattern is the sum of the self-interference at each wavelength, its Fourier transform (FT) gives the spectral shape of the light source. It is plausible that the FT of the measured interference pattern (black in (d)) recovers the original spectrum of the terylene (red line in Fig. 2(b)). Finally, in Fig. 2(e), in order to estimate the coherence length of this single photon source, the visibility is derived from the interference pattern and fitted with a decaying single-exponential to give the coherence length ( $l_{coh} = 4.36 \pm 0.20 \mu\text{m}$ ). The error comes from the uncertainty in the fitting process.

#### IV. TEMPORAL COHERENCE ANALYSIS OF SINGLE PHOTONS BY YOUNG'S INTERFEROMETER

The experimental setup used to generate a well-collimated single photon stream is the same as the one shown in Fig. 2(a). The double-slit interferometer is illustrated separately in Fig. 3(a). Two parallel slits with an opening width  $w$  and separation  $s$  are made in a thin ( $12.5 \mu\text{m}$ ) metallic film. The interference pattern formed by the double-slit is imaged into a small area by a focusing lens in order to increase the signal quality. The image captured by a high sensitivity CCD camera (ORCA-R2, Hamamatsu) is shown in the inset of Fig. 3(a). To obtain the interference intensity as a function of the optical path length, the pixel counts are integrated along the  $z$ -axis for each  $x$ -position, as shown in Fig. 3(b). In the fitting function, we assume a single-exponential decay of the interference visibility combined with the single-slit diffraction:

$$I_{double-slit}(\Delta) = 2I_0 \left[ 1 + \exp\left(-\frac{|\Delta|}{l_{coh}}\right) \times \cos\left(\frac{2\pi}{\lambda_{center}} \cdot \Delta\right) \right] \times \frac{\sin^2 \beta}{\beta^2},$$

$$\text{where } \lambda_{center} = \frac{\int d\lambda S(\lambda) \cdot \lambda}{\int d\lambda S(\lambda)}, \quad \beta = \frac{w}{2s} \cdot \frac{2\pi}{\lambda_{center}} \cdot \Delta, \quad w=40$$

$\mu\text{m}$ ,  $s=500 \mu\text{m}$  and  $I_0$  and  $l_{coh}$  are the two free fitting parameters. The fitting curve (red in Fig. 3(b)) successfully reconstructs the experimental curve (black). Note that the position in screen  $x$  is determined by the relation of  $\Delta = \frac{s \times x}{f}$ , where  $f$  ( $=210 \text{ mm}$ ) is the focal length of the

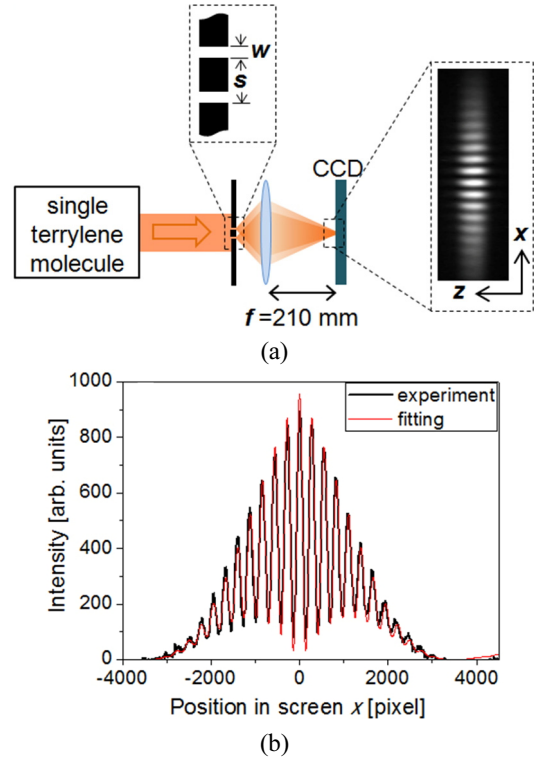


FIG. 3. A collimated beam of photons from a single terylene molecule is sent to a double-slit with a slit-width of  $w = 40 \mu\text{m}$  and a slit-separation of  $s = 500 \mu\text{m}$ . The interference pattern in the CCD screen is shown in the inset. (b) Interference intensity integrated along the  $z$ -axis (black), and a fitting function that assumes single exponential decay (red).

lens. The fast decay of the interference visibility can be characterized by virtue of the short coherence length. We performed the same measurements for six different molecules and obtained a coherence length  $l_{coh}$  of  $4.45 \pm 0.23 \mu\text{m}$ . The discrepancy of the coherence length compared to MI is only  $\sim 2\%$ . The total acquiring time for YDI is 10–30 min, depending on the brightness of the molecules, and the quantum efficiency of the CCD camera that we used is about 60%. The detector in MI has a quantum efficiency of  $\sim 65\%$  and the total measurement time is about 10–20 min. Therefore, the two systems require similar acquisition times.

#### V. CONCLUSION

We studied the temporal coherence of photons emitted from single molecules by applying two different interferometers - MI and YDI. The coherence lengths can be determined with high accuracy by both systems, and the theory based on the self-interference matches very well with the experimental results. When comparing the two interferometers, MI gave more detailed features in the interference pattern (e.g., the beating shape) but a dispersion-

related distortion in the interference pattern needs to be corrected. Alternatively, YDI has a rather simple configuration, which allows for an easy adjustment, and does not require dispersion correction. However, it was not possible to see the details in the interference pattern of YDI as compared to MI.

### ACKNOWLEDGMENT

This work was supported by the Basic Science Research Program through a grant from the National Research Foundation of Korea, funded by the Ministry of Science, ICT & Future Planning (2013R1A1A1011514).

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