

Measurement of branching fractions and CP violation parameters in $B \rightarrow \omega K$ decays with first evidence of CP violation in $B^0 \rightarrow \omega K_S^0$

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We present a measurement of the branching fractions and charge-parity- (CP) -violating parameters in $B \rightarrow \omega K$ decays. The results are obtained from the final data sample containing $772 \times 10^6 B\bar{B}$ pairs collected at the $\Upsilon(4S)$ resonance with the Belle detector at the KEKB asymmetric-energy e^+e^- collider. We obtain the branching fractions $\mathcal{B}(B^0 \rightarrow \omega K^0) = (4.5 \pm 0.4(\text{stat}) \pm 0.3(\text{syst})) \times 10^{-6}$, $\mathcal{B}(B^+ \rightarrow \omega K^+) = (6.8 \pm 0.4(\text{stat}) \pm 0.4(\text{syst})) \times 10^{-6}$ which are in agreement with their respective current world averages. For the CP -violating parameters, we obtain $\mathcal{A}_{\omega K_S^0} = -0.36 \pm 0.19(\text{stat}) \pm 0.05(\text{syst})$, $\mathcal{S}_{\omega K_S^0} = +0.91 \pm 0.32(\text{stat}) \pm 0.05(\text{syst})$, $\mathcal{A}_{\omega K^+} = -0.03 \pm 0.04(\text{stat}) \pm 0.01(\text{syst})$, where \mathcal{A} and \mathcal{S} represent the direct and mixing-induced CP asymmetry, respectively. We find no evidence of CP violation in the decay channel $B^+ \rightarrow \omega K^+$; however, we obtain the first evidence of CP violation in the $B^0 \rightarrow \omega K_S^0$ decay channel at the level of 3.1 standard deviations.

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I. INTRODUCTION

Violation of the combined charge-parity symmetry (CP violation) in the Standard Model (SM) arises from a single irreducible phase in the Cabibbo–Kobayashi–Maskawa (CKM) quark-mixing matrix [1,2]. A primary objective of the Belle experiment is to overconstrain the unitarity triangle of the CKM matrix related to $B_{u,d}$ decays. This permits a precision test of the CKM mechanism for

CP violation as well as the search for new physics effects. Mixing-induced CP violation in the B sector has been clearly established by Belle [3,4] and *BaBar* [5,6] in the $\bar{b} \rightarrow \bar{c}s\bar{s}$ -induced decay $B^0 \rightarrow J/\psi K^0$.

Interest has turned toward $b \rightarrow q\bar{q}s$ -mediated decays, where q is a u , d , or s quark, such as $B \rightarrow \omega(782)K$, for which the physical properties are the subject of this paper. These decays proceed predominantly by loop diagrams and are thereby possibly affected by new particles in various

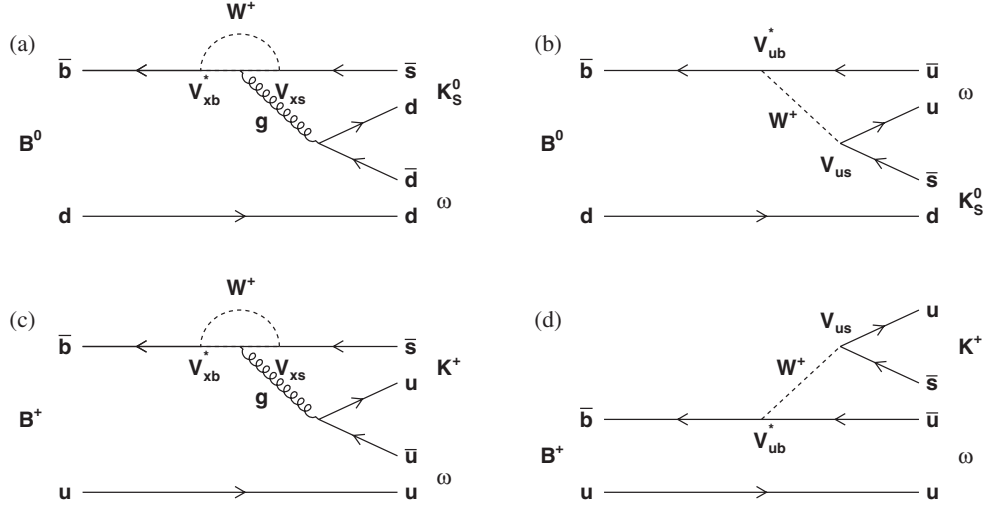


FIG. 1. Leading-order Feynman diagrams for $B \rightarrow \omega K$ decays. For $B^0 \rightarrow \omega K_S^0$, (a) shows the loop (penguin), while (b) shows the tree diagram. For $B^+ \rightarrow \omega K^+$, (c) and (d) are the corresponding diagrams. In the penguin diagrams, the subscript x in V_{xb} refers to the flavor of the intermediate-state up-type quark ($x = u, c, t$).

extensions of the SM [7]. The Feynman diagrams of the neutral and the charged decay modes $B^0 \rightarrow \omega K_S^0$ and $B^+ \rightarrow \omega K^+$ (with charge-conjugate modes included everywhere unless otherwise specified) are shown in Fig. 1. The $B^0 \rightarrow \omega K_S^0$ decays are sensitive to the interior angle of the unitarity triangle $\phi_1 \equiv \arg(-V_{cd}V_{cb}^*)/(V_{td}V_{tb}^*)$. Belle and BaBar have reported measurements on this CP -violating phase in this channel [8,9] and other related modes including $B^0 \rightarrow \eta' K^0$ [9,10], ϕK_S^0 [11,12], and $f_0(980)K_S^0$ [11–15].

The CKM phase ϕ_1 is accessible experimentally through interference between the direct decay of a B meson to one of the above-mentioned CP eigenstates and $B^0\bar{B}^0$ mixing followed by a decay into the same final state. This interference is observable through the time evolution of the decay. We reconstruct $B^0 \rightarrow \omega K_S^0$ from $\Upsilon(4S) \rightarrow B^0\bar{B}^0$ decays. As the two B mesons are produced in a coherent state, the B_{Rec} flavor can be obtained from the other B of the events (B_{Tag}). The proper time interval between B_{Rec} and B_{Tag} , which decay at times t_{Rec} and t_{Tag} , respectively, is defined as $\Delta t \equiv t_{\text{Rec}} - t_{\text{Tag}}$ measured in the $\Upsilon(4S)$ frame. For the coherent $B^0\bar{B}^0$ pairs, the time-dependent decay rate for a CP eigenstate when B_{Tag} possesses flavor q , where B^0 has $q = +1$ and \bar{B}^0 has $q = -1$, is given by

$$\mathcal{P}(\Delta t, q) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \times \{1 + q[\mathcal{A}_{\omega K_S^0} \cos \Delta m_d \Delta t + \mathcal{S}_{\omega K_S^0} \sin \Delta m_d \Delta t]\}. \quad (1)$$

Here, τ_{B^0} is the B^0 lifetime, and Δm_d is the mass difference between the two mass eigenstates of the neutral B meson. This time dependence assumes CPT invariance and that the

difference in the decay rates between the two mass eigenstates is negligible. The parameter $\mathcal{A}_{\omega K_S^0}$ measures the direct CP violation, while $\mathcal{S}_{\omega K_S^0}$ is a measure of the amount of mixing-induced CP violation. In the limit of a single penguin amplitude with the dominant t quark in the loop, we would expect $\mathcal{A}_{\omega K_S^0} = 0$, $\mathcal{A}_{\omega K^+} = 0$, and $\mathcal{S}_{\omega K_S^0} = \sin 2\phi_1$. However, additional CKM-suppressed contributions carrying different weak phases may not be negligible. As a consequence, direct CP violation can arise, and the measured $\mathcal{S}_{\omega K_S^0}$ may differ from $\sin 2\phi_1$.

For the charged mode, the direct CP -violating parameter $\mathcal{A}_{\omega K^+}$ is extracted from the rates of the $B^+ \rightarrow \omega K^+$ decay, for which the flavor can be determined directly from the charge of the kaon on the signal side,

$$\mathcal{A}_{\omega K^+} = \frac{\Gamma(B^- \rightarrow \omega K^-) - \Gamma(B^+ \rightarrow \omega K^+)}{\Gamma(B^- \rightarrow \omega K^-) + \Gamma(B^+ \rightarrow \omega K^+)}. \quad (2)$$

The measurements of the branching fractions and CP parameters in $B \rightarrow \omega K$ decays provide an important test of the QCD factorization (QCDF), perturbative QCD (pQCD), and soft collinear effective theory (SCET) approaches. The predictions made by these SM-based theoretical calculations are summarized in Table I. These approaches predict a relatively sizeable direct CP asymmetry in $B^+ \rightarrow \omega K^+$ and expect $\mathcal{S}_{\omega K_S^0}$ to be slightly higher than in $b \rightarrow c\bar{c}s$ decays. However, current experimental measurements of $\mathcal{S}_{\omega K_S^0}$ [8,9] could indicate the opposite, motivating more precise experimental determinations to reduce the large statistical uncertainties. Finally, combinations of measurements of the branching fractions and charge asymmetries of charmless B meson decays can be used in phenomenological fits to understand the relative importance of tree and penguin contributions and may

TABLE I. pQCD [16,17], QCDF [18], SCET 1 [19], and SCET 2 [19] theoretical predictions for the $B^0 \rightarrow \omega K_S^0$ and $B^+ \rightarrow \omega K^+$ branching fractions (in units of 10^{-6}) and CP parameters (in units of 10^{-2}). The meaning of each uncertainty for these approaches is given in the corresponding references.

Parameter	pQCD	QCDF	SCET 1	SCET 2
$\mathcal{B}(B^0 \rightarrow \omega K^0)$	$9.8^{+8.6+6.7}_{-4.9-4.3}$	$4.1^{+4.2+3.3}_{-1.7-2.2}$	$4.1^{+2.1+0.8}_{-1.7-0.7}$	$4.9^{+1.9+0.7}_{-1.6-0.6}$
$\mathcal{B}(B^+ \rightarrow \omega K^+)$	$10.6^{+10.4+7.2}_{-5.8-4.4}$	$4.8^{+4.4+3.5}_{-1.9-2.3}$	$5.1^{+2.4+0.9}_{-1.9-0.8}$	$5.9^{+2.1+0.8}_{-1.7-0.7}$
$\mathcal{A}_{\omega K_S^0}$	-3^{+2+2}_{-4-3}	$-4.7^{+1.8+5.5}_{-1.6-5.8}$	$5.2^{+8.0+0.6}_{-9.2-0.6}$	$3.8^{+5.2+0.3}_{-5.4-0.3}$
$\mathcal{S}_{\omega K_S^0}$	84^{+3+0}_{-7-2}	84^{+5+4}_{-5-6}	51^{+5+2}_{-6-2}	80^{+2+1}_{-2-1}
$\mathcal{A}_{\omega K^+}$	32^{+15+4}_{-17-5}	$22.1^{+13.7+14.0}_{-12.8-13.0}$	$11.6^{+18.2+1.1}_{-20.4-1.1}$	$12.3^{+16.6+0.8}_{-17.3-1.1}$

provide sensitivity to the CKM angle $\phi_3 \equiv \arg(-V_{ud}V_{ub}^*/V_{cd}V_{cb}^*)$ [20,21].

Experimentally, clear signals have been observed by Belle and *BaBar* for $B^0 \rightarrow \omega K^0$ and $B^+ \rightarrow \omega K^+$ with similar branching fractions [22,23]. Measurements of the CP -violation parameters and the branching fractions for these channels were reported by Belle and *BaBar*. All previous measurements are summarized in Table II.

In this paper, we present an updated measurement of the branching fractions and CP -violation parameters in $B \rightarrow \omega K$ decays using the full Belle data set with $772 \times 10^6 B\bar{B}$ pairs; this supersedes the previous Belle analysis. In Sec. II, we briefly describe the data set and Belle detector. The selection criteria used to identify signal candidates and suppress backgrounds along with the definition of the variables that will be used to extract the physical signal parameters are explained in Sec. III. Following that, the signal and background models for these variables will be discussed in Sec. IV. In Sec. V, the results of the fit are presented along with a discussion of the systematic uncertainties in Sec. VI. Finally, our conclusions are given in Sec. VII.

II. DATA SET AND BELLE DETECTOR

The results in this paper are based on the $Y(4S)$ final data sample containing $772 \times 10^6 B\bar{B}$ pairs collected with the Belle detector at the KEKB asymmetric-energy e^+e^- (3.5 on 8 GeV) collider [24]. At the $Y(4S)$ resonance ($\sqrt{s} = 10.58$ GeV), the Lorentz boost of the produced $B\bar{B}$ pairs is $\beta\gamma = 0.425$ nearly along the $+z$ direction, which is opposite the positron beam direction.

The Belle detector is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector (SVD), a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter (ECL) comprising CsI(Tl) crystals located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. An iron flux return located outside of the coil is instrumented to detect K_L^0 mesons and to identify muons. The detector is described in detail elsewhere [25]. Two inner detector configurations were used. A 2.0-cm-radius beampipe and a

three-layer silicon vertex detector (SVD1) were used for the first sample of $152 \times 10^6 B\bar{B}$ pairs, while a 1.5-cm-radius beampipe, a four-layer silicon detector (SVD2), and a small-cell inner drift chamber were used to record the remaining $620 \times 10^6 B\bar{B}$ pairs [26]. We use a GEANT-based Monte Carlo (MC) simulation to model the response of the detector and to determine its acceptance [27].

III. EVENT SELECTION

A. B candidate selection

We reconstruct B^0 (B^+) meson candidates from an ω and a K_S^0 (K^+) candidate. The ω candidates are reconstructed from $\pi^+\pi^-\pi^0$ combinations, where π^0 is reconstructed from two photons. Charged tracks forming an ω candidate and the prompt kaon track are identified using a loose requirement on the distance of closest approach with respect to the interaction point (IP) along the beam direction, $|dz| < 4.0$ cm, and in the transverse plane, $dr < 0.4$ cm. Additional SVD requirements of at least two z hits and one $r - \phi$ hit [28] are imposed on at least one charged track forming an ω candidate so that a good quality vertex of the reconstructed B meson candidate can be determined. Using information obtained from the CDC, ACC, and TOF, particle identification (PID) is determined from a likelihood ratio $\mathcal{L}_{i/j} \equiv \mathcal{L}_i/(\mathcal{L}_i + \mathcal{L}_j)$. Here, \mathcal{L}_i (\mathcal{L}_j) is the likelihood that the particle is of type i (j). To suppress background due to electron misidentification, ECL information is used to veto particles consistent with the electron hypothesis [29]. The PID ratios of all charged tracks $\mathcal{L}_{K/\pi}$ are used to identify them as a kaon or a pion.

A K_S^0 candidate consists of two oppositely charged π candidates. We only consider K_S^0 candidates with vertices displaced from the IP; the displacement depends on the K_S^0 momentum. Only events in the mass window $|M_{\pi\pi} - m_{K_S^0}| < 16$ MeV/ c^2 are accepted, where $m_{K_S^0}$ is the world average mass of the K_S^0 [30].

Photons (γ) are identified as isolated ECL clusters that are not matched to any charged particle track. To suppress the combinatorial background, the photons are required to have a minimum energy of $E_\gamma > 50$ MeV in the ECL barrel region and $E_\gamma > 100$ MeV in the ECL end cap regions, where the barrel region covers the polar angle range

TABLE II. Summary of $B \rightarrow \omega K$ branching fractions (in units of 10^{-6}) and CP violation parameters (in units of 10^{-2}) obtained by Belle [8,22] and *BaBar* [9,23]. For all parameters, the first uncertainty is statistical, and the second is systematic.

Parameter	Belle	Belle	<i>BaBar</i>
	(388×10^6 $B\bar{B}$ pairs)	(535×10^6 $B\bar{B}$ pairs)	(467×10^6 $B\bar{B}$ pairs)
$\mathcal{B}(B^0 \rightarrow \omega K_S^0)$	$4.4^{+0.8}_{-0.7} \pm 0.4$...	$5.4 \pm 0.8 \pm 0.3$
$\mathcal{A}_{\omega K_S^0}$...	$-9 \pm 29 \pm 6$	$52^{+20}_{-22} \pm 3$
$\mathcal{S}_{\omega K_S^0}$...	$11 \pm 46 \pm 7$	$55^{+26}_{-29} \pm 2$

Parameter	Belle (388×10^6 $B\bar{B}$ pairs)	<i>BaBar</i> (383×10^6 $B\bar{B}$ pairs)
	$\mathcal{B}(B^+ \rightarrow \omega K^+)$	$8.1 \pm 0.6 \pm 0.6$
$\mathcal{A}_{\omega K^+}$	$5^{+8}_{-7} \pm 1$	$-1 \pm 7 \pm 1$

$32^\circ < \theta < 130^\circ$ and the end cap regions cover the forward and backward regions in the ranges $12^\circ < \theta < 32^\circ$ and $130^\circ < \theta < 157^\circ$. Two γ candidates are combined to form a π^0 candidate that must satisfy $|M_{\gamma\gamma} - m_{\pi^0}| < 16 \text{ MeV}/c^2$, where m_{π^0} is the world average mass of the π^0 [30].

An ω candidate consists of two oppositely charged pion candidates and a π^0 candidate with the requirement $|M_{3\pi} - m_\omega| < 50 \text{ MeV}/c^2$, where m_ω is the world average mass of the ω [30]. The mass distribution of the ω candidates is shown in Figs. 2(d) and 3(d). The mass cuts given above correspond to about three times the typical experimental resolution of the K_S^0 , π^0 , and ω world average masses. We also reconstruct the cosine of the helicity angle $\mathcal{H}_{3\pi}$ of the ω candidates. This angle is defined as that between the direction of B_{Rec} and the normal to the three-pion decay plane, both calculated in the rest frame of the ω candidate. The $\mathcal{H}_{3\pi}$ distributions for all components are presented in Figs. 2(e) and 3(e).

Reconstructed B meson candidates are identified with two nearly uncorrelated kinematic variables: the beam-energy-constrained mass $M_{\text{bc}} \equiv \sqrt{(E_{\text{beam}}^{\text{CMS}})^2 - (p_B^{\text{CMS}})^2}$ and the energy difference $\Delta E \equiv E_B^{\text{CMS}} - E_{\text{beam}}^{\text{CMS}}$, where $E_{\text{beam}}^{\text{CMS}}$ is the beam energy and E_B^{CMS} (p_B^{CMS}) is the energy (momentum) of the B meson, all evaluated in the e^+e^- center-of-mass system (CMS). The B meson candidates that satisfy $M_{\text{bc}} > 5.25 \text{ GeV}/c^2$ and $-0.15 \text{ GeV} < \Delta E < 0.1 \text{ GeV}$ are retained for further analysis. The distributions of these two variables are shown in Figs. 2(a) and 3(a) and Figs. 2(b) and 3(b), respectively.

B. B vertex reconstruction

As the B_{Rec} and B_{Tag} are almost at rest in the CMS, the difference in decay time between the two B meson candidates, Δt , can be determined approximately from the displacement in z between the final-state decay vertices as

$$\Delta t \simeq \frac{(z_{\text{Rec}} - z_{\text{Tag}})}{\beta\gamma c} \equiv \frac{\Delta z}{\beta\gamma c}, \quad (3)$$

where $\beta\gamma = 0.425$ is the Lorentz boost of the $\Upsilon(4S)$ in the lab frame and c is the speed of light.

The B_{Rec} decay vertex is determined from one or two charged daughters of the ω , depending on whether they pass the SVD requirements. A single-track vertex is possible as an IP constraint using the known beam profile in the x - y plane is always included as a pseudotrack in the vertex finding algorithm. To obtain the Δt distribution, we also reconstruct the tag-side vertex from the tracks not used to reconstruct B_{Rec} [28]. Candidate events must satisfy the loose requirements $|\Delta t| < 70 \text{ ps}$ and $h_{\text{Rec, Tag}} < 50$, where $h_{\text{Rec, Tag}}$ is the multitrack vertex goodness of fit, calculated in three-dimensional space without the IP profile constraint [4]. To avoid the necessity of also modeling the event-dependent observables that describe the Δt resolution in the fit [31], the vertex uncertainty is required to satisfy $\sigma_z^{\text{Rec, Tag}} < 200 \mu\text{m}$ for multitrack vertices and $\sigma_z^{\text{Rec, Tag}} < 500 \mu\text{m}$ for vertices reconstructed from single tracks and the IP constraint. The efficiency of the vertexing algorithm is 91%.

C. Flavor tagging

The B_{Tag} flavor is determined from the remaining tracks and photons left over from the B_{Rec} reconstruction. The flavor-tagging procedure is described in Ref. [34]. The tagging information is represented by two parameters, the B_{Tag} flavor q and the flavor-tagging quality r . The parameter r is continuous and determined on an event-by-event basis with an algorithm trained on MC-simulated events, ranging from zero for no flavor discrimination to unity for an unambiguous flavor assignment. To obtain a data-driven replacement for r , we divide its range into seven regions and determine a probability of mistagging w for each r region using high statistics control samples. If MC describes the data perfectly, then $r = 1 - 2w$. The CP asymmetry in data is thus diluted by a factor $1 - 2w$ instead of the MC-determined r . The measure of the flavor-tagging algorithm performance is the total effective tagging efficiency $\epsilon_{\text{eff}} = (1 - 2w)^2 \epsilon_{\text{Tag}}$, rather than the raw tagging efficiency ϵ_{Tag} , as the statistical significance of the CP parameters is proportional to $(1 - 2w)\sqrt{\epsilon_{\text{Tag}}}$. These are determined from data to be $\epsilon_{\text{eff}} = 0.284 \pm 0.010$ and $\epsilon_{\text{eff}} = 0.301 \pm 0.004$ for the SVD1 and SVD2 data, respectively [4]. After the flavor-tagging algorithm has been applied, 99.8% of all signal candidates remain.

D. Continuum reduction

The dominant background in the reconstruction of B_{Rec} arises from $q\bar{q}$ (continuum) events, where $q = u, d, s, c$. Since their topology tends to be jetlike in contrast to the spherical $B\bar{B}$ decay, continuum events are suppressed

TABLE III. Summary of the detection efficiencies (eff.) (top) and PID correction factors (bottom) for $B^0 \rightarrow \omega K_S^0$ and $B^+ \rightarrow \omega K^+$. The values of the efficiency yields and their uncertainties are obtained from signal MC.

Decay	Eff. SVD1 ($\epsilon^{1,d}$)	Eff. SVD2 ($\epsilon^{2,d}$)
$B^0 \rightarrow \omega K_S^0$	0.1136 ± 0.0003	0.1454 ± 0.0004
$B^+ \rightarrow \omega K^+$	0.1828 ± 0.0004	0.2195 ± 0.0005
Decay	PID SVD1 ($\eta^{1,d}$)	PID SVD2 ($\eta^{2,d}$)
$B^0 \rightarrow \omega K_S^0$	0.961 ± 0.010	0.959 ± 0.020
$B^+ \rightarrow \omega K^+$	0.948 ± 0.018	0.923 ± 0.028

with a Fisher discriminant [32] based on modified Fox–Wolfram moments [33]. The $B\bar{B}$ training sample is taken from signal MC simulation, while the $q\bar{q}$ training sample is based on sideband data taken at the $\Upsilon(4S)$ resonance with minimal contamination from B mesons, defined as $M_{bc} < 5.25 \text{ GeV}/c^2$ and $0.05 \leq \Delta E \leq 0.2 \text{ GeV}$. The distributions of both samples are combined to form a likelihood ratio distribution, which peaks at unity for $B\bar{B}$ events and at zero for $q\bar{q}$ background. To further improve the signal-background distinction, the likelihood ratio of the Fisher discriminant is multiplied by the likelihood ratio of the polar angle of the B meson candidate in the CMS, $\cos\theta_B$, which follows a $1 - \cos^2\theta_B$ distribution for $B\bar{B}$ events while being flat for the continuum. We employ a loose selection on the resulting likelihood ratio, $\mathcal{L}_{B\bar{B}/q\bar{q}} \geq 0.2$, which reduces $q\bar{q}$ background by 62% with a signal efficiency of 94%. To make the likelihood ratio distribution easier to parametrize, it is transformed into a Gaussian-like distribution according to

$$\mathcal{F}_{B\bar{B}/q\bar{q}} = \log \frac{\mathcal{L}_{B\bar{B}/q\bar{q}} - 0.2}{1 - \mathcal{L}_{B\bar{B}/q\bar{q}}}. \quad (4)$$

The signal and background $\mathcal{F}_{B\bar{B}/q\bar{q}}$ distributions are shown in Figs. 2(c) and 3(c).

E. Reconstruction efficiency

After these selection criteria, we obtain from signal MC the detection efficiencies $\epsilon^{s,d}$ for each SVD configuration s and decay channel d . These are summarized in Table III. The uncertainties come from limited MC simulation statistics. We also determine correction factors to the

efficiency $\eta^{s,d}$ that account for the difference between data and MC simulation as calculated by independent studies at Belle. These correction factors in our reconstruction algorithm arise only from PID and are determined from an inclusive $D^+ \rightarrow D^0[K^-\pi^+]\pi^+$ sample. They are summarized in Table III.

About 15% of all events have more than one B candidate. For these events, an arbitrary candidate is selected. From MC simulation, 2% of signal events is found to be misreconstructed, defined as being events where at least one of the tracks entering the vertex reconstruction does not belong to the B meson of interest.

IV. EVENT MODEL

The two branching fractions and three CP -violation parameters of $B \rightarrow \omega K$ are extracted from a sequence of seven-dimensional unbinned extended maximum likelihood fits to ΔE , M_{bc} , $\mathcal{F}_{B\bar{B}/q\bar{q}}$, $M_{3\pi}$, $\mathcal{H}_{3\pi}$, Δt , and q performed simultaneously on the two data samples d , each divided into seven bins ($l = 0 \dots 6$) in the flavor-tag quality r and two SVD configurations s . In the first fit, the two branching fractions and CP parameters of the neutral mode are determined. In two further fits, the charged data sample is divided into two subsamples depending on the B charge. From these, two signal yields are extracted in order to determine $\mathcal{A}_{\omega K^+}$ according to Eq. (2). The following categories are considered in the event model: signal, misreconstructed signal, continuum, charm and charmless neutral and charged B meson decays, and charm and charmless peaking backgrounds. The probability density function (PDF) for each category is usually taken as the product of PDFs for each variable (unless otherwise stated), $\mathcal{P}^{l,s,d}(\Delta E, M_{bc}, \mathcal{F}_{B\bar{B}/q\bar{q}}, M_{3\pi}, \mathcal{H}_{3\pi}, \Delta t, q) \equiv \mathcal{P}^{l,s,d}(\Delta E) \times \mathcal{P}^{l,s,d}(M_{bc}) \times \mathcal{P}^{l,s,d}(\mathcal{F}_{B\bar{B}/q\bar{q}}) \times \mathcal{P}^{l,s,d}(M_{3\pi}) \times \mathcal{P}^{l,s,d}(\mathcal{H}_{3\pi}) \times \mathcal{P}^{l,s,d}(\Delta t, q)$, in each l, s, d bin as most correlations between the fit observables are negligible. We describe these fit models for each category explicitly in the following subsections.

A. Signal model

The signal shapes are determined from the signal MC events where the π^+ and π^- forming the ω candidate are correctly reconstructed. The PDF for ΔE is the sum of three Gaussian functions and a linear function,

$$\begin{aligned} \mathcal{P}_{\text{Sig}}^{l,s,d}(\Delta E) \equiv & f_1^{s,d} G(\Delta E; \mu_1^{s,d} + \mu_C^s, \sigma_1^{s,d} \sigma_C^s) \\ & + f_2^{s,d} G(\Delta E; \mu_2^{s,d} + \mu_1^{s,d} + \mu_C^s, \sigma_2^{s,d} \sigma_1^{s,d} \sigma_C^s) \\ & + f_3^{s,d} G(\Delta E; \mu_3^{s,d} + \mu_2^{s,d} + \mu_1^{s,d} + \mu_C^s, \sigma_3^{s,d} \sigma_2^{s,d} \sigma_1^{s,d} \sigma_C^s) \\ & + (1 - f_1^{s,d} - f_2^{s,d} - f_3^{s,d})(1 + c^{s,d} \Delta E), \end{aligned} \quad (5)$$

where the two-tail Gaussians are parametrized relative to the main Gaussian. This PDF also incorporates calibration parameters μ_C^s and σ_C^s , which correct for the difference between data and MC simulation. These parameters calibrate the mean and width of the main Gaussian component and are the only parameters shared between both data samples. They are fixed to zero and unity, respectively, in the fit to determine the signal model from MC, but are free in the fit to data. Because of the low signal yield of the neutral mode, we determine the calibration factors in a simultaneous fit of two decay channels instead of extracting them from a separate control sample fit. Thus, to first order, we do not need to consider the related systematic uncertainties that

arise from the difference between data and MC. Because of our definition of correctly reconstructed events, the linear part of the PDF is necessary to describe events where the π^0 or K_S^0 are incorrectly reconstructed.

The PDF for M_{bc} is taken to be the sum of three Gaussians and an empirically determined shape referred to as an ARGUS function (A) [35], which has an event-dependent cutoff at $E_{\text{beam}}^{\text{CMS}}$. The ARGUS function represents events analogous to those of the linear function models in ΔE . Because of correlations of 4–5% between ΔE and M_{bc} in the different data samples, the dependency of the main mean and relative fraction of the main Gaussian leads to the parametrization

$$\begin{aligned} \mathcal{P}_{\text{Sig}}^{l,s,d}(M_{bc}|\Delta E) &\equiv (f_1^{s,d} + \alpha^{s,d}|\Delta E|)G(M_{bc}; \mu_1^{s,d} + \mu_C^s + \beta^{s,d}\Delta E, \sigma_1^{s,d}\sigma_C^s) \\ &\quad + f_2^{s,d}G(M_{bc}; \mu_2^{s,d} + \mu_1^{s,d} + \mu_C^s + \beta^{s,d}\Delta E, \sigma_2^{s,d}\sigma_1^{s,d}\sigma_C^s) \\ &\quad + f_3^{s,d}G(M_{bc}; \mu_3^{s,d} + \mu_2^{s,d} + \mu_1^{s,d} + \mu_C^s + \beta^{s,d}\Delta E, \sigma_3^{s,d}\sigma_2^{s,d}\sigma_1^{s,d}\sigma_C^s) \\ &\quad + (1 - [f_1^{s,d} + \alpha^{s,d}|\Delta E|] - f_2^{s,d} - f_3^{s,d})A(M_{bc}; a^{s,d}), \end{aligned} \quad (6)$$

where $\alpha^{s,d}$ and $\beta^{s,d}$ represent the additional correlation parameters and $a^{s,d}$ is the shape parameter of the ARGUS function. As in ΔE , only the shared calibration parameters are free in the fit to data.

The PDF for $\mathcal{F}_{B\bar{B}/q\bar{q}}$ is taken to be the sum of three Gaussians in each flavor-tag bin l ,

$$\begin{aligned} \mathcal{P}_{\text{Sig}}^{l,s,d}(\mathcal{F}_{B\bar{B}/q\bar{q}}) &\equiv f_1^{l,s,d}G(\mathcal{F}_{B\bar{B}/q\bar{q}}; \mu_1^{l,s,d} + \mu_C^{l,s}, \sigma_1^{l,s,d}\sigma_C^{l,s}) \\ &\quad + f_2^{l,s,d}G(\mathcal{F}_{B\bar{B}/q\bar{q}}; \mu_2^{l,s,d} + \mu_1^{l,s,d} + \mu_C^{l,s}, \sigma_2^{l,s,d}\sigma_1^{l,s,d}\sigma_C^{l,s}) \\ &\quad + f_3^{l,s,d}G(\mathcal{F}_{B\bar{B}/q\bar{q}}; \mu_3^{l,s,d} + \mu_2^{l,s,d} + \mu_1^{l,s,d} + \mu_C^{l,s}, \sigma_3^{l,s,d}\sigma_2^{l,s,d}\sigma_1^{l,s,d}\sigma_C^{l,s}). \end{aligned} \quad (7)$$

This time, the shared calibration parameters also depend on l and are free in the fit to data.

The $M_{3\pi}$ PDF also consists of the sum of three Gaussians where the correlation of 27% between ΔE and $M_{3\pi}$ is considered as

$$\begin{aligned} \mathcal{P}_{\text{Sig}}^{l,s,d}(M_{3\pi}|\Delta E) &\equiv f_1^{s,d}G(M_{3\pi}; \mu_1^{s,d} + \mu_C^s + \alpha^{s,d}\Delta E, \sigma_1^{s,d}\sigma_C^s + \beta^{s,d}\Delta E^2) \\ &\quad + f_2^{s,d}G(M_{3\pi}; \mu_2^{s,d} + \mu_1^{s,d} + \mu_C^s + \alpha^{s,d}\Delta E, \sigma_2^{s,d}[\sigma_1^{s,d}\sigma_C^s + \beta^{s,d}\Delta E^2]) \\ &\quad + (1 - f_1^{s,d} - f_2^{s,d})G(M_{3\pi}; \mu_3^{s,d} + \mu_2^{s,d} + \mu_1^{s,d} + \mu_C^s + \alpha^{s,d}\Delta E, \sigma_3^{s,d}\sigma_2^{s,d}[\sigma_1^{s,d}\sigma_C^s + \beta^{s,d}\Delta E^2]), \end{aligned} \quad (8)$$

where $\alpha^{s,d}$ and $\beta^{s,d}$ are the correlation parameters.

The $\mathcal{H}_{3\pi}$ shape is modeled with the sum of symmetric Chebyshev polynomials C_i , up to fourth order and is determined from MC:

$$\mathcal{P}_{\text{Sig}}^{l,s,d}(\mathcal{H}_{3\pi}) \equiv 1 + \sum_{i=1}^2 c_{2i}^{s,d} C_{2i}(\mathcal{H}_{3\pi}). \quad (9)$$

The PDF of Δt and q for $B^0 \rightarrow \omega K_S^0$ is given by

$$\begin{aligned} \mathcal{P}_{\text{Sig}}^{l,s,\omega K_S^0}(\Delta t, q) &\equiv (1 - f_{\text{Out}}^s) \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \{1 - q\Delta w^{l,s} + q(1 - 2w^{l,s}) \times [\mathcal{A}_{\omega K_S^0} \cos \Delta m_d \Delta t + \mathcal{S}_{\omega K_S^0} \sin \Delta m_d \Delta t]\} \otimes R_{B^0 \bar{B}^0}^s(\Delta t) \\ &\quad + f_{\text{Out}}^s \frac{1}{2} G(\Delta t; 0, \sigma_{\text{Out}}^s), \end{aligned} \quad (10)$$

which accounts for CP dilution from the probability of incorrect flavor tagging $w^{l,s}$ and the wrong tag difference $\Delta w^{l,s}$ between B^0 and \bar{B}^0 . The values of $w^{l,s}$ and $\Delta w^{l,s}$ are determined from flavor-specific control samples using the method as described in Ref [34]. The physics parameters τ_{B^0} and Δm_d are fixed to their respective current world averages [30]. This PDF is convolved with the Δt resolution function for neutral B particles $R_{B^0\bar{B}^0}^s$, as given in Ref. [4], which describes Δt smearing effects due to detector resolution, the use of nonprimary tracks to form the tag-side vertex, and the kinematic approximation of calculating Δt from the one-dimensional separation Δz . To account for the possibility of remaining outlier Δt events that cannot be described by the Δt resolution function, a broad Gaussian centered at zero is introduced with a relative fraction f_{Out}^s and width σ_{Out}^s parameters given in Ref. [4]. For $B^+ \rightarrow \omega K^+$, the PDF is given by

$$\mathcal{P}_{\text{Sig}}^{l,s,\omega K^+}(\Delta t, q) \equiv (1 - f_{\text{Out}}^s) \frac{e^{-|\Delta t|/\tau_{B^+}}}{4\tau_{B^+}} \otimes R_{B^+B^-}^s(\Delta t) + f_{\text{Out}}^s \frac{1}{2} G(\Delta t; 0, \sigma_{\text{Out}}^s), \quad (11)$$

where $R_{B^+B^-}^s$ is the Δt resolution function for charged B meson decays [4]. There are no free parameters in this case.

B. Misreconstructed signal model

The misreconstructed model shape is determined from signal MC simulation events with an incorrectly reconstructed vertex. The PDFs for ΔE and $M_{3\pi}$ are the sum of a Gaussian and a linear function, while the M_{bc} PDF is a combination of an asymmetric Gaussian and an ARGUS function. The shape of $\mathcal{F}_{B\bar{B}/q\bar{q}}$ is the same as Eq. (7) from the signal model and shares most of the parameters including calibration factors; however, the main mean in each flavor-tag bin is determined from the misreconstructed sample. For $\mathcal{H}_{3\pi}$, the sum of symmetric Chebyshev polynomials up to second order is used. The variables Δt and q are modeled with the same PDF shape as the correctly reconstructed signal events but with an effective lifetime rather than τ_{B^0} . This lifetime is obtained from MC and is necessary due to the presence of a tag-side track in the vertex reconstruction. This has the effect of reducing the average Δz separation between B_{Rec} and B_{Tag} . We found from MC that, although the vertex reconstruction was incorrect, the CP information was mostly retained, so the CP parameters are shared with signal and are free in the fit to data. The difference between the generated CP parameters in MC and misreconstructed signal events is then considered in the systematics.

C. Continuum model

The parametrization of the continuum model is based on the sideband data; however, all the shape parameters of ΔE ,

M_{bc} , $\mathcal{F}_{B\bar{B}/q\bar{q}}$, and $M_{3\pi}$ are floated in the fit to data. ΔE and M_{bc} are modeled by a linear and an ARGUS function, respectively, with parameters defined in bins of s, d . The variable $\mathcal{F}_{B\bar{B}/q\bar{q}}$ is modeled by the sum of either one or two Gaussian functions in each l, s, d bin depending on the amount of data available in each bin. The PDF for $M_{3\pi}$ is a combination of a Gaussian and a linear function, while $\mathcal{H}_{3\pi}$ is the sum of a Gaussian centered around zero and a constant. The parameters of both these PDFs are determined in each s, d bin. The Δt model is fixed from the sideband,

$$\mathcal{P}_{q\bar{q}}^{l,s,d}(\Delta t, q) \equiv \frac{1}{2} \left[(1 - f_{\delta}^d) \frac{e^{-|\Delta t|/\tau_{q\bar{q}}^d}}{2\tau_{q\bar{q}}^d} + f_{\delta}^d \delta(\Delta t - \mu_{\delta}^{s,d}) \right] \otimes R_{q\bar{q}}^{s,d}(\Delta t), \quad (12)$$

and contains a finite-lifetime and prompt component with a fraction f_{δ}^d and a mean $\mu_{\delta}^{s,d}$. The two components account for the long-lived charm and charmless contributions, respectively. The total distribution is convolved with a sum of two Gaussian functions

$$R_{q\bar{q}}^{s,d}(\Delta t) \equiv (1 - f_{\text{tail}}^{s,d}) G(\Delta t; \mu_{\text{mean}}^{s,d}, S_{\text{main}}^{s,d} \sigma) + f_{\text{tail}}^{s,d} G(\Delta t; \mu_{\text{mean}}^{s,d}, S_{\text{main}}^{s,d} S_{\text{tail}}^{s,d} \sigma), \quad (13)$$

which uses the event-dependent Δt error constructed from the estimated vertex resolution $\sigma \equiv (\sqrt{\sigma_{\text{Rec}}^2 + \sigma_{\text{Tag}}^2})/\beta\gamma c$ as a scale factor of the width parameters S_{main}^s and S_{tail}^s .

D. $B\bar{B}$ model

The next-largest background comes from neutral and charged charm $b \rightarrow c$ and neutral and charged charmless $b \rightarrow u, d, s$ decays of the B meson. Some of these B decays exhibit peaking structure in the signal region due to the reconstruction of particular channels with identical final states. These are modeled separately from the nonpeaking $B\bar{B}$ background, which is described in this subsection. The charm and charmless B meson background shapes are determined from a large sample of MC simulation events based on $b \rightarrow c$ and $b \rightarrow u, d, s$ transitions, respectively. The two data sets are further subdivided into neutral and charged B meson samples to account for their different effective lifetimes.

For all $B\bar{B}$ background shapes except for the charged charm samples, the ΔE distribution is modeled with the sum of a linear function and a Gaussian accounting for six-pion final states from which only five pions were reconstructed and thus peak roughly around $-0.14 \text{ GeV}/c^2$. The remaining charged charm samples are modeled with the sum of Chebyshev polynomials up to second order. We model M_{bc} in the neutral charm category with an ARGUS function and in the charged charm category with a

histogram PDF. In the charmless models, the PDF for M_{bc} is the sum of an asymmetric Gaussian and an ARGUS function. A sizable correlation of 12% is found between M_{bc} and $\mathcal{F}_{B\bar{B}/q\bar{q}}$ in the neutral charmless model for $B^0 \rightarrow \omega K_S^0$ and in the charged charmless model for $B^+ \rightarrow \omega K^+$, which is taken into account by further parametrizing this shape of M_{bc} in terms of $\mathcal{F}_{B\bar{B}/q\bar{q}}$,

$$\begin{aligned} \mathcal{P}_{\text{Charmless}}^{l,s,d}(M_{bc}|\mathcal{F}_{B\bar{B}/q\bar{q}}) \\ \equiv f^{s,d}G(M_{bc};\mu^{s,d},\sigma_l^{s,d},\sigma_r^{s,d}) \\ + (1-f^{s,d})A(M_{bc};a^{s,d}+\gamma^{s,d}\mathcal{F}_{B\bar{B}/q\bar{q}},E_{\text{beam}}), \quad (14) \end{aligned}$$

where $\gamma^{s,d}$ is the correlation parameter. In $\mathcal{F}_{B\bar{B}/q\bar{q}}$, the shape borrows from the signal model, where, again, the main mean in each flavor-tag bin is obtained from the relevant $B\bar{B}$ MC simulation sample. In the charm samples, $M_{3\pi}$ is modeled with a linear function; in the charmless samples, an additional Gaussian component is necessary. The variable $\mathcal{H}_{3\pi}$ in the charm sample is taken to be a histogram PDF; in the charmless model, the sum of a Gaussian and a linear function is used. We fit Δt and q with the same lifetime function as for the signal, but instead of the world average for the B meson lifetime, we determine an effective lifetime of the various B meson decays from their respective MC samples. In general, the effective lifetime is smaller than the generated B meson lifetime because a track in B_{Rec} can originate from the tag side. The CP parameters are fixed to zero.

E. Peaking charm $B\bar{B}$ model

In the neutral decay mode $B^0 \rightarrow \omega K_S^0$, this category includes the charm decays $B^0 \rightarrow D^{*-}[D^0\{K_S^0\pi^0\}\pi^-]\pi^+$, $B^0 \rightarrow D^-[K_S^0\pi^-\pi^0]\pi^+$, and $B^0 \rightarrow D^-[K_S^0\pi^-\rho^+][\pi^+\pi^0]$. For the charged decay mode $B^+ \rightarrow \omega K^+$, this includes only $B^+ \rightarrow D^0[K^+\pi^-]\rho^+[\pi^+\pi^0]$. To account for the peaking structure in ΔE , its PDF is taken to be the same as that of the signal; however, the parameters of the linear component and its relative fraction are determined from the peaking charm $B\bar{B}$ MC simulation. The model for M_{bc} is taken to be the combination of a Gaussian function and an ARGUS function. Because of a correlation between ΔE and M_{bc} of up to 12%, the fraction of the Gaussian component is linearly parametrized in terms of ΔE . The variable $\mathcal{F}_{B\bar{B}/q\bar{q}}$ also borrows from the signal model with the main mean and width of the distribution in each flavor-tag bin determined from the peaking charm $B\bar{B}$ MC simulation. In the neutral mode, $\mathcal{H}_{3\pi}$ is modeled with a Gaussian centered around zero; in the charged mode, a symmetrized histogram is used. The variables Δt and q are fitted with a lifetime function with an effective lifetime determined from MC simulation.

F. Peaking charmless $B\bar{B}$ model

This category only affects the charged decay mode $B^+ \rightarrow \omega K^+$ and includes the charmless decays $B^+ \rightarrow a_1^0[\pi^+\pi^-\pi^0]K^+$ and $B^+ \rightarrow \omega[\pi^+\pi^-\pi^0]\pi^+$. In ΔE , two peaks are visible in the distribution: one around zero and one shifted to positive values near the difference between the kaon and pion mass, originating from $B^+ \rightarrow \omega[\pi^+\pi^-\pi^0]\pi^+$ decays, where a pion is misidentified as a kaon. Both peaks are modeled with the triple Gaussian component of the signal PDF for ΔE , where the mean of the misidentified peak is determined from the peaking charmless $B\bar{B}$ MC simulation. The combinatorial component is modeled with a first-order Chebyshev, for which the shape and fraction are also determined from MC. The model for M_{bc} is the sum of two Gaussians and an ARGUS function. Because of up to a 14% correlation between M_{bc} and ΔE , the main width and fraction of the Gaussian as well as the ARGUS slope parameter are parametrized in terms of ΔE . Once again, $\mathcal{F}_{B\bar{B}/q\bar{q}}$ borrows from the signal model with the main mean and width in each flavor-tag bin determined from peaking charmless $B\bar{B}$ MC simulation. The $\mathcal{H}_{3\pi}$ variable is modeled with the sum of symmetric Chebyshev polynomials up to fourth order. Finally, Δt and q are fitted with a lifetime function with an effective lifetime determined from MC simulation.

G. Full model

The total extended likelihood is given by

$$\begin{aligned} \mathcal{L} \equiv \prod_{l,s,d} \frac{e^{-\sum_j N_j^{s,d} f_j^{l,s,d}} N_{l,s,d}^{N_{l,s,d}}}{N_{l,s,d}!} \prod_{i=1} \sum_j N_j^{s,d} f_j^{l,s,d} \mathcal{P}_j^{l,s,d} \\ \times (\Delta E^i, M_{bc}^i, \mathcal{F}_{B\bar{B}/q\bar{q}}^i, M_{3\pi}^i, \mathcal{H}_{3\pi}^i, \Delta t^i, q^i), \quad (15) \end{aligned}$$

which iterates over i events, j categories, l flavor-tag bins, s detector configurations, and the d data samples $B^0 \rightarrow \omega K_S^0$ and $B^+ \rightarrow \omega K^+$. The fraction of events in each l, s, d bin, for category j , is denoted by $f_j^{l,s,d}$. With the exception of the continuum, for which the fit fractions are free in the fit to the data, these parameters are fixed for each category from their respective MC samples. The fraction of signal events in each l, s, d bin, $f_{\text{Sig}}^{l,s,d}$, is corrected using common correction factors for $B^0 \rightarrow \omega K_S^0$ and $B^+ \rightarrow \omega K^+$, which are also free parameters in the fit to the data. Additional free fit parameters include the $N_{q\bar{q}}^{s,d}$ yields. Instead of obtaining separate signal yields for SVD1 and SVD2 $N_{\text{Sig}}^{s,d}$, this parameter is transformed so that the branching fraction becomes a single free parameter between s samples and is incorporated into the fit with

$$N_{\text{Sig}}^{s,d} = \mathcal{B}^d(B \rightarrow \omega K) \times N_{B\bar{B}}^s e^{s,d} \eta_{\text{Sig}}^{s,d}, \quad (16)$$

TABLE IV. Summary of yields fixed relative to other yields in the fit for $B^0 \rightarrow \omega K_S^0$ (top) and $B^+ \rightarrow \omega K^+$ (bottom). The values of the yields and their uncertainties are obtained from MC statistics.

Yield	SVD1	SVD2
$N_{\text{Mis}}^{s,\omega K_S^0}$	$(0.0192 \pm 0.0004)N_{\text{Sig}}^{1,\omega K_S^0}$	$(0.0187 \pm 0.0004)N_{\text{Sig}}^{2,\omega K_S^0}$
$N_{\text{Charm}B^0\bar{B}^0}^{s,\omega K_S^0}$	12 ± 3	56 ± 7
$N_{\text{Charm}B^+B^-}^{s,\omega K_S^0}$	$(1.066 \pm 0.094)N_{\text{Charm}B^0\bar{B}^0}^{1,\omega K_S^0}$	$(1.268 \pm 0.048)N_{\text{Charm}B^0\bar{B}^0}^{2,\omega K_S^0}$
$N_{\text{Charmless}B^0\bar{B}^0}^{s,\omega K_S^0}$	$(5.992 \pm 0.216)N_{\text{Charm}B^0\bar{B}^0}^{1,\omega K_S^0}$	$(7.191 \pm 0.109)N_{\text{Charm}B^0\bar{B}^0}^{2,\omega K_S^0}$
$N_{\text{Charmless}B^+B^-}^{s,\omega K_S^0}$	$(4.537 \pm 0.193)N_{\text{Charm}B^0\bar{B}^0}^{1,\omega K_S^0}$	$(6.295 \pm 0.106)N_{\text{Charm}B^0\bar{B}^0}^{2,\omega K_S^0}$
$N_{\text{Peaking} \text{Charm}B^0\bar{B}^0}^{s,\omega K_S^0}$	$(0.719 \pm 0.077)N_{\text{Charm}B^0\bar{B}^0}^{1,\omega K_S^0}$	$(0.780 \pm 0.036)N_{\text{Charm}B^0\bar{B}^0}^{2,\omega K_S^0}$
Yield	SVD1	SVD2
$N_{\text{Mis}}^{s,\omega K^+}$	$(0.0182 \pm 0.0003)N_{\text{Sig}}^{1,\omega K^+}$	$(0.0182 \pm 0.0003)N_{\text{Sig}}^{2,\omega K^+}$
$N_{\text{Charm}B^0\bar{B}^0}^{s,\omega K^+}$	25 ± 5	147 ± 12
$N_{\text{Charm}B^+B^-}^{s,\omega K^+}$	$(3.334 \pm 0.115)N_{\text{Charm}B^0\bar{B}^0}^{1,\omega K^+}$	$(2.808 \pm 0.044)N_{\text{Charm}B^0\bar{B}^0}^{2,\omega K^+}$
$N_{\text{Charmless}B^0\bar{B}^0}^{s,\omega K^+}$	$(6.000 \pm 0.147)N_{\text{Charm}B^0\bar{B}^0}^{1,\omega K^+}$	$(5.556 \pm 0.060)N_{\text{Charm}B^0\bar{B}^0}^{2,\omega K^+}$
$N_{\text{Charmless}B^+B^-}^{s,\omega K^+}$	$(9.913 \pm 0.198)N_{\text{Charm}B^0\bar{B}^0}^{1,\omega K^+}$	$(8.828 \pm 0.077)N_{\text{Charm}B^0\bar{B}^0}^{2,\omega K^+}$
$N_{\text{Peaking} \text{Charm}B^+B^-}^{s,\omega K^+}$	$(1.504 \pm 0.077)N_{\text{Charm}B^0\bar{B}^0}^{1,\omega K^+}$	$(1.300 \pm 0.029)N_{\text{Charm}B^0\bar{B}^0}^{2,\omega K^+}$
$N_{\text{Peaking} \text{Charmless}B^+B^-}^{s,\omega K^+}$	$(7.130 \pm 0.168)N_{\text{Charm}B^0\bar{B}^0}^{1,\omega K^+}$	$(6.792 \pm 0.068)N_{\text{Charm}B^0\bar{B}^0}^{2,\omega K^+}$

where $N_{B\bar{B}}^s$ is the number of $B\bar{B}$ pairs collected by the Belle detector and $\epsilon_{\text{Sig}}^{s,d}$ and $\eta_{\text{Sig}}^{s,d}$ are detection efficiencies and selection criteria correction factors, respectively, given in Table III. The yield of the misreconstructed signal events is fixed with respect to the signal yield with a relative fraction determined from MC. The remaining $N_{B\bar{B}}^s$ yields are fixed from their expected amounts as determined from MC simulation and given in Table IV. In total, there are 204 free parameters in the fit: 54 belonging to signal and the remaining 150 to the continuum.

Following this, two additional fits are performed to calculate $\mathcal{A}_{\omega K^+}$ by measuring the two terms in Eq. (2). In these fits, we divide the $B^+ \rightarrow \omega K^+$ sample based on the kaon charge so that we may separately extract $\mathcal{B}(B^+ \rightarrow \omega K^+)$ and $\mathcal{B}(B^- \rightarrow \omega K^-)$. The only three free parameters in these fits are the signal branching fraction and the continuum yields $N_{q\bar{q}}^{s,\omega K^+}$. The $B\bar{B}$ yields for each $B^+ \rightarrow \omega K^+$ subsample are also recalculated as needed based on the relevant kaon charge. All remaining parameters are fixed to those found in the initial fit to the data.

H. Fit validation and improvements

To determine the branching fractions and CP -violation parameters, in contrast to the previous Belle analyses [8,22], we fit all variables and the two decay channels simultaneously. Extracting common calibration parameters between the two decay modes from the data allows us to

neglect systematic uncertainties in the low statistics neutral mode arising from the difference between data and MC simulation. An important difference from the previous Belle analyses is the improved tracking algorithm applied to the SVD2 data sample. This, combined with a looser cut on $\mathcal{L}_{B\bar{B}/q\bar{q}}$, improves the efficiency compared to the previous Belle branching fraction analysis [22] by a factor of 4 for the neutral mode and 2 for the charged mode. To improve the statistical precision of the branching fraction over the previous measurement, $\mathcal{F}_{B\bar{B}/q\bar{q}}$ has been included in the fit. Another improvement over both previous analyses is the inclusion of the $\mathcal{H}_{3\pi}$ observable into the fit, which significantly improves background discrimination. To determine the CP parameters, the previous Belle analysis [8] applied a two-step procedure where an initial fit without Δt and q was performed to obtain a signal yield. This allowed the event-dependent probabilities of each component to be determined and then used as input to set the fractions of each component in a fit to Δt and q . Our procedure of combining all variables together in a single fit has the added benefit of further discrimination against the continuum with the Δt variable and makes the treatment of systematic uncertainties more straightforward, at a cost of analysis complexity and longer computational time.

To test the validity of this model, we determine a possible fit bias from a pseudoexperiment MC simulation study in which the signal and the $B\bar{B}$ backgrounds are generated from GEANT-simulated events while the continuum

background is generated from our model of the sideband data. We find a bias for the branching fraction values of 16% and 45% of their statistical uncertainties for the neutral and charged mode, respectively. We correct the central values by these amounts and assign half the bias as a systematic uncertainty. Additionally, a linearity test across

the physical $\mathcal{A}_{\omega K_S^0} - \mathcal{S}_{\omega K_S^0}$ region is performed, showing no significant bias. This pseudoexperiment study indicates 30% improvement in the statistical uncertainty of the branching fractions of $B \rightarrow \omega K$, 15-20% improvement in the statistical uncertainty of the $B^0 \rightarrow \omega K_S^0$ time-dependent CP parameters and 30% improvement of $\mathcal{A}_{\omega K^+}$ over the

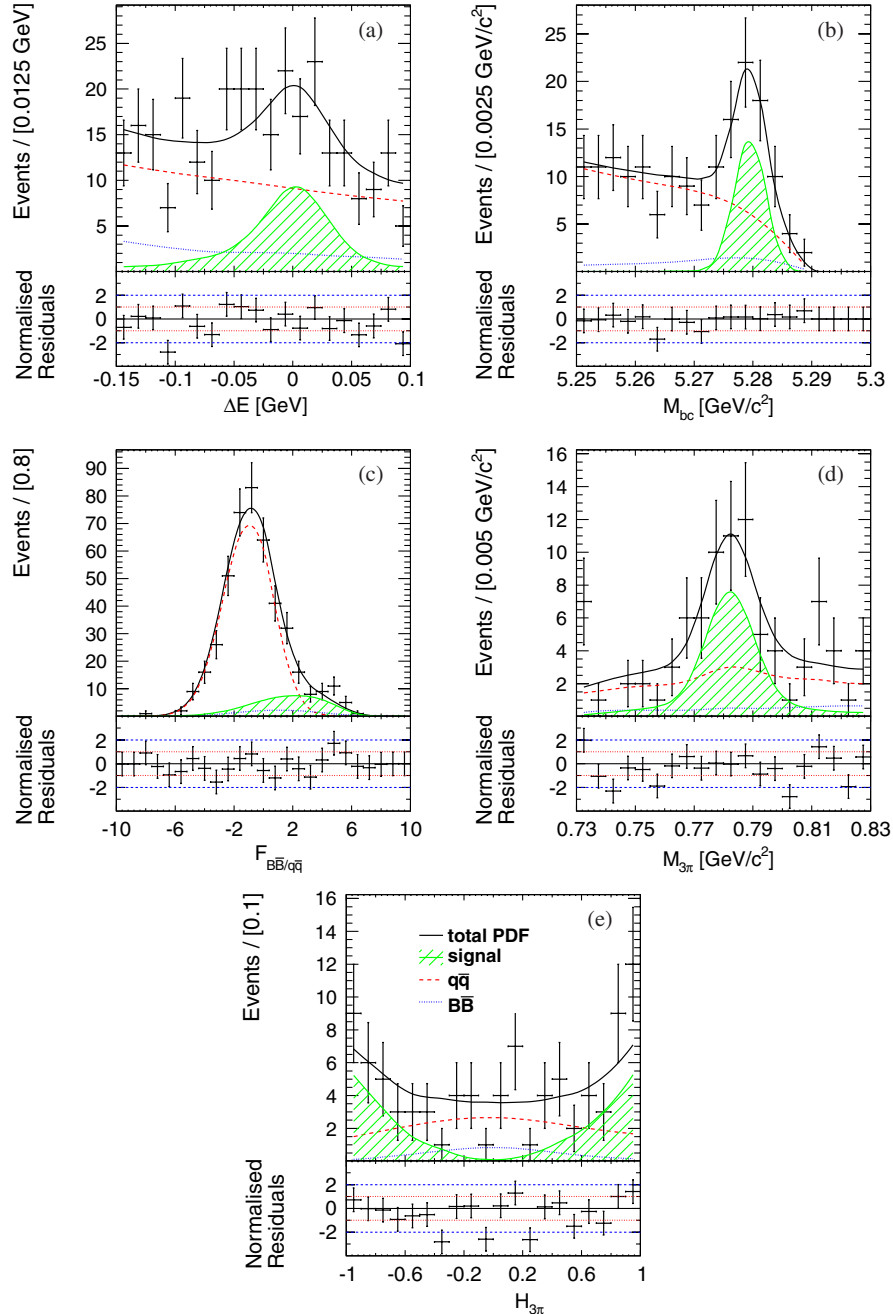


FIG. 2 (color online). Projections of the fit to the $B^0 \rightarrow \omega K_S^0$ data enhanced in the signal region. Points with error bars represent the data, and the solid black curves or histograms represent the fit results. The signal enhancements, $-0.04 \text{ GeV} < \Delta E < 0.03 \text{ GeV}$, $M_{bc} > 5.27 \text{ GeV}/c^2$, $\mathcal{F}_{B\bar{B}/q\bar{q}} > 1$, and $r > 0.5$, except for the enhancement of the fit observable being plotted, are applied to each projection. (a), (b), (c), (d), and (e) show the ΔE , M_{bc} , $\mathcal{F}_{B\bar{B}/q\bar{q}}$, $M_{3\pi}$, and $\mathcal{H}_{3\pi}$ projections, respectively. Green hatched curves show the $B^0 \rightarrow \omega K_S^0$ signal component, dashed red curves indicate the $q\bar{q}$ background, and blue dotted curves show the $B\bar{B}$ background component.

previous analysis methods. These numbers are calculated by scaling all uncertainties from the previous analyses to that expected with the final data set.

To test the validity of the Δt resolution description and reconstruction procedure, we perform a separate fit releasing the B^0 and B^+ lifetimes while blinding the physics

parameters; the results for τ_{B^0} and τ_{B^+} are consistent with their respective current world averages [30] within two standard deviations. As a further check of the Δt resolution function and the parameters describing the probability of mistagging, we fit for the time-dependent CP parameters of the $B^+ \rightarrow \omega K^+$ sample by substituting Eq. (10) for

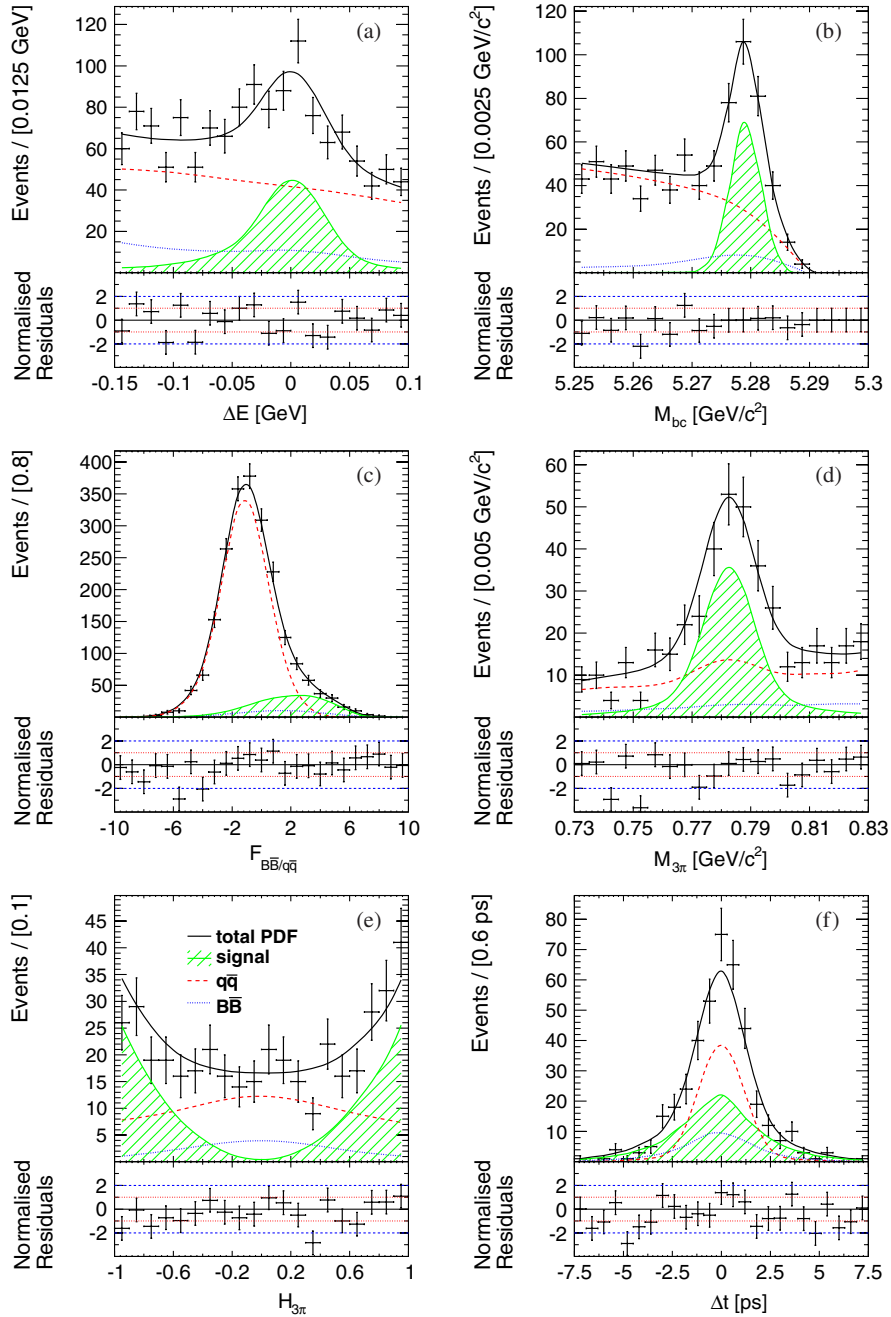


FIG. 3 (color online). Projections of the fit to the $B^+ \rightarrow \omega K^+$ data enhanced in the signal region. Points with error bars represent the data, and the solid black curves or histograms represent the fit results. The signal enhancements, $-0.04 \text{ GeV} < \Delta E < 0.03 \text{ GeV}$, $M_{bc} > 5.27 \text{ GeV}/c^2$, $\mathcal{F}_{B\bar{B}/q\bar{q}} > 1$, and $r > 0.5$, except for the enhancement of the fit observable being plotted, are applied to each projection. (a), (b), (c), (d), (e), and (f) show the ΔE , M_{bc} , $\mathcal{F}_{B\bar{B}/q\bar{q}}$, $M_{3\pi}$, $\mathcal{H}_{3\pi}$, and Δt projections, respectively. Green hatched curves show the $B^+ \rightarrow \omega K^+$ signal component, dashed red curves indicate the $q\bar{q}$ background, and blue dotted curves show the $B\bar{B}$ background component.

Eq. (11); the results are consistent within one standard deviation with $\mathcal{A}_{\omega K^+}$ obtained from the nominal fit and with null asymmetry for $\mathcal{S}_{\omega K^+}$.

V. RESULTS

From the fits to the data containing 17860 $B^0 \rightarrow \omega K_S^0$ and 88007 $B^+ \rightarrow \omega K^+$ candidates, the branching fractions and CP -violation parameters

$$\begin{aligned} \mathcal{B}(B^0 \rightarrow \omega K^0) &= (4.5 \pm 0.4(\text{stat}) \pm 0.3(\text{syst})) \times 10^{-6}, \\ \mathcal{B}(B^+ \rightarrow \omega K^+) &= (6.8 \pm 0.4(\text{stat}) \pm 0.4(\text{syst})) \times 10^{-6}, \\ \mathcal{A}_{\omega K_S^0} &= -0.36 \pm 0.19(\text{stat}) \pm 0.05(\text{syst}), \\ \mathcal{S}_{\omega K_S^0} &= +0.91 \pm 0.32(\text{stat}) \pm 0.05(\text{syst}), \\ \mathcal{A}_{\omega K^+} &= -0.03 \pm 0.04(\text{stat}) \pm 0.01(\text{syst}) \quad (17) \end{aligned}$$

are obtained, where the first uncertainty is statistical and the second is systematic, which is discussed below (Sec. VI). The statistical correlation coefficients between the branching fractions and the CP parameters are below 10^{-5} except for the 0.4% correlation between $\mathcal{A}_{\omega K_S^0}$ and $\mathcal{S}_{\omega K_S^0}$. Signal-enhanced fit projections are shown in Figs. 2, 3, and 4. The $B^0 \rightarrow \omega K_S^0$ and $B^+ \rightarrow \omega K^+$ branching fractions have been bias corrected, corresponding to signal event yields of $N(B^0 \rightarrow \omega K_S^0) = 234 \pm 22$ and $N(B^+ \rightarrow \omega K^+) = 1114 \pm 59$ where the uncertainties are statistical only. Before the bias correction, the central values of the branching fractions are $\mathcal{B}(B^0 \rightarrow \omega K^0) = 4.5 \times 10^{-6}$ and $\mathcal{B}(B^+ \rightarrow \omega K^+) = 6.9 \times 10^{-6}$. From the yields obtained in the fit to the data, the relative contributions of each component in the neutral mode are found to be 1.3% for the

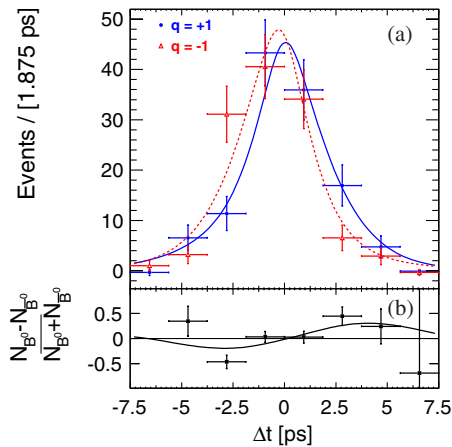


FIG. 4 (color online). Background subtracted time-dependent fit results for $B^0 \rightarrow \omega K_S^0$. (a) shows the Δt distribution for each B_{Tag} flavor q . The solid blue and dashed red curves represent the Δt distributions for B^0 and \bar{B}^0 tags, respectively. (b) shows the asymmetry of the plot above them, $(N_{B^0} - N_{\bar{B}^0}) / (N_{B^0} + N_{\bar{B}^0})$, where N_{B^0} ($N_{\bar{B}^0}$) is the measured signal yield of B^0 (\bar{B}^0) events in each bin of Δt .

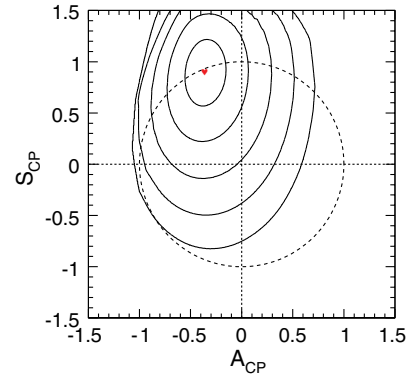


FIG. 5 (color online). Likelihood scan in the $\mathcal{A}_{\omega K_S^0}$ - $\mathcal{S}_{\omega K_S^0}$ plane including systematic uncertainties. The dashed circle represents the physical boundary of CP violation. Starting from the red marker in the center that identifies the fit result, the concentric curves represent the contours from 1 to 5 standard deviations from the fit result.

signal $B^0 \rightarrow \omega K_S^0$, 96.5% for the continuum, and 2.2% for the $B\bar{B}$ background. For the charged mode, we obtain 1.3% signal $B^+ \rightarrow \omega K^+$, 96.8% continuum, and 1.9% $B\bar{B}$. All results are consistent with the previous Belle measurements [8,22] within two standard deviations. The statistical errors obtained in our fit to the data agree with those expected obtained from the pseudoexperiment study mentioned in the previous section.

These results, apart from $\mathcal{S}_{\omega K_S^0}$, are the world's most precise measurements of the branching fractions and CP -violation parameters in $B \rightarrow \omega K$ decays. To estimate the significance of CP violation, we perform a two-dimensional likelihood scan in the $\mathcal{A}_{\omega K_S^0}$ - $\mathcal{S}_{\omega K_S^0}$ plane. This distribution is convolved with a two-dimensional Gaussian with means of zero and widths set to the relevant systematic uncertainty in $\mathcal{A}_{\omega K_S^0}$ and $\mathcal{S}_{\omega K_S^0}$. The resulting distribution is then used to obtain contours in units of significance from which we find the first evidence for CP violation in the $B^0 \rightarrow \omega K_S^0$ decay with 3.1 standard deviations, as shown in Fig. 5.

As a test of the accuracy of the result, we perform a fit on the data set containing the first 535×10^6 $B\bar{B}$ pairs, which corresponds to the integrated luminosity used in the previous analysis. We obtain $\mathcal{A}_{\omega K_S^0} = -0.17 \pm 0.24$ and $\mathcal{S}_{\omega K_S^0} = +0.42 \pm 0.40$, which are in agreement with the previous Belle results shown in Table II, considering the new tracking algorithm, the 37% increase in detection efficiency with respect to that given in Ref. [8], and the improved analysis strategy of including $\mathcal{H}_{3\pi}$, which provides powerful discrimination between signal and background. Using a pseudoexperiment technique based on the fit result, we estimate the probability of a statistical fluctuation in the new data set causing the observed shift in the central value of $\mathcal{S}_{\omega K_S^0}$ from our measurement with the first 535×10^6 $B\bar{B}$ pairs to be 7%.

VI. SYSTEMATIC UNCERTAINTIES

Systematic uncertainties from various sources are considered and estimated with both model-specific and-independent studies and cross-checks. All uncertainties are summarized in Table V. The systematic uncertainty due to the error on the total number of $B\bar{B}$ pairs is calculated from the on- and off-resonance luminosity, taking into account efficiency and luminosity scaling corrections. The uncertainty arising from π^0 reconstruction is evaluated by comparing data-MC differences of the yield ratio between $\eta \rightarrow \pi^0\pi^0\pi^0$ and $\eta \rightarrow \pi^+\pi^-\pi^0$. The uncertainties due to K_S^0 reconstruction and tracking efficiencies are calculated by comparing data-MC differences of the reconstruction efficiency of $D^* \rightarrow D^0[K^-\pi^+]\pi^0$. The uncertainty due to particle identification efficiency is determined using inclusive $D^{*+} \rightarrow D^0[K^-\pi^+]\pi^+$ decays, where the PID of each particle is unambiguously determined by the charge.

TABLE V. Systematic uncertainties of the branching fractions and CP asymmetries. The uncertainties on the CP parameters are absolute, while those on the branching fractions are given as its percentage.

Category	$\delta\mathcal{B}(\omega K^0)$ (%)	$\delta\mathcal{A}_{\omega K_S^0}$ (10^{-2})	$\delta\mathcal{S}_{\omega K_S^0}$ (10^{-2})	$\delta\mathcal{B}(\omega K^+)$ (%)	$\delta\mathcal{A}_{\omega K^+}$ (10^{-2})
$N_{B\bar{B}}$	1.4	N/A	N/A	1.4	N/A
π^0 reconstruction	4.0	N/A	N/A	4.0	N/A
K_S^0 reconstruction	0.8	N/A	N/A	N/A	N/A
PID	1.8	N/A	N/A	2.8	N/A
Tracking	0.7	N/A	N/A	1.1	N/A
IP profile	0.4	0.1	1.2	0.2	N/A
B_{Tag} track selection	0.5	0.2	0.3	0.2	N/A
Track helix error	0.0	0.0	0.0	0.0	N/A
Δt selection	0.6	0.0	0.1	0.1	N/A
Vertex quality selection	0.9	0.3	0.5	0.9	N/A
Δz bias	N/A	0.5	0.4	N/A	N/A
Misalignment	N/A	0.4	0.2	N/A	N/A
Physics parameters	0.0	0.1	0.1	0.0	0.0
Δt resolution function	0.6	2.6	4.4	0.8	0.7
Flavor tagging	0.0	0.3	0.8	0.0	N/A
Misreconstruction	0.9	0.1	0.3	0.7	0.1
$B\bar{B}$ background yields	0.8	0.2	0.5	0.9	0.3
Parametric shape	1.8	0.5	1.5	1.0	0.5
Nonparametric shape	0.1	0.1	0.2	0.1	0.3
Fit bias	0.6	0.7	0.1	0.9	0.3
Detector bias	N/A	N/A	N/A	N/A	0.3
Background CP violation	N/A	1.5	1.4	N/A	0.1
Tag-side interference	N/A	3.2	0.2	N/A	N/A
Total	5.5	4.6	5.2	5.6	1.0

The vertices of B_{Rec} and B_{Tag} are constructed with an IP constraint smeared in the $x - y$ plane by $21 \mu\text{m}$ to account for the finite flight length of the B meson. This systematic error is estimated by varying the amount of smearing by $\pm 10 \mu\text{m}$. The track selection cut values on the tag side are varied by $\pm 10\%$, and the difference in the fit result is taken as a systematic uncertainty. The charged track parametrization errors are corrected by global scaling factors obtained from cosmic rays. The effect of these corrections is studied by looking at the difference in fit results with and without the corrected errors. The requirement of $|\Delta t| < 70 \text{ ps}$ is varied by $\pm 30 \text{ ps}$. The B vertex quality selection criteria, $h < 50$, is varied by ${}_{-25}^{+50}$ and the z vertex error requirements, $\sigma < 200(500) \mu\text{m}$ for multi- (single-)track vertices is varied by $\pm 100 \mu\text{m}$. A Δz bias can be caused by an unknown intrinsic misalignment within the SVD or relative misalignment between the SVD and CDC. This scenario is considered by generating MC with and without misalignment effects and taking the difference as a systematic error.

The fit model systematics in the signal PDF include the fixed physics parameters τ_{B^0} and Δm_d , which are varied within their world-average uncertainties [30]. It also includes the Δt resolution function parameters of $R_{B^0\bar{B}^0}^s(\Delta t)$ and $R_{B^+B^-}^s(\Delta t)$, as well as the flavor-tagging performance parameters w and Δw , which are varied within $\pm 1\sigma$ of their experimental uncertainties determined from a control sample [4,34]. The fixed $B\bar{B}$ background yields are also accounted for, where the nonpeaking background yields are varied within their MC errors, while the peaking background yields are varied taking into account the world-average uncertainties on their branching fractions. The parametric and nonparametric shapes describing the background are varied within their uncertainties. For nonparametric shapes (i.e., histograms), we vary the contents of the histogram bins by $\pm 1\sigma$. We vary the fractions of the Chebyshev and ARGUS components of the ΔE and M_{bc} signal PDFs by their full amounts in order to estimate the uncertainty due to the presence of misreconstructed π^0 and K_S^0 in the signal model. The systematic error due to the uncertainty of the relative yield of the misreconstructed signal component is estimated by varying its fraction by the full value estimated from MC simulation.

We study the uncertainties arising from CP violation in the $B\bar{B}$ background by introducing an artificial CP -violating component, which is set conservatively at 20% of all neutral $B\bar{B}$ events, and vary the CP parameters maximally between $\mathcal{A}_{\omega K_S^0} = \pm 1$ and $\mathcal{S}_{\omega K_S^0} = \pm 1$. Half the fit bias obtained from pseudoexperiment MC studies is taken as an additional systematic uncertainty. A detector bias uncertainty is assigned to $\mathcal{A}_{\omega K^+}$, accounting for effects such as asymmetry in PID and tracking efficiencies, material effect using $D_S^+ \rightarrow \phi[K^+K^-]\pi^+$

and $D^0 \rightarrow K^- \pi^+$ samples [36]. Finally, a large number of MC pseudoexperiments are generated, and an ensemble test is performed to obtain possible systematic biases from interference on the tag side arising between the CKM-favored $b\bar{d} \rightarrow (c\bar{u}d)\bar{d}$ and doubly CKM-suppressed $\bar{b}d \rightarrow (\bar{u}c\bar{d})d$ amplitudes in the final states used for flavor tagging [37].

VII. CONCLUSION

We report an improved measurement of the branching fraction and CP -violation parameters in $B \rightarrow \omega K$ decays. The measurements are based on the full Belle data sample after reprocessing with a new tracking algorithm and with an optimized analysis performed with a simultaneous fit; they supersede those of the previous Belle analyses [8,22]. These are now the world's most precise measurements, apart from $\mathcal{S}_{\omega K_S^0}$, and the obtained values are mostly consistent with previous measurements from Belle and *BaBar* [8,9,22,23], apart from a 3σ tension between the Belle and *BaBar* result for $\mathcal{A}_{\omega K_S^0}$. The results for the branching fractions, $\mathcal{A}_{\omega K_S^0}$ and $\mathcal{A}_{\omega K^+}$, are in agreement with the predictions of the pQCD, QCDF, and SCET theories within one to two standard deviations. The value obtained for $\mathcal{S}_{\omega K_S^0}$ is consistent with the prediction of the SM (see Table I) within one standard deviation, and the first evidence for CP violation in $B^0 \rightarrow \omega K_S^0$ is found at the level of 3.1 standard deviations.

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