

# Measurement of branching fractions for $B \rightarrow J/\psi \eta K$ decays and search for a narrow resonance in the $J/\psi \eta$ final state

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 We report an observation of the  $B^\pm \rightarrow J/\psi\eta K^\pm$  and  $B^0 \rightarrow J/\psi\eta K_S^0$  decays using  $772 \times 10^6 BB$  pairs collected at the  $\Upsilon(4S)$  resonance with the Belle detector at the KEKB asymmetric-energy  $e^+e^-$  collider. We obtain the branching fractions  $\mathcal{B}(B^\pm \rightarrow J/\psi\eta K^\pm) = (1.27 \pm 0.11(\text{stat.}) \pm 0.11(\text{syst.})) \times 10^{-4}$  and  $\mathcal{B}(B^0 \rightarrow J/\psi\eta K_S^0) = (5.22 \pm 0.78(\text{stat.}) \pm 0.49(\text{syst.})) \times 10^{-5}$ . We search for a new narrow charmonium(-like) state  $X$  in the  $J/\psi\eta$  mass spectrum and find no significant excess. We set upper limits on the product of branching fractions,  $\mathcal{B}(B^\pm \rightarrow XK^\pm)\mathcal{B}(X \rightarrow J/\psi\eta)$ , at  $3872 \text{ MeV } c^{-2}$  where a  $C$ -odd partner of  $X(3872)$  may exist, at  $\psi(4040)$  and  $\psi(4160)$  assuming their known mass and width, and over a range from  $3.8$  to  $4.8 \text{ GeV } c^{-2}$ . The obtained upper limits at 90% confidence level for  $X^{C\text{-odd}}(3872)$ ,  $\psi(4040)$ , and  $\psi(4160)$  are  $3.8 \times 10^{-6}$ ,  $15.5 \times 10^{-6}$ , and  $7.4 \times 10^{-6}$ , respectively.  
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Subject Index C07, C21

The discovery of a narrow charmonium-like resonance,  $X(3872)$ , in the  $J/\psi\pi^+\pi^-$  final state by the Belle collaboration in 2003 [1] opened a new era in the spectroscopy of charmonium and charmonium-like exotic states [2]. In addition to  $J/\psi\pi^+\pi^-$ ,  $X(3872)$  decays are also seen in the  $D^0\bar{D}^{*0}$  [3,4],  $J/\psi\pi^+\pi^-\pi^0$  [5], and  $J/\psi\gamma$  [6,7] final states. Observation of the  $X(3872) \rightarrow J/\psi\gamma$  mode confirms that its  $C$ -parity is even. The studies of angular distributions of the decay products in the  $X(3872) \rightarrow J/\psi\pi^+\pi^-$  mode by CDF [8] and Belle [9] as well as the  $3\pi$  invariant mass spectrum in  $J/\psi\pi^+\pi^-\pi^0$  mode by BaBar [5] restrict  $J^{PC}$  to be either  $1^{++}$  and  $2^{-+}$  but do not allow a definitive determination. A full five-dimensional amplitude analysis of the angles among the decay products in  $B^+ \rightarrow X(3872)K^+$ ,  $X(3872) \rightarrow J/\psi\pi^+\pi^-$  recently performed by the LHCb collaboration has unambiguously assigned  $J^{PC} = 1^{++}$  to the  $X(3872)$  [10].

The very small width ( $\Gamma < 1.2 \text{ MeV}$ ) [9] of the  $X(3872)$  and its mass ( $M = 3871.7 \pm 0.2 \text{ MeV } c^{-2}$ ) close to the  $D^0\bar{D}^{*0}$  threshold [11] make its interpretation as a  $D^0\bar{D}^{*0}$  molecule [12,13] quite plausible. However, other models such as tetraquark [14], hybrid ( $c\bar{c}g$ ) [15], and the admixture of molecular and charmonium states [16] are not excluded. In both the molecule and tetraquark pictures [17,18], a  $C$ -odd partner ( $X^{C\text{-odd}}$ ) or a charged partner ( $X^\pm$ ) of  $X(3872)$  can exist. So far, searches for the charged partner  $X^\pm \rightarrow J/\psi\pi^\pm\pi^0$  have given negative results [9,19]. This might be only because the  $X^\pm$  is too broad, given the current statistics; it leaves open the possibility of a moderately narrow  $C$ -odd partner, as postulated by the tetraquark model [17]. Recently, the Belle collaboration has searched for the  $X^{C\text{-odd}} \rightarrow \chi_{c1}\gamma$  transition in  $B \rightarrow \chi_{c1}\gamma K$  decays and reported evidence for a narrow resonance at  $3823 \text{ MeV } c^{-2}$  [20]. This resonance is presumably the  $1^3D_2c\bar{c}(\psi_2)$  rather than the  $X^{C\text{-odd}}$ , since its mass, decay width, and the discovery decay mode are consistent with theoretical prediction for this charmonium state [21–23].

Alternatively, the  $X^{C\text{-odd}}$  might appear in the  $J/\psi\eta$  final state. The photon energy in  $\eta \rightarrow \gamma\gamma$  is well above the energy threshold to be detected in  $B$ -factory experiments even in the case where the

resonance is just above the  $J/\psi\eta$  mass threshold. Therefore, the  $J/\psi\eta$  system in the three-body  $B \rightarrow J/\psi\eta K$  decay is a suitable final state to search for a missing  $C$ -odd partner of the  $X(3872)$  as well as any yet-unseen charmonium(-like) resonances. The  $J/\psi\eta$  final state is also sensitive to the  $\psi(4040)$  and  $\psi(4160)$  resonances, whose decays into  $J/\psi\eta$  were recently reported by BESIII in  $e^+e^-$  annihilation [24] and Belle in the initial state radiation process [25]. Since the total width and partial width to  $e^+e^-$  are known for these charmonia [11], this observation implies  $\psi(4040)$  and  $\psi(4160)$  have branching fractions of a few percent to  $J/\psi\eta$ . If the branching fractions for  $B^\pm \rightarrow \psi(4040)K^\pm$  or  $\psi(4160)K^\pm$  are as high as  $\sim 10^{-3}$ , these decay channels are accessible with Belle's data set.

The branching fraction for  $B \rightarrow J/\psi\eta K$  decay may also shed light on the inclusive spectrum of  $B \rightarrow J/\psi X$ , which is fairly well described by non-relativistic QCD calculations [26] except for an excess in the low momentum region [27–29]. There have been several models proposed to explain this excess, such as  $B \rightarrow J/\psi K_g$  (where  $K_g$  is a hybrid meson with  $\bar{s}qg$  constituents) [30], or a still-undiscovered charmonium(-like) state that decays into  $J/\psi$  [31]. Such exotic or new states can be constrained by measurements of multibody  $B$  decay modes into  $J/\psi$ , such as  $B \rightarrow J/\psi\eta K$ , because they populate the region of the above-mentioned excess.

A previous study by the BaBar collaboration [32] reported an observation of  $B^\pm \rightarrow J/\psi\eta K^\pm$  and evidence for  $B^0 \rightarrow J/\psi\eta K_S^{01}$  using  $90 \times 10^6 B\bar{B}$  pairs ( $N_{B\bar{B}}$ ), but no signal of a narrow resonance was found in the  $J/\psi\eta$  spectrum. In this paper, we present a study of  $B \rightarrow J/\psi\eta K$  decays based on a data sample of  $772 \times 10^6 B\bar{B}$  events collected with the Belle detector at the KEKB asymmetric-energy  $e^+e^-$  collider [33,34] at the  $\Upsilon(4S)$  resonance.

The Belle detector is a large solid-angle magnetic spectrometer that consists of a silicon vertex detector (SVD), a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter (ECL) comprised of CsI(Tl) crystals located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. An iron flux return located outside of the coil is instrumented to detect  $K_L^0$  mesons and to identify muons (KLM). The detector is described in detail in Ref. [35]; see also the detector section in Ref. [36]. Two inner detector configurations were used. A 2.0 cm radius beampipe and a three-layer silicon vertex detector were used to collect the first sample of  $152 \times 10^6 B\bar{B}$  pairs, while a 1.5 cm radius beampipe, a four-layer silicon detector, and a small-cell inner drift chamber were used to record the remaining  $620 \times 10^6 B\bar{B}$  pairs [37].

Charged tracks coming from  $B$  decays should originate from the interaction point (IP). The closest approach with respect to the IP is required to be within 5.0 cm along the beam direction ( $z$ -axis) and within 2.0 cm in the transverse plane. Photons are reconstructed as ECL clusters without an associated charged track that have transverse shower shape variables consistent with an electromagnetic cascade hypothesis. For  $\eta$  reconstruction, the daughter photon has an energy greater than 100 MeV in the laboratory frame.

The  $J/\psi$  meson is reconstructed in its decay to  $\ell^+\ell^-$  ( $\ell = e$  or  $\mu$ ). From the selected charged tracks,  $e^\pm$  candidates are identified by combining specific-ionization ( $dE/dx$ ) information from the CDC,  $E/p$  (where  $E$  is the shower energy detected in the ECL and  $p$  is the momentum measured by the SVD and the CDC), and shower shape in the ECL. In addition, the ACC information and the position difference between the electron track candidate and the matching ECL cluster are used in the

<sup>1</sup> Inclusion of charge-conjugate modes is implied.

identification of electron candidates. In the  $J/\psi \rightarrow e^+e^-$  mode, in order to recover bremsstrahlung photons and final state radiation, the four-momenta of all photons within 50 mrad of each of the leptons are included in the invariant mass that is hereinafter denoted as  $M_{e^+e^-(\gamma)}$ . Identification of  $\mu$  candidates is based on the track penetration depth and hit pattern in the KLM system [38]. The reconstructed invariant mass of a  $J/\psi$  candidate must satisfy  $2.95 \text{ GeV } c^{-2} < M_{e^+e^-(\gamma)} < 3.13 \text{ GeV } c^{-2}$  or  $3.04 \text{ GeV } c^{-2} < M_{\mu^+\mu^-} < 3.13 \text{ GeV } c^{-2}$ . In order to improve the momentum resolution, a vertex-constrained fit followed by a mass-constrained fit is applied for the  $J/\psi$  candidates and convergence of both fits is required.

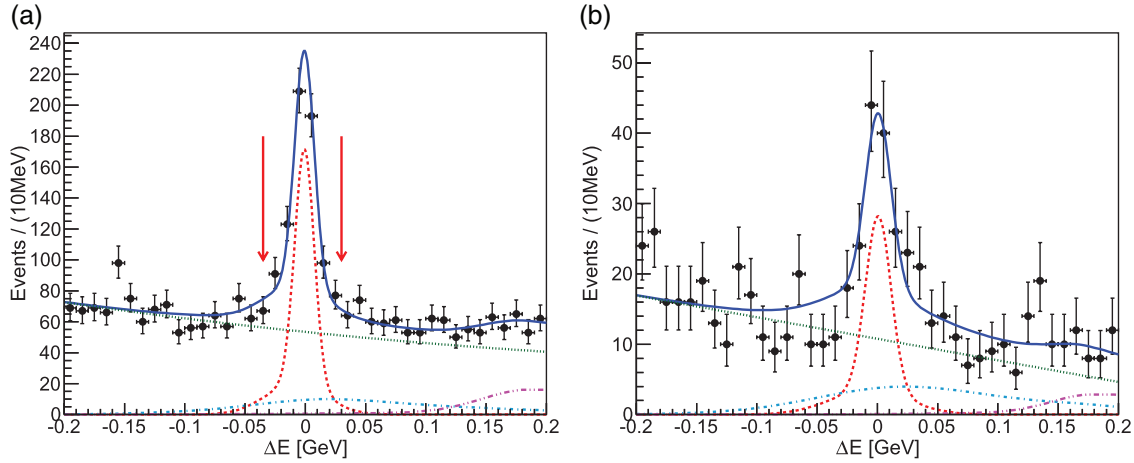
Pairs of photons are combined to form  $\eta$  candidates within the mass range  $510 \text{ MeV } c^{-2} < M_{\gamma\gamma} < 575 \text{ MeV } c^{-2}$ . To further reduce combinatorial background, the  $\eta \rightarrow \gamma\gamma$  candidates are required to have an energy balance parameter ( $|E_1 - E_2|/(E_1 + E_2)$ ) smaller than 0.8, where  $E_1$  ( $E_2$ ) is the energy of the first (second) photon in the laboratory frame. To suppress the background photons from  $\pi^0$  decays, we reject any photon forming a  $\pi^0$  candidate ( $117 \text{ MeV } c^{-2} < M_{\gamma\gamma} < 153 \text{ MeV } c^{-2}$ ) with any other photon in the event. For the selected  $\eta$  candidates, a mass-constrained fit is performed to improve the momentum resolution.

Charged kaons are identified by combining information from the CDC, TOF, and ACC systems. The kaon identification efficiency is about 90% while the probability of misidentifying a pion as a kaon is about 10% for the corresponding momentum range.  $K_S^0$  mesons are reconstructed by combining two oppositely charged tracks (both assumed to be pions) and requiring the invariant mass  $M_{\pi^+\pi^-}$  to be between 482 and 514  $\text{MeV } c^{-2}$ . The selected candidates are required to have a vertex displaced from the IP as described in Ref. [39].

A  $B \rightarrow J/\psi \eta K$  candidate is formed from the  $J/\psi$ ,  $\eta$  and kaon candidates and is identified by two kinematic variables defined in the  $\Upsilon(4S)$  rest frame (cms): the energy difference ( $\Delta E \equiv E_B^* - E_{\text{beam}}^*$ ) and the beam-energy constrained mass ( $M_{\text{bc}} \equiv \sqrt{(E_{\text{beam}}^*)^2 - (P_B^*)^2}$ ). Here,  $E_{\text{beam}}^*$  is the cms beam energy and  $E_B^*$  and  $P_B^*$  are the cms energy and momentum, respectively, of the reconstructed  $B$  candidate. Events having at least one  $B$  candidate satisfying  $M_{\text{bc}} > 5.27 \text{ GeV } c^{-2}$  and  $|\Delta E| < 0.2 \text{ GeV}$  are retained for further analysis.

Among the retained events, 29% have more than one  $B$  candidate. This is predominantly due to the wrong combination in forming the  $\eta$  candidate or, far less frequently, due to an incorrect  $J/\psi \rightarrow \ell^+\ell^-$  reconstruction; cases with an incorrect kaon candidate are negligible. Therefore, we select the  $B$  candidate having the smallest goodness of fit, defined as  $\chi^2 \equiv (M_{\ell^+\ell^-} - m_{J/\psi})^2/\sigma_{\ell^+\ell^-}^2 + (M_{\gamma\gamma} - m_\eta)^2/\sigma_{\gamma\gamma}^2$ , where  $M_{\ell^+\ell^-}$  denotes  $M_{e^+e^-(\gamma)}$  or  $M_{\mu^+\mu^-}$ ,  $\sigma_{\ell^+\ell^-}$  denotes the  $M_{\ell^+\ell^-}$  resolutions (11.1  $\text{MeV } c^{-2}$  for  $M_{e^+e^-(\gamma)}$  and 8.9  $\text{MeV } c^{-2}$  for  $M_{\mu^+\mu^-}$ ),  $M_{\gamma\gamma}$  is the photon pair mass, and  $\sigma_{\gamma\gamma}$  is the  $M_{\gamma\gamma}$  resolution (13.8  $\text{MeV } c^{-2}$ ). Here,  $m_{J/\psi}$  and  $m_\eta$  are the nominal meson masses [11].

To suppress continuum background, we reject events having a ratio  $R_2$  of the second to zeroth Fox–Wolfram moments [40] greater than 0.5. Among the backgrounds from  $B\bar{B}$  events, those that contain a real  $J/\psi \rightarrow \ell^+\ell^-$  decay dominate. A large sample of  $B \rightarrow J/\psi X$  Monte Carlo (MC) decays, corresponding to 100 times the data sample, is used to model this background component's  $M_{\text{bc}}$  and  $\Delta E$  distributions. When  $\psi'$  decays to the final states other than  $J/\psi \eta$ , the  $B \rightarrow \psi' K$  decay mode forms a significant portion of the background. We denote this contribution as the  $B \rightarrow \psi' (\not{=} J/\psi \eta) K$  process. In order to reduce this background, we reject a  $J/\psi$  that, when combined with a  $\pi^+\pi^-$  pair, forms a  $\psi'$  candidate with a mass difference in the range  $0.58 \text{ GeV } c^{-2} < M_{J/\psi\pi^+\pi^-} - m_{J/\psi} < 0.60 \text{ GeV } c^{-2}$ . The non- $J/\psi$  background is estimated using the  $M_{\ell^+\ell^-}$  sideband events in the data and is found to be negligible.

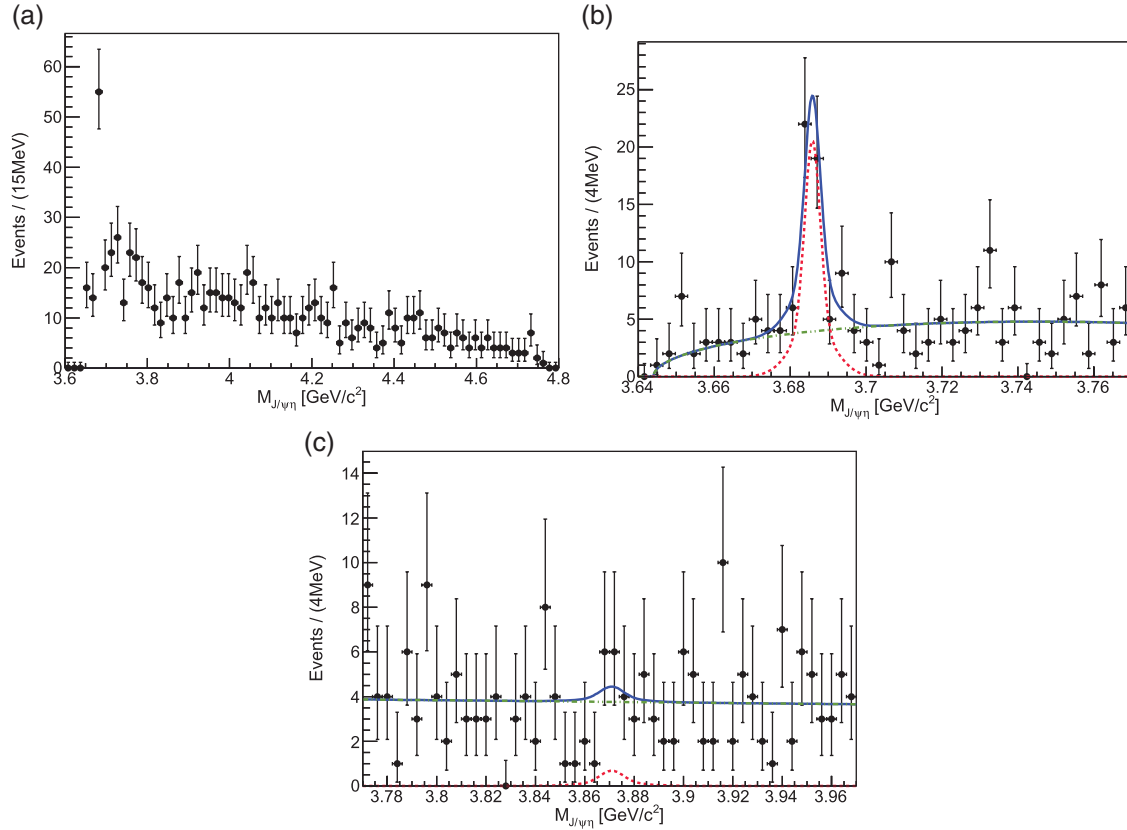


**Fig. 1.** (color online).  $\Delta E$  distribution of (a)  $B^\pm \rightarrow J/\psi\eta K^\pm$  and (b)  $B^0 \rightarrow J/\psi\eta K_S^0$  candidates in  $M_{bc} > 5.27 \text{ GeV } c^{-2}$ . The signal-enhanced region for  $B^\pm \rightarrow J/\psi\eta K^\pm$  is shown by the red arrows in (a). Data are shown by points with error bars. The red dashed line is signal, the cyan dot-dashed line is  $B \rightarrow \psi'(\not\rightarrow J/\psi\eta)K$  background, the magenta dot-dot-dashed line is  $B \rightarrow \chi_{c1}K$  background, and the green dotted line is other backgrounds.

The  $B$  decay signal extraction is carried out by performing an extended unbinned maximum likelihood (UML) fit to the  $\Delta E$  distribution. Figure 1 shows the  $\Delta E$  distribution for the charged and neutral  $B$  decay candidates together with the fit results. Clear signal peaks are seen on the smoothly distributing background for both cases. For these decays, a sum of two Gaussians is used to model the probability density function (PDF) for signal events. For the  $B^\pm \rightarrow J/\psi\eta K^\pm$  decay mode, the mean and width of the core Gaussian are floated and the remaining parameters are fixed to values obtained by fitting the signal MC distribution. Since we have smaller statistics for  $B^0 \rightarrow J/\psi\eta K_S^0$ , the parameters of the signal PDF are fixed to the values of data obtained by the  $B^\pm \rightarrow J/\psi\eta K^\pm$  sample. Since the  $B \rightarrow \psi'(\not\rightarrow J/\psi\eta)K$  and  $B \rightarrow \chi_{c1}K$  decay modes are expected to have different features compared to other backgrounds in the  $\Delta E$  distribution, these two processes are treated separately. We use a bifurcated Gaussian to describe these decay modes whose parameters are fixed from large MC simulation samples. Since the branching fractions for these decay modes are known [11], their yields are also fixed. To model the remaining featureless combinatorial background in the  $\Delta E$  projection, we use a second-order (first-order) Chebyshev polynomial for the  $B^\pm \rightarrow J/\psi\eta K^\pm$  ( $B^0 \rightarrow J/\psi\eta K_S^0$ ) decay mode. We obtain signal yields of  $428 \pm 37$  events and  $94 \pm 14$  events for the  $B^\pm \rightarrow J/\psi\eta K^\pm$  and  $B^0 \rightarrow J/\psi\eta K_S^0$  decay modes, respectively. The detection efficiency estimation for  $B^\pm \rightarrow J/\psi\eta K^\pm$  is described in more detail later. The three-body phase space distribution is assumed for  $B^0 \rightarrow J/\psi\eta K_S^0$ . Their branching fractions are  $(1.27 \pm 0.11 \pm 0.11) \times 10^{-4}$  and  $(5.22 \pm 0.78 \pm 0.49) \times 10^{-5}$ , where the first uncertainty is statistical and the second is systematic uncertainty; these uncertainties are described later in detail. We calculate the statistical significance,  $\sqrt{-2 \ln \mathcal{L}_0 / \mathcal{L}_{\max}}$ , where  $\mathcal{L}_{\max}$  ( $\mathcal{L}_0$ ) denote the likelihood value when the signal yield is allowed to vary (is set to zero). The significance is found to be  $17\sigma$  ( $7\sigma$ ) for the  $B^\pm \rightarrow J/\psi\eta K^\pm$  ( $B^0 \rightarrow J/\psi\eta K_S^0$ ) decay mode. We observe the  $B^0 \rightarrow J/\psi\eta K_S^0$  decay mode for the first time with the significance more than  $5\sigma$ . Equal production of neutral and charged  $B$  meson pairs in the  $\Upsilon(4S)$  decay is assumed. We used the secondary branching fractions reported in Ref. [11]. The results of the fits are presented in Table 1.

**Table 1.** Summary of the detection efficiency ( $\epsilon$ ), signal yield ( $N_{\text{sig}}$ ), and branching fraction ( $\mathcal{B}$ ) in  $-0.2 \text{ GeV } c^{-2} < \Delta E < 0.2 \text{ GeV } c^{-2}$ , where the first and second errors are statistical and systematic.

Decay mode	$\epsilon(\%)$	$N_{\text{sig}}$	$\mathcal{B}$
$B^\pm \rightarrow J/\psi\eta K^\pm$	9.37	$428 \pm 37$	$(1.27 \pm 0.11 \pm 0.11) \times 10^{-4}$
$B^0 \rightarrow J/\psi\eta K_S^0$	7.23	$94 \pm 14$	$(5.22 \pm 0.78 \pm 0.49) \times 10^{-5}$



**Fig. 2.** (color online). The  $J/\psi\eta$  invariant mass ( $M_{J/\psi\eta}$ ) distribution of  $B^\pm \rightarrow J/\psi\eta K^\pm$  candidates for: (a) the entire mass distribution, (b) the region around the  $\psi'$ , and (c) the  $X(3872)$  region. Data is shown by points with error bars; overall fit is shown by blue solid line. For (b) and (c), the red dashed line is for signal ( $\psi'$  and  $X(3872)$  in (b) and (c), respectively) and the green two dotted-dashed line is for the remainder.

Since the  $B^\pm \rightarrow J/\psi\eta K^\pm$  signal is strong, we use the  $J/\psi\eta$  mass spectrum ( $M_{J/\psi\eta}$ ) to resolve the intermediate states in this three-body final state. For this purpose, we select events having  $-35 \text{ MeV} < \Delta E < 30 \text{ MeV}$ . This requirement corresponds to  $\pm 3.5\sigma$  ( $\pm 1.3\sigma$ ) of the narrower (wider) Gaussian. The  $B$  decay signal yield in this signal-enhanced region is  $403 \pm 35$  events.

The  $M_{J/\psi\eta}$  distribution for this subsample is shown in Fig. 2(a). We find a clear peak corresponding to the  $\psi' \rightarrow J/\psi\eta$  decay at  $3686 \text{ MeV } c^{-2}$  with a yield of  $46 \pm 8$  events by performing a UML fit to the  $M_{J/\psi\eta}$  distribution in the range from the kinematical threshold to  $3770 \text{ MeV } c^{-2}$ . We parametrize the  $\psi'$  signal and remaining contributions by the sum of two Gaussians and a threshold function, respectively, as shown in Fig. 2(b). The  $\psi'$  shape is fixed to that found by a fit to the MC distribution, which is calibrated by the difference in resolution between data and simulation. The  $M_{J/\psi\eta}$  calibration factor is taken from the  $\Delta E$  distribution, since both resolutions are dominated by that of the  $\eta$  (reconstructed from photons rather than charged tracks). The threshold function is taken

**Table 2.** Summary of the detection efficiency ( $\epsilon$ ), signal yield ( $N_{\text{sig}}$ ), and branching fraction ( $\mathcal{B}$ ), where the first and second errors are statistical and systematic, respectively. For  $B^\pm \rightarrow \psi' K^\pm$ , followed by  $\psi' \rightarrow J/\psi \eta$ ,  $\mathcal{B}$  denotes the products of the branching fractions,  $\mathcal{B}(B^\pm \rightarrow \psi' K^\pm)\mathcal{B}(\psi' \rightarrow J/\psi \eta)$ . For the  $B^\pm$  decays, all relevant numbers are defined in the signal enhanced region,  $-35 \text{ MeV} < \Delta E < 30 \text{ MeV}$ .

Decay mode	$\epsilon(\%)$	$N_{\text{sig}}$	$\mathcal{B}$
$B^\pm \rightarrow J/\psi \eta K^\pm$ (Total)	8.82	$403 \pm 35$	$(1.27 \pm 0.11 \pm 0.11) \times 10^{-4}$
$B^\pm \rightarrow \psi' K^\pm, \psi' \rightarrow J/\psi \eta$	8.42	$46 \pm 8$	$(0.15 \pm 0.03 \pm 0.01) \times 10^{-4}$
$B^\pm \rightarrow J/\psi \eta K^\pm$ (excl. $\psi' K^\pm$ )	8.88	$357 \pm 38$	$(1.12 \pm 0.11 \pm 0.10) \times 10^{-4}$

as  $a(M_{J/\psi \eta} - m_0)^{1/2} + b(M_{J/\psi \eta} - m_0)^{3/2} + c(M_{J/\psi \eta} - m_0)^{5/2}$ , where  $m_0 = 3.644 \text{ GeV } c^{-2}$  and the shape determined by  $a$ ,  $b$ , and  $c$  is fixed to MC simulation; its normalization is floated in the fit. We obtain  $\mathcal{B}(B^\pm \rightarrow \psi' K^\pm)\mathcal{B}(\psi' \rightarrow J/\psi \eta) = (0.15 \pm 0.03(\text{stat.}) \pm 0.01(\text{syst.})) \times 10^{-4}$ , which is in agreement with the PDF value [11]. The rest of the  $B$  decay signal does not show any peaking structure and is consistent with three-body phase space.

The efficiency that is used to obtain the total branching fraction is determined by weighting the  $B^\pm \rightarrow \psi' K^\pm$  and the three-body phase components according to the observed  $M_{J/\psi \eta}$  spectrum. After subtracting the yield of  $46 \pm 8$  events for  $B^\pm \rightarrow \psi' K^\pm$  followed by  $\psi' \rightarrow J/\psi \eta$  (as described earlier), the remaining  $B$  decay signal yield is  $357 \pm 38$  events and is used to extract the branching fraction in Table 2.

The major source of systematic uncertainty in the branching fraction measurements is from the PDF uncertainty. It is estimated by varying all fixed parameters by  $\pm 1\sigma$  and summing all the variations in quadrature; it amounts to 7.3% for  $B^\pm \rightarrow J/\psi \eta K^\pm$  and 8.4% for  $B^0 \rightarrow J/\psi \eta K_S^0$ . The uncertainty of the tracking efficiency is estimated to be 0.35% per track. Small differences in the lepton and kaon identification efficiency between the data and MC simulation are included in the detection efficiency estimation and the relevant uncertainty is assigned as a systematic error. The uncertainty of electron identification is studied using the  $J/\psi \rightarrow e^+e^-$  sample and estimated to be 0.9% per  $e^+e^-$  pair. A similar approach for muon identification results in a systematic error of 3.9% per  $\mu^+\mu^-$  pair. A kaon identification uncertainty is determined to be 1.4% from the study using the  $D^{*+} \rightarrow D^0(\rightarrow K^-\pi^+)\pi^+$  sample. The uncertainty on the  $\eta \rightarrow \gamma\gamma$  efficiency is estimated to be 3.0% [41]. The  $K_S^0$  efficiency contributes a 0.7% error in the  $B^0 \rightarrow J/\psi \eta K_S^0$  mode. The uncertainties due to signal MC simulation statistics (0.5%) and the secondary branching fractions (0.7%) have only a small effect. The uncertainty of  $N_{B\bar{B}}$  is 1.4%. Table 3 summarizes the systematic uncertainties. The overall systematic error is obtained by adding all the contributions in quadrature; it is 8.6% for  $B^\pm \rightarrow J/\psi \eta K^\pm$  and 9.4% for  $B^0 \rightarrow J/\psi \eta K_S^0$ .

In order to probe the contribution of the  $X^{C\text{-odd}}$  partner, assuming that it has same mass and width as the  $X(3872)$ , a sum of two Gaussians for signal and a first-order polynomial for background is used. For signal, all the parameters are fixed after applying the same MC-data shape-parameter calibrations used in the  $\psi'$  case. The  $X(3872)$  region is shown in Fig. 2(c). The fit result for the  $X^{C\text{-odd}}$  yield is found to be  $2.3 \pm 5.2$  events and we determine a 90% confidence level (C.L.) upper limit (U.L.) on the product of the branching fractions,  $\mathcal{B}(B^\pm \rightarrow X^{C\text{-odd}} K^\pm)\mathcal{B}(X^{C\text{-odd}} \rightarrow J/\psi \eta) < 3.8 \times 10^{-6}$ , using a frequentist approach. For a given signal yield, a large number of MC simulation sets, including signal and background components, are generated according to their PDFs, and a fit is performed to each set. The C.L. is determined from the fraction of sets that give a yield larger than the one observed in data. The input signal yield is varied until we obtain 90% C.L.; this input yield is the U.L. for the observed signal yield. To take into account the systematic uncertainty, the input signal yield for the



**Table 3.** Contributions to the systematic uncertainty of the branching fraction. The value of PDF shape in parenthesis is for the  $B^\pm \rightarrow \psi' K^\pm$  decay followed by  $\psi' \rightarrow J/\psi\eta$ .

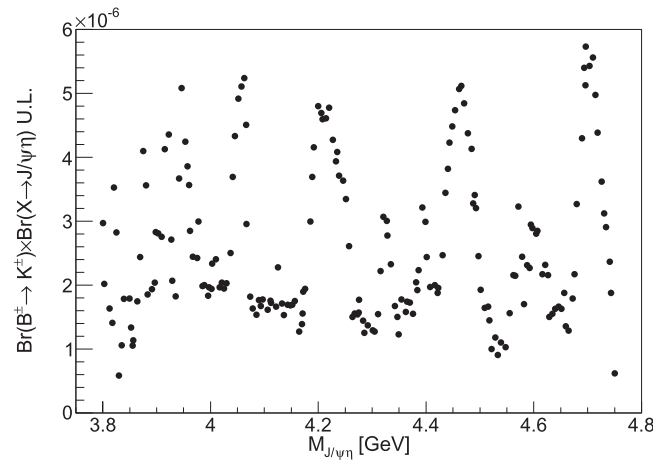
Source	Contribution (%)	
	$B^\pm \rightarrow J/\psi\eta K^\pm$	$B^0 \rightarrow J/\psi\eta K_S^0$
PDF shape ( $B^\pm \rightarrow \psi' K^\pm, \psi' \rightarrow J/\psi\eta$ )	7.3 (5.8)	8.4
Tracking efficiency	1.05	0.7
Lepton identification	2.4	2.4
Charged kaon identification	1.4	—
$\eta \rightarrow \gamma\gamma$ efficiency	3.0	3.0
$K_S^0 \rightarrow \pi^+\pi^-$ efficiency	—	0.7
Signal MC simulation stat.	0.5	0.5
Secondary $\mathcal{B}$	0.7	0.7
$N_{B\bar{B}}$	1.4	1.4
Total (inc. $\psi' K^\pm$ )	8.6 (7.4)	9.4

**Table 4.** The U.L. for the product of the branching fractions  $\mathcal{B}(B^\pm \rightarrow X(\rightarrow J/\psi\eta)K^\pm) \equiv \mathcal{B}(B^\pm \rightarrow XK^\pm)\mathcal{B}(X \rightarrow J/\psi\eta)$  at 3872 and the  $\psi$  states recently found to decay into  $J/\psi\eta$ . Note that  $\epsilon$  is the corrected detection efficiency and the signal yield  $N_{\text{sig}}$  is given as an U.L. at 90% confidence level.

$M_X$ or $\psi$	$\epsilon(\%)$	$N_{\text{sig}}$	$\mathcal{B}(B^\pm \rightarrow X(\rightarrow J/\psi\eta)K^\pm)$
3872	8.1	<10.6	< $3.8 \times 10^{-6}$
$\psi(4040)$	9.2	<51.4	< $1.55 \times 10^{-5}$
$\psi(4160)$	9.2	<24.3	< $0.74 \times 10^{-5}$

simulated sets follows a Gaussian distribution whose width corresponds to the systematic uncertainty. This ensures that the yield fluctuations within the simulated sets exceed those due solely to Poisson statistics. We divide the 3.8 to 4.8 GeV  $c^{-2}$  region into five 200 MeV  $c^{-2}$ -wide intervals and use the PDF and efficiency estimated at 4070, 4270, 4470, and 4670 MeV  $c^{-2}$ . For the  $\psi(4040)$  and  $\psi(4160)$  cases, we describe the resonance by a Breit–Wigner function with the mass and width fixed to the values reported in Ref. [11]. Table 4 summarizes the U.L. for the  $X^{C\text{-odd}}$  and  $\psi(4040, 4160)$ . As shown in Fig. 3, we also provide the U.L. at 90% C.L. of narrow resonances over a range from 3.8 to 4.8 GeV  $c^{-2}$ , with 5 MeV  $c^{-2}$  steps, using the same procedure as for the  $X^{C\text{-odd}}$  U.L. estimation.

In summary, we observe the  $B^\pm \rightarrow J/\psi\eta K^\pm$  and  $B^0 \rightarrow J/\psi\eta K_S^0$  decay modes and present the most precise measurements to date of the branching fractions,  $\mathcal{B}(B^\pm \rightarrow J/\psi\eta K^\pm) = (1.27 \pm 0.11(\text{stat.}) \pm 0.11(\text{syst.})) \times 10^{-4}$  and  $\mathcal{B}(B^0 \rightarrow J/\psi\eta K_S^0) = (5.22 \pm 0.78(\text{stat.}) \pm 0.49(\text{syst.})) \times 10^{-5}$ . For the  $B^\pm \rightarrow J/\psi\eta K^\pm$  signal, the  $M_{J/\psi\eta}$  distribution is used to resolve each possible contribution to search for a resonance in the  $J/\psi\eta$  final state. Except for the known  $\psi' \rightarrow J/\psi\eta$  decay, the  $M_{J/\psi\eta}$  spectrum is found to be featureless and follows a non-resonant distribution. Because no signal is seen, we obtain an U.L. on the product of the branching fractions,  $\mathcal{B}(B^\pm \rightarrow X^{C\text{-odd}} K^\pm)\mathcal{B}(X^{C\text{-odd}} \rightarrow J/\psi\eta) < 3.8 \times 10^{-6}$  at 90% C.L.; this is less than one half of the corresponding value in  $X(3872) \rightarrow J/\psi\pi^+\pi^-$  [11]  $\psi(4040)$  and  $\psi(4160)$  decays into  $J/\psi\eta$  are observed in the initial state radiation process [25], production of those charmonia and their decays to the  $J/\psi\eta$  final state in  $B$  decays are found to be insignificant. The obtained U.L.s exclude a large branching fraction,  $\mathcal{O}(10^{-3})$ , for  $B^\pm \rightarrow \psi(4040)K^\pm$  and  $B^\pm \rightarrow \psi(4160)K^\pm$ . Nevertheless, values comparable to  $B^\pm \rightarrow \psi' K^\pm$  or  $B^\pm \rightarrow \psi(3770)K^\pm$ ,  $\mathcal{O}(10^{-4})$ , are still possible. Our results show



**Fig. 3.** 90% C.L. upper limit of the  $\mathcal{B}(B^\pm \rightarrow XK^\pm)\mathcal{B}(X \rightarrow J/\psi\eta)$  for a narrow resonance  $X$  as a function of the mass, with a  $5 \text{ MeV } c^{-2}$  interval.

that either the production of the  $C$ -odd partner of the  $X(3872)$  resonance in two-body  $B$  decay and/or its decay into  $J/\psi\eta$  is suppressed.

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