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## Search for $B^{0} \rightarrow \boldsymbol{p} \bar{\Lambda} \boldsymbol{\pi}^{-} \gamma$ at Belle

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#### Abstract

We search for the charmless $B^{0}$ decay with final state particles $p \bar{\Lambda} \pi^{-} \gamma$ using the full data sample that contains $772 \times 10^{6} B \bar{B}$ pairs collected at the $\Upsilon(4 S)$ resonance with the Belle detector at the KEKB asymmetric-energy $e^{+} e^{-}$collider. This decay is predicted to proceed predominantly via the $b \rightarrow s \gamma$ radiative penguin process with a high energy photon. No significant signal is found. We set an upper limit of $6.5 \times 10^{-7}$ for the branching fraction of $B^{0} \rightarrow p \bar{\Lambda} \pi^{-} \gamma$ at the $90 \%$ confidence level.


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In the Standard Model (SM), the heavy $b$ quark can decay to an energetic $s$ quark and a hard photon via the penguin loop diagram. The inclusive measurement of the branching fraction from $B$ meson decays for the above process, $\mathcal{B}\left(B \rightarrow X_{s} \gamma\right){ }^{1}$, is very sensitive to physics beyond the SM since new heavy particles can contribute in the loop at the leading order. The up-to-date next-to-next-to-leading order SM calculation gives $\mathcal{B}\left(B \rightarrow X_{s} \gamma\right)=$ $(3.15 \pm 0.23) \times 10^{-4}$ for $E_{\gamma}>1.6 \mathrm{GeV}$ [1], which is consistent with the current world average of the experimental results, $\mathcal{B}\left(B \rightarrow X_{s} \gamma\right)=(3.40 \pm 0.21) \times 10^{-4}[2-5]$.

In the Monte Carlo (MC) simulation of the $s \rightarrow X_{s}$ fragmentation and hadronization processes by JETSET [6], the $X_{s}$ with a $\Lambda$ in the final state contributes only at the $1 \%$

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level. This is consistent with the known baryonic $B$ decay rate, $\mathcal{B}\left(B^{+} \rightarrow p \bar{\Lambda} \gamma\right)=\left(2.45_{-0.38}^{+0.44} \pm 0.22\right) \times 10^{-6} \quad[5,7]$. There is an intriguing feature of this three-body decay: the mass of the $p \bar{\Lambda}$ system is peaked near threshold. A similar feature is seen in many other hadronic three-body $B$ decay processes. In multibody hadronic baryonic $B$ decays, hierarchy in the branching fractions is also observed; e.g., $\mathcal{B}\left(B^{+} \rightarrow p \bar{\Lambda} \pi^{+} \pi^{-}\right)>\mathcal{B}\left(B^{0} \rightarrow p \bar{\Lambda} \pi_{-}^{-}\right)>\mathcal{B}\left(B^{+} \rightarrow p \bar{\Lambda}\right)$ and $\mathcal{B}\left(B^{0} \rightarrow p \bar{\Lambda}_{c}^{-} \pi^{+} \pi^{-}\right)>\mathcal{B}\left(B^{+} \rightarrow p \bar{\Lambda}_{c}^{-} \pi^{+}\right)>\mathcal{B}\left(B^{0} \rightarrow p \bar{\Lambda}_{c}^{-}\right)$ [5,7-15].
These features motivate our interest in the search for $B^{0} \rightarrow p \bar{\Lambda} \pi^{-} \gamma$. Figure 1 shows the lowest order SM decay diagram for $B^{0} \rightarrow p \bar{\Lambda} \pi_{-}^{-} \gamma$. It proceeds via the radiative penguin process. The $p \bar{\Lambda}$ system in this decay will have a smaller maximum kinetic energy than in $B^{+} \rightarrow p \bar{\Lambda} \gamma$ due to the extra pion in the $X_{s}$ fragmentation process. This matches the threshold enhancement effect naturally and


FIG. 1. Decay diagram of $B^{0} \rightarrow p \bar{\Lambda} \pi^{-} \gamma$
implies a higher decay rate [16]. The measured branching fraction of $B^{0} \rightarrow p \bar{\Lambda} \pi^{-} \gamma$ can be useful to tune the parameters in JETSET, and, in the case of a large enhancement of the branching fraction, the uncertainty on the measurement of $\mathcal{B}\left(B \rightarrow X_{s} \gamma\right)$ would be reduced using a sum of exclusive final states.

We use the full data sample ( $711 \mathrm{fb}^{-1}$ ) that contains $772 \times 10^{6} B \bar{B}$ pairs collected at the $\Upsilon(4 S)$ resonance with the Belle detector [17] at the KEKB asymmetric-energy $e^{+} e^{-}$collider [18] for this search. The Belle detector is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector (SVD), a 50 -layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF) and an electromagnetic calorimeter comprised of $\mathrm{CsI}(\mathrm{Tl})$ crystals located inside a superconducting solenoid that provides a 1.5 T magnetic field. An iron flux return located outside the solenoid is instrumented to detect $K_{L}^{0}$ mesons and to identify muons. The detector is described in detail elsewhere [17]. The data set used in this analysis was collected with two different inner detector configurations. About $152 \times 10^{6} B \bar{B}$ pairs were collected with a beam pipe of radius 2 cm and with three layers of SVD, while the rest of the data set was collected with a beam pipe of radius 1.5 cm and four layers of SVD [19].

Large MC samples for signal and different backgrounds are generated with EvtGen [20] and simulated under GEANT3 [21] with the configuration of the Belle detector. These samples are used to obtain the expected distributions of various physical quantities for signal and background, optimize the selection criteria, and determine the signal selection efficiency.

The selection criteria for the final state charged particles in $B^{0} \rightarrow p \bar{\Lambda} \pi^{-} \gamma$ are based on information obtained from the tracking systems (SVD and CDC) and the hadron identification systems (CDC, ACC, and TOF). The proton and pion from $B^{0}$ decay are required to have a point of closest approach to the interaction point (IP) within $\pm 0.3 \mathrm{~cm}$ in the transverse ( $x-y$ ) plane, and within $\pm 3 \mathrm{~cm}$ along the $z$ axis, where the $+z$ direction is opposite the positron beam direction. The likelihood values of each track for different particle types, $L_{p}, L_{K}$, and $L_{\pi}$, are
determined from the information provided by the hadron identification system. The track is identified as a proton if $L_{p} /\left(L_{p}+L_{K}\right)>0.6$ and $L_{p} /\left(L_{p}+L_{\pi}\right)>0.6$ or as a pion if $L_{\pi} /\left(L_{\pi}+L_{K}\right)>0.6$. The efficiency for identifying a pion is about $95 \%$, depending on the momentum of the track, while the probability for a kaon to be misidentified as a pion is less than $10 \%$. The efficiency for identifying a proton is about $95 \%$, while the probability for a kaon or a pion to be misidentified as a proton is less than $10 \%$. The efficiency and misidentification probability are averaged over the momentum of the particles in the final state. We reconstruct a $\Lambda$ candidate from its decay to $p \pi^{-}$. Each $\Lambda$ candidate must have a displaced vertex with its momentum vector being consistent with an origin at the IP. The proton from $\Lambda$ decay is required to satisfy the proton criteria described above, whereas the pion daughter has no such requirement. The reconstructed $\Lambda$ mass should satisfy $1.111 \mathrm{GeV} / c^{2}<M_{p \pi^{-}}<1.121 \mathrm{GeV} / c^{2}$, and this constraint retains about $82 \%$ of total signal events. The hard photon must have an energy greater than 1.7 GeV in the c.m. frame.

Candidate $B$ mesons are identified with kinematic variables calculated in the c.m. frame: the beam-energyconstrained mass $M_{\mathrm{bc}} \equiv \sqrt{E_{\text {beam }}^{2} / c^{4}-\left|p_{B} / c\right|^{2}}$ and the energy difference $\Delta E \equiv E_{B}-E_{\text {beam }}$, where $E_{\text {beam }}$ is the beam energy and $p_{B}$ and $E_{B}$ are the momentum and energy of the reconstructed $B$ meson, respectively. The candidate region is defined as $M_{\mathrm{bc}}>5.24 \mathrm{GeV} / c^{2}$ and $-0.4 \mathrm{GeV}<\Delta E<0.3 \mathrm{GeV}$, and the signal region is defined as $M_{\mathrm{bc}}>5.27 \mathrm{GeV} / c^{2}$ and $|\Delta E|<0.05 \mathrm{GeV}$.

The dominant background for $B^{0} \rightarrow p \bar{\Lambda} \pi^{-} \gamma$ in the candidate region is from the continuum $e^{+} e^{-} \rightarrow q \bar{q}(q=$ $u, d, s, c)$ processes. We distinguish the jetlike continuum background relative to the more spherical $B \bar{B}$ signal using a Fisher discriminant discussed in Ref. [22]. The Fisher discriminant is a linear combination of several event shape variables with coefficients that are optimized to separate signal and background. An independent variable, $\cos \theta_{B}$, where $\theta_{B}$ is the angle between the reconstructed $B$ flight direction and the beam direction in the c.m. frame, is combined with the Fisher discriminant to form signal and background probability density functions (PDFs). These PDFs, obtained separately from signal and continuum MC simulations, give the event-by-event signal and background likelihoods, $\mathcal{L}_{S}$ and $\mathcal{L}_{B}$. We apply a selection on the likelihood ratio, $\mathcal{R} \equiv \mathcal{L}_{S} /\left(\mathcal{L}_{S}+\mathcal{L}_{B}\right)>0.85$, to suppress the continuum background. The value of the $\mathcal{R}$ selection is determined by maximizing the figure of merit, defined as $N_{S} / \sqrt{N_{S}+N_{B}}$, where $N_{S}$ denotes the expected number of signal events in the signal region with an assumed branching fraction $\left(10^{-5}\right)$, and $N_{B}$ denotes the expected number of continuum background events in the signal region. The selection on $\mathcal{R}$ removes $97 \%$ of the continuum background while retaining $61 \%$ of the signal.

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If more than one $B$ candidate is found in a single event, we choose the one with the smallest $\chi_{B}^{2}+\chi_{\Lambda}^{2}$ value, using the goodness-of-fit values $\chi_{B}^{2}$ and $\chi_{\Lambda}^{2}$ that are $\chi^{2}$ from the $B$ and $\Lambda$ vertex fits, respectively. The vertex fits only use the charged daughters. Multiple candidates are mainly due to the misreconstruction using a pion from the other $B$ meson and are found in $9.8 \%$ of the data; the average multiplicity is 2.2.

Other important backgrounds in the candidate region include $B$ decays through the $b \rightarrow c$ process (generic $B$ decays), charmless (i.e., "rare") $B$ decays, and the selfcrossfeed events. Since the generic $B$ decays do not cause any peaking structure in the candidate region and their yields are much less than that of continuum background, we merge these with the continuum background. The remaining backgrounds have a peaking structure in $\Delta E$ and $M_{\mathrm{bc}}$, although the overall shapes are quite different from the signal shapes. Based on the rare- $B \mathrm{MC}$ simulation, the following seven modes are found to contribute to the candidate region: $B^{0} \rightarrow p \bar{\Lambda} \rho_{-}^{-}, B^{0} \rightarrow p \bar{\Sigma}^{0} \underline{\rho}^{-}$, $B^{0} \rightarrow p \bar{\Lambda} \pi^{-} \eta, \quad B^{+} \rightarrow p \bar{\Lambda} \pi^{0}, \quad B^{+} \rightarrow p \bar{\Sigma}^{0} \pi^{0}, \quad B^{+} \rightarrow p \bar{\Lambda} \gamma$, and $B^{+} \rightarrow p \bar{\Lambda} \eta$. Only two of these, $B^{+} \rightarrow p \bar{\Lambda} \pi^{0}$ and $B^{+} \rightarrow$ $p \bar{\Lambda} \gamma[5,7]$, have been measured experimentally. For the $B^{0} \rightarrow p \bar{\Lambda} \pi^{-} \gamma$ self-crossfeed events, candidate $B$ events are misreconstructed using a slow pion from the other $B$ meson. According to MC simulation, we find $42 \%$ of events are self-crossfeed events and cannot be removed without losing significant signal. We rely on the fitting method to distinguish signal from these backgrounds.

The signal yield of the $B^{0} \rightarrow p \bar{\Lambda} \pi^{-} \gamma$ mode is extracted from a two-dimensional extended unbinned maximum likelihood fit, with the likelihood defined as

$$
\begin{equation*}
\mathcal{L}=\frac{e^{-\sum_{j} N_{j}}}{N!} \prod_{i=1}^{N}\left(\sum_{j} N_{j} P_{j}\left(M_{\mathrm{bc}}^{i}, \Delta E^{i}\right)\right) \tag{1}
\end{equation*}
$$

where $N$ is the total number of candidate events, $N_{j}$ is the number of events in category $j, P_{j}$ represents the value of the corresponding two-dimensional PDF, and $M_{\mathrm{bc}}^{i}\left(\Delta E^{i}\right)$ is the $M_{\mathrm{bc}}(\Delta E)$ value of the $i$ th candidate. There are five PDFs in the fit: signal, self-crossfeed, continuum background, and the two measured rare decay modes ( $B^{+} \rightarrow p \bar{\Lambda} \pi^{0}$ and $B^{+} \rightarrow p \bar{\Lambda} \gamma$ ). The other five rare- $B$ modes are considered only in the systematic uncertainties, as discussed later. We use two-dimensional smoothed histograms to represent the $M_{\mathrm{bc}}-\Delta E$ PDFs of the signal, selfcrossfeed, and two measured rare- $B$ modes. The signal PDF is calibrated by comparing the difference between data and MC simulation for the $B^{+} \rightarrow K^{*+} \gamma$ control sample. The PDF that describes the continuum background is a product of an ARGUS function [23] in $M_{\mathrm{bc}}$ and a second-order polynomial in $\Delta E$. The ratio of self-crossfeed events to signal events is fixed, which is estimated from the MC simulation, and the yields of two measured rare modes are also fixed according to the measured branching fractions

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FIG. 2 (color online). Fit results of $B^{0} \rightarrow p \bar{\Lambda} \pi^{-} \gamma$. The top plot shows the $\Delta E$ distribution for $M_{\mathrm{bc}}>5.27 \mathrm{GeV} / c^{2}$, and the bottom one shows $M_{\mathrm{bc}}$ for $|\Delta E|<0.05 \mathrm{GeV}$. The points with error bars are data, the solid line is the fit result, the green dotted line is continuum background, the blue dash-dotted line is the combination of $B^{+} \rightarrow p \bar{\Lambda} \pi^{0}$ and $B^{+} \rightarrow p \bar{\Lambda} \gamma$, and the red area is the combination of the signal and self-crossfeed.
[5,7]. The free parameters in the fit are the signal yield, the continuum yield, and the continuum shape parameters.

The projections of the fit are shown in Fig. 2. The fitted signal yield is $9.5_{-10.7}^{+11.5}$ with a statistical significance of 0.9 . The statistical significance is defined as $\sqrt{-2 \ln \left(\mathcal{L}_{0} / \mathcal{L}_{\text {max }}\right)}$, where $\mathcal{L}_{0}$ and $\mathcal{L}_{\text {max }}$ are the likelihood values obtained by the fit with and without the signal yield fixed to zero, respectively.

The branching fraction is calculated using

$$
\begin{equation*}
\mathcal{B}=\frac{N_{\mathrm{sig}}}{\epsilon \times N_{B \bar{B}}}, \tag{2}
\end{equation*}
$$

where $N_{\text {sig }}, N_{B \bar{B}}$, and $\epsilon$ are the fitted signal yield, the number of $B \bar{B}$ pairs, and the reconstruction efficiency of signal, respectively. We assume that charged and neutral $B \bar{B}$ pairs are produced equally at the $\Upsilon(4 S)$. We calibrate the reconstruction efficiency estimated using the MC simulation by including in $\epsilon$ a factor $\varepsilon_{\mathcal{R}} \times \varepsilon_{\mathrm{HID}}$, where $\varepsilon_{\mathcal{R}}(=0.973 \pm 0.018)$ and $\varepsilon_{\mathrm{HID}}(=0.928 \pm 0.011)$ refer

TABLE I. Summary of the systematic uncertainties (in \%) on the branching fraction.

| $N_{B \bar{B}}$ | 1.4 |
| :--- | :---: |
| Tracking | $1.4(4$ tracks $)$ |
| Hadron identification | $0.6(2$ protons $)$ |
|  | 1.1 (pion $)$ |
| $\Lambda$ selection | 3.3 |
| Photon selection | 2.2 |
| Reconstruction efficiency (MC statistics) | 2.2 |
| $\mathcal{B}\left(\Lambda \rightarrow p \pi^{-}\right)$ | 0.8 |
| $\mathcal{R}$ selection | 1.9 |
| PDF shape | 4.1 |
| Signal decay model | 5.1 |
| Rare $B$ decays | 8.2 |
| Total | 11.8 |

to the corrections due to the selection on $\mathcal{R}$ and the hadron identification, respectively. Here, $\varepsilon_{\mathcal{R}}$ is obtained from the control sample study of $B^{+} \rightarrow K^{*+} \gamma ; \varepsilon_{\text {HID }}$ is determined by various control samples with different particle types such as $\Lambda \rightarrow p \pi^{-}$and $D^{*+} \rightarrow D^{0} \pi^{+}$with $D^{0} \rightarrow K^{-} \pi^{+}$. The calibrated reconstruction efficiency for the signal $\epsilon$ is about 5.3\%.

Sources of various systematic uncertainties on the branching fraction calculation are shown in Table I. The uncertainty due to the total number of $B \bar{B}$ pairs is $1.4 \%$. The uncertainty due to the charged-track reconstruction efficiency is estimated to be $0.35 \%$ per track by using the partially reconstructed $D^{*+} \rightarrow D^{0} \pi^{+}$with $D^{0} \rightarrow \pi^{+} \pi^{-} K_{S}^{0}$ events. The uncertainty due to $\Lambda$ selection is estimated by a control sample study of $\Lambda \rightarrow p \pi^{-}$. The uncertainty due to photon selection is evaluated with a radiative Bhabha sample to be $2.2 \%$. The uncertainties due to the $\mathcal{R}$ selection and the signal PDF shape are estimated using the control sample of $B^{+} \rightarrow K^{*+} \gamma$. Because of the presence of the selfcrossfeed PDF in the fit, the uncertainty due to the signal PDF shape is inflated by a factor of $\sqrt{2}$. The uncertainty due to the signal decay model is estimated to be $5.1 \%$ by using different decay models. For instance, the base decay model of our study is $B^{0} \rightarrow X_{s} \gamma$ with $X_{s} \rightarrow p \bar{\Lambda} \pi^{-}$decaying uniformly in phase space; the mass of $X_{s}$ has a simple Breit-Wigner distribution with a mean value at $2.5 \mathrm{GeV} / c^{2}$ and a $0.3 \mathrm{GeV} / c^{2}$ width. An alternate model is $X_{s} \rightarrow X_{p l} \pi^{-}$with $X_{p l} \rightarrow p \bar{\Lambda}$, where $X_{p l}$ stands for the threshold peak measured in Ref. [7]. The uncertainties for the two measured rare modes discussed above are estimated by varying each yield in the fit by $\pm 1 \sigma$, where $\sigma$ denotes the measurement error on the branching fraction. The uncertainty for the five unmeasured rare modes discussed above is estimated by incorporating their PDFs in the fit and floating their yields. As the signal yield is reduced by this fit, we did not include this effect in the upper limit calculation described below to get a conservative upper limit. The overall systematic uncertainty due to rare $B$ decays is $8.2 \%$ and dominates in this measurement.

Since the observed yield for $B^{0} \rightarrow p \bar{\Lambda} \pi^{-} \gamma$ is not significant, we evaluate the $90 \%$ confidence-level Bayesian upper limit branching fraction $\left(\mathcal{B}_{\mathrm{UL}}\right)$. This upper limit is obtained by integrating the likelihood function

$$
\begin{equation*}
\int_{0}^{\mathcal{B}_{\mathrm{UL}}} \mathcal{L}(\mathcal{B}) d \mathcal{B}=0.9 \int_{0}^{1} \mathcal{L}(\mathcal{B}) d \mathcal{B} \tag{3}
\end{equation*}
$$

where $\mathcal{L}(\mathcal{B})$ denotes the likelihood value. The systematic uncertainties are taken into account by replacing $\mathcal{L}(\mathcal{B})$ with a smeared likelihood function. We thus determine the upper limit on the branching fraction of $\mathcal{B}\left(B^{0} \rightarrow\right.$ $\left.p \bar{\Lambda} \pi^{-} \gamma\right)$ to be $6.5 \times 10^{-7}$ at the $90 \%$ confidence level.

In conclusion, we have performed a search for $B^{0} \rightarrow p \bar{\Lambda} \pi^{-} \gamma$, which proceeds via the $b \rightarrow s \gamma$ radiative penguin process, by using the full $\Upsilon(4 S)$ data sample of $772 \times 10^{6} B \bar{B}$ pairs collected by Belle. No significant signal yield is found, and we set the upper limit on the branching fraction to be $6.5 \times 10^{-7}$ at the $90 \%$ confidence level. We also conclude that the decay under study does not follow the expected hierarchy; instead, we find $\mathcal{B}\left(B^{0} \rightarrow p \bar{\Lambda} \pi^{-} \gamma\right)<\mathcal{B}\left(B^{+} \rightarrow p \bar{\Lambda} \gamma\right)$.

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[^0]:    ${ }^{1}$ Throughout this paper, inclusion of charge-conjugate decay modes is always implied.

